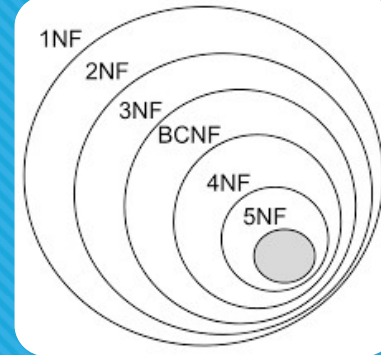


# CSCI 5333: DBMS

## Chapter 8

### Normalization for Relational Databases



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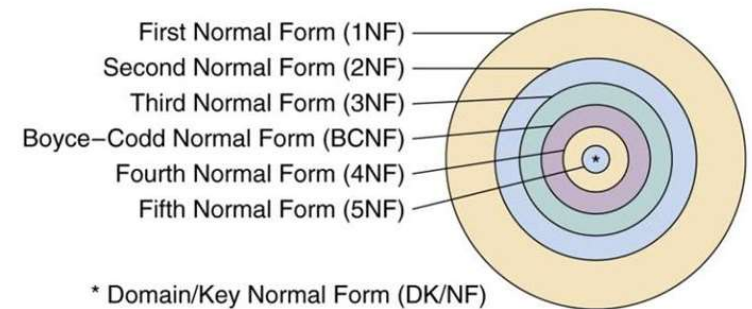
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# Chapter Outline

- Drawback in Relational Database Design
- Decomposition of Relations
- Informal guideline of Normalization
- Functional Dependencies
- Armstrong Axioms
- Attribute Closure
- Canonical Cover
- 3<sup>rd</sup> Normal Form (3NF)
- Boyce Code Normal Form (BCNF)

Relationship of Normal Forms



\* Domain/Key Normal Form (DK/NF)

# Drawback in Relational Database Design

- Relational database design requires that we find a “good” collection of relation schemas. A bad design may lead to:
  - Repetition of Information.
  - Inability to represent certain information.
- Design Goals:
  - Avoid redundant data
  - Ensure that relationships among attributes are represented
  - Facilitate the checking of updates for violation of database integrity constraints.



# Example

- Consider the relation schema:

*Lending = (branch-name, branch-city, assets, customer-name, loan-number, amount)*

<i>branch-name</i>	<i>branch-city</i>	<i>assets</i>	<i>customer-name</i>	<i>loan-number</i>	<i>amount</i>
Downtown	Brooklyn	9000000	Jones	L-17	1000
Redwood	Palo Alto	2100000	Smith	L-23	2000
Perryridge	Horseneck	1700000	Hayes	L-15	1500
Downtown	Brooklyn	9000000	Jackson	L-14	1500

- Redundancy:

- Data for *branch-name*, *branch-city*, *assets* are repeated for each loan that a branch makes
- Wastes space
- Complicates updating, introduces possibility of inconsistency of *assets* value

- Null values

- Cannot store information about a branch if no loans exist
- Can use null values, but they are difficult to handle.

# Decomposition

- The way which we eliminate inconsistency in relations is to decompose that relation into two or more *sub-relations*.
- We check to see if a relation is in a *normal form* e.g. BCNF or 3NF, and if it does not meet the criteria, we split the relation into sub-relations
- In the case that a relation  $R$  is not in “*good*” form, decompose it into a set of relations  $\{R_1, R_2, \dots, R_n\}$  such that:
  - each relation is in good form
  - the decomposition is a *lossless-join* decomposition
- Our theory is based on:
  - functional dependencies
  - multivalued dependencies

# Decomposition

- Decompose the relation schema *Lending-schema* into:  
Branch = (branch-name, branch-city, assets)  
Loan-info = (loan-number, customer-name, branch-name, amount)
- All attributes of an original schema ( $R$ ) must appear in the decomposed schemas ( $R_1, R_2$ ):  
 $R = R_1 \cup R_2$
- Lossless-join decomposition:  
For all possible relations  $r$  on schema  $R$   
 $r = \Pi_{R_1}(r) \bowtie \Pi_{R_2}(r)$

# Decomposition (Example)

R

	title	year	length	type	studioName	starName
	Star Wars	1977	124	Sci-Fi	Fox	Carrie Fisher
	Star Wars	1977	124	Sci-Fi	Fox	Mark Hamill
	Braveheart	1994	280	Action	Universal	Mel Gibson
	Breakfast Club	1986	200	Comedy	Paramount	Molly Ringwal
	Breakfast Club	1986	200	Comedy	Paramount	Emilo Estavez

Record: 5 of 5

S

	title	year	length	type	studioName
	Star Wars	1977	124	Sci-Fi	Fox
	Braveheart	1994	280	Action	Universal
	Breakfast Club	1986	200	Comedy	Paramount

Record: 3 of 3

T

	title	year	starName
	Star Wars	1977	Carrie Fisher
	Star Wars	1977	Mark Hamill
	BraveHeart	1994	Mel Gibson
	Breakfast Club	1986	Molly Ringwal
	Breakfast Club	1986	Emilo Estavez

Record: 6 of 6



# Decomposing Relations

- In previous, we saw that we could 'decompose' the bad relation schema like the following:

Data(sid, sname, addrs, cid, cname, grade)

to a 'better' set of relation schema

Student(sid, sname, addrs)

Course(cid, cname)

Enrolled(sid, cid, grade)



# Are all Decompositions good?

- Consider our motivating example:

`Data = (sid, sname, address, cid, cname, grade)`

- Alternatively we could decompose into

`R1 = (sid, sname, address)`

`R2 = (cid, cname, grade)`

- But this decomposition loses information about the relationship between students and courses.
- We require to understand the **data semantics as well**.

