

Energy & Heat Transfer



Lecture 3

By: Mohammad Mehrali

RECAP OF LECTURE 2

- **Efficiency** $\eta = \frac{\text{useful work}}{\text{inputted energy}} = \frac{\text{useful power}}{\text{inputted power}}$

Energy is always conserved!

- **Temperature Difference is the driving force for the transfer of heat**
- **Heat transfer rate:** \dot{Q} (W) ; **Heat flux:** $\dot{q} = \dot{Q} / A$ (W/m²)

RECAP OF LECTURE 2

- Conduction
- Fourier conduction equation for different geometries

– Plane surface: $\dot{Q} = -k A \frac{T_2 - T_1}{x_2 - x_1} = \frac{T_1 - T_2}{R}$ with $R = \frac{\Delta x}{kA}$ ($\frac{K}{W}$)

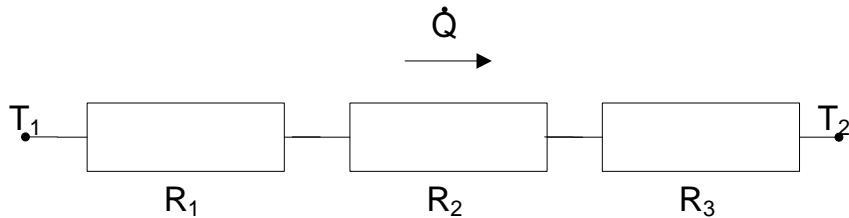
– Cylindrical tube: $\dot{Q} = \frac{T_1 - T_2}{R}$ with $R = \frac{\ln(\frac{D_2}{D_1})}{2\pi L k}$

– Spherical shell: $\dot{Q} = \frac{T_1 - T_2}{R}$ with $R = \frac{D_2 - D_1}{2\pi k D_1 D_2}$

- Building resistance networks

RECAP OF LECTURE 2

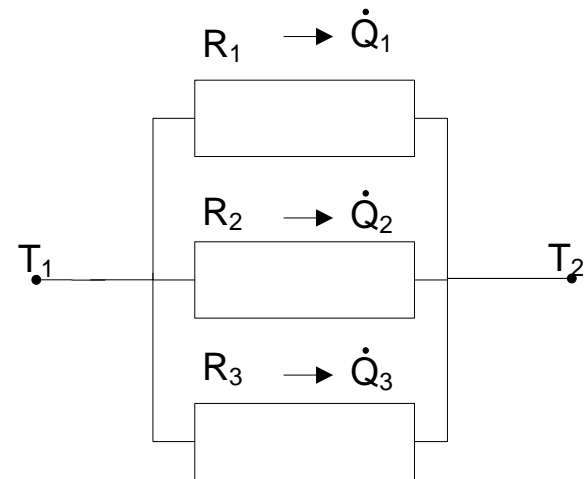
Series Resistors



$$R_{tot} = \sum_i R_i$$

(Add Resistors)

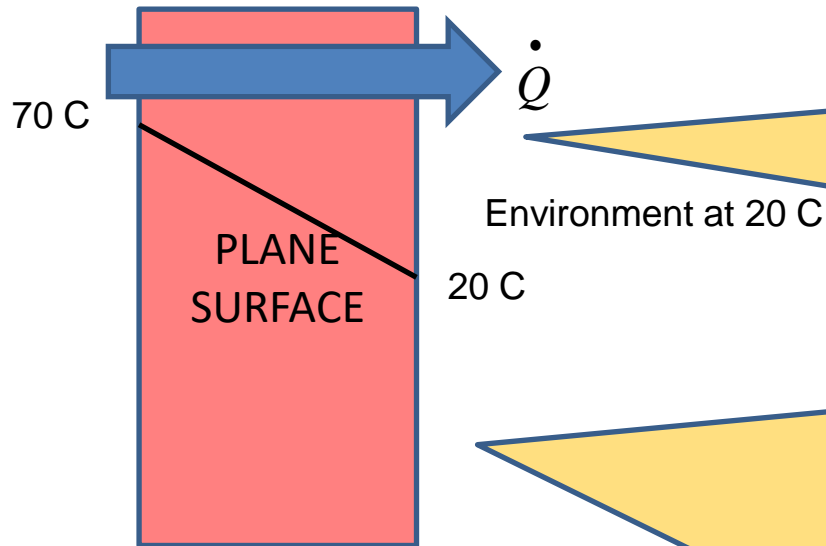
Parallel Resistors



$$\frac{1}{R_{tot}} = \sum_i \frac{1}{R_i}$$

(Add Heat Flows)

WHY HEAT TRANSFER



Engineers are interested to know the rate at which heat was transferred. In other words, Rate of Heat transfer \dot{Q} is of importance in engineering applications.

\dot{Q}
Depends on mode of heat transfer and various factors.

In the case of conduction

\dot{Q}

Depends on

- 1> Temperature Difference
- 2> Thermal conductivity of the object
- 3> Surface area
- 4> Thickness of the object

$$\dot{Q} = -k A \frac{T_2 - T_1}{x_2 - x_1} = \frac{T_1 - T_2}{R} \quad \text{with} \quad R = \frac{\Delta x}{kA} \quad \left(\frac{\text{K}}{\text{W}}\right)$$

