



**GCE**

**Mathematics B MEI**

**H640/03: Pure Mathematics and Comprehension**

A Level

**Mark Scheme for June 2023**

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This mark scheme is published as an aid to teachers and students, to indicate the requirements of the examination. It shows the basis on which marks were awarded by examiners. It does not indicate the details of the discussions which took place at an examiners' meeting before marking commenced.

All examiners are instructed that alternative correct answers and unexpected approaches in candidates' scripts must be given marks that fairly reflect the relevant knowledge and skills demonstrated.

Mark schemes should be read in conjunction with the published question papers and the report on the examination.

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## MARKING INSTRUCTIONS

### PREPARATION FOR MARKING

#### RM ASSESSOR

1. Make sure that you have accessed and completed the relevant training packages for on-screen marking: *RM Assessor Online Training; OCR Essential Guide to Marking*.
2. Make sure that you have read and understood the mark scheme and the question paper for this unit. These are posted on the RM Cambridge Assessment Support Portal <http://www.rm.com/support/ca>
3. Log-in to RM Assessor and mark the **required number** of practice responses (“scripts”) and the **number of required** standardisation responses.

### MARKING

1. Mark strictly to the mark scheme.
2. Marks awarded must relate directly to the marking criteria.
3. The schedule of dates is very important. It is essential that you meet the RM Assessor 50% and 100% (traditional 40% Batch 1 and 100% Batch 2) deadlines. If you experience problems, you must contact your Team Leader (Supervisor) without delay.

**4. Annotations**

Annotation	Meaning
✓ and ✗	
BOD	Benefit of doubt
FT	Follow through
ISW	Ignore subsequent working
M0, M1	Method mark awarded 0, 1
A0, A1	Accuracy mark awarded 0, 1
B0, B1	Independent mark awarded 0, 1
E	Explanation mark 1
SC	Special case
^	Omission sign
MR	Misread
BP	Blank Page
Seen	
Highlighting	

<b>Other abbreviations in mark scheme</b>	<b>Meaning</b>
E1	Mark for explaining a result or establishing a given result
dep*	Mark dependent on a previous mark, indicated by *. The * may be omitted if only one previous M mark
cao	Correct answer only
oe	Or equivalent
rot	Rounded or truncated
soi	Seen or implied
www	Without wrong working
AG	Answer given
awrt	Anything which rounds to
BC	By Calculator
DR	This question included the instruction: In this question you must show detailed reasoning.
BP	Blank Page
Seen	
Highlighting	

## 5. Subject Specific Marking Instructions

- a. Annotations must be used during your marking. For a response awarded zero (or full) marks a single appropriate annotation (cross, tick, M0 or ^) is sufficient, but not required.

For responses that are not awarded either 0 or full marks, you must make it clear how you have arrived at the mark you have awarded and all responses must have enough annotation for a reviewer to decide if the mark awarded is correct without having to mark it independently.

It is vital that you annotate standardisation scripts fully to show how the marks have been awarded.

### Award NR (No Response)

- if there is nothing written at all in the answer space and no attempt elsewhere in the script
- OR if there is a comment which does not in any way relate to the question (e.g. 'can't do', 'don't know')
- OR if there is a mark (e.g. a dash, a question mark, a picture) which isn't an attempt at the question.

Note: Award 0 marks only for an attempt that earns no credit (including copying out the question).

If a candidate uses the answer space for one question to answer another, for example using the space for 8(b) to answer 8(a), then give benefit of doubt unless it is ambiguous for which part it is intended.

- b. An element of professional judgement is required in the marking of any written paper. Remember that the mark scheme is designed to assist in marking incorrect solutions. Correct solutions leading to correct answers are awarded full marks but work must not always be judged on the answer alone, and answers that are given in the question, especially, must be validly obtained; key steps in the working must always be looked at and anything unfamiliar must be investigated thoroughly. Correct but unfamiliar or unexpected methods are often signalled by a correct result following an apparently incorrect method. Such work must be carefully assessed. When a candidate adopts a method which does not correspond to the mark scheme, escalate the question to your Team Leader who will decide on a course of action with the Principal Examiner.

If you are in any doubt whatsoever you should contact your Team Leader.

- c. The following types of marks are available.

