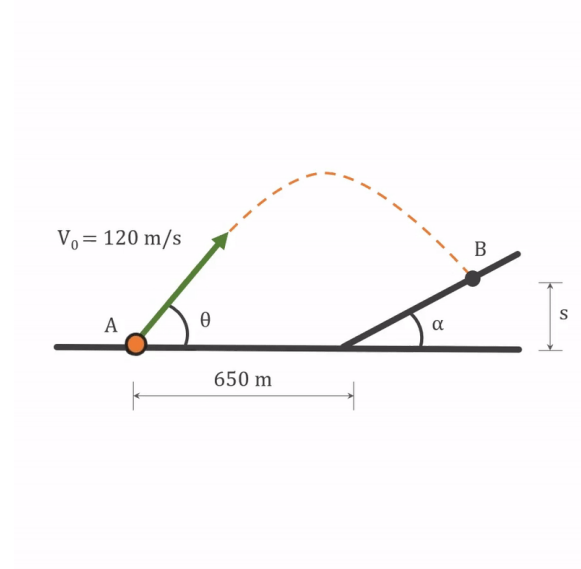


Trajectory of Ball



A ball is launched from point A with the initial conditions shown. Find an expression for the horizontal displacement $x(t)$.

Neglect all air resistances.

Using known expressions (for constant acceleration):

$$a = \frac{dv}{dt} \Rightarrow dv = a dt \quad (1)$$

$$\int_{v_0}^{v(t)} dv = a \int_0^t dt \quad (2)$$

$$v(t) = at + v_0 \quad (3)$$

$$v = \frac{ds}{dt} \Rightarrow ds = v dt = (at + v_0) dt \quad (4)$$

$$\int_{s_0}^{s(t)} ds = \int_0^t (at + v_0) dt \quad (5)$$

$$s(t) = \frac{1}{2} at^2 + v_0 t + s_0 \quad (6)$$

Solution:

For the horizontal displacement in x -direction, equation (6) results in:

$$x(t) = \frac{1}{2}a_x t^2 + v_{x,0}t + s_{x,0} \quad (7)$$

Since $a_x = 0 \text{ m/s}^2$ and $s_{x,0} = 0 \text{ m}$, the resulting equation reduces to:

$$x(t) = v_{x,0}t \quad (8)$$

Where $v_{x,0} = v_0 \cos \theta$. Substituting for $s_{x,0}$ gives the final expression:

$$x(t) = v_0 t \cos \theta \quad (9)$$