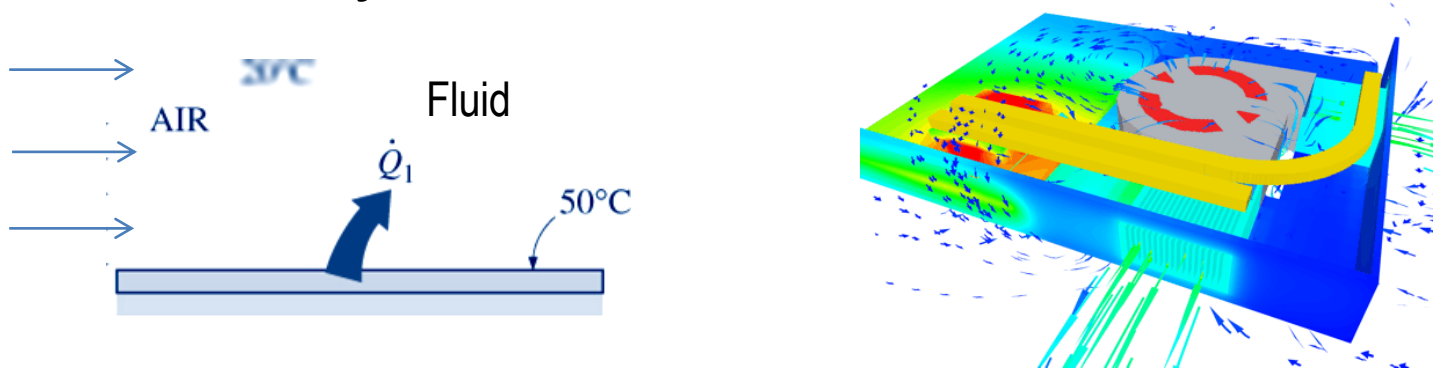
LEARNING OBJECTIVES LECTURE 3

- **Defining Convective Heat Transfer**
- Convective Heat Transfer Types
- Heat Transfer Rate in Convection
 - Newton's Law
 - Convection Resistance
 - Nusselt Number
- Forced Convection
 - Flow Parameters
 - Convective Heat Transfer Coefficient
 - Laminar and Turbulent Flow
 - Using additional correlations for various configurations
- Step-by-step plan for convection calculations

CONVECTIVE HEAT TRANSFER

Convection:

Is the mode of energy transfer between a **solid surface** and the **adjacent liquid or gas (Fluid)** that is in motion, and it involves the combined effects of *conduction and fluid motion*.

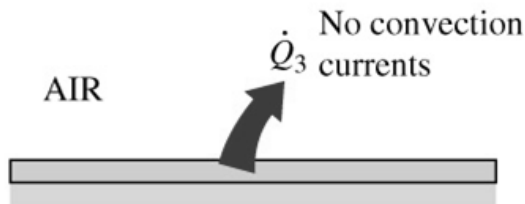


Convection and conduction are similar in that both mechanisms require the presence of a material medium.

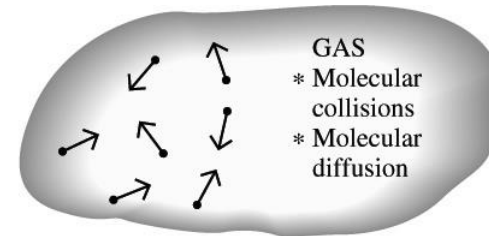
Flowing Fluid removes heat from the hot surface
Fluid: flowable medium (gas / liquid)

CONVECTIVE HEAT TRANSFER

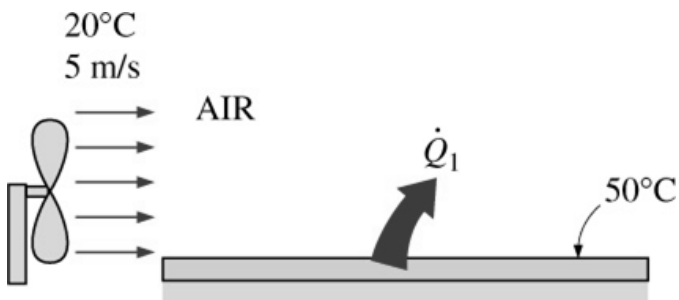
Conduction: heat transfer between molecules
(“bulk speed” equals zero)



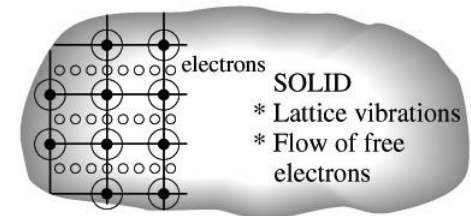
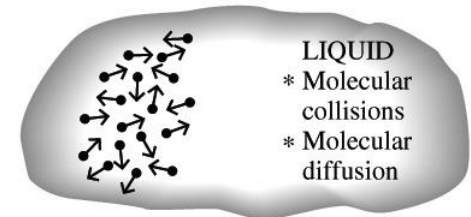
- Stationary air conducts heat away from the surface.



Convection:



- Flowing air removes more heat
- Conduction still exists, supply “fresh” molecules and discharge “heated” ones accelerates process



Fluid: flowable medium (gas / liquid)

LEARNING OBJECTIVES LECTURE 3

● Defining Convective Heat Transfer

● **Convective Heat Transfer Types**

○ Heat Transfer Rate in Convection

○ Newton's Law

○ Convection Resistance

○ Nusselt Number

○ Forced Convection

○ Flow Parameters

○ Convective Heat Transfer Coefficient

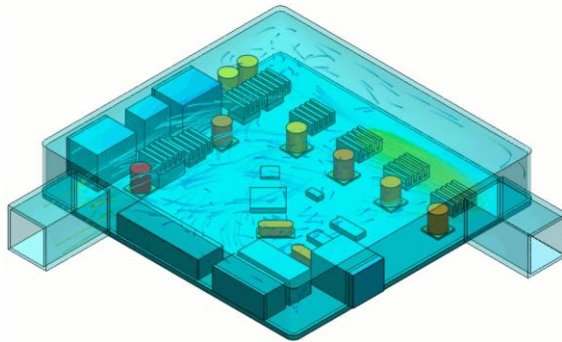
○ Laminar and Turbulent Flow

○ Using additional correlations for various configurations

○ Step-by-step plan for convection calculations

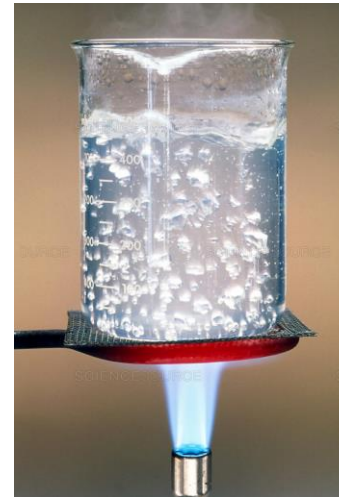
Convective heat transfer types

Forced convection



Imposed flow (by pump, fan, ...)