### M

A suitable method has been selected and applied in a manner which shows that the method is essentially understood. Method marks are not usually lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using

some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, e.g. by substituting the relevant quantities into the formula. In some cases the nature of the errors allowed for the award of an M mark may be specified.

A method mark may usually be implied by a correct answer unless the question includes the DR statement, the command words "Determine" or "Show that", or some other indication that the method must be given explicitly.

**A**

Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated Method mark is earned (or implied). Therefore M0 A1 cannot ever be awarded.

**B**

Mark for a correct result or statement independent of Method marks.

**E**

A given result is to be established or a result has to be explained. This usually requires more working or explanation than the establishment of an unknown result.

Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored. Sometimes this is reinforced in the mark scheme by the abbreviation isw. However, this would not apply to a case where a candidate passes through the correct answer as part of a wrong argument.

- d. When a part of a question has two or more 'method' steps, the M marks are in principle independent unless the scheme specifically says otherwise; and similarly where there are several B marks allocated. (The notation 'dep\*' is used to indicate that a particular mark is dependent on an earlier, asterisked, mark in the scheme.) Of course, in practice it may happen that when a candidate has once gone wrong in a part of a question, the work from there on is worthless so that no more marks can sensibly be given. On the other hand, when two or more steps are successfully run together by the candidate, the earlier marks are implied and full credit must be given.
- e. The abbreviation FT implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, A and B marks are given for correct work only – differences in notation are of course permitted. A (accuracy) marks are not given for answers obtained from incorrect working. When A or B marks are awarded for work at an intermediate stage of a solution, there may be various alternatives that are equally acceptable. In such cases, what is acceptable will be detailed in the mark scheme. If this is not the case please, escalate the question to your Team Leader who will decide on a course of action with the Principal Examiner.

Sometimes the answer to one part of a question is used in a later part of the same question. In this case, A marks will often be ‘follow through’. In such cases you must ensure that you refer back to the answer of the previous part question even if this is not shown within the image zone. You may find it easier to mark follow through questions candidate-by-candidate rather than question-by-question.

- f. Unless units are specifically requested, there is no penalty for wrong or missing units as long as the answer is numerically correct and expressed either in SI or in the units of the question. (e.g. lengths will be assumed to be in metres unless in a particular question all the lengths are in km, when this would be assumed to be the unspecified unit.)

We are usually quite flexible about the accuracy to which the final answer is expressed; over-specification is usually only penalised where the scheme explicitly says so.

- When a value is given in the paper only accept an answer correct to at least as many significant figures as the given value.
- When a value is not given in the paper accept any answer that agrees with the correct value to 2 s.f. unless a different level of accuracy has been asked for in the question, or the mark scheme specifies an acceptable range.

NB for Specification A the rubric specifies 3 s.f. as standard, so this statement reads “3 s.f.”.

Follow through should be used so that only one mark in any question is lost for each distinct accuracy error.

Candidates using a value of 9.80, 9.81 or 10 for g should usually be penalised for any final accuracy marks which do not agree to the value found with 9.8 which is given in the rubric.

- g. Rules for replaced work and multiple attempts:

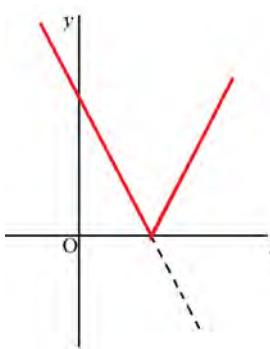
- If one attempt is clearly indicated as the one to mark, or only one is left uncrossed out, then mark that attempt and ignore the others.
- If more than one attempt is left not crossed out, then mark the last attempt unless it only repeats part of the first attempt or is substantially less complete.
- if a candidate crosses out all of their attempts, the assessor should attempt to mark the crossed out answer(s) as above and award marks appropriately.

- h. For a genuine misreading (of numbers or symbols) which is such that the object and the difficulty of the question remain unaltered, mark according to the scheme but following through from the candidate’s data. A penalty is then applied; 1 mark is generally appropriate, though this may differ for some units. This is achieved by withholding one A or B mark in the question. Marks designated as cao may be awarded as long as there are no other errors.

If a candidate corrects the misread in a later part, do not continue to follow through. E marks are lost unless, by chance, the given results are established by equivalent working. Note that a miscopy of the candidate’s own working is not a misread but an accuracy error.