# Informal Guidelines for Normalization

- Let's say we want to create a table of user information, and we want to store each users' Name, Company, Company Address, and some personal bookmarks, or urls.
- You might start by defining a table structure like this:

users				
name	company	company_address	url1	url2
Joe	ABC	1 Work Lane	abc.com	xyz.com
Jill	XYZ	1 Job Street	abc.com	xyz.com

# First Normal Form

- First Normal Form: **NO REPEATING GROUPS**
  1. Eliminate repeating groups in individual tables.
  2. Create a separate table for each set of related data.
  3. Identify each set of related data with a primary key.
- Historically, it was defined to disallow multi-valued attributes, composite attributes, and their combinations
- Create another table in first normal form by eliminating the repeating group (Url#), as shown below:

users				
Userld	name	company	company_address	url
1	Joe	ABC	1 Work Lane	abc.com
1	Joe	ABC	1 Work Lane	xyz.com
2	Jill	XYZ	1 Job Street	abc.com
2	Jill	XYZ	1 Job Street	xyz.com

# Second Normal Form

- Second Normal Form: **ELIMINATE REDUNDANT DATA**

1. Create *separate tables* for sets of values that apply to multiple records.
2. Relate these tables with a *foreign key*.

users			
userId	name	company	company_address
1	Joe	ABC	1 Work Lane
2	Jill	XYZ	1 Job Street

urls	
relUserId	url
1	abc.com
1	xyz.com
2	abc.com
2	xyz.com

- what happens when we want to add another employee of company ABC?



# Third Normal Form (3NF)

## ○ Third Normal Form: ELIMINATE DATA NOT DEPENDENT ON KEY

- Eliminate fields that do not depend on the key.
- Relate these tables with a foreign key.

users		
userId	name	relCompId
1	Joe	1
2	Jill	2

companies		
compId	company	company_address
1	ABC	1 Work Lane
2	XYZ	1 Job Street

urls	
relUserId	url
1	abc.com
1	xyz.com
2	abc.com
2	xyz.com

# Functional Dependencies

- Definition of FD
- Closure of a Set of FDs
- Armstrong's Axioms
- Trivial Dependencies

# Functional Dependency

- Functional dependencies are constraints on the set of legal relations.
- Requires that the value for a certain set of attributes determines uniquely the value for another set of attributes.
- A functional dependency is a generalization of the notion of a key which can be used in normalization
- **Definition:**
  - If two tuples of R agree in attribute A then they must agree in another attribute B
- Written as
  - $A \rightarrow B$
  - A functionally determines B
  - B is functionally dependent on A



# Functional Dependencies (Cont.)

- Let  $R$  be a relation schema

$$\alpha \subseteq R \text{ and } \beta \subseteq R$$

- The **functional dependency**  $\alpha \rightarrow \beta$  **holds on  $R$**  if and only if for any legal relations  $r(R)$ , whenever any two tuples  $t_1$  and  $t_2$  of  $r$  agree on the attributes  $\alpha$ , they also agree on the attributes  $\beta$ . That is,

$$t_1[\alpha] = t_2[\alpha] \Rightarrow t_1[\beta] = t_2[\beta]$$

- Example: Consider  $r(A, B)$  with the following instance of  $r$ .

1	4
1	5
3	7

- On this instance,  $A \rightarrow B$  does **NOT** hold, but  $B \rightarrow A$  does hold.



**A → B**

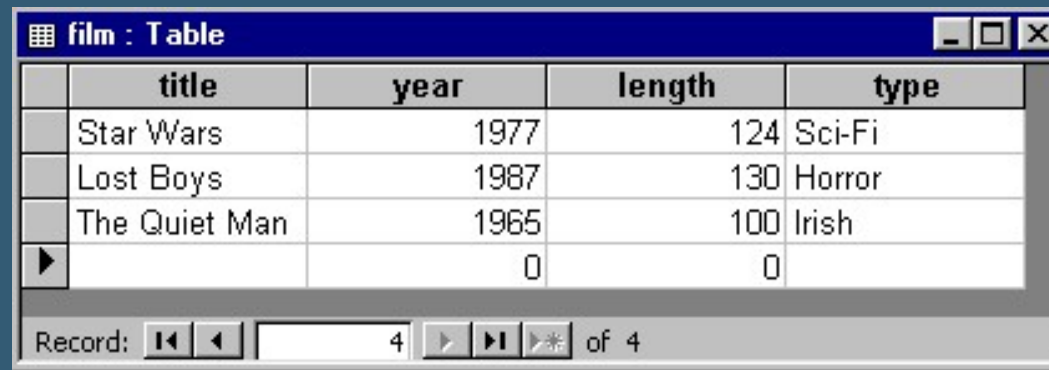
tuple **t**

tuple **u**



FunD : Table		
	A	B
/		
*		
Record: 3		

- If tuple **t** and tuple **u** agree on the value of attribute **A**, then they must also agree on the value of attribute **B**

# Example One



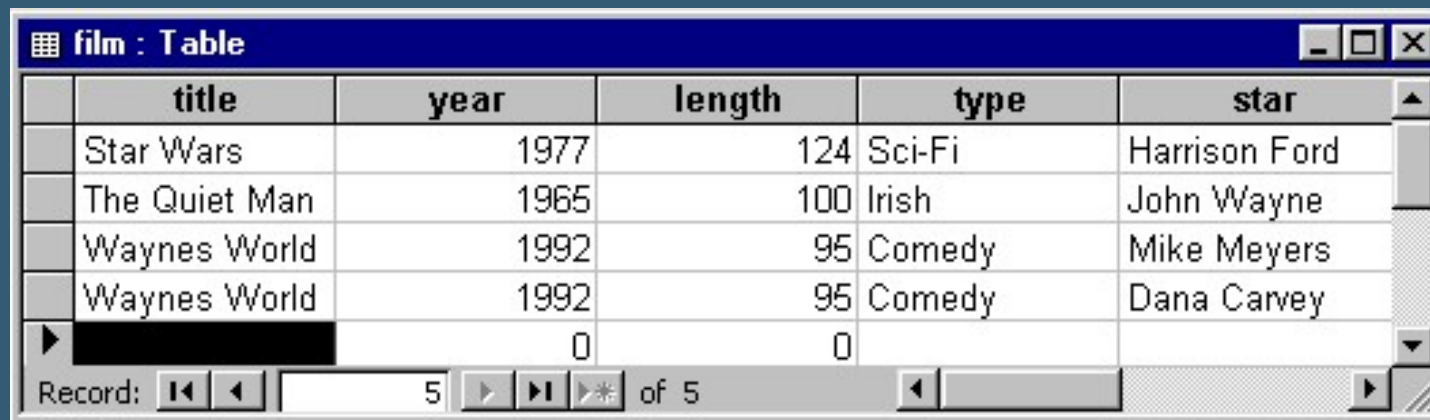
	title	year	length	type
	Star Wars	1977	124	Sci-Fi
	Lost Boys	1987	130	Horror
	The Quiet Man	1965	100	Irish
▶		0	0	

