

ECEN 4638: Lab X.1P

Rane Brown
Kate Schneider

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1 Description

The purpose of this lab is to explore the torsion disc system and experimentally collect data that will help in the design of a proportional controller. The torsion disc system consists of a platform with three discs aligned above a driving motor. There are various configurations for the torsion disc system and this lab will use a basic setup described below.

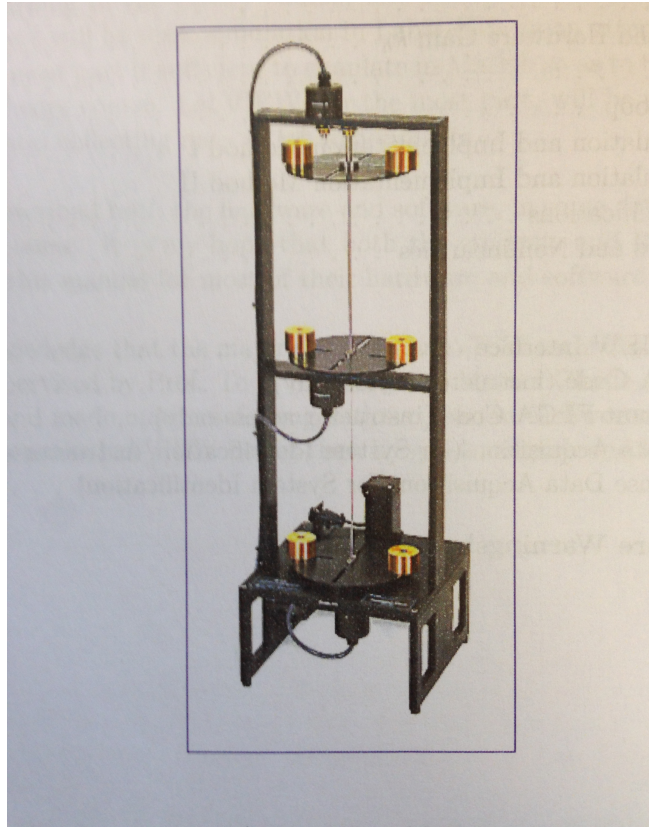


Figure 1: Torsion Disc System

2 Setup

There are three main components that will be necessary for this lab: LabView, Matlab, and the Torsion Disc System. LabView and Matlab do not require any setup as they are installed on all lab computers. On the other hand, the torsion disc system must be configured for proper use. For this experiment the top two discs and any attached weights should be removed. After the weights and discs are removed the system cables can be connected.

Detailed Steps

1. loosen allen key screws on all weights attached to the top two discs and remove the weights.
2. loosen allen key screws on top two discs and detach the discs (each disc is two pieces)

to the Simulink model used in LabX. As seen in figure ?? and figure ??, the results from LabView and simulink are comparable.

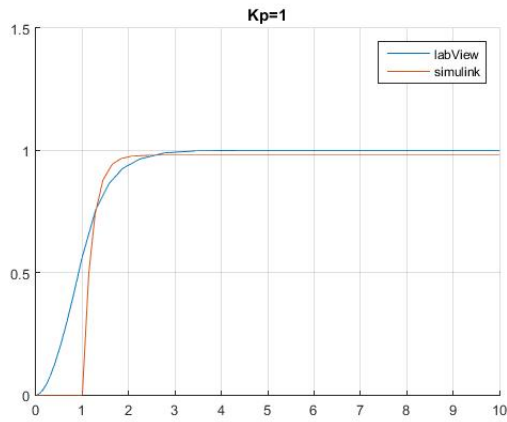


Figure 3: figure
P Controller $K_p = 1$

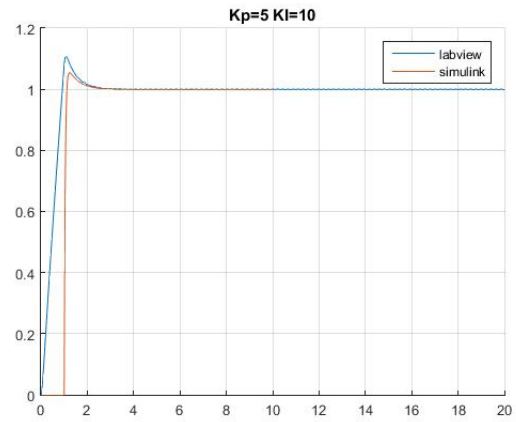


Figure 4: figure
PI Controller $K_p = 5$ $K_I = 10$

3.3 Disturbance

As a final experiment a disturbance was introduced to the LabView model that simulates a hill. The P and P_I values were chosen in order to produce a fast response with a small amount of overshoot and a reasonable settle time. In this case, values of $K_I = 20$ and $K_I = 60$ worked well. The results of this experiment are shown in figure ??.

