

W06

You are an engineer working on the design of an insulated spherical gas storage tank. The tank is used to store pressurized gas, and maintaining the gas at a specific temperature range is crucial for its stability and performance. To achieve this, the tank is equipped with a multi-layer insulated spherical wall.



Figure 11: Spherical gas storage tank

This innovative design operates with four specialized layers. The gas resides within a spherical vessel of inner diameter $d_i = 10 \text{ m}$. The innermost layer is stainless steel with thermal conductivity $k_{ss} = 50 \text{ W/mK}$ and thickness $x_{ss} = 10 \text{ mm}$, ensuring core stability. Wrapped around it, a robust fiberglass composite layer, $k_{fc} = 20 \text{ W/mK}$ and $x_{fc} = 30 \text{ mm}$ thick, provides strength and insulation. The third layer is EPS with $k_{EPS} = 0.03 \text{ W/mK}$ and $x_{EPS} = 20 \text{ mm}$ thickness, buffering temperature for stability. The outermost layer features a precision-crafted aluminum sheet with thermal conductivity $k_{al} = 237 \text{ W/mK}$, $x_{al} = 5 \text{ mm}$ thickness, and optical properties $\rho = 0.95$, $\tau = 0$ acting as a grey body, adding elegance.

The gas is being stored at a temperature of $T_g = 750 \text{ }^\circ\text{C}$ with an inner convective coefficient of $h_{in} = 150 \text{ W/m}^2\text{K}$. The tank loses heat ambient with a temperature of $T_{amb} = 21 \text{ }^\circ\text{C}$ by convection and radiation.

- a) Provide a diagram of the thermal network, incorporating all temperatures, resistances, and the direction of heat flow. Elaborate on each component's function.
- b) Present a graphical representation of the temperature profile. The depicted range should encompass both the gas's internal temperature and the external ambient temperature.
- c) Calculate the rate of heat loss from the tank, assuming steady-state operational conditions.
- d) Maintaining a constant gas temperature costs approximately 0.01 € / kWh . Determine the potential annual savings if the insulating material's thickness is doubled. Reason whether this strategy is advisable.