CSE221

Lab Assignment 03 Summer 2023

Submission Guidelines:

- 1. You can code all of them either in Python, CPP, or Java. But you should choose a specific language for all tasks.
- 2. For each task write separate python files like task1.py, task2.py, and so on.
- 3. For each problem, take input from files called "inputX.txt" and output at "outputX.txt", where X is the task number.
- 4. Add a hand written explanation of 3-4 lines for each of your solutions in a separate document. You may compile all of your explanations in a single file.
- 5. Finally zip all the files and rename this zip file as per this format:LabSectionNo_ID_CSE221LabAssignmentNo_Summer2023.zip

 [Example:LabSection01_21101XXX_CSE221LabAssignment03_Summer2023.zip]
- 6. Don't copy from your friends.
- 7. You MUST follow all the guidelines, naming/file/zipping convention stated above.

Failure to follow instructions will result in a straight 50% mark deduction.

Task 01 [15 Points]:

Somewhere in the universe, the Biannual Regional Alien Competition is taking place.

There are N aliens standing in a line. You will be given a permutation of N, which denotes the height of each alien. A sequence of N numbers is called a permutation if it contains all integers from 1 to N exactly once. For example, the sequences [3,1,4,2], [1] and [2,1] are permutations, but [1,2,1], [0,1] and [1,3,4] — are not.

In the competition, for each alien, the judge wants to count how many aliens are standing on its right side with a strictly

smaller height. Then the judge wants to add up all the counts. To do this, the judge writes the following piece of code.

```
count = 0
for i in range(n):
   for j in range(i+1,n):
     if H[i] > H[j]:
        count+=1
```

However, their algorithm wasn't efficient at all. Hence, the alien calls you to write a better solution for the program.

More formally, you have to count how many pairs of aliens are standing in the line such that H[i] > H[j] and i < j. Here, A is a permutation of the aliens' heights. And i,j denote the Aliens' positions.

Input

The first line contains a single integer 1 <= N <= 10 6 - the number of total aliens.

The next line contains N integers $H_1, H_2, \dots, H_n (1 \le H_i \le N)$ — the height of the i-th alien. It is guaranteed that the given heights will be a permutation of N.

Output

Print a single integer, which denotes the total number of pairs (i, j) such that i < j and $H_i > H_{\uparrow}$.

Sample Input/Output:

Sample Input 1	Sample Output 1
5	0

1 2 3 4 5	
Sample Input 2	Sample Output 2
5 5 4 3 2 1	10
Sample Input 3	Sample Output 3
8 2 7 4 1 5 6 8 3	11

Sample Input 3 Explanation:

In the sample input 3, the following pairs on alien's heights satisfy the condition: (2,1), (7,4), (7,1), (7,5), (7,6), (7,3), (4,1), (4,3), (5,3), (6,3), (8,3)

Task 02 [15 points]

You are given a list A of N integers. You have to choose two indices i and j such that $1 \le i \le j \le N$ and $A[i] + A[j]^2$ is maximum possible. Here, we are considering 1-based indexing.

Write a code which will find the maximum value of $A[i] + A[j]^2$ in O(N) or $O(N \log N)$.

Input

The first line contains a single integer 1 <= N <= 10^{6} - the length of the list.

The next line contains N integers A_1 , A_2 ,, A_n (-10 8 \leq A_i \leq $10<math>^8$) separated by a space.

Output

Print a single integer - which denotes the maximum possible value of $A[i] + A[j]^2$.

Sample Input/Output:

Sample Input 1	Sample Output 1
5 9 6 5 8 2	73
Sample Input 2	Sample Output 2
8 5 10 4 -3 1 6 -10 2	110
Sample Input 3	Sample Output 3
7 -5 -2 -6 -7 -1 8 2	63

Task 03 [10 Points]

In this problem, you will be given a list of numbers. You have to sort the list using the Quick Sort algorithm in ascending order.

Pseudocode of Quick Sort Algorithm:

QUICKSORT(A, p, r)1 **if** p < r2 q = PARTITION(A, p, r)3 QUICKSORT(A, p, q - 1)4 QUICKSORT(A, q + 1, r)

```
PARTITION(A, p, r)

1 x = A[r]

2 i = p - 1

3 for j = p to r - 1

4 if A[j] \le x

5 i = i + 1

6 exchange A[i] with A[j]

7 exchange A[i + 1] with A[r]

8 return i + 1
```

[The code snippet has been taken from the book: Introduction to Algorithms]

Input

The first line contains an integer N (1 <= N <= 10^5), denoting the length of Alice's list. In the next line, there will be N integers separated by space.

Output:

You have to sort the number using the Quick Sort algorithm in ascending order and show the sorted list.

Sample Input/Output:

Sample Input 1	Sample Output 1
8 9 5 4 6 1 3 2 9	1 2 3 4 5 6 9 9
Sample Input 2	Sample Output 2
1 10	10
Sample Input 3	Sample Output 3
6 8 1 4 2 1 3	1 1 2 3 4 8

Sample Input 4	Sample Output 4
7 7 6 5 4 3 2 1	1 2 3 4 5 6 7

Task 04 [10 Points]

In this problem, you will be given a list of numbers. You have to find the ${\bf k}$ -th smallest value from the list without sorting using the Partition function of Quick sort.

We will consider the 1-based indexing of the list.

Input

The first line contains an integer N (1 <= N <= 10^6), denoting the length of the list.

The next line contains N integers A_1, A_2, \dots, A_n ($1 \le A_i \le 10^6$) separated by a space.

The third line contains a single integer Q (1 \leq Q \leq 100) - which denotes the number of queries you have to answer.

Each of the next Q lines will contain a single integer K ($1 \le K \le N$).

Output:

For each query, you have to find the K-th smallest number from the given list.

Sample Input/Output:

Sample Input 1	Sample Output 1
9 // Total Elements	9
10 11 10 6 7 9 8 15 2	7
4 // Total queries	6

5	10
3	
2	
7	