Record:  4  of 4

title, year → length  
title, year → type

- This says that if two tuples have the same value in their *title* and *year* attributes, then these two tuples **must** have the same values in their *length* and *type* attributes.

# Example Two



	title	year	length	type	star
	Star Wars	1977	124	Sci-Fi	Harrison Ford
	The Quiet Man	1965	100	Irish	John Wayne
	Waynes World	1992	95	Comedy	Mike Meyers
	Waynes World	1992	95	Comedy	Dana Carvey
▶		0	0		

Record: 5 of 5

title, year → length

title, year → type

title, year → star???

## Example Three

- Consider the schema  
**loan-info(loan-number, customer, amount)**
- The following functional dependency *holds* on **loan-info**
  - **loan-number** → **amount**
- If more than one person can own a loan does
  - **loan-number** → **customer** hold?



# Exercise

Do the following FD's hold for the above relation?

$A \rightarrow B$

$B \rightarrow C$

$C \rightarrow D$

$A \rightarrow C$

$A \rightarrow D$

$B \rightarrow D$

A	B	C	D
A1	B1	C1	D1
A1	B2	C1	D2
A2	B2	C2	D2
A2	B3	C2	D3
A3	B3	C2	D4

# Trivial Dependencies

- A functional dependency,  $\alpha \rightarrow \beta$ , is said to be **trivial** if  $\beta \subseteq \alpha$ 
  - *customer-name, loan-number  $\rightarrow$  customer-name*
  - *customer-name  $\rightarrow$  customer-name*
- **nontrivial** if at least one of the attributes in  $\beta$  is not in  $\alpha$ 
  - *customer-name, loan-number  $\rightarrow$  customer-name, city*
- **completely nontrivial** if none of the attributes in  $\beta$  are in  $\alpha$ 
  - *customer-name, loan-number  $\rightarrow$  city*

## Closure of a Set of FDs ( $F^+$ )

- Given a set  $F$  set of functional dependencies, there are certain other functional dependencies that are logically implied by  $F$ .
  - E.g. If  $A \rightarrow B$  and  $B \rightarrow C$ , then we can infer that  $A \rightarrow C$ .

A	B	C
A1	B1	C3
A1	B1	C3
A2	B4	C5

## Closure of a Set of FDs ( $F^+$ )

- The set of all functional dependencies logically implied by  $F$  is the *closure* of  $F$ .
- We denote the *closure* of  $F$  by  $F^+$ .
- We can find all of  $F^+$  by applying Armstrong's Axioms:
  - if  $\beta \subseteq \alpha$ , then  $\alpha \rightarrow \beta$  (reflexivity)
  - if  $\alpha \rightarrow \beta$ , then  $\gamma \alpha \rightarrow \gamma \beta$  (augmentation)
  - if  $\alpha \rightarrow \beta$ , and  $\beta \rightarrow \gamma$ , then  $\alpha \rightarrow \gamma$  (transitivity)
- These rules are
  - sound (generate only functional dependencies that actually hold) and
  - complete (generate all functional dependencies that hold).



# Armstrong's Axioms

- Armstrong's axioms are a set of three rules and by applying these rules repeatedly we can find all of  $F^+$

- **Reflexivity Rule**

- If  $\alpha$  is a set of attributes and  $\beta \subseteq \alpha$ , then  $\alpha \rightarrow \beta$  holds

- **Example:**  $\alpha = (A, B, C, D)$ ,  $\beta = (A, B)$

$(A, B, C, D) \rightarrow (A, B)$  holds

- **Augmentation Rule**

- If  $\alpha \rightarrow \beta$  holds and  $\gamma$  is a set of attributes, then  $\gamma\alpha \rightarrow \gamma\beta$  holds

- **Example:**  $\alpha = (A, B, C, D)$ ,  $\beta = (X, Y)$ ,  $\gamma = (M, N)$  then  $\gamma\alpha \rightarrow \gamma\beta$

$(A, B, C, D, M, N) \rightarrow (M, N, X, Y)$  holds

# Armstrong's Axioms

## ○ Transitivity Rule

○ If  $\alpha \rightarrow \beta$  holds and  $\beta \rightarrow \gamma$  holds, then  $\alpha \rightarrow \gamma$  holds

○ Example:  $\alpha = (A, B, C, D)$ ,  $\beta = (X, Y)$ ,  $\gamma = (M, N)$

$\alpha \rightarrow \beta$   $(A, B, C, D) \rightarrow (X, Y)$

$\beta \rightarrow \gamma$   $(X, Y) \rightarrow (M, N)$

$\alpha \rightarrow \gamma$   $(A, B, C, D) \rightarrow (M, N)$  holds

- These rules are *sound*, i.e. they do not generate any incorrect functional dependencies
- The rules are also *complete*, i.e. they generate ALL the possible functional dependencies from the original set that form  $F^+$

# Example

- $R = (A, B, C, G, H, I)$
- $F = \{ A \rightarrow B, A \rightarrow C, CG \rightarrow H, CG \rightarrow I, B \rightarrow H \}$
- Some members of  $F^+$ 
  - $A \rightarrow H$ 
    - by transitivity from  $A \rightarrow B$  and  $B \rightarrow H$
  - $AG \rightarrow I$ 
    - by augmenting  $A \rightarrow C$  with  $G$ , to get  $AG \rightarrow CG$  and then transitivity with  $CG \rightarrow I$
  - $CG \rightarrow HI$ 
    - Augmentation of  $CG \rightarrow I$  to infer  $CG \rightarrow CGI$ , augmentation of  $CG \rightarrow H$  to infer  $CGI \rightarrow HI$ , and then transitivity
    - from  $CG \rightarrow H$  and  $CG \rightarrow I$ : “union rule” can be inferred from

