# ctheorems

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## https://github.com/sahasatvik/typst-theorems

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# 1. Introduction

The ctheorems package provides Typst functions that help create numbered theorem environments. This is heavily inspired by the \newtheorem functionality of LaTeX.

A *theorem environment* lets you wrap content together with automatically updating *numbering* information. Such environments use internal state counters for this purpose. Environments can

- share the same counter (Theorems and Lemmas often do so)
- keep a global count, or be attached to
  - other environments (Corollaries are often numbered based upon the parent Theorem)
  - headings
- have a numbering level depth fixed (for instance, use only top level heading numbers)
- be referenced elsewhere in the document, via labels

# 2. Using ctheorems

Import all functions provided by ctheorems using

```
#import "@preview/ctheorems:1.1.2": *
#show: thmrules
```

The second line is crucial for displaying thmenvs and references correctly!

The core of this module consists of thmenv. The functions thmbox, thmplain, and thmproof provide some simple defaults for the appearance of thmenvs.

## 3. Feature demonstration

Create box-like *theorem environments* using thmbox, a wrapper around thmenv which provides some simple defaults.

Such definitions are convenient to place in the preamble or a template; use the environment in your document via

```
#theorem("Euclid")[
  There are infinitely many primes.
] <euclid>
```

This produces the following.

```
Theorem 3.1 (Euclid): There are infinitely many primes.
```

Note that the name is optional. This theorem environment will be numbered based on its parent heading counter, with successive theorems automatically updating the final index.

The <euclid> label can be used to refer to this Theorem via the reference @euclid. Go to Section 3.5 to read more.

You can create another environment which uses the same counter, say for *Lemmas*, as follows.

```
Lemma 3.2: If n divides both x and y, it also divides x - y.
```

You can *attach* other environments to ones defined earlier. For instance, *Corollaries* can be created as follows.

```
If n divides two consecutive natural numbers, then n = 1.
```

**Corollary 3.2.1**: If n divides two consecutive natural numbers, then n = 1.

Note that we have provided a numbering string; this can be any valid numbering pattern as described in the <u>numbering</u> documentation.

#### 3.1. Proofs

The thmproof function gives nicer defaults for formatting proofs.

```
#let proof = thmproof("proof", "Proof")

#proof([of @euclid])[
   Suppose to the contrary that $p_1, p_2, dots, p_n$ is a finite enumeration
   of all primes. Set $P = p_1 p_2 dots p_n$. Since $P + 1$ is not in our list,
   it cannot be prime. Thus, some prime factor $p_j$ divides $P + 1$. Since
   $p_j$ also divides $P$, it must divide the difference $(P + 1) - P = 1$, a
   contradiction.
]
```

Proof of <u>Theorem 3.1</u>: Suppose to the contrary that  $p_1, p_2, ..., p_n$  is a finite enumeration of all primes. Set  $P = p_1 p_2 ... p_n$ . Since P+1 is not in our list, it cannot be prime. Thus, some prime factor  $p_j$  divides P+1. Since  $p_j$  also divides P, it must divide the difference (P+1)-P=1, a contradiction.

If your proof ends in a block equation, or a list/enum, you can place qedhere to correctly position the qed symbol.

```
#theorem[
   There are arbitrarily long stretches of composite numbers.]
#proof[
   For any $n > 2$, consider $
      n! + 2, quad n! + 3, quad ..., quad n! + n #qedhere
   $
]
```

**Theorem 3.1.1**: There are arbitrarily long stretches of composite numbers.

*Proof*: For any n > 2, consider

$$n! + 2, \quad n! + 3, \quad \dots, \quad n! + n$$

Caution: The qedhere symbol does not play well with numbered/multiline equations!

You can set a custom qed symbol (say  $\square$ ) by setting the appropriate option in thmrules as follows.

```
#show: thmrules.with(qed-symbol: $square$)
```

# 3.2. Suppressing numbering

Supplying numbering: none to an environment suppresses numbering for that block, and prevents it from updating its counter.

```
#let example = thmplain(
   "example",
   "Example"
).with(numbering: none)

#example[
   The numbers $2$, $3$, and $17$ are prime.
]
```

Example: The numbers 2, 3, and 17 are prime.