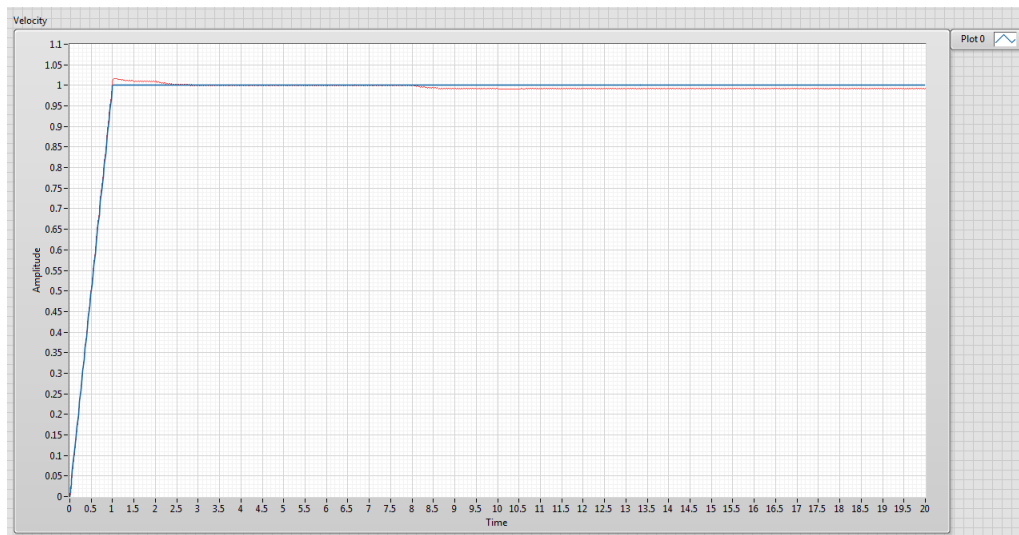


Figure 5: Response with disturbance

4 Data Collection

To create a LTI model for the Torsion Disc system it was necessary to collect data that could be used to estimate system parameters. A LabView model was used to control the system and collect necessary data. The LabView model shown in figure ?? was provided for this experiment and can be found on the ITLL share drive. Two experiments were conducted to collect the needed data. *NOTE: equations are found in section ??.*

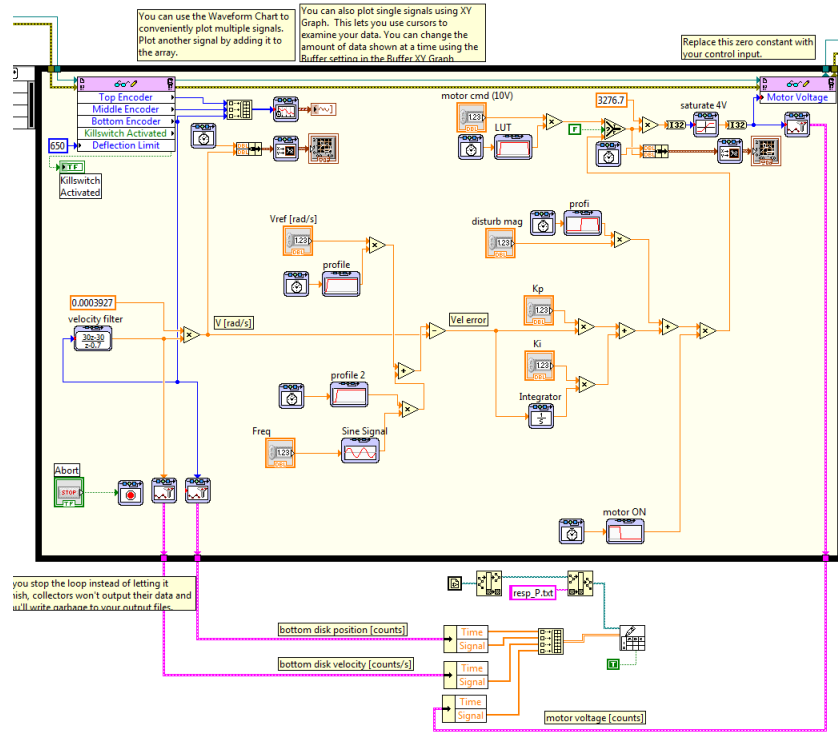


Figure 6: LabView Control System

4.1 No motor voltage

The first experiment was conducted with no power connected to the Torsion Disc motor. This was done in order to eliminate some of the parameters from the LTI model in order to estimate the value of c . Data was collected for three different weight positions as shown in table ?. Each weight position gives a different inertia value for the system. The data is collected by first selecting a weight position and then manually spinning the disc by hand. *If only 2 weights are used they must be located along the hub split line.*