Natural/free convection



Temperature difference itself starts the flow

General: flow velocity and heat transfer rates are larger for forced convection

Convective heat transfer types



Fluid Viscosity

Fluid Density

Flow Regime

Flow Velocity

Flow Geometry

Roughness of the solid surface

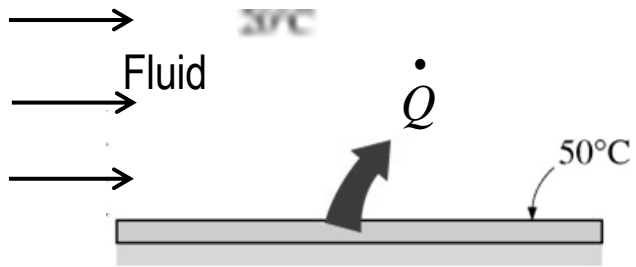
Thermal conductivity

Specific heat (C_p)

LEARNING OBJECTIVES LECTURE 3

- Defining Convective Heat Transfer
- Convective Heat Transfer Types
- **Heat Transfer Rate in Convection**
 - **Newton's Law**
 - Convection Resistance
 - Nusselt Number
- Forced Convection
 - Flow Parameters
 - Convective Heat Transfer Coefficient
 - Laminar and Turbulent Flow
 - Using additional correlations for various configurations
- Step-by-step plan for convection calculations

HEAT TRANSFER RATE IN CONVECTION



Newton's Law:

$$\dot{Q} = h \cdot A \cdot \Delta T (W)$$

In the case of Convection

\dot{Q}

Depends on :

- 1) Temperature Difference
- 2) convection heat transfer coefficient
- 3) Surface area of the object

h is the “convection heat transfer coefficient” which basically takes care of various effects of fluid properties and flow properties

Unit: $\frac{W}{m^2 \cdot K}$

LEARNING OBJECTIVES LECTURE 3

- Defining Convective Heat Transfer
- Convective Heat Transfer Types
- **Heat Transfer Rate in Convection**
 - Newton's Law
 - **Convection Resistance**
 - Nusselt Number
- Forced Convection
 - Flow Parameters
 - Convective Heat Transfer Coefficient
 - Laminar and Turbulent Flow
 - Using additional correlations for various configurations
- Step-by-step plan for convection calculations

CONVECTION REISTANCE

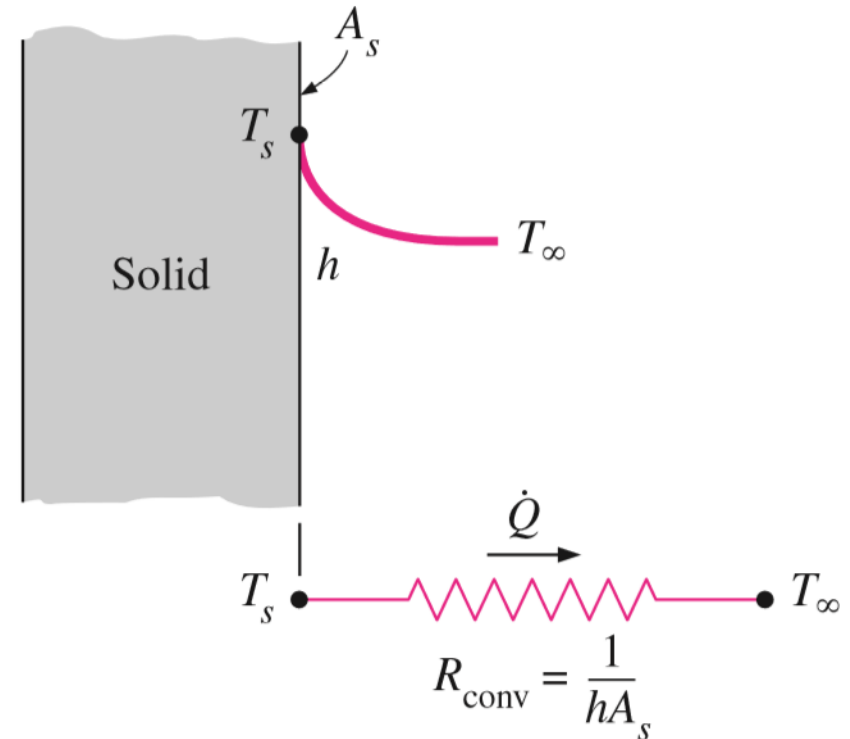
$$\dot{Q} = hA\Delta T = \frac{\Delta T}{\frac{1}{hA}} \text{ with } \Delta T = T_s - T_\infty$$

$$\Rightarrow \dot{Q} = \frac{\Delta T}{R_{conv}}$$

Where **convection resistance**:

$$R_{conv} = \frac{1}{hA} \left(\frac{\text{K}}{\text{W}} \right)$$

Remember $R_{Cond, plane} = \frac{\Delta x}{kA} \left(\frac{\text{K}}{\text{W}} \right)$



Example : The heat loss through windows

Given :

Area : 0.8m-high and 1.5m-wide

Thermal conductivity of Glass: $k = 0.78 \text{ W/m} \cdot ^\circ\text{C}$

The room temperature: 20°C

The temperature of the outdoor: -10°C

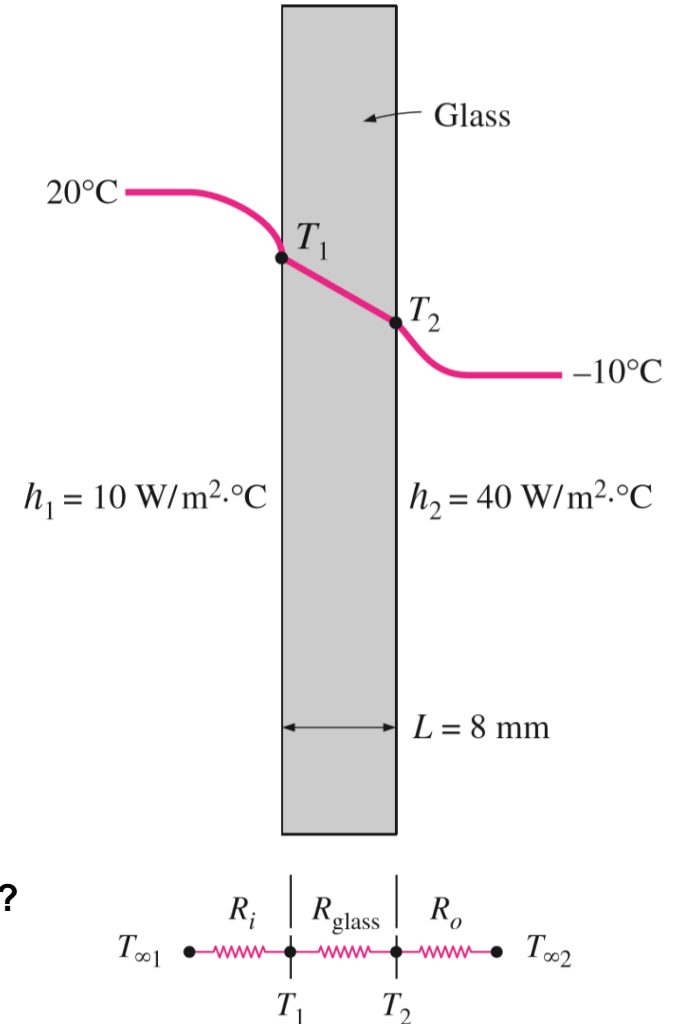
Convection heat transfer coefficient (Inside): $h_1 = 10 \text{ W/m}^2 \cdot ^\circ\text{C}$

Convection heat transfer coefficient (outside): $h_2 = 40 \text{ W/m}^2 \cdot ^\circ\text{C}$

Asked:

Determine the heat loss?