# Exercise

- Consider the schema
  - $R(A, B, C, D)$
- and the FD's
  - $F = \{AB \rightarrow C, C \rightarrow D, D \rightarrow A\}$
- What are the **nontrivial** functional dependencies that follow from the given set?
  - $AB \rightarrow D, \cancel{AB \rightarrow A}$



## Closure of a Set of FDs ( $F^+$ )

- There are also some additional rules that are not part of Armstrong's axioms
- We can further simplify manual computation of  $F^+$  by using the following additional rules.
  - If  $\alpha \rightarrow \beta$  holds and  $\alpha \rightarrow \gamma$  holds, then  $\alpha \rightarrow \beta\gamma$  holds (**union**)
  - If  $\alpha \rightarrow \beta\gamma$  holds, then  $\alpha \rightarrow \beta$  holds and  $\alpha \rightarrow \gamma$  holds (**decomposition**)
  - If  $\alpha \rightarrow \beta$  holds and  $\gamma\beta \rightarrow \delta$  holds, then  $\alpha\gamma \rightarrow \delta$  holds (**pseudotransitivity**)
- The above rules can be inferred from Armstrong's axioms.

# Union Rule

If  $\alpha \rightarrow \beta$  holds and  $\alpha \rightarrow \gamma$  holds, then  
 $\alpha \rightarrow \beta\gamma$  holds

$$\alpha = (A, B, C, D), \quad \beta = (X, Y), \quad \gamma = (M, N)$$

$$\alpha \rightarrow \beta \quad (A, B, C, D) \rightarrow (X, Y)$$

$$\alpha \rightarrow \gamma \quad (A, B, C, D) \rightarrow (M, N)$$

$$\alpha \rightarrow \beta\gamma \quad (A, B, C, D) \rightarrow (X, Y, M, N)$$

# Decomposition Rule

If  $\alpha \rightarrow \beta \gamma$  holds, then  
 $\alpha \rightarrow \beta$  and  $\alpha \rightarrow \gamma$  holds

$$\alpha = (A, B, C, D), \beta = (X, Y), \gamma = (M, N)$$

$$\alpha \rightarrow \beta \gamma \quad (A, B, C, D) \rightarrow (X, Y, M, N)$$

$$\alpha \rightarrow \beta \quad (A, B, C, D) \rightarrow (X, Y)$$

$$\alpha \rightarrow \gamma \quad (A, B, C, D) \rightarrow (M, N)$$

# Pseudotransitivity Rule

If  $\alpha \rightarrow \beta$  holds and  $\gamma \beta \rightarrow \delta$ , then  
 $\alpha \gamma \rightarrow \delta$  holds

$\alpha = (A, B, C, D)$ ,  $\beta = (X, Y)$ ,  $\gamma = (M, N)$ ,  $\delta = (P, Q)$

$\alpha \rightarrow \beta$   $(A, B, C, D) \rightarrow (X, Y)$

$\gamma \beta \rightarrow \delta$   $(M, N, X, Y) \rightarrow (P, Q)$

$\alpha \gamma \rightarrow \delta$   $(A, B, C, D, M, N) \rightarrow (P, Q)$



# Determining Keys

- We can also use functional dependencies to determine what are the candidate keys of a relation by using the following definition
  - A set of one or more attributes,  $\alpha$ , is a candidate key for a relation  $R$  if and only of
    - $\alpha$  functionally determine all other attributes of the relation ( $\alpha \rightarrow R$ ), i.e. it is impossible for two distinct tuples of  $R$  to agree on all attributes in the set,  $\alpha$  (superkeys)
    - no proper subset of  $\alpha$  functionally determines all other attributes of  $R$  (candidate keys)
- Note: A specific instance of a relation schema may satisfy a functional dependency even if the functional dependency does not hold on all legal instances. e.g., *loan-number*  $\rightarrow$  *customer-name*

# Example

Customer : Table					
	ID	Name	Address	Phone	DOB
▶					
Record: ◀ ◁ 1 ▷ ▶* of 1 ◀ ▶					

(ID, Name, Address, Phone, DOB)

(ID, Name, Address, DOB)

(ID, Name, Phone, DOB)

(ID, Name)

(ID, Address)

(ID, Phone)

(ID, DOB)

(ID) → Candidate key

Superkeys

# Closure of Attribute Sets

- To test whether a set  $\alpha$  is a superkey, we must determine the set of attributes functionally determined by  $\alpha$
- Given a set of attributes  $\alpha$ , define the *closure* of  $\alpha$  under  $F$  (denoted by  $\alpha^+$ ) as the set of attributes that are functionally determined by  $\alpha$  under  $F$ :

$$\alpha \rightarrow \beta \text{ is in } F^+ \Leftrightarrow \beta \subseteq \alpha^+$$

- Algorithm to compute  $\alpha^+$ , the closure of  $\alpha$  under  $F$

```
result :=  $\alpha$ ;  
while (changes to result) do  
  for each  $\beta \rightarrow \gamma$  in  $F$  do  
    begin  
      if  $\beta \subseteq \text{result}$  then  $\text{result} := \text{result} \cup \gamma$   
    end
```

## Example of Attribute Set Closure

- $R = (A, B, C, G, H, I)$
- $F = \{A \rightarrow B, A \rightarrow C, CG \rightarrow H, CG \rightarrow I, B \rightarrow H\}$
- $(AG)^+$ 
  1.  $result = AG$
  2.  $result = ABCG$  ( $A \rightarrow C$  and  $A \rightarrow B$ )
  3.  $result = ABCGH$  ( $CG \rightarrow H$  and  $CG \subseteq AGBC$ )
  4.  $result = ABCGHI$  ( $CG \rightarrow I$  and  $CG \subseteq AGBCH$ )
- Is AG a candidate key?
  1. Is AG a super key?
    1. Does  $AG \rightarrow R$ ?
  2. Is any subset of AG a superkey?
    1. Does  $A^+ \rightarrow R$ ?
    2. Does  $G^+ \rightarrow R$ ?