Steps

1. set the weights to a desired radius on the lower disc
2. make sure the bolts holding the weights are firmly tightened

3. begin data collection in LabView
4. manually spin the disc and allow it to come to a stop
5. data is saved as a text file
6. change filename to reflect the weight position

Number of weights	Radius	Inertia J
4	9 cm	0.0192
4	7.5 cm	0.0143
2	4.5 cm	0.0043

Table 1: Weights and Position

4.2 Powered Torsion Disc System

The second data collection experiment was conducted with the power connected to the Torsion Disc system. In this case the values of various system parameters are adjusted in LabView while the weights remain in the same position. The collected data is then used to create a proportional controller.

Steps

1. set reference speed to 3.14 rad/sec
2. set disturbance to 0
3. set K_p to 1
4. adjust experiment length to 12 seconds in order to collect data as the system comes to a stop
5. **Ensure there is someone with their finger on the power of button in case the system goes unstable**
6. turn the power on
7. press the run button in LabView, data is saved as a text file
8. rename file to reflect parameter values
9. repeat for the values listed in below table

Fill in values

Reference rad/sec	K_p	Disturbance
rad/sec	k_p	dist
rad/sec	k_p	dist
rad/sec	k_p	dist

Table 2: Data Collection Parameters

5 LTI Model

The Torsion Disc system can be modeled as an LTI system with the below equation.

$$J\dot{\omega} + c\omega = k_h u \quad (1)$$

Where J = total system inertia, ω = velocity rad/sec, c = system drag, k_h = hardware gain, u = reference.

5.1 Calculating parameter J

The inertia of the system can be calculated from the system parameters (inertia of the torsion disk, J_{disk} , inertia of the motor, J_{motor} , and inertia of the weights, J_{weight}) as follows:

$$J_{disk} = 0.0019 \quad (2)$$

$$J_{motor} = 0.0005 \quad (3)$$

$$J_{weight} = \sum_{i=1}^N \frac{1}{2} m r^2 + m R^2 \quad (4)$$

Thus the total inertia is:

$$J_{tot} = J_{disk} + J_{motor} + J_{weight}$$

$$J_{tot} = 0.0019 + 0.0005 + \sum_{i=1}^N \frac{1}{2} m r^2 + m R^2 \quad (5)$$

5.2 Estimating parameter c

From the LTI model above, system drag c can be estimated as follows:

$$\omega(t) = e^{\frac{-c}{J}t_1} \omega(t_0)$$

$$\ln \left(\frac{\omega(t_1)}{\omega(t_0)} \right) = \frac{-c}{J} (t_1 - t_0)$$

$$c = \frac{-J \ln \left(\frac{\omega(t_1)}{\omega(t_0)} \right)}{t_1 - t_0} \quad (6)$$

To estimate c from collected data, the natural logarithm of angular velocity ω is plotted against time. A reasonably straight part of the curve is chosen, from time t_0 to time t_1 . The total system inertia and angular velocities $\omega(t_0)$ and $\omega(t_1)$ are then used with equation ?? to estimate system

drag c . Plots of filtered and unfiltered angular velocity data were analyzed, and filtering was found not to significantly affect the plot or c value obtained from the data. Thus, the unfiltered velocity data alone was used to estimate c . This was repeated for several experiments and c values were averaged, resulting in a c value of

$$c = 0.0079$$

A sample plot is shown below for $k_p = 1$ and a reference input of $\omega_{ref} = 6.28$ rad/s. The relatively linear section from $t_0 = 7.5s$ to $t_1 = 8.5s$ was chosen for estimating c . Choosing a time period when angular velocity was well above 0 reduced the influence of motor poles on the system and the estimation of c .