Determine the inner surface temperature of the window glass (T_1)?



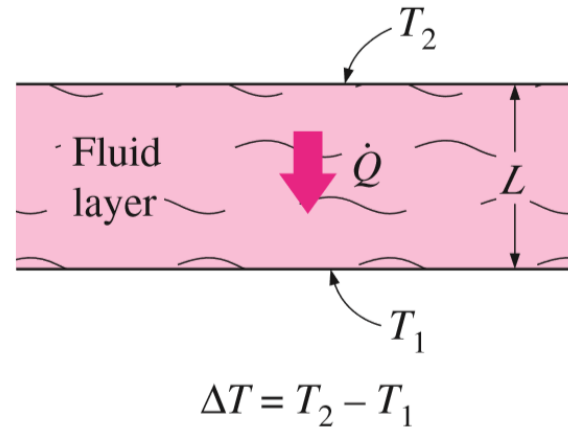
LEARNING OBJECTIVES LECTURE 3

- Defining Convective Heat Transfer
- Convective Heat Transfer Types
- **Heat Transfer Rate in Convection**
 - Newton's Law
 - Convection Resistance
 - **Nusselt Number**
- Forced Convection
 - Flow Parameters
 - Convective Heat Transfer Coefficient
 - Laminar and Turbulent Flow
 - Using additional correlations for various configurations
- Step-by-step plan for convection calculations

NUSSELT NUMBER

$$\dot{q}_{\text{conv}} = h\Delta T$$

$$\dot{q}_{\text{cond}} = k \frac{\Delta T}{L}$$



Taking their ratio gives

$$\frac{\dot{q}_{\text{conv}}}{\dot{q}_{\text{cond}}} = \frac{h\Delta T}{k\Delta T/L} = \frac{hL}{k} = \text{Nu}$$

- The larger the Nusselt number, the more effective the convection.
- A Nusselt number of $\text{Nu}=1$ for a fluid layer represents heat transfer across the layer by pure conduction.

LEARNING OBJECTIVES LECTURE 3

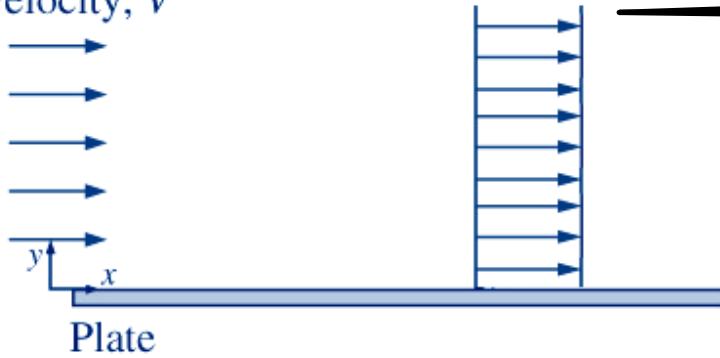
- Defining Convective Heat Transfer
- Convective Heat Transfer Types
- **Heat Transfer Rate in Convection**
 - Newton's Law
 - Convection Resistance
 - Nusselt Number
- **Forced Convection**
 - **Flow Parameters**
 - Convective Heat Transfer Coefficient
 - Laminar and Turbulent Flow
 - Using additional correlations for various configurations
- Step-by-step plan for convection calculations

FLOW PARAMETERS

First consider forced convection over a flat plate (2D)

External Flow

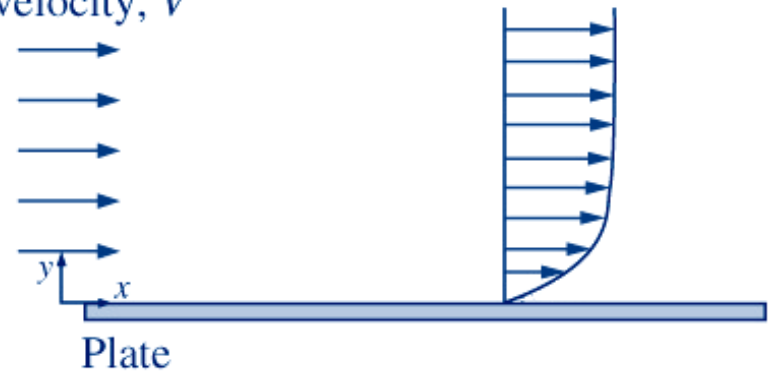
Uniform
approach
velocity, V



Idealized (non physical)

Velocity profile

Uniform
approach
velocity, V



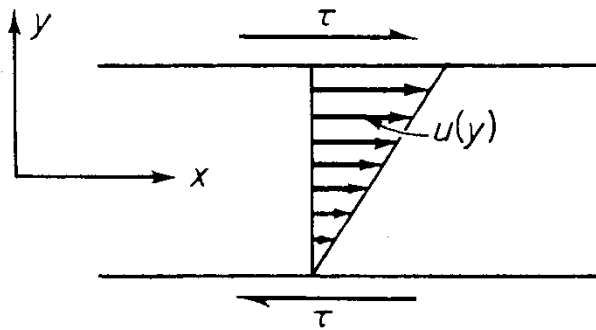
Reality

FLOW PARAMETERS

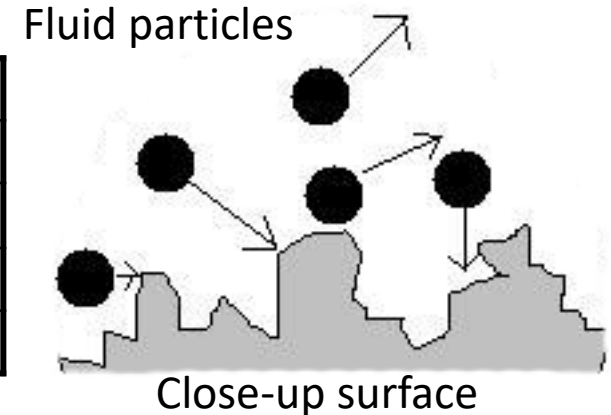
Why the velocity profile is not uniform ?