- i. If a calculator is used, some answers may be obtained with little or no working visible. Allow full marks for correct answers, provided that there is nothing in the wording of the question specifying that analytical methods are required such as the bold “In this question you must show detailed reasoning”, or the command words “Show” or “Determine”. Where an answer is wrong but there is some evidence of method, allow appropriate method marks. Wrong answers with no supporting method score zero. If in doubt, consult your Team Leader.
- j. If in any case the scheme operates with considerable unfairness consult your Team Leader.

Question		Answer	Marks	AO	Guidance
1		<b>DR</b> $\frac{4}{13} + \cos^2 \theta = 1$ oe $\cos^2 \theta = \frac{9}{13}$ $\cos \theta = -\frac{3}{\sqrt{13}}$ <b>Alternative method</b> $13 = 4 + a^2$ or correct triangle $(2, 3, \sqrt{13})$ seen $a = (\pm)3$ soi $\cos \theta = -\frac{3}{\sqrt{13}}$	<b>M1</b>  <b>A1</b>  <b>A1</b>  <b>M1</b>  <b>A1</b>  <b>A1</b>  [3]	<b>1.1a</b>  <b>1.1</b>  <b>2.2a</b>  <b>1.1</b>  <b>1.1</b>	<b>M0</b> if decimal angles (d, r, g) seen unless superceded by correct method  OR $\cos \theta = -\frac{3\sqrt{13}}{13}$ If decimals seen (as check) isw

Question		Answer	Marks	AO	Guidance
2	(a)		B1  [1]	1.1	Going over the given line above the $x$ -axis and to the left of the $y$ -axis and then going up from the $x$ -axis at the same angle (by eye) Condone right hand line segment dotted/dashed
2	(b)	$-3 < 5 - 2x < 3$ $2 < 2x < 8$ $1 < x < 4 \text{ oe e.g. '1} < x \text{ and } x < 4\text{'}$	M1  A2  [3]	1.1a  1.1  1.1	Could be treated as two separate inequalities (at least one correct) in $x$ not $ x $ OR $(5 - 2x)^2 < 9$ If only one linear inequality in $x$ stated scores M0 A0 A0 OR $4x^2 - 20x + 16 < 0$ or $x^2 - 5x + 4 < 0$ OR $(x - 1)(x - 4) < 0$ Allow M1 if treated as equations in $x$ not $ x $ A1 if only one inequality correct OR for $1 \leq x \leq 4$ OR for $1 < x, x < 4$ OR for ' $1 < x$ or $x < 4$ ' 

Question		Answer	Marks	AO	Guidance
3		<b>DR</b> $\frac{\sqrt{6}-\sqrt{5}}{6-5} + \frac{\sqrt{7}-\sqrt{6}}{7-6}$ oe  $\sqrt{7}-\sqrt{5}$ or $\frac{\sqrt{5}-\sqrt{7}}{-1}$  $\frac{k}{\sqrt{5}+\sqrt{7}} = \frac{k(\sqrt{7}-\sqrt{5})}{7-5} = \sqrt{7}-\sqrt{5}$  so $k = 2$	<b>M1</b>  <b>A1</b>  <b>A1</b>	<b>3.1a</b>  <b>1.1</b>  <b>2.2a</b>	Rationalising denominators. This is the minimum working needed for <b>M1</b> Accept 1 for “6 – 5” and – 1 for “5 – 6” etc
		<b>Alternative</b> $(\sqrt{6}+\sqrt{7})(\sqrt{5}+\sqrt{7}) + (\sqrt{5}+\sqrt{6})(\sqrt{5}+\sqrt{7})$ $= k(\sqrt{5}+\sqrt{6})(\sqrt{6}+\sqrt{7})$  $(2\sqrt{5}\sqrt{6} + 2\sqrt{5}\sqrt{7} + 2\sqrt{6}\sqrt{7} + 12)$ $= k(\sqrt{5}\sqrt{6} + \sqrt{5}\sqrt{7} + \sqrt{6}\sqrt{7} + 6)$  $2(\sqrt{5}\sqrt{6} + \sqrt{5}\sqrt{7} + \sqrt{6}\sqrt{7} + 6)$ $= k(\sqrt{5}\sqrt{6} + \sqrt{5}\sqrt{7} + \sqrt{6}\sqrt{7} + 6)$  so $k = 2$	<b>M1</b>  <b>A1</b>  <b>A1</b>		For dealing appropriately with fractions (working with both sides) e.g. clearing the fractions or making $k$ the subject with the RHS as a single fraction. $k = \frac{(\sqrt{5}+\sqrt{7}+2\sqrt{6})(\sqrt{5}+\sqrt{7})}{(\sqrt{5}+\sqrt{6})(\sqrt{6}+\sqrt{7})}$  Expanding brackets and collecting like surds $k = \frac{12 + 2\sqrt{5}\sqrt{7} + 2\sqrt{5}\sqrt{6} + 2\sqrt{6}\sqrt{7}}{6 + \sqrt{5}\sqrt{7} + \sqrt{5}\sqrt{6} + \sqrt{6}\sqrt{7}}$
			[3]		Finding $k$ convincingly after <b>M1</b>

