

Derive an expression for the Joule-Thomson coefficient of a gas if the state equation of the gas is $(P + a)(v - b) = RT$.

General expression Joule Thomson coefficient: $\mu_{JT} = \frac{v(T\beta - 1)}{c_P}$

$$(P + a)(v - b) = RT \rightarrow v = \frac{RT}{P + a} + b \rightarrow \frac{R}{P + a} = \frac{v - b}{T}$$

$$\beta = \frac{1}{v} \left(\frac{\partial v}{\partial T} \right)_P = \frac{1}{v} \left(\frac{R}{P + a} \right) = \frac{1}{v} \left(\frac{v - b}{T} \right)$$

$$\mu_{JT} = \frac{v(T\beta - 1)}{c_P} = \frac{v \left(T \frac{1}{v} \left(\frac{v - b}{T} \right) - 1 \right)}{c_P} = \frac{(v - b - v)}{c_P} = \frac{b}{c_P}$$