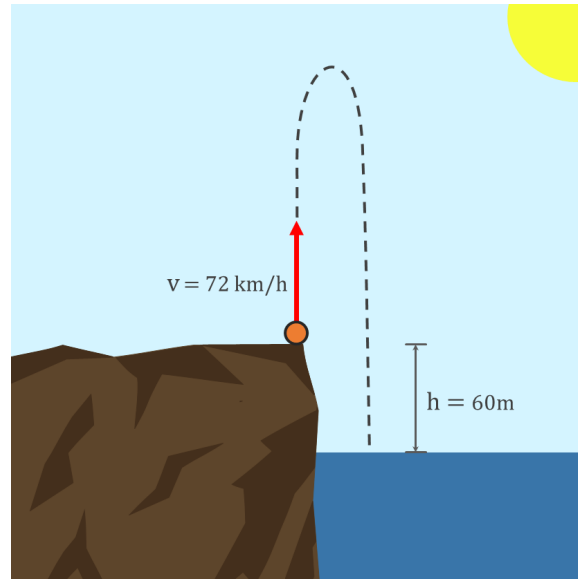


Ball Thrown from Cliff



A ball is thrown vertically up with a velocity of 72 km/h at the edge of a 60 meter high cliff. What is the maximum height the ball reaches with respect to the cliff? Neglect air resistance and take $g = 10 \text{ m/s}^2$.

Using known expressions:

$$a = \frac{dv}{dt} \Rightarrow dv = a dt \quad (1)$$

$$\int_{v_0}^v dv = a \int_0^t dt \quad (2)$$

$$v(t) = a \cdot t + v_0 \quad (3)$$

$$v = \frac{ds}{dt} \Rightarrow ds = v dt = (a \cdot t + v_0) dt \quad (4)$$

$$\int_{s_0}^s ds = \int_0^t (a \cdot t + v_0) dt \quad (5)$$

$$s(t) = \frac{1}{2} a \cdot t^2 + v_0 \cdot t + s_0 \quad (6)$$

For the vertical displacement in y-direction, this results in:

$$y(t) = \frac{1}{2} a_y \cdot t^2 + v_{y,0} \cdot t + s_{y,0} \quad (7)$$

Given:

Initial velocity in y-direction: $v_{y,0} = 72\text{km/h} = 20\text{m/s}$

Initial height of the ball (with respect to the cliff): $H_0 = s_{y,0} = 0\text{m}$

Gravitational constant: $g = 10\text{m/s}^2$

At the instant the ball reaches its maximum height its velocity is zero. The acceleration on the ball is the gravitational acceleration: $a_y = -g$. Combining this into Equation 3 yields an equation for the time until the ball reaches its maximum point:

$$v_y(t) = a_y \cdot t + v_{y,0} \quad \Rightarrow \quad 0 = -g \cdot t + v_{y,0} \quad (8)$$

Rewriting gives:

$$t = \frac{-v_{y,0}}{-g} = \frac{20}{10} = 2\text{s} \quad (9)$$

Inserting $t = 2\text{s}$ into Equation 7 yields:

$$H_{\max} = y(2) = -\frac{1}{2} \cdot 10 \cdot 2^2 + 20 \cdot 2 = 20\text{m} \quad (10)$$