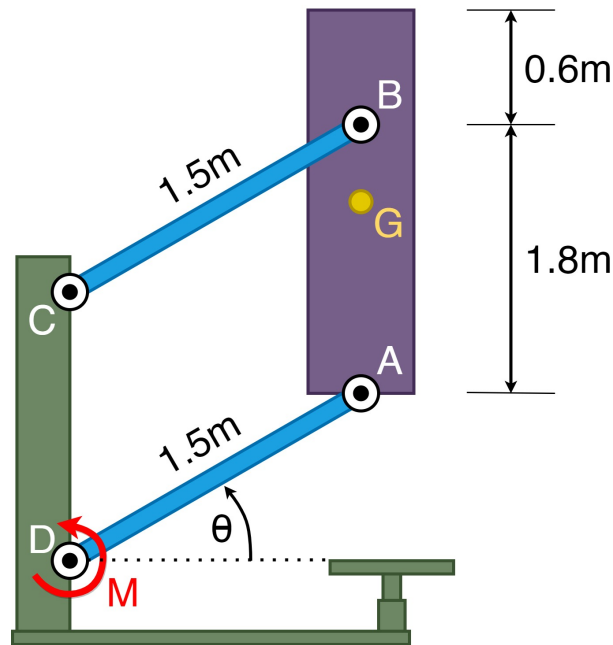


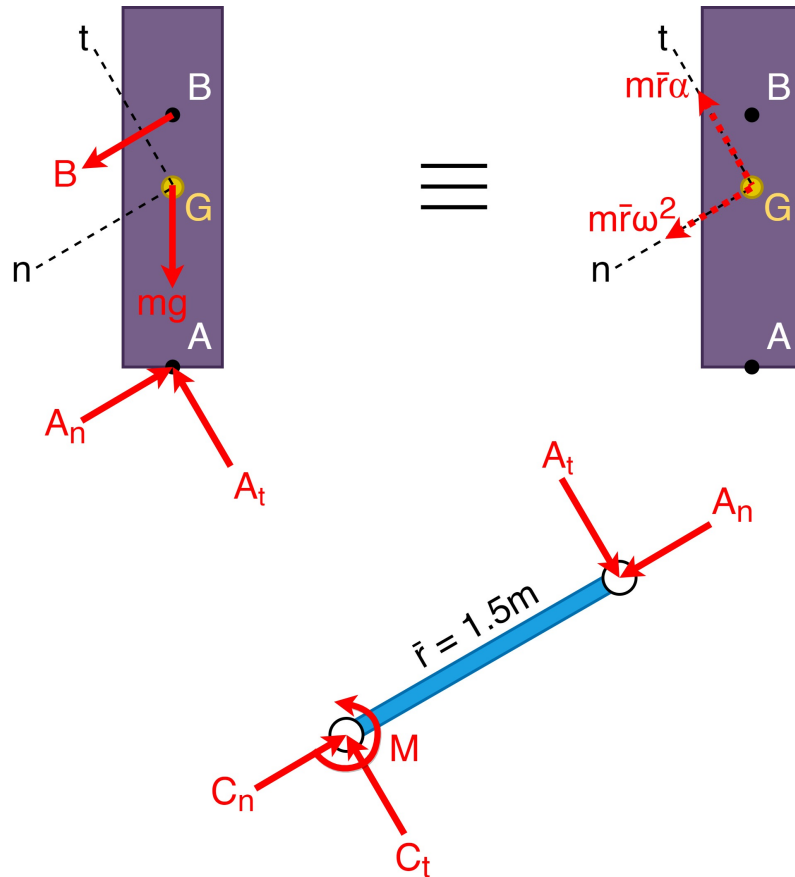
Curvilinear translation of a bar (b)



The vertical bar AB has a mass of 150 kg with the centre of mass G midway between the ends. The bar is elevated from rest at $\theta = 0^\circ$ by means of the parallel links of negligible mass, with a constant couple $M = 5 \text{ kNm}$ applied to the lower link at C.

Determine the angular velocity ω of the links when $\theta = 30^\circ$.

Make the reference axes coincide with the directions in which the components of the mass-centre acceleration are expressed!



The motion of the bar is seen to be curvilinear translation since the bar itself does not rotate during the motion. With the circular motion of the mass centre G, we choose n- and t-coordinates as the most convenient description. With a negligible mass of the links, the tangential component A_t of the force at A is obtained from the free-body diagram of AC, where $\sum M_c \approx 0$ and $A_t = M/AC = 5/1.5 = 3.33$ kN (The force and moment equations for a body of negligible mass become the same as the equations of equilibrium!). The force at B is along the link. All applied forces are shown on the free-body diagram of the bar, and the kinetic diagram is also indicated, where the $m\bar{a}$ resultant is shown in terms of its two components.

$$[\sum F_t = m\bar{a}_t] \quad 3.33 - 0.15(9.81) \cos\theta = 0.15(1.5\alpha)$$

$$\alpha = 14.81 - 6.54 \cos\theta \text{ rad/s}^2$$

With α a known function of θ , the angular velocity ω of the links is obtained from

$$[\omega \, d\omega = \alpha \, d\theta] \quad \int_0^\omega \omega \, d\omega = \int_0^\theta (14.81 - 6.54 \cdot \cos \theta) \, d\theta$$

$$\omega^2 = 29.6 \cdot \theta - 13.08 \cdot \sin \theta$$

Substitution of $\theta = 30^\circ$ gives

$$(\omega^2)_{30^\circ} = 8.97 \text{ (rad/s)}^2 \quad \alpha_{30^\circ} = 9.15 \text{ rad/s}^2$$