Question		Answer	Marks	AO	Guidance
4		<p><b>DR</b></p> $x^3 - 2x^2 - 5x + 6 = 0$ <p>For <math>x = 1</math>, <math>1^3 - 2(1)^2 - 5(1) + 6 = 0</math> oe so <math>x = 1</math> is a root or <math>(x - 1)</math> is a factor</p> $(x - 1)(x^2 - x - 6)$ $(x - 1)(x - 3)(x + 2)$ $(1, 0), (3, 0), (-2, 0)$	<b>M1</b> <b>M1</b> <b>DM1</b> <b>A1</b> <b>[4]</b>	<b>1.1a</b> <b>1.1</b> <b>1.1</b> <b>1.1</b>	<p>Finding one root or factor by factor theorem or division to a remainder of 0. A conclusion is needed for this <b>M1</b>.</p> <p>Factorising to find quadratic factor or division (method seen) or factor theorem again (substitution shown) to get a different root/factor</p> <p>Completion, all 3 factors/roots seen, dep on previous <b>M1</b> Might not be in same place</p> <p>All 3 points as coordinates or pairs of values Dep on <b>M3</b></p>

Question		Answer	Marks	AO	Guidance	
5	(a)	<p><b>DR</b></p> $\frac{dy}{dx} = 3x^2 - 10x + 6$ <p>When <math>x = 0 \quad \frac{dy}{dx} = 6</math></p> <p>Tangent goes through origin so equation is <math>y = 6x</math> cao</p>	<p><b>M1</b></p> <p><b>M1</b></p> <p><b>A1</b></p> <p>[3]</p>	<p><b>1.1</b></p> <p><b>1.1</b></p> <p><b>1.1</b></p>	<p>At least two terms correct</p> <p>FT <i>their</i> <math>\frac{dy}{dx}</math></p> <p><b>Need reasoning</b> eg <math>y - 0 = 6(x - 0)</math> or use of <math>y = mx + c</math> <math>y = 6x</math> implies previous <b>M</b> mark</p>	
5	(b)	<p><b>DR</b></p> <p>When <math>x = 1 \quad \frac{dy}{dx} = -1</math></p> <p>Gradient of normal is 1</p> <p><math>[(y - 2) = (x - 1)]</math> so <math>y = x + 1</math></p>	<p><b>M1</b></p> <p><b>M1</b></p> <p><b>A1</b></p> <p>[3]</p>	<p><b>1.1</b></p> <p><b>1.1</b></p> <p><b>1.1</b></p>	<p>FT <i>their</i> <math>\frac{dy}{dx}</math> from (a)</p> <p>FT negative reciprocal of <i>their</i> <math>\frac{dy}{dx}</math>.</p> <p>oe but constant terms should be collected</p>	
5	(c)	<p><b>DR</b></p> <p><math>6x = x + 1</math></p> <p><math>x = \frac{1}{5}, \quad y = \frac{6}{5}</math> oe</p>	<p><b>M1</b></p> <p><b>A1</b></p> <p>[2]</p>	<p><b>1.1</b></p> <p><b>1.1</b></p>	<p>Eliminate a variable FT their equations from (a) and (b) for <b>M1</b> only</p>	