Here, we have used the thmplain function, which is identical to thmbox but sets some plainer defaults. You can also write

```
#lemma(numbering: none)[
  The square of any even number is divisible by $4$.
]
#lemma[
  The square of any odd number is one more than a multiple of $4$.
]
```

**Lemma**: The square of any even number is divisible by 4.

**Lemma 3.2.1**: The square of any odd number is one more than a multiple of 4.

Note that the last *Lemma* is *not* numbered 3.1.2!

You can also override the automatic numbering as follows.

```
#lemma(number: "42")[
   The square of any natural number cannot be two more than a multiple of 4.
]
```

Lemma 42: The square of any natural number cannot be two more than a multiple of 4.

Note that this does *not* affect the counters either!

### 3.3. Limiting depth

You can limit the number of levels of the base numbering used as follows.

```
#definition("Prime numbers")[
  A natural number is called a _prime number_ if it is greater than $1$ and
  cannot be written as the product of two smaller natural numbers. <prime>
1
```

**Definition 3.1** (Prime numbers): A natural number is called a *prime number* if it is greater than 1 and cannot be written as the product of two smaller natural numbers.

Note that this environment is *not* numbered 3.2.1!

```
#definition("Composite numbers")[
  A natural number is called a _composite number_ if it is greater than $1$
  and not prime.
]
```

**Definition 3.2** (Composite numbers): A natural number is called a *composite number* if it is greater than 1 and not prime.

Setting a base\_level higher than what base provides will introduce padded zeroes.

```
#example(base_level: 4, numbering: "1.1")[
  The numbers $4$, $6$, and $42$ are composite.
]
```

Example 3.3.0.0.1: The numbers 4, 6, and 42 are composite.

# 3.4. Custom formatting

The thmbox function lets you specify rules for formatting the title, the name, and the body individually. Here, the title refers to the head and number together.

```
#let proof-custom = thmplain(
   "proof",
   "Proof",
   base: "theorem",
   titlefmt: smallcaps,
   bodyfmt: body => [
     #body #h(1fr) $square$ // float a QED symbol to the right
   ]
).with(numbering: none)

#lemma[
   All even natural numbers greater than 2 are composite.
]
#proof-custom[
   Every even natural number $n$ can be written as the product of the natural numbers $2$ and $n\/2$. When $n > 2$, both of these are smaller than $2$ itself.
]
```

### Lemma 3.4.1: All even natural numbers greater than 2 are composite.

PROOF: Every even natural number n can be written as the product of the natural numbers 2 and n/2. When n > 2, both of these are smaller than 2 itself.

You can go even further and use the thmenv function directly. It accepts an identifier, a base, a base level, and a fmt function.

```
#let notation = thmenv(
                              // identifier
  "notation",
                              // base - do not attach, count globally
  none,
                              // base_level - use the base as-is
  none,
  (name, number, body, color: black) => [
                              // fmt - format content using the environment
                              // name, number, body, and an optional color
    #text(color)[#h(1.2em) *Notation (#number) #name*]:
    #h(0.2em)
    #bodv
    \#v(0.5em)
).with(numbering: "I") // use Roman numerals
#notation[
  The variable $p$ is reserved for prime numbers.
#notation("for Reals", color: green)[
  The variable $x$ is reserved for real numbers.
```

**Notation (I)**: The variable p is reserved for prime numbers.

**Notation** (II) for Reals: The variable x is reserved for real numbers.

Note that the color: green named argument supplied to the theorem environment gets passed to the fmt function. In general, all extra named arguments supplied to the theorem will be passed to fmt. On the other hand, the positional argument "for Reals" will always be interpreted as the name argument in fmt.

```
#lemma(title: "Lem.", stroke: 1pt)[
  All multiples of 3 greater than 3 are composite.
]
```

```
Lem. 3.4.2: All multiples of 3 greater than 3 are composite.
```

Here, we override the title (which defaults to the head) as well as the stroke in the fmt produced by thmbox. All block arguments can be overridden in thmbox environments in this way.