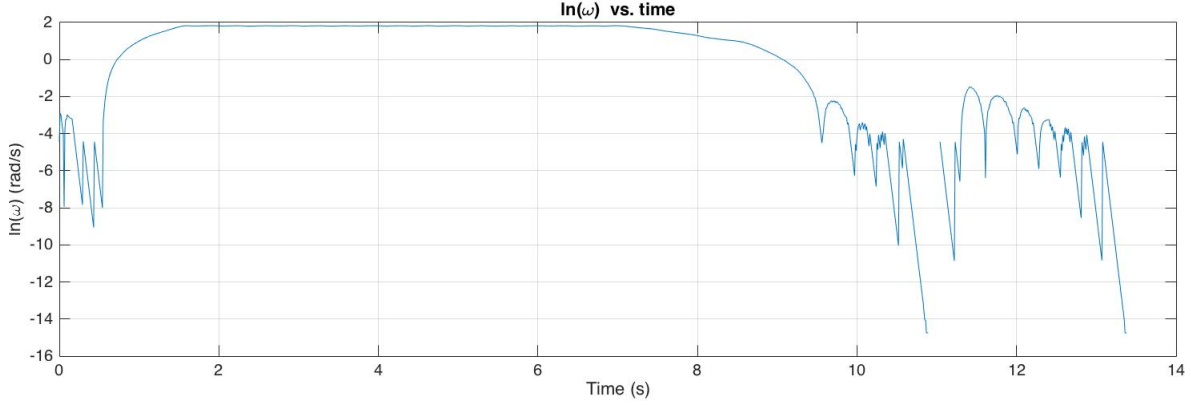


Figure 7: $\ln(\omega)$ vs. time

5.3 Estimating parameter k

When angular acceleration $\dot{\omega} = 0$, the equation describing our LTI system becomes

$$\begin{aligned} c\omega &= k_h u \\ k_h &= \frac{\omega}{u} c \end{aligned} \tag{7}$$

Hardware gain k_h can be estimated from the above equation, where c is calculated as in the previous section, ω is the average rotational velocity of the system, and u is the average motor voltage when the system is running at a constant speed. Parameters ω and u were plotted against time to determine when the system was at a constant speed. ω and u were averaged over the chosen time period and equation $k_h = \frac{\omega}{u} c$ was then used to estimate k_h . This was repeated for several experiments and ω and u values were averaged. The resulting k_h value is

$$k_h = 0.3598$$

This value for k_h is very close to the nominal value calculated from system parameters

<i>Pulley Magnification</i>	$k_p = 3$	$\frac{Nm}{Nm}$
<i>Drive Motor Torque Constant</i>	$k_m = 0.086$	$\frac{Nm}{Nm}$
<i>Drive Motor Amplifier Current Gain</i>	$k_a = 1.5$	$\frac{A}{V}$

$$k_{hnominal} = k_p k_m k_a$$

$$k_{hnominal} = 0.387$$

Sample plots used to evaluate average rotational velocity ω and average motor voltage u are shown below. The time period from $t_0 = 2$ seconds to $t_1 = 7$ seconds was used to calculate average ω and u .

