

BT 6270 : Computational Neuroscience Assignment

General Instructions:

- ✓ The goal of this assignment is simulating and Understanding FitzHugh-Nagumo neuron model taught in the class.
- ✓ This is an individual assignment.
- ✓ You may use MATLAB for your implementation.
- ✓ You have to turn in the well commented code along with a detailed report of the study.
- ✓ Your report should contain answers for all of the questions/cases asked below.

Simulate the two variable FitzHugh-Nagumo neuron model using the following equations :

$$\frac{dv}{dt} = f(v) - w + I_m$$

where $f(v) = v(a - v)(v - 1)$

$$\frac{dw}{dt} = bv - rw$$

where $a=0.5$; choose b, r values as discussed in the class (small positive values, say 0.1)

Use single forward Euler Integration

$$dv/dt = \Delta v / \Delta t$$

$$\Delta v(t) = v(t+1) - v(t) = [f(v(t)) - w(t) + I_{\text{ext}}(t)] * \Delta t \text{ given } v(0) \rightarrow v(\Delta t) \rightarrow v(2 * \Delta t) \rightarrow \dots$$

Case 1: $I_{\text{ext}} = 0$

(a) Draw a Phase Plot superimposed (use hold on command in MATLAB)

(b) Plot $V(t)$ vs t and $W(t)$ vs t and also show the trajectory on the phase plane for the both cases

(i) $V(0) < a$ and $w(0) = 0$

(ii) $V(0) > a$ and $w(0) = 0$

Case 2: Choose some current value $I_1 < I_{\text{ext}} < I_2$ where it exhibit oscillations. Find the values of I_1 and I_2 .

(a) Draw a Phase Plot for some sample value of I_{ext}

(b) Show that the fixed point is unstable i.e., for a small perturbation there is a no return to the fixed point (show the trajectory on the phase plane) – also show limit cycle on the phase plane

(c) Plot $V(t)$ vs t and $W(t)$ vs t

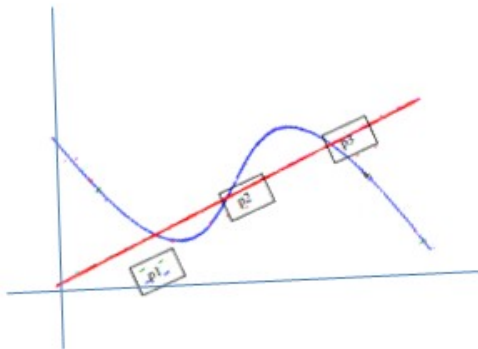
Case 3: Choose some $I_{\text{ext}} > I_2$

(a) Draw a Phase Plot for some sample value of I_{ext}

(b) Show that the fixed point is stable i.e., for a small perturbation there is a return to the fixed point (show the trajectory on the phase plane)

(c) Plot $V(t)$ vs t and $W(t)$ vs t

Case 4: Fine suitable values of I_{ext} and (b/r) such that the graph looks as phase plot shown as below.



(a) Redraw the Phase plot

(b) Show suitability of P1, P2, P3

(c) Plot $V(t)$ vs t and $W(t)$ vs t