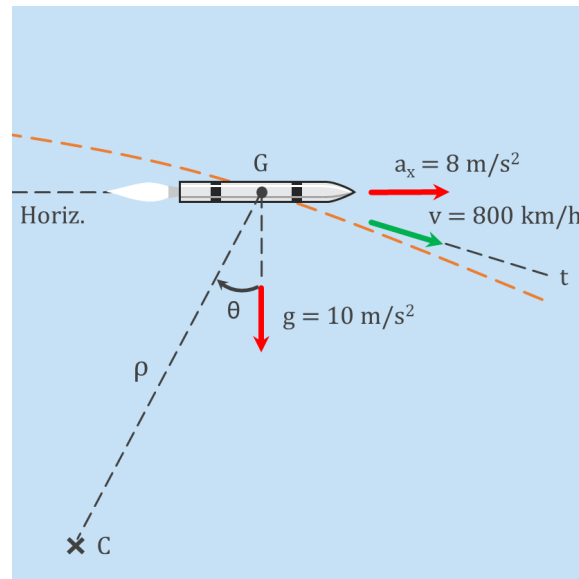
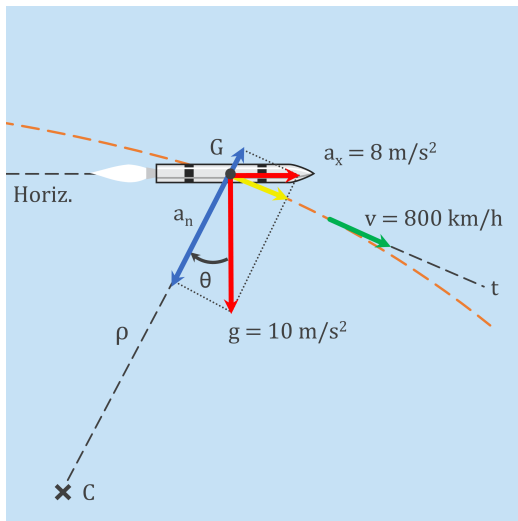


## Rocket Accelerates



A rocket maintains at horizontal attitude of its axis during the powered phase of its flight. The acceleration due to horizontal thrust is  $8 \text{ m/s}^2$ , and the downward acceleration due to gravity is  $g = 10 \text{ m/s}^2$ . At the instant represented, the velocity of the mass centre G of the rocket along the  $\theta = 15^\circ$  direction of its trajectory is  $800 \text{ km/h}$ . Determine for this position the rate at which the velocity is increasing. Round to the nearest integer.



The rate at which the velocity increases is the tangential acceleration. The tangential acceleration  $a_t$  is parallel to  $v$ . Figure 1 shows the acceleration vectors  $a_x$  and  $g$  deconstructed in the normal direction (blue) and the tangential direction (yellow). It can be easily seen that  $g$  and  $a_x$  deconstructed in the tangential-direction are equal to  $g \cdot \sin(\theta)$  and  $a_x \cdot \cos(\theta)$  respectively. Resulting in the final answer:

$$a_t = g \cdot \sin(\theta) + a_x \cdot \cos(\theta) \quad (1)$$

Figure 1: Rocket Accelerates

*Given:*

Angle:  $\theta = 15^\circ$

Gravitational acceleration:  $g = 10m/s^2$

Horizontal acceleration:  $a_x = 8m/s^2$

Velocity:  $v = 800km/h = 222.22m/s$

Inserting  $\theta$ ,  $g$  and  $a_x$  into Equation 1 results in:

$$a_t = g \cdot \sin(\theta) + a_x \cdot \cos(\theta) \quad \Rightarrow \quad a_t = 10 \cdot \sin(15) + 8 \cdot \cos(15) = 10m/s^2 \quad (2)$$