- **No slip condition** (velocity zero at surface)
- **Viscosity**

Viscosity μ : “stickiness”, resistance to deformation (shear)



	μ (Pa·s)
Oil	0.10 - 0.86
Water	0.0010
Air	0.000018
Peanut butter	150 – 250



On small scale all surfaces are rough
→ fluid doesn't flow there

LEARNING OBJECTIVES LECTURE 3

- Defining Convective Heat Transfer
- Convective Heat Transfer Types
- **Heat Transfer Rate in Convection**
 - Newton's Law
 - Convection Resistance
 - Nusselt Number
- Forced Convection
 - Flow Parameters
 - **Convective Heat Transfer Coefficient**
 - Laminar and Turbulent Flow
 - Using additional correlations for various configurations
- Step-by-step plan for convection calculations

Convective Heat Transfer Coefficient

h is complexly related to fluid properties and fluid flow parameters. Experiments, formulations and research have lead to grouping these parameters as follows as. **This is particularly for the case of forced convection:**

$$\frac{hL}{k} = a \left(\frac{\rho UL}{\mu} \right)^b \left(\frac{\mu c_p}{k} \right)^c$$

With a, b, c constants dependent on **geometry** and **flow type**

Proof follows from laws of conservation of mass, momentum and energy

$$Nu = a \cdot Re^b \cdot Pr^c$$

Nusselt Number : $Nu = \frac{hL}{k}$

Reynolds number: $Re = \frac{\rho U L}{\mu}$

Prandtl number: $Pr = \frac{\mu c_p}{k}$

Parameters:

Flow velocity : U (m/s)

Thermal conductivity : k (W/m.k)

Density : ρ (kg/m³)

Distance from leading edge/length: x, L (m)

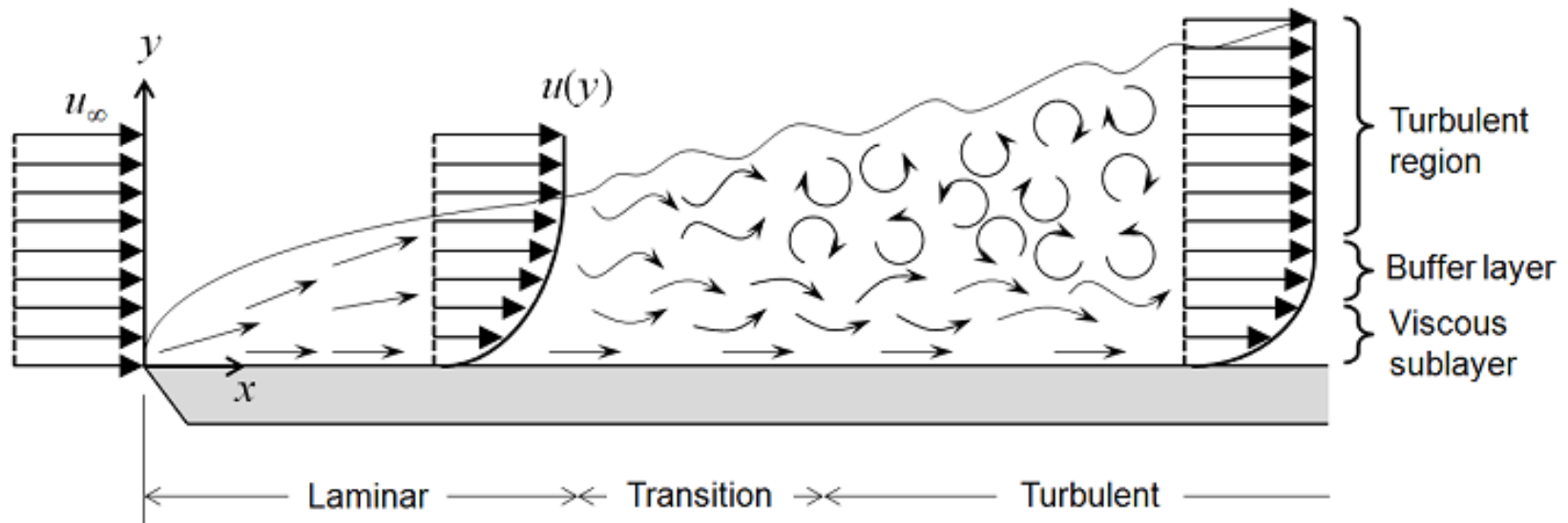
Dynamic viscosity : μ (N · s/m²)

Specific heat capacity : C_p (J/kg · K)

LEARNING OBJECTIVES LECTURE 3

- Defining Convective Heat Transfer
- Convective Heat Transfer Types
- **Heat Transfer Rate in Convection**
 - Newton's Law
 - Convection Resistance
 - Nusselt Number
- Forced Convection
 - Flow Parameters
 - Convective Heat Transfer Coefficient
 - **Laminar and Turbulent Flow**
 - Using additional correlations for various configurations
- Step-by-step plan for convection calculations