#### 3.5. Labels and references

You can place a <label> outside a theorem environment, and reference it later via @ references! For example, go back to <a href="https://example.com/nearth-

Recall that there are infinitely many prime numbers via @euclid.

Recall that there are infinitely many prime numbers via Theorem 3.1.

You can reference future environments too, like @oddprime[Cor.].

You can reference future environments too, like Cor. 3.5.1.1.

```
#lemma(supplement: "Lem.", refnumbering: "(1.1)")[
  All primes apart from $2$ and $3$ are of the form $6k plus.minus 1$.
] <primeform>
```

You can modify the supplement and numbering to be used in references, like <a href="mailto:oprimeform">oprimeform</a>.

#### **Lemma 3.5.1**: All primes apart from 2 and 3 are of the form $6k \pm 1$ .

You can modify the supplement and numbering to be used in references, like Lem. (3.5.1).

Caution: Links created by references to thmenvs will be styled according to #show link: rules.

## 3.6. Overriding base

```
#let remark = thmplain("remark", "Remark", base: "heading")
#remark[
   There are infinitely many composite numbers.
]

#corollary[
   All primes greater than $2$ are odd.
] <oddprime>
#remark(base: "corollary")[
   Two is a _lone prime_.
]
```

*Remark 3.6.1*: There are infinitely many composite numbers.

Corollary 3.5.1.1: All primes greater than 2 are odd.

Remark 3.5.1.1.1: Two is a lone prime.

This remark environment, which would normally be attached to the current *heading*, now uses the corollary as a base.

# 4. Function reference

#### 4.1. thmenv

The thmenv function produces a *theorem environment*.

The fmt function must accept a theorem name, number, body, and produce formatted content. It may also accept additional positional arguments, via args.

A *theorem environment* is itself a map of the following form.

Positional arguments in args are as follows

• name: The name of the theorem, typically displayed after the title.

All additional named arguments in args will be passed on to the associated fmt function supplied in thmenv.

#### 4.2. thmbox and thmplain

The thmbox wraps thmenv, supplying a box-like fmt function.

```
#let thmbox(
             // identifier
 identifier,
               // head - common name, used in the title
 head.
 padding: (top: 0.5em, bottom: 0.5em),
               // box padding, passed to #pad
 namefmt: x \Rightarrow [(\#x)], // formatting for name
 bodyfmt: x => x,
               // formatting for body
 separator: [\#h(0.1em):\#h(0.2em)],
               // separator inserted between name and body
 ) = { ... }
```

The thmbox function sets the following defaults for the block.

```
(
  width: 100%,
  inset: 1.2em,
  radius: 0.3em,
  breakable: false,
)
```

The thmplain function is identical to thmbox, except with plainer defaults.

```
#let thmplain = thmbox.with(
  padding: (top: 0em, bottom: 0em),
  breakable: true,
  inset: (top: 0em, left: 1.2em, right: 1.2em),
  namefmt: name => emph([(#name)]),
  titlefmt: emph,
)
```

#### 4.3. thmproof, proof-bodyfmt and gedhere

The thmproof function is identical to thmplain, except with defaults appropriate for proofs.

The proof-bodyfmt function is a bodyfmt function that automatically places a qed symbol at the end of the body.

You can place #qedhere inside a block equation, or at the end of a list/enum item to place the qed symbol on the same line.

#### 4.4. thmrules

The thmrules show rule sets important styling rules for theorem environments, references, and equations in proofs.

# 5. Acknowledgements

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- MJHutchinson for suggesting and implementing the base level and base: none features,
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- DVDTSB for contributing
  - the idea of passing named arguments from the theorem directly to the fmt function.
  - the number: ... override feature.
  - the title: ... override feature in thmbox.
- The awesome devs of <u>typst.app</u> for their support.