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<b>Question</b>		<b>Answer</b>	<b>Marks</b>	<b>AO</b>	<b>Guidance</b>	
<b>6</b>	<b>(a)</b>	<b>(i)</b> P (0.5, 0) Q (5.5, 0.5) R (4, 3.5) S (-1, 3)	<b>B1</b> <b>B1</b>  [2]	<b>1.1</b> <b>1.1</b>	Any midpoint correct All midpoints correct If no labels BOD for 1 or 2 marks	

<b>6</b>	<b>(a)</b>	<b>(ii)</b>	<p>Gradient PQ = 0.1 or length of PQ = <math>\frac{\sqrt{101}}{2}</math> or vector <math>\overrightarrow{PQ} = \begin{pmatrix} 5 \\ 0.5 \end{pmatrix}</math></p> <p>Gradient SR is <math>\frac{0.5}{5} = 0.1 =</math> gradient PQ or length of SR = <math>\sqrt{0.5^2 + 5^2} = \frac{\sqrt{101}}{2}</math> or vector <math>\overrightarrow{SR} = \begin{pmatrix} 4 - 1 \\ 3.5 - 3 \end{pmatrix} = \begin{pmatrix} 5 \\ 0.5 \end{pmatrix}</math></p> <p>Gradient PS = -2 or length of PS = <math>\frac{3\sqrt{5}}{2}</math> or vector <math>\overrightarrow{PS} = \begin{pmatrix} -1.5 \\ 3 \end{pmatrix}</math></p> <p>Gradient QR is <math>\frac{3}{-1.5} = -2</math> or length of QR = <math>\sqrt{1.5^2 + 3^2} = \frac{3\sqrt{5}}{2}</math> or vector <math>\overrightarrow{QR} = \begin{pmatrix} 4 - 5.5 \\ 3.5 - 0.5 \end{pmatrix} = \begin{pmatrix} -1.5 \\ 3 \end{pmatrix}</math></p> <p>Repeat process (as above) for other pair of opposite sides and conclude it's a parallelogram</p>	<b>B1</b>	<b>1.1</b>	<p>Gradient, length or vector of any one side of PQRS Or <b>SC1</b> if KLMN used</p>	
				<b>M1</b>	<b>2.2a</b>	<p>Gradient of opposite side of PQRS <b>shown</b> to be equal or length or vector of opposite side <b>shown</b> to be equal. ie some working must be seen</p>	Condone confusion of labels (eg length for gradient etc) for <b>M1/B1</b>
				<b>E1</b>	<b>2.4</b>	<p>Convincing completion dep on <b>M1</b></p>	Watch out for valid alternatives e.g. 2 sides equal length and equal gradient
				[3]			

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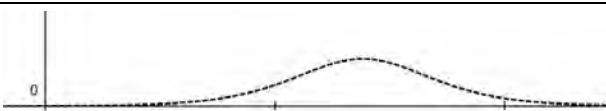
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<b>6</b>	<b>(b)</b>	<b>(i)</b>	$\overrightarrow{WX} = -3\mathbf{c} - 3\mathbf{a} + 3\mathbf{b}$ $= 3(-\mathbf{a} + \mathbf{b} - \mathbf{c})$	<b>B1</b> [1]	<b>2.2a</b>	Credible completion $\overrightarrow{WX} = \overrightarrow{WV} + \overrightarrow{VT} + \overrightarrow{TX}$	
<b>6</b>	<b>(b)</b>	<b>(ii)</b>	$\overrightarrow{AH} = -\mathbf{a} + \mathbf{b}$ $\overrightarrow{WX} = -3\mathbf{c} - 3\mathbf{a} + 3\mathbf{b}$ $\overrightarrow{WE} = -\mathbf{c} - \mathbf{a} + \mathbf{b}$ $\overrightarrow{DE} = \mathbf{c} - \mathbf{c} - \mathbf{a} + \mathbf{b} = -\mathbf{a} + \mathbf{b}$ <p>So AH is parallel to DE</p>	<b>B1</b> [2]	<b>1.1</b>		
<b>6</b>	<b>(b)</b>	<b>(iii)</b>	$\overrightarrow{BC} = \mathbf{a} + \mathbf{c}$ $\overrightarrow{GF} = \mathbf{b} - (-\mathbf{c} - \mathbf{a} + \mathbf{b}) = \mathbf{c} + \mathbf{a}$ $\overrightarrow{BC} = \overrightarrow{GF}$ so they are parallel	<b>B1</b> [2]	<b>2.2a</b>	$\overrightarrow{GF}$ from any correct route, must be shown Credible completion with conclusion	