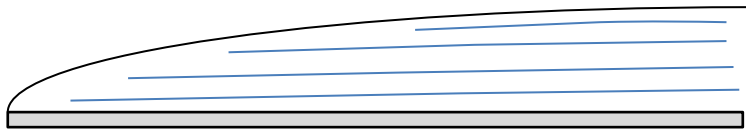
LAMINAR AND TURBULENT FLOW



INFLUENCE OF REYNOLDS NUMBER

Low Re: Laminar flow

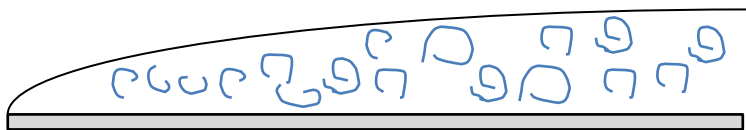
- Viscosity dominates momentum → neatly ‘layered’ flow



$$Re = \frac{\rho U L}{\mu}$$

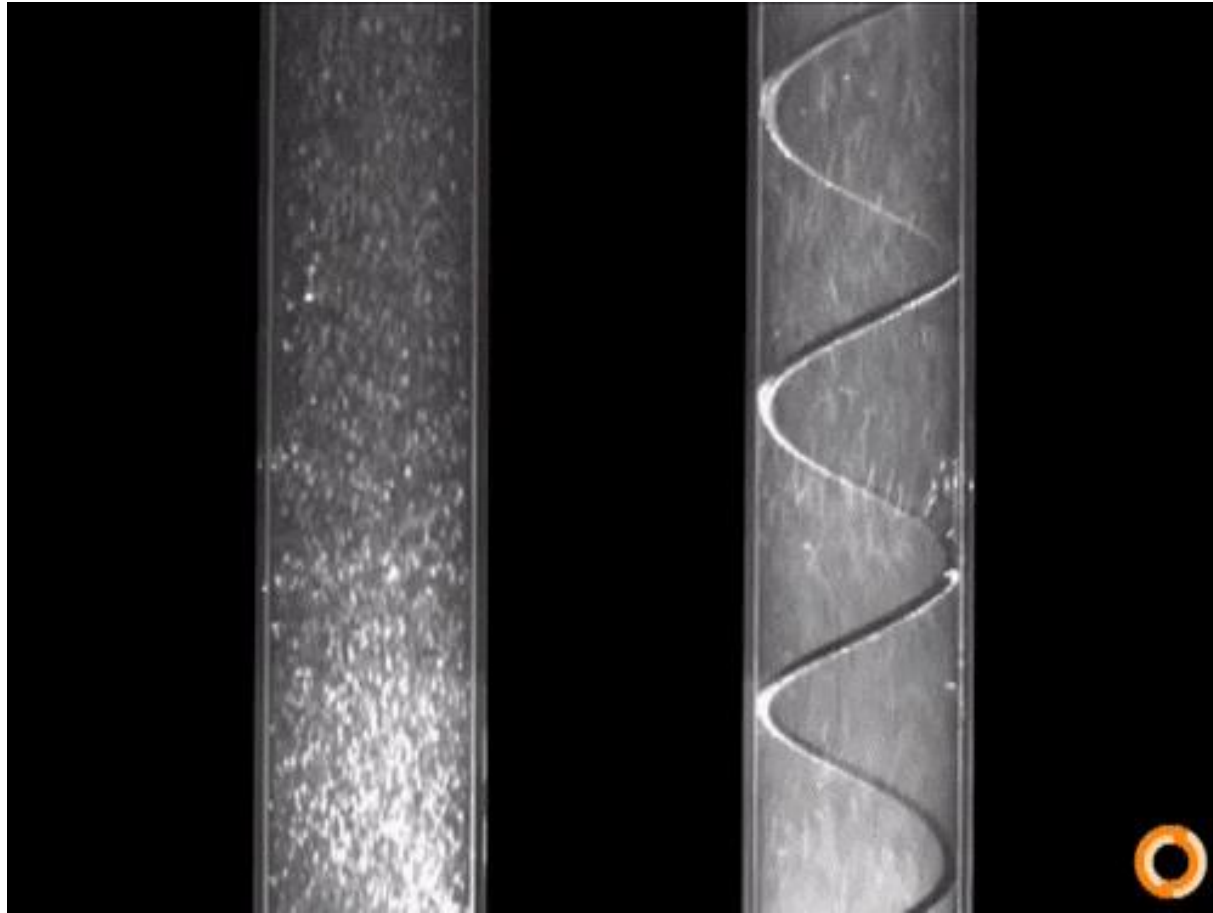
High Re: turbulent flow

- Momentum dominates viscosity → flow starts to swirl (**chaos!**)



Turbulence: fluid particles have individual irregular deviations from the mean “bulk speed” because of high momentum

LAMINAR VS. TURBULENT



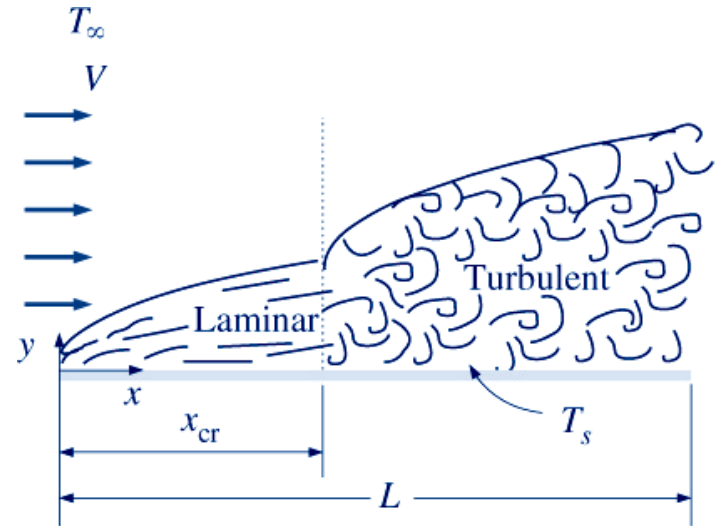
LAMINAR VS. TURBULENT

Turbulent boundary layer has **higher h** :

- Heat spreads better through chaotic mixing of particles

Laminar or turbulent?

- Close to leading edge always laminar
- transition laminar \rightarrow turbulent
- Here only extremes: either totally laminar or totally turbulent



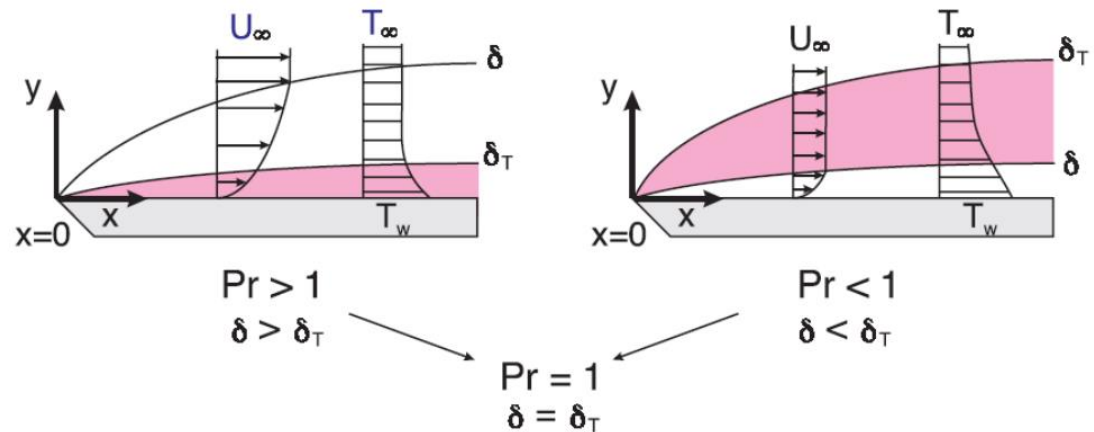
This also holds for surfaces other than a flat plate!

