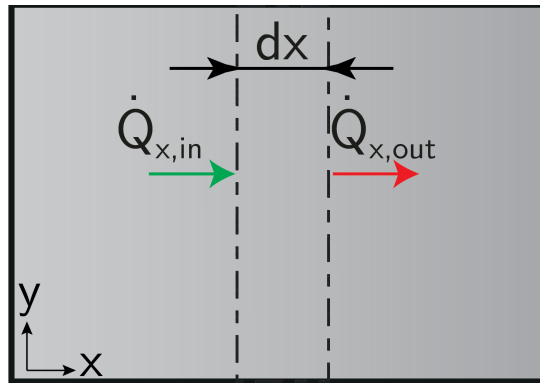


## EB - Cond. - IE 3

Setup the energy balance to calculate the one-dimensional steady-state temperature profile inside the wall.

### 1 Setting up the balance:

To derive the one-dimensional steady-state temperature profile, an energy balance around an infinitesimal element is needed. Heat is conducted in and out of the element.



Hence, the steady-state balance reads:

$$\dot{Q}_{x,in} - \dot{Q}_{x,out} = 0,$$

the sum of the in- and outgoing fluxes should equal zero, because of steady-state conditions.

### 2 Defining the elements within the balance:

The ingoing flux described by use of Fourier's law:

$$\dot{Q}_{x,in} = -\lambda A \frac{\partial T}{\partial x},$$

and the outgoing flux is approximated by the use of the Taylor series expansion.

$$\begin{aligned} \dot{Q}_{x,out} &= \dot{Q}_{x,in} + \frac{\partial \dot{Q}_{x,in}}{\partial x} \cdot dx \\ &= -\lambda A \frac{\partial T}{\partial x} + \left( -\lambda A \frac{\partial T}{\partial x} \right) \cdot dx. \end{aligned}$$

### 3 Inserting and rearranging:

$$-\lambda A \frac{\partial T}{\partial x} + \lambda A \frac{\partial T}{\partial x} - \frac{\partial}{\partial x} \left( -\lambda A \frac{\partial T}{\partial x} \right) dx = 0,$$

$A$  and  $\lambda$  are constant, hence cancel out:

$$\Rightarrow \frac{\partial^2 T}{\partial x^2} = 0.$$