

W3-8-1 Exact differential 1

Consider $dq = \left(\frac{RT}{P}\right) dp - RdT$
Is this an exact differential?

$$dq = \left(\frac{RT}{P}\right) dP - RdT$$

$$\left(\frac{\partial}{\partial T}\left(\frac{RT}{P}\right)\right)_P = \frac{R}{P} \quad \text{and} \quad \left(\frac{\partial}{\partial P}(-R)P\right)_T = -R$$

The combined differentials are not equal, so dq is not an exact differential.