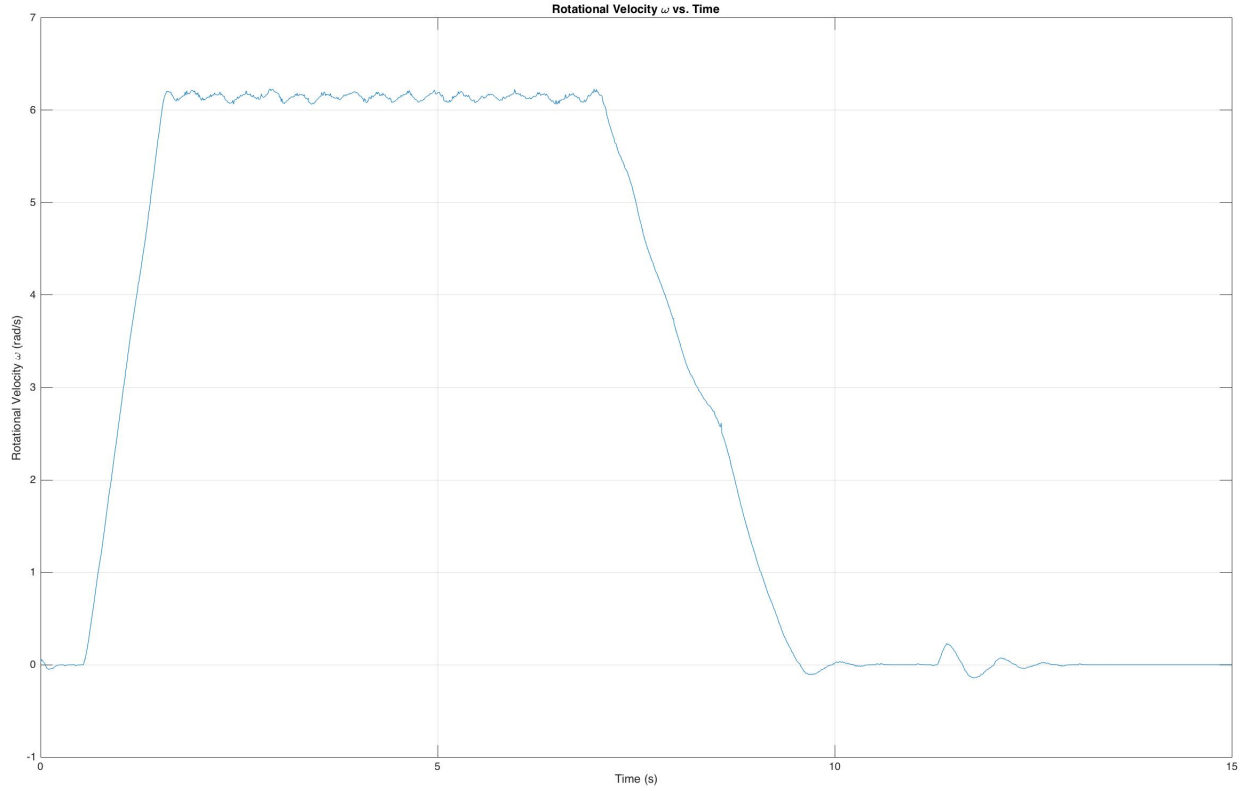


Figure 8: Rotational Velocity ω vs. Time

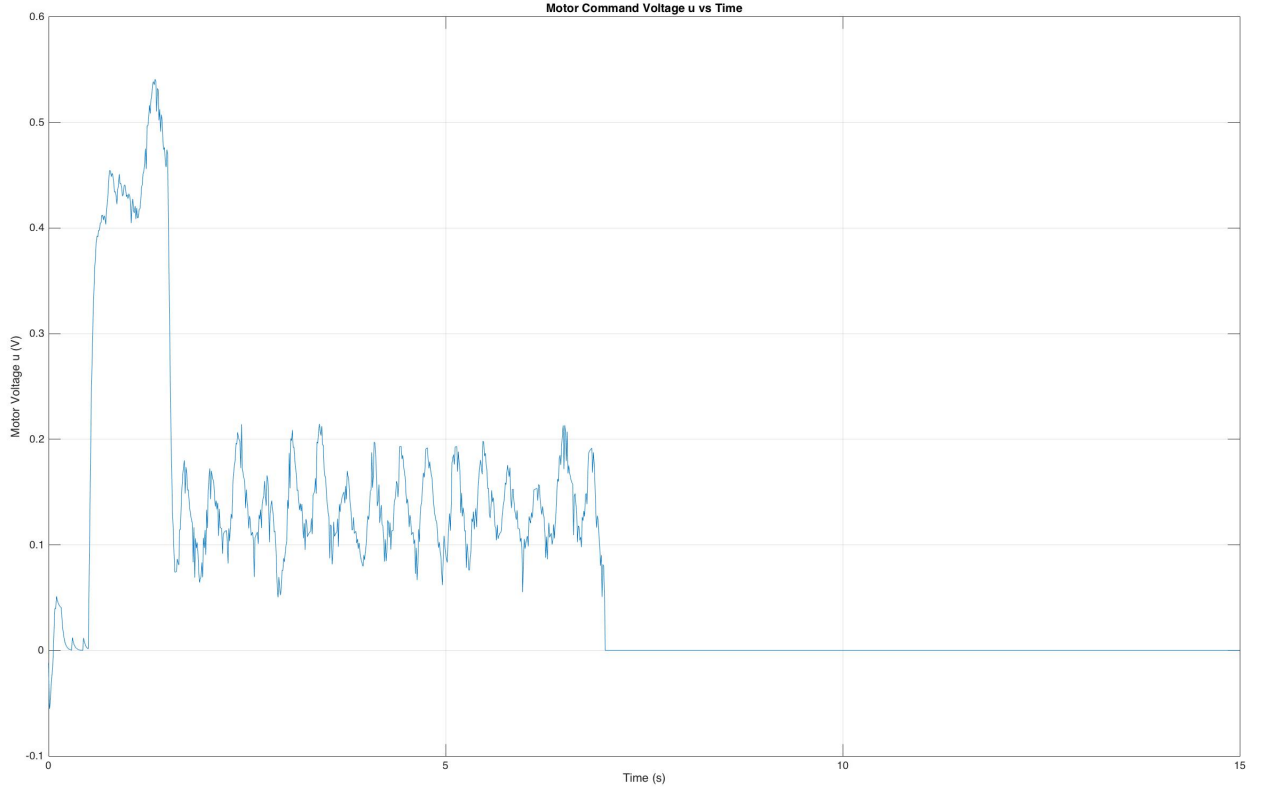


Figure 9: Motor Voltage u vs. Time

6 Introducing sinusoid to reference

6.1 Frequency response and Bode analysis

With proportional control k_p , we see that the closed-loop transfer function of our system is

$$H(s) = \frac{\frac{k_p k}{J}}{s + \frac{c + k_p k}{J}} \quad (8)$$

Substituting our values for k_p and c in the system, for a gain of $k = 1$, and an arrangement of 4 masses at 9 cm from the center of the disk ($J = 0.0192$), the transfer function becomes