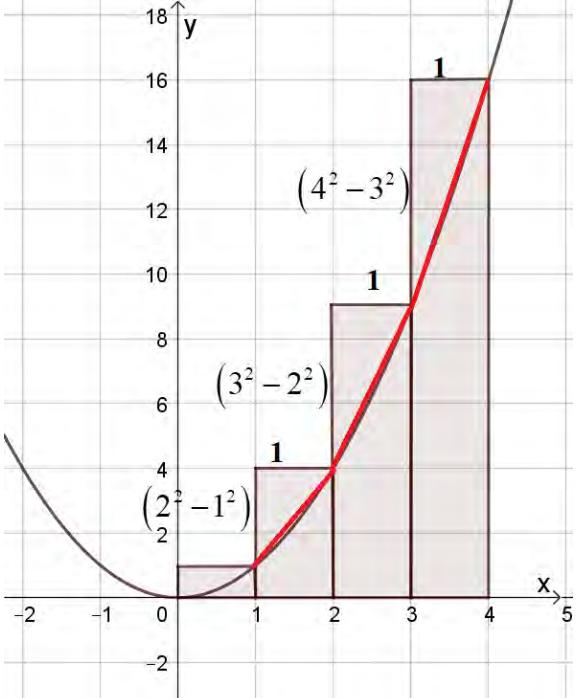
Question		Answer	Marks	AO	Guidance	
7		<p>[Perimeter =] <math>2r + r\theta = 10</math></p> $\theta = \frac{10 - 2r}{r}$ $A = \frac{1}{2}r^2\theta$ so $A = \frac{r(10 - 2r)}{2} = 5r - r^2$ $A = 2.5^2 - (2.5 - r)^2$ <p>This has a max when <math>2.5 - r = 0</math></p> <p>Max = 6.25 [cm<sup>2</sup>]</p> <p><b>Alternative method 1</b></p> $\frac{dA}{dr} = 5 - 2r$ $\frac{d^2A}{dr^2} = -2$ so max	<b>M1</b> <b>B1</b> <b>M1</b> <b>M1</b> <b>B1</b> <b>A1</b>	<b>1.1</b> <b>3.1a</b> <b>3.1a</b> <b>3.1a</b> <b>2.4</b> <b>2.2a</b>	OR $r = \frac{10}{2 + \theta}$ OR $A = \frac{100\theta}{2(2 + \theta)^2} = \frac{50\theta}{(2 + \theta)^2}$ Completing the square Convincing explanation that there is a max	Expression for one of $r, \theta$ in terms of the other Area in terms of either <i>their</i> $r$ or <i>their</i> $\theta$ . Need not expand brackets.

Question		Answer	Marks	AO	Guidance	
8		<p>Sketch diagram consistent with information in the question</p> $60 = 2 \times \frac{1}{2} \times 8 \times 12 \times \sin B$ $\sin B = \frac{5}{8} \text{ so } B = 38.7^\circ \text{ (0.675 rads)}$ <p>OR <math>B = 141.3^\circ</math> (2.47 rads)</p> $AC^2 = 8^2 + 12^2 - 2 \times 8 \times 12 \cos 38.7$ $= 58.1$ $AC = 7.62 \text{ cm}$ $AC^2 = 8^2 + 12^2 - 2 \times 8 \times 12 \cos 141.3$ $= 357.9$ $AC = 18.9 \text{ cm}$	<b>B1</b> <b>M1</b> <b>A1</b> <b>A1</b> <b>M1</b> <b>A1</b> <b>A1</b> <b>[7]</b>	<b>2.5</b> <b>3.1a</b> <b>1.1a</b> <b>3.2a</b> <b>3.1a</b> <b>1.1</b> <b>1.1</b>	<p>Triangle ADC or ABC or quadrilateral ABCD and 8 and 12 indicated eg side lengths or radii. Circles may or may not be shown.</p> <p><b>M1</b> implies previous <b>B1</b> These next 3 marks can be for angles <math>B</math> or <math>D</math>.</p> <p>One value of <math>B</math> or <math>\cos B</math></p> <p>Other value of <math>B</math> or <math>\cos B</math></p> <p>Use of cosine rule</p> <p>Accept 7.6 www</p> <p>Accept 19 www <b>A0</b> if more than 2 answers</p>	$\cos B = \frac{\sqrt{39}}{8}$ $\cos B = -\frac{\sqrt{39}}{8}$