# Uses of Attribute Closure

- There are several *uses* of the attribute closure algorithm:
- **Testing for superkey:**
  - To test if  $\alpha$  is a superkey, we compute  $\alpha^+$  and check if  $\alpha^+$  contains all attributes of  $R$ .
- **Testing for functional dependencies**
  - To check if a functional dependency  $\alpha \rightarrow \beta$  holds (or, in other words, is in  $F^+$ ), just check if  $\beta \subseteq \alpha^+$ .
  - That is, we compute  $\alpha^+$  by using attribute closure, and then check if it contains  $\beta$ .
  - Is a simple and cheap test, and very useful
- **Computing closure of  $F$** 
  - For each  $\gamma \subseteq R$ , we find the closure  $\gamma^+$ , and for each  $S \subseteq \gamma^+$ , we output a functional dependency  $\gamma \rightarrow S$ .

# Normalization of the Relations

- Canonical Cover
- Properties of Decomposition
- Boyce-Codd Normal Form (BCNF)
- Third Normal Form (3NF)

# Canonical Cover

- Sets of functional dependencies may have **redundant** dependencies that can be inferred from the others
  - Parts of a functional dependency may be redundant
    - E.g. on **RHS**:  $\{A \rightarrow B, B \rightarrow C, A \rightarrow CD\}$  can be simplified to  $\{A \rightarrow B, B \rightarrow C, A \rightarrow D\}$
    - E.g. on **LHS**:  $\{A \rightarrow B, B \rightarrow C, AC \rightarrow D\}$  can be simplified to  $\{A \rightarrow B, B \rightarrow C, A \rightarrow D\}$
- Intuitively, a canonical cover of  $F$  is a “**minimal**” set of functional dependencies equivalent to  $F$ , with **no redundant dependencies** or having redundant parts of dependencies



# Extraneous Attributes

- Consider a set  $F$  of functional dependencies and the functional dependency  $\alpha \rightarrow \beta$  in  $F$ .
  - Attribute  $A$  is **extraneous** in  $\alpha$  if  $A \in \alpha$  and  $F$  logically implies  $(F - \{\alpha \rightarrow \beta\}) \cup \{(\alpha - A) \rightarrow \beta\}$ .
  - Attribute  $A$  is **extraneous** in  $\beta$  if  $A \in \beta$  and the set of functional dependencies  $(F - \{\alpha \rightarrow \beta\}) \cup \{\alpha \rightarrow (\beta - A)\}$  logically implies  $F$ .
- **Example:** Given  $F = \{A \rightarrow C, AB \rightarrow C\}$ 
  - $B$  is extraneous in  $AB \rightarrow C$  because  $A \rightarrow C$  logically implies  $AB \rightarrow C$ .
- **Example:** Given  $F = \{A \rightarrow C, AB \rightarrow CD\}$ 
  - $C$  is extraneous in  $AB \rightarrow CD$  since  $A \rightarrow C$  can be inferred even after deleting  $C$



# Testing if an Attribute is Extraneous

- Consider a set  $F$  of functional dependencies and the functional dependency  $\alpha \rightarrow \beta$  in  $F$ .
- To test if attribute  $A \in \alpha$  is extraneous in  $\alpha$ 
  1. compute  $(\alpha - \{A\})^+$  using the dependencies in  $F$
  2. check that  $(\alpha - \{A\})^+$  contains  $\beta$ ; if it does,  $A$  is extraneous in  $\alpha$
- To test if attribute  $A \in \beta$  is extraneous in  $\beta$ 
  1. compute  $\alpha^+$  using only the dependencies in  $F = (F - \{\alpha \rightarrow \beta\}) \cup \{\alpha \rightarrow (\beta - A)\}$ ,
  2. check that  $\alpha^+$  contains  $A$ ; if it does,  $A$  is extraneous

# Canonical Cover ( $F_c$ )

- To compute a canonical cover for  $F$ :

$$F_c = F$$

**repeat**

Use the union rule to replace any dependencies in  $F$

$\alpha_1 \rightarrow \beta_1$  and  $\alpha_1 \rightarrow \beta_2$  with  $\alpha_1 \rightarrow \beta_1 \beta_2$

Find a functional dependency  $\alpha \rightarrow \beta$  with an  
extraneous attribute either in  $\alpha$  or in  $\beta$

If an extraneous attribute is found, delete it from  $\alpha \rightarrow \beta$

**until**  $F$  does not change

- Note: Union rule may become applicable after some extraneous attributes have been deleted, so it has to be re-applied

# Example of Computing a Canonical Cover

- $R = (A, B, C)$
- $F = \{A \rightarrow BC$   
     $B \rightarrow C$   
     $A \rightarrow B$   
     $AB \rightarrow C\}$
- Combine  $A \rightarrow BC$  and  $A \rightarrow B$  into  $A \rightarrow BC$  (*union rule*)
  - Set is now  $\{A \rightarrow BC, B \rightarrow C, AB \rightarrow C\}$
- $A$  is extraneous in  $AB \rightarrow C$  because  $B \rightarrow C$  logically implies  $AB \rightarrow C$ .
  - Compute  $B^+$  and check it contains  $C$  or not. True, it contains  $C$
  - Set is now  $\{A \rightarrow BC, B \rightarrow C\}$
- $C$  is extraneous in  $A \rightarrow BC$  since  $A \rightarrow BC$  is logically implied by  $A \rightarrow B$  and  $B \rightarrow C$ .
  - Update  $F$  and then compute  $A^+$  contains  $C$  or not. True, it contains  $C$ ; so  $C$  is redundant
- The canonical cover is:

$$F_c = \{ A \rightarrow B$$
$$B \rightarrow C \}$$

# Canonical Cover

- We compute the canonical cover of  $F$  by
  - using the union rule to combine FD's with the same left hand side
  - finding and removing extraneous attributes
- A *canonical cover* for  $F$  is a set of dependencies  $F_c$  such that:
  - $F$  logically implies all dependencies in  $F_c$ , and
  - $F_c$  logically implies all dependencies in  $F$ , and
  - No functional dependency in  $F_c$  contains an extraneous attribute, and
  - Each left side of functional dependency in  $F_c$  is unique.



