

update $\rightarrow dt$

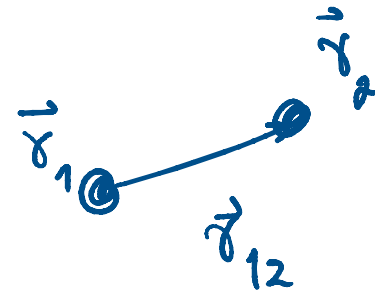
$$\begin{cases} \vec{r}(t)_i, & i \in [1, N] \\ \vec{v}(t)_i, & i \in [1, N] \end{cases}$$

Numerical integration

$$\vec{a}(t)_i = \frac{\vec{F}_i}{m_i}$$

$$U_{ij} = \frac{1}{4\pi\epsilon} \frac{q_i q_j}{r_{ij}}$$

$$U_{\text{tot}} = \sum_{i>j} U_{ij}$$



$$\vec{F}_{j \rightarrow i} = -\Delta U_{ij}$$

$$\vec{F}_i = \sum_{i \neq j} \vec{F}_{j \rightarrow i}$$

Energy

1) Coulomb

$$U_{ij} = \frac{1}{4\pi\epsilon_0} \frac{q_i q_j}{r_{ij}^2}$$

Attraction
Repulsive

2) vdW

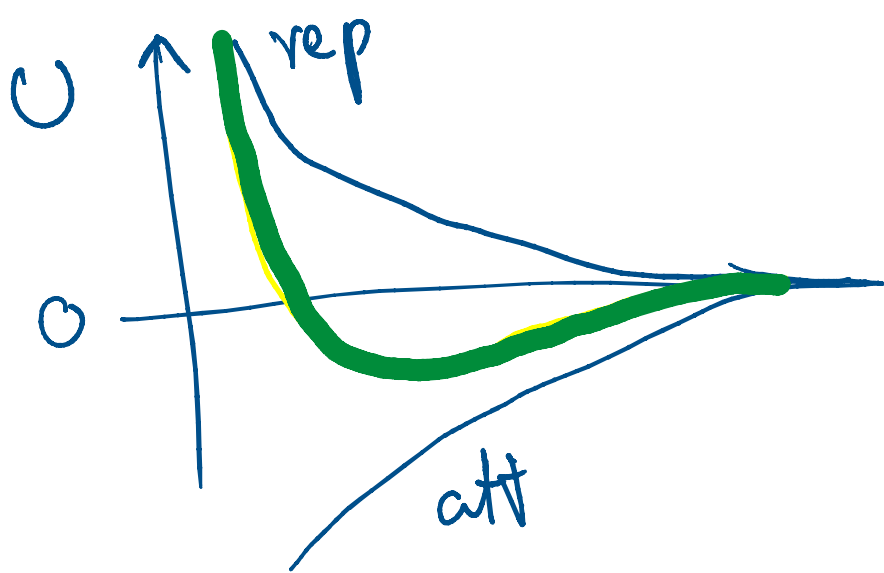
$$U_{\text{vdW}} = -\frac{A}{r^6}$$

Attraction - Cohesive

dipole-dipole interaction

$r \rightarrow \infty$ 3) Electronic

$$U = -\frac{A}{r^{12}}$$



velocity-verlet scheme

No velocity in calculation

$$\vec{r}(t+dt) \underset{\text{Taylor expansion}}{=} \vec{r}(t) + \frac{d\vec{r}(t)}{dt} \cdot dt + \frac{1}{2} \frac{d^2\vec{r}(t)}{dt^2} dt^2 + \dots \quad - (1)$$

$$\vec{r}(t-dt) \underset{\text{Taylor expansion}}{=} \vec{r}(t) - \frac{d\vec{r}(t)}{dt} \cdot dt + \frac{1}{2} \frac{d^2\vec{r}(t)}{dt^2} dt^2 - \dots \quad - (2)$$

① - ②

$$\vec{r}(t+dt) - \vec{r}(t-dt) = 2 \frac{d\vec{r}(t)}{dt} \cdot dt$$

$$v(t) = \frac{\vec{r}(t+dt) - \vec{r}(t-dt)}{2 \cdot dt}$$