THERMAL BOUNDARY LAYER

Similar to velocity boundary layer, a **thermal boundary layer** develops when a fluid at specific temperature flows over a surface which is at different temperature.

Prandtl number:

$$Pr = \frac{\mu c_p}{k}$$



The thickness of the thermal boundary layer δ_t is defined as the distance at which:

$$\frac{T - T_s}{T_\infty - T_s} = 0.99$$

LEARNING OBJECTIVES LECTURE 3

- Defining Convective Heat Transfer
- Convective Heat Transfer Types
- **Heat Transfer Rate in Convection**
 - Newton's Law
 - Convection Resistance
 - Nusselt Number
- Forced Convection
 - Flow Parameters
 - Convective Heat Transfer Coefficient
 - Laminar and Turbulent Flow
 - **Using additional correlations for various configurations**
- Step-by-step plan for convection calculations

CHARACTERISTIC LENGTH

Numbers sometimes based on L , sometimes D , ...

General notation:

$$\text{Nu} = \frac{h L_c}{k} \quad \text{Re} = \frac{\rho U L_c}{\mu}$$

Per geometry L_c is defined

- Flow over flat surface: length L
- Flow around sphere/cylinder: diameter D
- Other cases: Lecture 4

Subscripts:

Re_D, Re_L useful
 Nu_D, Nu_L useful
 $\text{Re}_{Lc}, \text{Nu}_{Lc}$ not useful

- Numbers sometimes based on L , sometimes D (official notation: Re_L, Re_D)
- Per geometry distinction between Reynolds Numbers (flow regime)

CORRELATIONS FOR h – FORCED CONVECTION

External flow

$$\text{Nu} = a \cdot \text{Re}^b \text{Pr}^c$$

where a , b , and c are constants. The properties of the fluid are usually evaluated at the **film temperature** defined as:

$$T_f = \frac{T_s + T_\infty}{2}$$

CORRELATIONS FOR h – FORCED CONVECTION

External flow

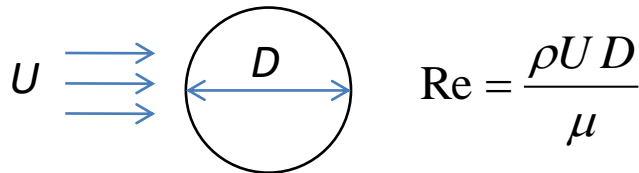
$$Nu = a \cdot Re^b Pr^c$$



$$a = 0,664; b = 0,5; c = 1/3 \quad (Re < 5 \cdot 10^5)$$

$$a = 0,037; b = 0,8; c = 1/3 \quad (Re > 5 \cdot 10^5)$$

$$Re = \frac{\rho U L}{\mu}$$

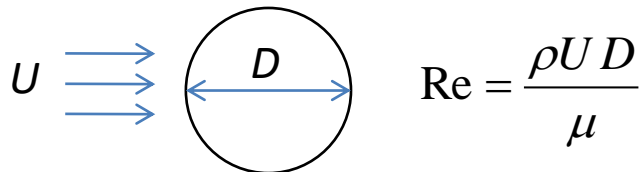


$$Re = \frac{\rho U D}{\mu}$$

$$a = 0,193; b = 0,618; c = 1/3 \quad (4000 < Re < 40.000)$$

$$a = 0,027; b = 0,805; c = 1/3 \quad (40.000 < Re < 400.000)$$

$$Nu_{cyl} = \frac{hD}{k} = 0.3 + \frac{0.62 Re^{1/2} Pr^{1/3}}{[1 + (0.4/Pr)^{2/3}]^{1/4}} \left[1 + \left(\frac{Re}{282,000} \right)^{5/8} \right]^{4/5}$$



$$Re = \frac{\rho U D}{\mu}$$

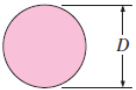

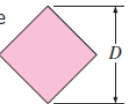
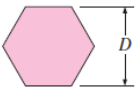
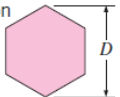

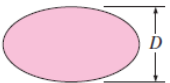
$$Nu \approx 2 + [0,4Re^{1/2} + 0,06Re^{2/3}] Pr^{0,4}$$

(optimal for $Re < 80.000$)

CORRELATIONS FOR h – FORCED CONVECTION

TABLE 7-1

Empirical correlations for the average Nusselt number for forced convection over circular and noncircular cylinders in cross flow (from Zukauskas, Ref. 14, and Jakob, Ref. 6)

Cross-section of the cylinder	Fluid	Range of Re	Nusselt number
Circle 	Gas or liquid	0.4–4 4–40 40–4000 4000–40,000 40,000–400,000	$Nu = 0.989Re^{0.330} Pr^{1/3}$ $Nu = 0.911Re^{0.385} Pr^{1/3}$ $Nu = 0.683Re^{0.466} Pr^{1/3}$ $Nu = 0.193Re^{0.618} Pr^{1/3}$ $Nu = 0.027Re^{0.805} Pr^{1/3}$
Square 	Gas	5000–100,000	$Nu = 0.102Re^{0.675} Pr^{1/3}$
Square (tilted 45°) 	Gas	5000–100,000	$Nu = 0.246Re^{0.588} Pr^{1/3}$
Hexagon 	Gas	5000–100,000	$Nu = 0.153Re^{0.638} Pr^{1/3}$
Hexagon (tilted 45°) 	Gas	5000–19,500 19,500–100,000	$Nu = 0.160Re^{0.638} Pr^{1/3}$ $Nu = 0.0385Re^{0.782} Pr^{1/3}$
Vertical plate 	Gas	4000–15,000	$Nu = 0.228Re^{0.731} Pr^{1/3}$
Ellipse 	Gas	2500–15,000	$Nu = 0.248Re^{0.612} Pr^{1/3}$