# Desirable Properties of Decomposition

- Desirable properties of a decomposition are:
  - Attribute preservation
  - Lossless-join decomposition
  - Dependency preservation
  - No Redundancy (i.e., 3NF or BCNF)
- **Attribute preservation:**
  - When we decompose a relation schema  $R$  into several sub-schemas  $R_1, R_2, \dots, R_n$  we want
  - $R = R_1 \cup R_2 \cup \dots \cup R_n$
  - That is, all attributes of an original schema ( $R$ ) must appear in the decomposition ( $R_1, R_2, \dots, R_n$ ):

# Desirable Properties of Decomposition

## ○ Lossless-Join Decomposition

- An important property of decomposition is that it should be possible to retrieve exactly the same information from the resulting relations as was present in the original relation.
- Computed using the *natural join*
- A decomposition of a relation  $R$  into relations  $R_1, R_2, \dots, R_n$  is called a *lossless-join* decomposition if the relation  $R$  is always the natural join of the relations  $R_1, R_2, \dots, R_n$

$$r = \Pi_{R_1}(r) \bowtie \Pi_{R_2}(r)$$

# Desirable Properties of Decomposition

## ○ Lossless-Join Decomposition (Cont....)

○ Given  $R$  decomposed into  $R_1$  and  $R_2$ , the decomposition is lossless if one of two conditions hold;

○  $R_1 \cap R_2 \rightarrow R_1$

○  $R_1 \cap R_2 \rightarrow R_2$

○ That is, the common attributes of  $R_1$  and  $R_2$  must include a candidate key of either  $R_1$  or  $R_2$


○ That is, you can check whether  $R_1 \subseteq (R_1 \cap R_2)^+$  or  $R_2 \subseteq (R_1 \cap R_2)^+$

# Desirable Properties of Decomposition

## Lossless-Join Decomposition Example


	title	year	length	type	studioName	starName
	Star Wars	1977	124	Sci-Fi	Fox	Carrie Fisher
	Star Wars	1977	124	Sci-Fi	Fox	Mark Hamill
	Braveheart	1994	280	Action	Universal	Mel Gibson
	Breakfast Club	1986	200	Comedy	Paramount	Molly Ringwal
	Breakfast Club	1986	200	Comedy	Paramount	Emilo Estavez

Record: 5 of 5



	title	year	length	type	studioName
	Star Wars	1977	124	Sci-Fi	Fox
	Braveheart	1994	280	Action	Universal
	Breakfast Club	1986	200	Comedy	Paramount

Record: 3 of 3



	title	year	starName
	Star Wars	1977	Carrie Fisher
	Star Wars	1977	Mark Hamill
	BraveHeart	1994	Mel Gibson
	Breakfast Club	1986	Molly Ringwal
	Breakfast Club	1986	Emilo Estavez

Record: 6 of 6



# Desirable Properties of Decomposition

## ○ Example of Lossy-Join Decomposition

○ Lossy-join decompositions result in information loss.

○ Example: Decomposition of  $R = (A, B, C, D)$   
 $S = (A, B)$     $T = (C, D)$

**R**

A	B	C	D
a <sub>1</sub>	b <sub>1</sub>	c <sub>1</sub>	d <sub>1</sub>
a <sub>2</sub>	b <sub>2</sub>	c <sub>2</sub>	d <sub>2</sub>
a <sub>3</sub>	b <sub>3</sub>	c <sub>3</sub>	d <sub>3</sub>

**S**

A	B
a <sub>1</sub>	b <sub>1</sub>
a <sub>2</sub>	b <sub>2</sub>
a <sub>3</sub>	b <sub>3</sub>

**T**

C	D
c <sub>1</sub>	d <sub>1</sub>
c <sub>2</sub>	d <sub>2</sub>
c <sub>3</sub>	d <sub>3</sub>

**S ⋈ T**


A	B	C	D
a <sub>1</sub>	b <sub>1</sub>	c <sub>1</sub>	d <sub>1</sub>
a <sub>1</sub>	b <sub>1</sub>	c <sub>2</sub>	d <sub>2</sub>
a <sub>1</sub>	b <sub>1</sub>	c <sub>3</sub>	d <sub>3</sub>
a <sub>2</sub>	b <sub>2</sub>	c <sub>1</sub>	d <sub>1</sub>
a <sub>2</sub>	b <sub>2</sub>	c <sub>2</sub>	d <sub>2</sub>
a <sub>2</sub>	b <sub>2</sub>	c <sub>3</sub>	d <sub>3</sub>
a <sub>3</sub>	b <sub>3</sub>	c <sub>1</sub>	d <sub>1</sub>
a <sub>3</sub>	b <sub>3</sub>	c <sub>2</sub>	d <sub>2</sub>
a <sub>3</sub>	b <sub>3</sub>	c <sub>3</sub>	d <sub>3</sub>

# Desirable Properties of Decomposition

## Lossy-Join Decomposition Example


	student	course	date-enrolled	room	instructor
▶	James	C++	12FEB	101	Coburn
	Sarah	C++	20JAN	101	Coburn
	Fred	Java	12FEB	200	Smith
	Mary	Networks	23JAN	104	Park
	James	Maths	12FEB	100	Oshea

Record: 1 of 5



	student	course	date-enrolled
	James	C++	12FEB
	James	Maths	12FEB
	Sarah	C++	20JAN
	Fred	Java	12FEB
	Mary	Networks	23JAN