<b>Question</b>		<b>Answer</b>	<b>Marks</b>	<b>AO</b>	<b>Guidance</b>
<b>9</b>	<b>(a)</b>	<b>(i)</b> 0.3 [MWh]	<b>B1</b> [1]	<b>3.4</b>	
<b>9</b>	<b>(a)</b>	<b>(ii)</b> 27 [MWh]	<b>B1</b> [1]	<b>3.4</b>	$P = 0.3e^{0.5 \times 9} = 27.0051\dots$
<b>9</b>	<b>(b)</b>	Reason why model is not suitable, e.g. <ul style="list-style-type: none"> <li>The model is only based on data up to 2009</li> <li>The model predicts unlimited growth in solar energy and that is not possible</li> </ul>	<b>B1</b> [1]	<b>3.5b</b>	Very large prediction in 2025 (80 501MWh) in unrealistic “Extrapolation” alone does not score, it would need explaining/clarifying
<b>9</b>	<b>(c)</b>	The graph gives a value close to 27 when $t = 9$	<b>E1</b> [1]	<b>3.2b</b>	Correct reasoning (answer given)
<b>9</b>	<b>(d)</b>	<b>(i)</b> 	<b>B1</b> <b>B1</b> [2]	<b>2.2a</b> <b>2.2a</b>	Gradient increasing from near zero to maximum for value of $t$ somewhere between 10 and 20 Gradient decreasing to near zero from max value
<b>9</b>	<b>(d)</b>	<b>(ii)</b> 14	<b>B1</b> [1]	<b>1.2</b>	Answer in range 13 to 15
<b>9</b>	<b>(d)</b>	<b>(iii)</b> This is when the rate of increase of electricity production is greatest	<b>E1</b> [1]	<b>3.2a</b>	
<b>9</b>	<b>(e)</b>	300 [MWh]	<b>B1</b> [1]	<b>2.2a</b>	Accept answer in range 300 to 305

Question		Answer	Marks	AO	Guidance	
10	(a)	$\begin{aligned}1 - \frac{3}{4} \sin^2 2\theta &= 1 - \frac{3}{4} (2 \sin \theta \cos \theta)^2 \\&= 1 - 3 \sin^2 \theta \cos^2 \theta \\(\sin^2 \theta + \cos^2 \theta)^3 &= \sin^6 \theta + \cos^6 \theta + 3 \sin^4 \theta \cos^2 \theta + 3 \sin^2 \theta \cos^4 \theta \\ \sin^6 \theta + \cos^6 \theta &= 1 - (3 \sin^4 \theta \cos^2 \theta + 3 \sin^2 \theta \cos^4 \theta) \\ \sin^6 \theta + \cos^6 \theta &= 1 - 3 \sin^2 \theta \cos^2 \theta (\sin^2 \theta + \cos^2 \theta) \\&= 1 - 3 \sin^2 \theta \cos^2 \theta \\ \text{So LHS} &= \text{RHS as required}\end{aligned}$	[4]	M1  M1  M1  E1	<b>3.1a</b>  <b>3.1a</b>  <b>2.2a</b>  <b>2.1</b>	Use of double angle formula Allow 1 error  Use of given result with sin and cos Both sides seen but might not be equated  Use of $\sin^2 \theta + \cos^2 \theta = 1$  Convincing completion
10	(b)	$\begin{aligned}1 - \frac{3}{4} \sin^2 2\theta \text{ has min value when } \sin^2 2\theta = 1 \text{ oe} \\ \text{Min value is } \frac{1}{4}\end{aligned}$	[2]	M1  A1	<b>1.1</b>  <b>2.2a</b>	$\frac{1}{4}$ unsupported does not score