$$H(s) = \frac{18.74}{s + 19.15} \quad (9)$$

A Bode plot of the system transfer function is shown below.

The bandwidth of the system is determined from the Bode plot to be 19.015 Hz.

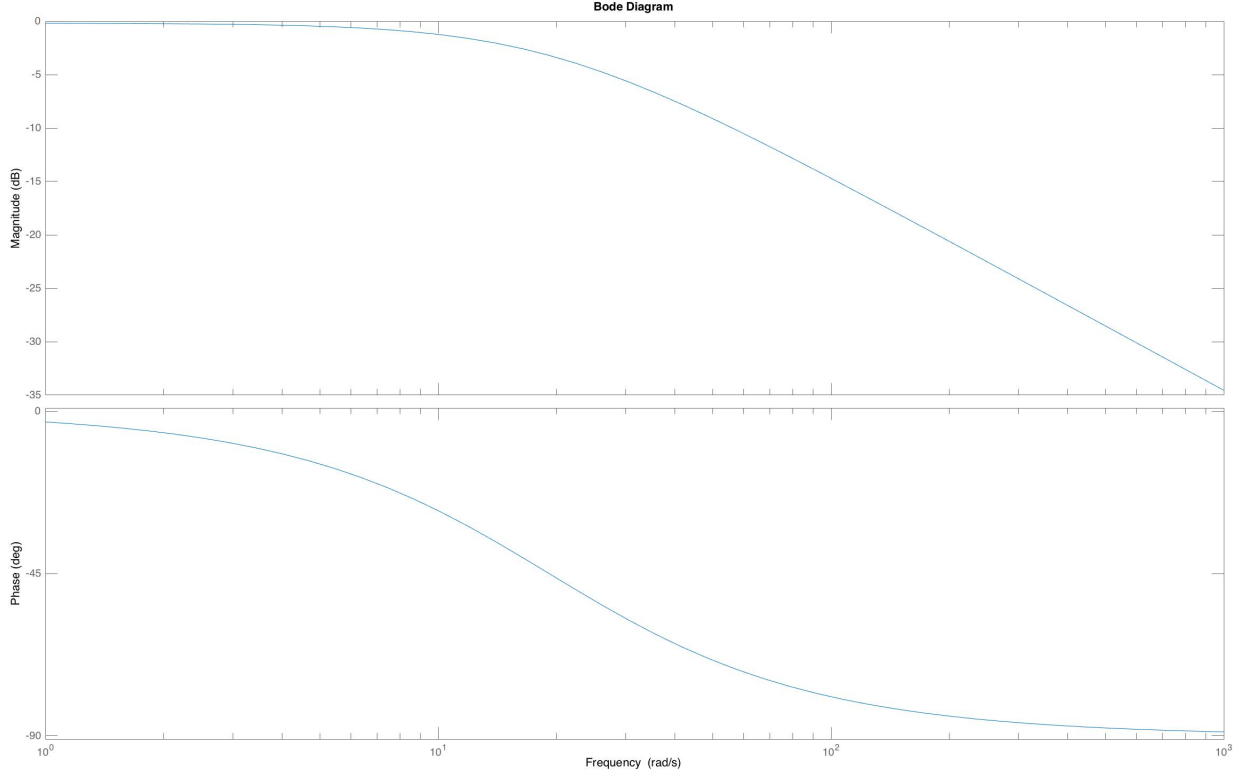


Figure 10: Bode Plot of System Transfer Function $H(s)$

6.2 System response to sinusoidal input

A sinusoidal input can be introduced to the system to further investigate the frequency response and time/phase delay of the system. For the LTI model, the introduction of a time delay results in the system equation