Record: 3 of 5



	date-enrolled	room	instructor
	12FEB	101	Coburn
	12FEB	200	Smith
	12FEB	100	Oshea
	20JAN	101	Coburn
▶	23JAN	104	Park

Record: 5 of 5

# Desirable Properties of Decomposition

## ○ Dependency Preservation

- If we decompose a relation, then the set of functional dependencies that held on the original set
  - should also hold on the resulting relations as a whole
  - no **joins** should be needed to when testing the FD's
- Let  $F$  be the dependencies on a relation  $R$  which is decomposed in relations  $R_1, R_2, \dots, R_n$
- We have to partition the dependencies given by  $F$  to  $F_1, F_2, \dots, F_n$  such that
- $F_1, F_2, \dots, F_n$  are dependencies that only involve attributes from relations  $R_1, R_2, \dots, R_n$  respectively
- Need to ensure that  $(F_1 \cup F_2 \cup \dots \cup F_n)^+ = F^+$

# Desirable Properties of Decomposition

## ○ Dependency Preservation

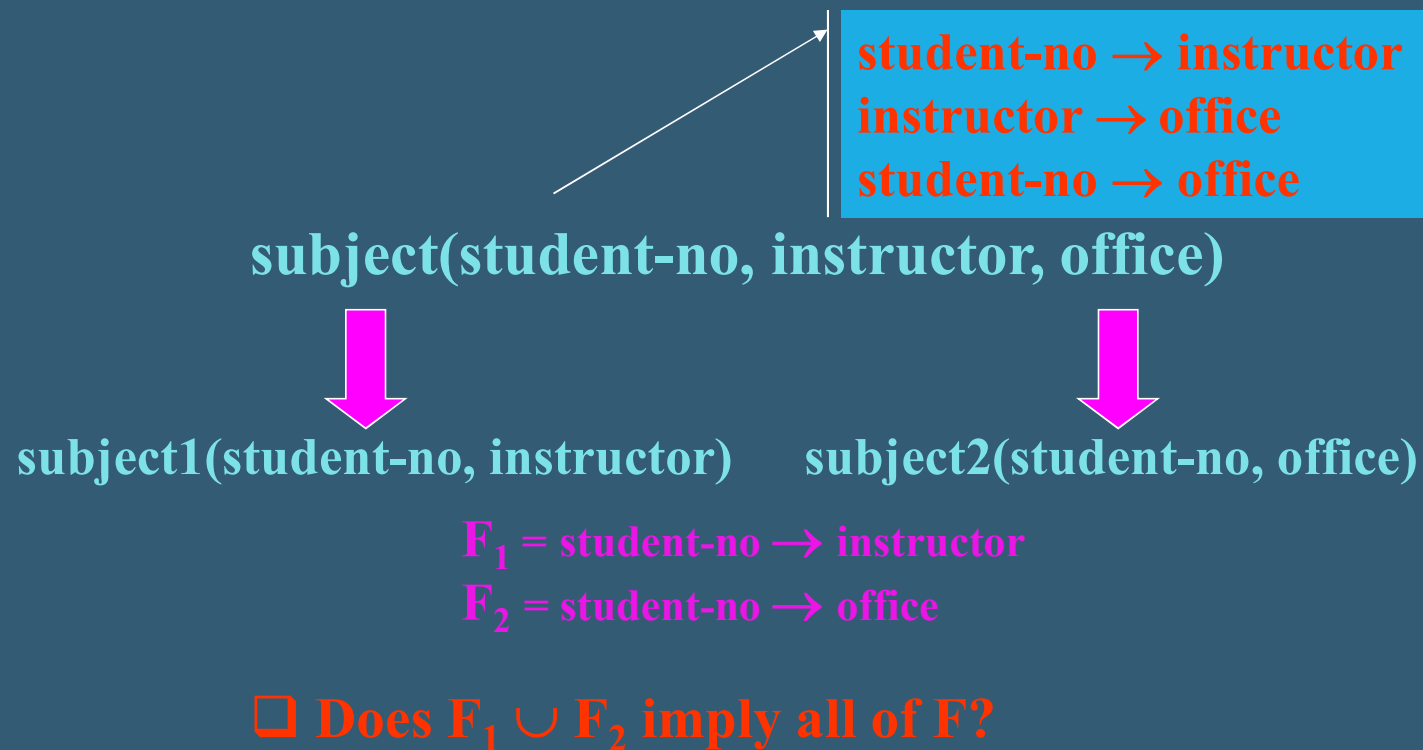
- If the union of dependencies  $F_i$  imply all the dependencies in  $F$ , then we say that the decomposition has preserved dependencies, otherwise the dependencies has not been preserved
- If dependencies not preserved then checking updates for violation of functional dependencies may require computing joins, which is expensive

## ○ Example:

$R = (A, B, C, G, H, I), F = \{A \rightarrow B, A \rightarrow C, CG \rightarrow H, G \rightarrow I, C \rightarrow H\}$

- If we decompose  $R$  to  $R_1=(A, B, C)$  and  $R_2=(G, H, I)$  then we need to decompose  $F$  to
- $F_1 = \{A \rightarrow B, A \rightarrow C\}$
- $F_2 = \{G \rightarrow I\}$
- $F_1 \cup F_2 \neq F$ , Hence, dependency not preserved

# Desirable Properties of Decomposition





# Boyce-Codd Normal Form

- A relation schema  $R$  is in **BCNF** with respect to a set  $F$  of functional dependencies if for all functional dependencies in  $F^+$  of the form  $\alpha \rightarrow \beta$ , where  $\alpha \subseteq R$  and  $\beta \subseteq R$ , at least one of the following holds:
  - $\alpha \rightarrow \beta$  is **trivial** (i.e.,  $\beta \subseteq \alpha$ )
  - $\alpha$  is a **superkey** for  $R$
- When we have a FD in the form  $\alpha \rightarrow \beta$  on a relation  $R$  that violates BCNF we will decompose the schema into several sub-schemas.
- The resulting relations themselves are not guaranteed to be in BCNF. We may need to further decompose the resulting relations

