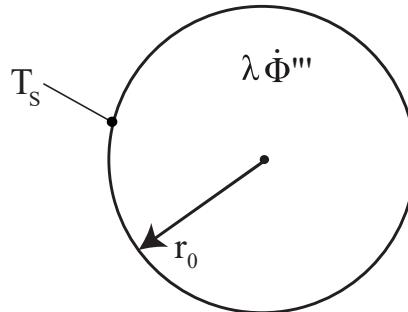


1.10 Resistance wire

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A long homogeneous resistance wire is being used to heat the air in a room by the passage of electric current. Heat is generated in the wire uniformly at a constant rate $\dot{\Phi}'''$ as a result of resistance heating. Assume the problem to be one-dimensional steady-state heat transfer in radial direction.



Tasks:

- Derive the heat conduction equation by setting up an energy balance.
- Determine the temperature at $r = 3.5$ mm after steady operation conditions are reached.

Hints

- Radiation can be neglected.

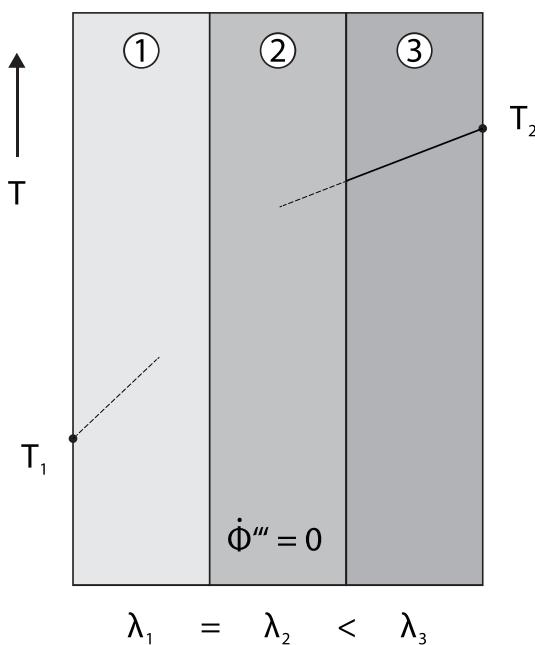
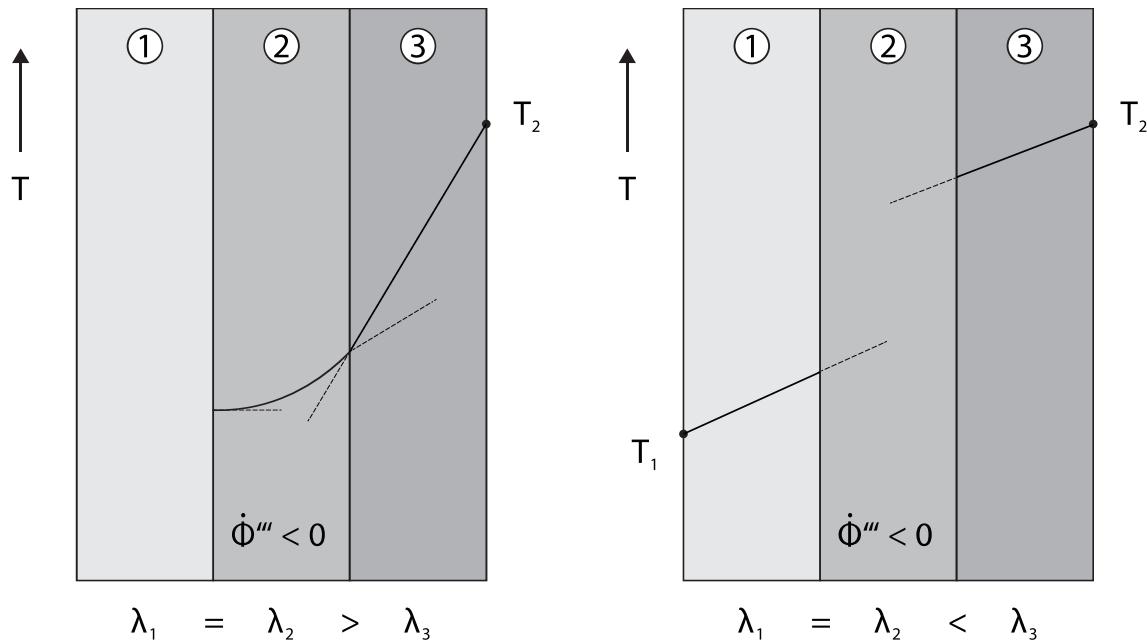
Given parameter

- Outer radius of the wire: $r_0 = 5$ mm
- Heat generation in the wire: $\dot{\Phi}''' = 5 \cdot 10^7$ W/m³
- Temperature of the outer surface of the wire: $T_s = 180$ °C
- Thermal conductivity of the wire: $\lambda = 6$ W/mK

1.11 Draw temperature profiles

★★

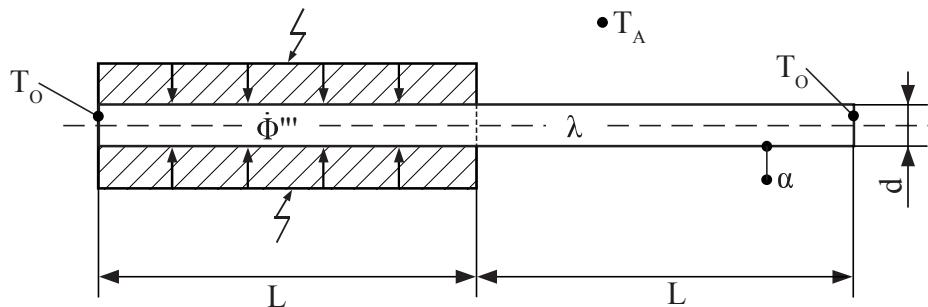
Complete the temperature profiles in the three-layered walls, shown below. Consider the information given in each drawing.



1.12 Copper rod

★ ★ ★

Both ends of a copper rod with a length L and a diameter d are kept at the same temperature T_O . The left half of the rod is insulated against all radial heat losses. An electric heating element generates Joule's heat of heat flux density $\dot{\Phi}'''$. The right half of the rod is subjected to a flow of the ambient air with an air temperature of T_A , yielding a heat transfer coefficient α . The thermal conductivity of the rod is given as λ .



Tasks:

- Derive the equation for the temperature profile in the rod by setting up an energy balance.
- Determine the value of $\dot{\Phi}'''$ so that the temperature in the center of the rod equals the temperature T_O at its ends.
- Calculate $\dot{\Phi}'''$ using the following data: $L = 1 \text{ m}$; $d = 5.2 \text{ mm}$; $T_O = 120^\circ\text{C}$; $T_A = 100^\circ\text{C}$; $\alpha = 6 \text{ W/m}^2\text{K}$; $\lambda = 372 \text{ W/m K}$ for the conditions postulated in b).
- Determine the extremes of the temperature distribution for the given values. Give their position and values, additionally, sketch the temperature profile.

Hint:

- Place the origin of the coordinate system in the middle of the rod.