$$J(\omega b_{\omega} \cos(\omega t) - \omega a_{\omega} \sin(\omega t) + c(a_{\omega} \cos(\omega t) + b_{\omega} \sin(\omega t))) = a_u \cos(\omega(t - T_D)) + b_u \sin(\omega(t - T_D)). \quad (10)$$

This representation of the system is explored in more detail in the third data collection experiment, which was conducted with the power connected to the Torsion Disc system and a sinusoidal reference input $\delta V_{ref} = 2 \sin \pi f t$ added to the constant reference input. In this case the values of system parameters k_p and f are adjusted in LabView while the weights remain in the same position. The collected data is then used to investigate frequency response of the system.

Steps

1. set reference speed to 6.28 rad/sec

2. set disturbance to 0
3. set K_p to 1
4. adjust experiment length to 15 seconds in order to collect data as the system comes to a stop
5. **Ensure there is someone with their finger on the power of button in case the system goes unstable**
6. turn the power on
7. press the run button in LabView, data is saved as a text file
8. rename file to reflect parameter values
9. repeat for the values listed in below table

Reference rad/sec	K_p	Frequency
6.28	0.5	4Hz
6.28	1	5Hz

Table 3: Frequency Response Parameters

From further experimentation with the system, we found that increasing the frequency of our input sinusoid above the bandwidth of the system did not cause the expected roll-off in amplitude even with a slight increase in k_p , $k_p > \text{what was the highest } k_p \text{ where this worked?}$. The input motor voltage was saturated for too high a k_p , suggesting additional dynamics at play in our system.

6.3 Fourier fit of sinusoidal input and response

The sinusoidal input for motor voltage u and output for rotational velocity ω can be graphically fit using fourier series, and the fourier coefficients can be obtained from this nonlinear curve fitting. Below the data for u and ω are plotted (data points) along with their best fit sinusoids (blue line) for $k_p = 1$ and $f = 5\text{Hz}$.

The fourier coefficients obtained from the sinusoidal curve fitting are

$$a_\omega = -0.5444 \quad b_\omega = 1.289 \quad a_u = 2.712 \quad b_u = -1.435$$

Inserting the above parameters into the fourier form of our LTI system equation, and separating into sine and cosine parts, we get

$$J\omega b_\omega(\omega) + ca_\omega(\omega) = k(a_u(\omega)\cos(\omega T_D) - b_u(\omega)\sin(\omega T_d)) \quad (11)$$

$$J\omega 1.289 + (-0.544)c = k(2.712\cos(\omega T_D) + 1.435\sin(\omega T_d)) \quad (12)$$

what to do with this?? The time delay T_D is estimated to be on the order of several hundredths of a second. Time delay and its impact on system stability will be examined in further experiments involving the torsion disk system.

