

Exercise V-2

Given:

Linear elastic isotropic material $E = 2 \cdot 10^5 \text{ N/mm}^2$
One principal stress is given: 8 N/mm^2

Questions:

- Find the other principal (eigen) stresses
- Find the eigen-directions and plot these in a graph.

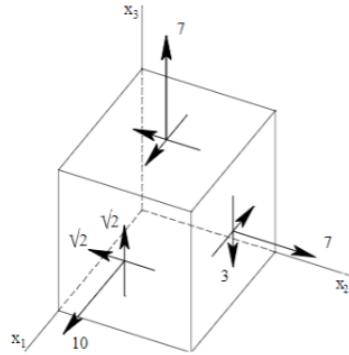
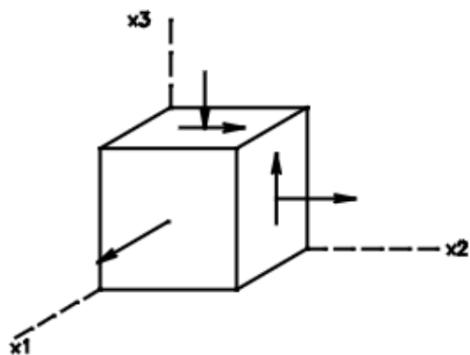


Figure 1: Stress matrix

Exercise V.3



Given: a stress-state: $\begin{bmatrix} 60 & 0 & 0 \\ 0 & 20 & 20 \\ 0 & 20\sqrt{3} & -20 \end{bmatrix}$ $E = 2 \cdot 10^5$ $v = 0.25$

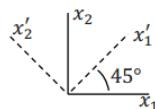
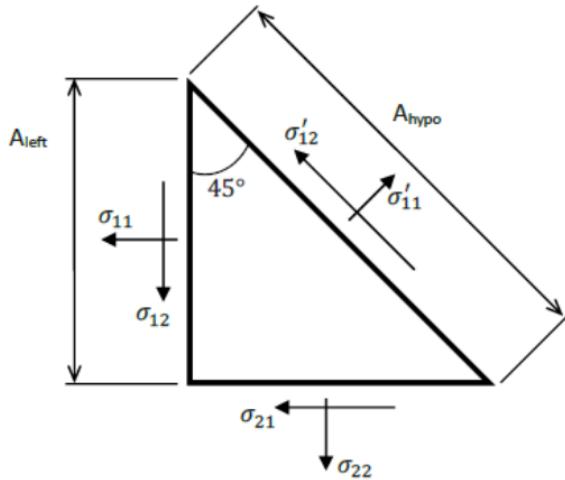
- a) Compute the principal stresses
- b) Compute the eigen-directions
- c) Compute the maximal shear-stress

Exercise V.10

Problem:

Given:

- In a point P of a body we have a plane-stress state with: $\sigma_{13} = \sigma_{23} = \sigma_{33} = 0$
- Given are these (mixed) stress components:
 $\sigma_{11} = 92 \text{ MPa}$
 $\sigma'_{11} = 194 \text{ MPa}$
 $\sigma'_{12} = -42 \text{ MPa}$
- The material is linear elastic with:
 $E = 2 \cdot 10^5 \text{ MPa}$
 $v = 0.25$



Questions:

- Give the stress tensor in the original $x_1x_2x_3$ system.
- Give the stress tensor in the new $x'_1x'_2x'_3$ coordinate system, as obtained by a rotation of the coordinates about 45° around the x_3 -axis, as sketched above.
- Compute the eigen-stresses and the eigen-directions.
- Give the strain tensor in the $x'_1x'_2x'_3$ coordinate system.