CONCLUSION FORCED CONVECTION

General (also natural convection):

$$\dot{Q} = hA\Delta T \quad (\text{W}) \quad \text{Newton's cooling law} \quad \dot{q} = h\Delta T \quad (\text{W/m}^2)$$

“Supporting” equations for h (*Forced Convection*):

$$\text{Nu} = a \cdot \text{Re}^b \text{Pr}^c \quad a, b, c \text{ dependent on geometry and flow regime (laminar / turbulent)}$$

Nusselt Number $\text{Nu}_L = \frac{hL}{k}; \text{Nu}_D = \frac{hD}{k} \quad (-)$

Reynolds Number $\text{Re}_L = \frac{\rho U L}{\mu}; \text{Re}_D = \frac{\rho U D}{\mu} \quad (-)$

Prandtl Number $\text{Pr} = \frac{\mu c_p}{k}$

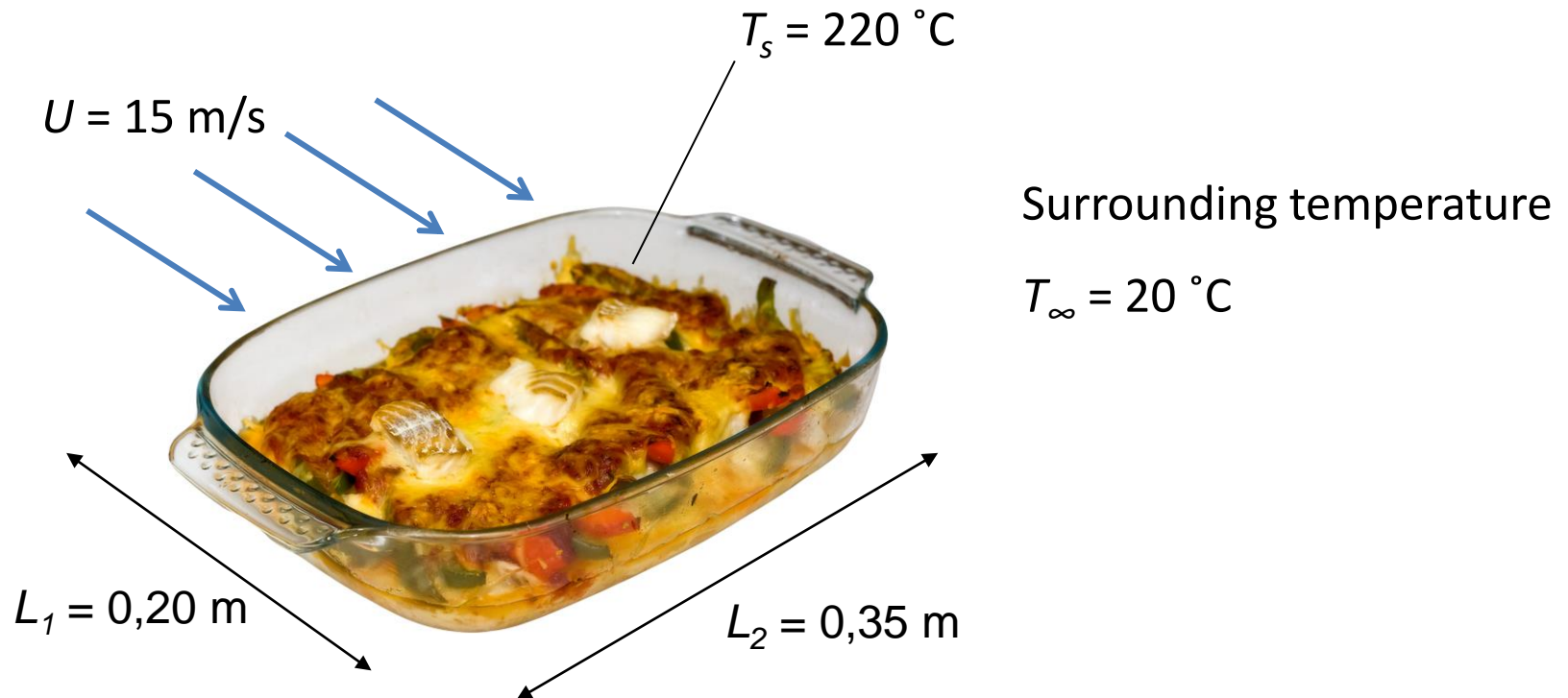
Dimensionless numbers
make similar shaped
situations comparable;
“universal” parameters

LEARNING OBJECTIVES LECTURE 3

- Defining Convective Heat Transfer
- Convective Heat Transfer Types
- **Heat Transfer Rate in Convection**
 - Newton's Law
 - Convection Resistance
 - Nusselt Number
- Forced Convection
 - Flow Parameters
 - Convective Heat Transfer Coefficient
 - Laminar and Turbulent Flow
 - Using additional correlations for various configurations
- **Step-by-step plan for convection calculations**

EXAMPLE

Calculate the heat transfer rate?



SUMMARY

- **Heat Transfer Equation**

$$\dot{Q} = hA\Delta T \quad \text{Newton's cooling law}$$

- **Convection resistance**

$$\dot{Q} = hA\Delta T = \frac{\Delta T}{R_{conv}} \quad \text{with } R_{conv} = \frac{1}{hA} \quad (\text{K/W})$$

- **Heat Transfer correlations**

Forced convection: Nu as function of Re, Pr : $\text{Nu} = f(\text{Re}, \text{Pr})$

Natural convection: next lecture

SUMMARY

Dimensionless Numbers

Nusselt Number $\text{Nu}_L = \frac{hL}{k}; \text{Nu}_D = \frac{hD}{k} \quad (-)$

Reynolds Number $\text{Re}_L = \frac{\rho U L}{\mu}; \text{Re}_D = \frac{\rho U D}{\mu} \quad (-)$

Prandtl Number $\text{Pr} = \frac{\mu c_p}{k}$



Exercise:

Show Nu , Pr and Re are dimensionless

LECTORIAL 2

- ⇒ Lecture 2- Preparation (HEATQUIZ & Slides)
- ⇒ On campus Lectorial : 15Sept: 13:45 – 15:30
- ⇒ Group Assignments
- ⇒ Deadlines: schedule on Canvas

*Ready, set,
GO!...*