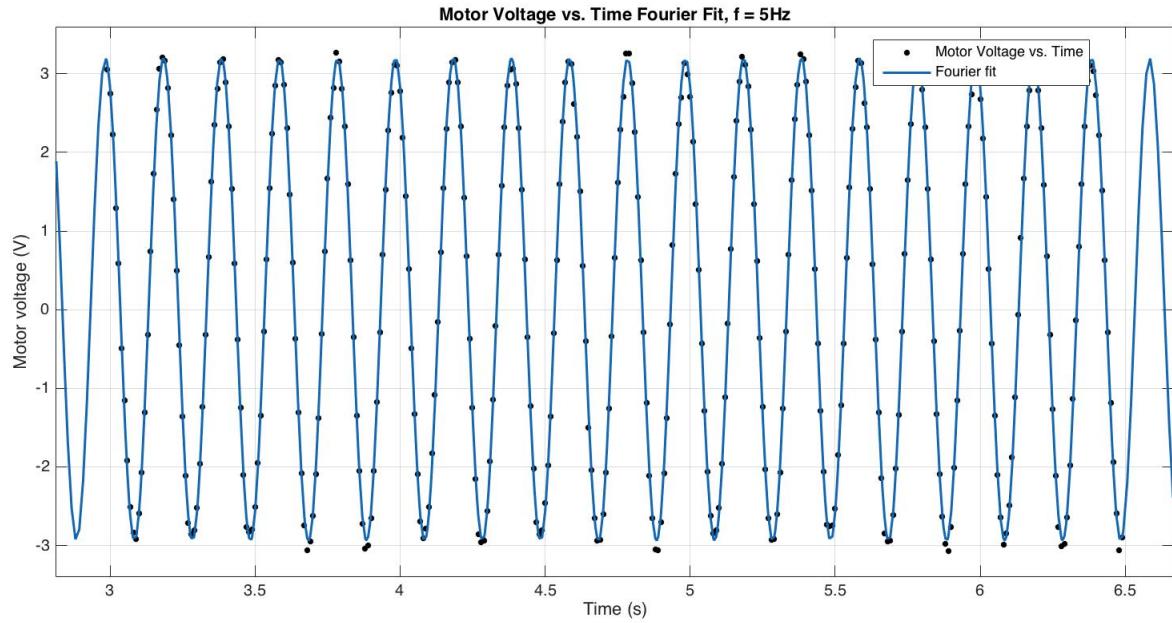


Figure 11: Fourier Fit of Motor Command Voltage u

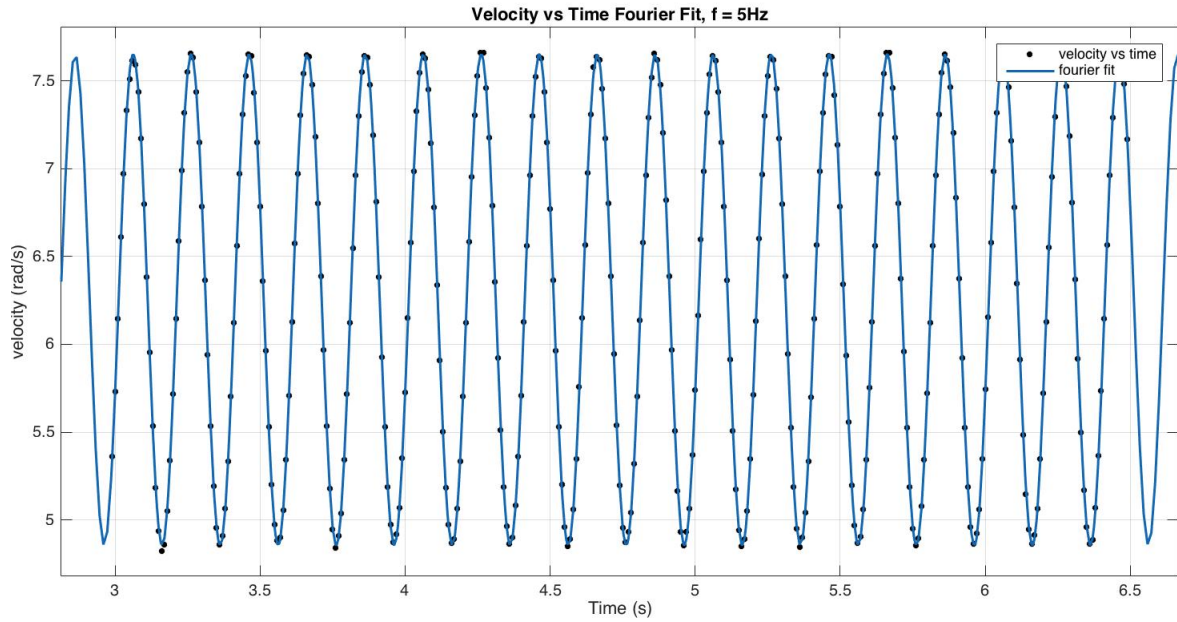


Figure 12: Fourier Fit of Rotational Velocity ω

7 Proportional Controller Design

The proportional controller for the torsion disk cruise control system must provide a relatively fast response, minimal overshoot, little error in steady state when tracking a constant velocity reference

input, and some small finite error in disturbance rejection as well, so that bumps and hills do not greatly affect the system's performance. These objectives suggest a relatively large value for k_p . However, when a non-constant input, such as a sinusoid, is introduced to the system, it was discovered that a much smaller value of k_p was desired to avoid motor voltage saturation and to keep the system stable.