Question		Answer	Marks	AO	Guidance
<b>11</b>	(a)	55	<b>B1</b> [1]	<b>1.1</b>	Method need not be shown May be done BC
<b>11</b>	(b)	$\int_1^5 x^2 dx + \frac{5^2 + 1^2}{2} + \frac{1^2 - 2^2}{12} - \frac{5^2 - 6^2}{12}$ $\left[ \frac{x^3}{3} \right]_1^5 + \frac{26}{2} - \frac{3}{12} + \frac{11}{12} = \frac{124}{3} + \frac{41}{3} = 55$	<b>M1</b>  <b>A1</b> [2]	<b>1.1</b>  <b>2.2a</b>	Correct substitution into formula Condone $r$ but not $n$ instead of $x$ Square numbers may be evaluated  Correct completion. Integration may be done BC At least one step to be shown

Question	Answer	Marks	AO	Guidance
12	 <p>Each triangle has area half base times height so  <math>\frac{(2^2 - 1^2)}{2}</math>, <math>\frac{(3^2 - 2^2)}{2}</math> and <math>\frac{(4^2 - 3^2)}{2}</math>.</p>	B1 B1 B1 	3.2a 2.2a 2.4 [3]	Correct triangles identified At least one height correctly found and related to diagram Correct completion (including base =1 either labelled on at least one triangle or stated (probably in calculation)) Dep on B2

Question		Answer	Marks	AO	Guidance	
13		$\int_1^n x^2 dx + \frac{n^2 + 1^2}{2} + \frac{1^2 - 2^2}{12} - \frac{n^2 - (n+1)^2}{12}$ $\left[ \frac{x^3}{3} \right]_1^n + \frac{6n^2 + 6 + 1 - 4 - n^2 + n^2 + 2n + 1}{12}$ $\frac{n^3 - 1}{3} + \left[ \frac{6n^2 + 2n + 4}{12} \right]$ $\frac{2n^3 + 3n^2 + n}{6}$ $\frac{n(2n^2 + 3n + 1)}{6} = \frac{n(n+1)(2n+1)}{6}$	B1     B1     B1     B1	1.1a     1.1     2.1     2.2a	Substitute correctly into formula Condone $r$ but not $n$ instead of $x$  Integral correctly evaluated  Correct single fraction – may not be fully simplified  Correct completion Intermediate step needed Dep on B3	OR $\frac{n(n+1)(2n+1)}{6}$ $= \frac{2n^3 + 3n^2 + n}{6}$  OR convincing comparison of $\frac{n(n+1)(2n+1)}{6}$ and $\frac{n^3 - 1}{3} + \frac{6n^2 + 2n + 4}{12}$

Question		Answer	Marks	AO	Guidance	
14		$\frac{1}{2n} + \frac{1}{2} + \frac{1}{12} - \frac{1}{24} - \frac{1}{12n} + \frac{1}{12(n+1)}$ $\left[ \int_1^n \frac{1}{x} dx \right] = [\ln x]_1^n = \ln n - \ln 1 = \ln n$ $\ln n + \frac{13}{24} + \frac{6(n+1)-1}{12n(n+1)} = \ln n + \frac{13}{24} + \frac{6n+5}{12n(n+1)}$	<b>M1</b> <b>B1</b> <b>A1</b> [3]	<b>1.1a</b> <b>1.1</b> <b>2.2a</b>	Or better Integral correctly evaluated $\ln 1$ or “ $\ln n - 0$ ” seen. AG. Convincing completion	

Question		Answer	Marks	AO	Guidance	
15		$\sum_{r=1}^6 \frac{1}{r} = \frac{49}{20}$ $\ln 6 + \frac{13}{24} + \frac{36+5}{12 \times 6 \times 7} = 2.41477..$ $\% \text{ error} = 100 \times \frac{0.0352..}{2.45} = 1.438\%$ <p>This is less than 1.5%</p> <p>OR 1.5 % of actual and compare with 0.03523</p>	<b>B1</b> <b>B1</b> [2]	<b>1.1</b> <b>2.2a</b>	2.45 (need not have working) Convincing completion	May be done BC

H640/03

Mark Scheme

June 2023

**APPENDIX****Exemplar responses for Q9(b)**

<b>Response</b>	<b>Mark</b>

**Exemplar responses for Q9(d)(iii)**

<b>Response</b>	<b>Mark</b>

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