# Example

- $R = (A, B, C)$   
 $F = \{A \rightarrow B, B \rightarrow C\}$
- Check whether  $R$  is in BCNF or not?
  - No,  $R$  is not in BCNF
- Decomposition  $R_1 = (A, B), R_2 = (B, C)$
- After decomposing  $R$  to  $R_1$  and  $R_2$ , you need to check the following decomposition properties.
  - Attribute Preserving
  - Lossless-join decomposition
  - Dependency preserving
  - $R_1$  and  $R_2$  in BCNF
- If any one of the above doesn't satisfy then the decomposition is not correct. Need to decompose the schema in different way

# Testing for BCNF

- To check if a non-trivial dependency  $\alpha \rightarrow \beta$  causes a violation of BCNF
  1. compute  $\alpha^+$  (the attribute closure of  $\alpha$ ), and
  2. verify that it includes all attributes of  $R$ , that is, it is a superkey of  $R$ .
- **Simplified test:** To check if a relation schema  $R$  with a given set of functional dependencies  $F$  is in BCNF, it suffices to check only the dependencies in the given set  $F$  for violation of BCNF, rather than checking all dependencies in  $F^+$ .
  - We can show that if none of the dependencies in  $F$  causes a violation of BCNF, then none of the dependencies in  $F^+$  will cause a violation of BCNF either.

# Testing for BCNF

- However, using only  $F$  is **incorrect** when testing a relation in a decomposition of  $R$ 
  - E.g. Consider  $R(A, B, C, D)$ , with
$$F = \{ A \rightarrow B, B \rightarrow C \}$$
    - Decompose  $R$  into  $R_1(A, B)$  and  $R_2(A, C, D)$
    - $F_1 = \{ A \rightarrow B \}$ ,  $F_2 = \{ \emptyset \}$
    - Neither of the dependencies in  $F$  contain only attributes from  $(A, C, D)$  so we might be misled into thinking  $R_2$  satisfies BCNF.
    - In fact, dependency  $A \rightarrow C$  in  $F^+$  shows  $R_2$  is **not in** BCNF.



# BCNF Example

- State why the following relation is **not in BCNF** and decompose it so that the resulting tables are in BCNF

**Movie(title, year, stuidoName, president, presAdd)**

- **title, year → stuidoName**
- **stuidoName → president**
- **president → presAdd**
- **Movie1(title, year, stuidoName) , Check in BCNF? (Yes)**
- **Movie2(stuidoName, president, presAdd), Check in BCNF?(Yes)**

# BCNF and Dependency Preservation

- It is not always possible to get a BCNF decomposition that is dependency preserving
- $R = (J, K, L)$   
 $F = \{JK \rightarrow L, L \rightarrow K\}$
- $R$  is not in BCNF
- Any decomposition of  $R$  will fail to preserve

$$JK \rightarrow L$$

# Third Normal Form: Motivation

- There are some situations where
  - BCNF is not dependency preserving, and
  - efficient checking for FD violation on updates is important
- **Solution:** define a weaker normal form, called Third Normal Form.
  - Allows some redundancy (with resultant problems; we will see examples later)
  - But FDs can be checked on individual relations without computing a join.
  - There is always a lossless-join, dependency-preserving decomposition into 3NF.

# Third Normal Form(3NF)

- A relation schema  $R$  is in third normal form (3NF) if for all  $\alpha \rightarrow \beta$  in  $F^+$ , at least one of the following holds:
  - $\alpha \rightarrow \beta$  is trivial (i.e.,  $\beta \in \alpha$ )
  - $\alpha$  is a superkey for  $R$
  - **Each attribute  $A$  in  $\beta - \alpha$  is contained in a candidate key for  $R$ .** *That is,  $A$  is a member of a candidate key.*  
(NOTE: each attribute may be in a different candidate key)
- If a relation is in BCNF it is in 3NF (since in BCNF one of the first two conditions above must hold).
- Third condition is a minimal relaxation of BCNF to ensure dependency preservation (will see why later).



# Third Normal Form(3NF)

## ○ Example

○  $R = (J, K, L)$   
   $F = \{JK \rightarrow L, L \rightarrow K\}$

○ Two candidate keys:  $JK$  and  $JL$

○  $R$  is in 3NF

$JK \rightarrow L$      $JK$  is a superkey  
   $L \rightarrow K$      $K$  is contained in a candidate key of  $R$

□ BCNF decomposition has  $(JL)$  and  $(LK)$

  □ Testing for  $JK \rightarrow L$  requires a join

○ There is some redundancy in this schema

# Testing for 3NF

- **Optimization:** Need to check only FDs in  $F$ , need not check all FDs in  $F^+$ .
- Use attribute closure to check, for each dependency  $\alpha \rightarrow \beta$ , if  $\alpha$  is a superkey.
- If  $\alpha$  is not a superkey, we have to verify if each attribute in  $\beta$  is contained in a candidate key of  $R$ 
  - this test is rather more expensive, since it involve finding candidate keys

# Comparison of BCNF and 3NF

- It is always possible to decompose a relation into relations in 3NF and
  - attribute preserved
  - the decomposition is lossless
  - the dependencies are preserved
- It is always possible to decompose a relation into relations in BCNF and
  - attribute preserved
  - the decomposition is lossless
  - it may not be possible to preserve dependencies.

# Design Goals

- Goal for a relational database design is:
  - Boyce-Codd Normal Form (BCNF).
  - Lossless join.
  - Attribute preservation
  - Dependency preservation.
- If we cannot achieve this, we accept one of:
  - Lack of dependency preservation (need to perform join)
  - Redundancy due to use of 3NF



# Summary

1NF

- Get rid of any columns that hold the same data
- Split up data that can be
- Each Row must be unique

2NF

- Get rid of data not dependant on EVERY part Primary Key

3NF

- Keep Splitting it up.
- No Non-key attribute should be dependant on another non-key attribute

**Thank You for your  
Attention**