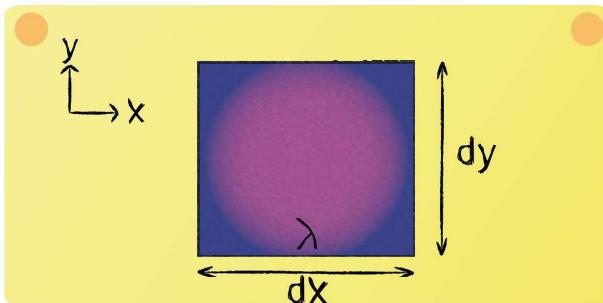


## Lecture 2 - Question 5



Give the energy balance and describe the heat fluxes. Assume two-dimensional steady-state heat transfer with a source in x- and y-direction. Take  $dz = 1m$ .

**Energy balance:**

$$\dot{Q}_{x,in} + \dot{Q}_{y,in} - \dot{Q}_{x,out} - \dot{Q}_{y,out} + \dot{\Phi} = 0$$

It is denoted that we are dealing with a source. For that reason the term  $\dot{\Phi}$  should be positive.

**Heat fluxes:**

$$\dot{Q}_{x,in} = -\lambda A \frac{\partial T}{\partial x}$$

$$\dot{Q}_{y,in} = -\lambda A \frac{\partial T}{\partial y}$$

$$\dot{Q}_{x,out} = -\lambda A \frac{\partial T}{\partial x} + \frac{\partial \dot{Q}_{x,in}}{\partial x} dx$$

$$\dot{Q}_{y,out} = -\lambda A \frac{\partial T}{\partial y} + \frac{\partial \dot{Q}_{y,in}}{\partial y} dy$$

$$\dot{\Phi} = \dot{\Phi}'' \cdot V = \dot{\Phi}'' \cdot dx \cdot dy$$



The heat fluxes are described by conductive heat transfer. The outgoing heat fluxes can be approximated by use of the Taylor series expansion.

