

Analysis of Multi-Scale Energy Markets using Stochastic Optimization Techniques

ISyE 719 Course Project

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Abstract

Electricity markets operate at multiple timescales (from hours to milliseconds) to ensure that supply and demands are matched in real time. These markets involve uncertainties because future electricity prices and demands are unknown at the time of decision-making, e.g. energy sale and purchase commitments by generators. We use stochastic programming techniques to study flexibility and economic opportunities provided by a battery in these markets, namely day-ahead (1-hour timescale) and real-time (5-minute timescale) markets. In this work we consider uncertainty only in electricity loads and determine optimal participation strategies using methods like receding horizon scheme, dual dynamic programming and *fullproblem (scenario sampling)*. We also determine bounds on expected policy costs by using perfect information and two-stage approximation (with restriction on states). We compare the costs of participation in exclusively in day-ahead market and both day-ahead and real-time markets. Our results show that market participation only in day-ahead energy markets can *significantly* reduce economic flexibility as compared to participating in both levels of markets.

1 Introduction

A diverse set of energy systems such as generators, batteries, wind turbines and flywheels can participate in electricity markets. This participation is governed by rules set by ISOs (Independent System Operators) such as California ISO, PJM (Pennsylvania-New Jersey-Maryland) Interconnection and Midcontinent ISO, under whose jurisdiction the market falls. The markets are structured at multiple time levels, namely day ahead (hourly market commitments) and real time markets (commitments ranging from minutes to seconds). In day-ahead markets the electricity is traded in intervals of 1 hour with the prices being constant in each interval of 1 hour and varying with intervals. Real time markets, on the other hand can have varying time scales depending on the ISO operating it. The real-time market is a spot market in which utilities can buy power to meet the last few increments of demand not covered in their day ahead schedules. It is also the market that secures energy reserves, held ready and available for ISO use if needed, and the energy needed to regulate transmission line

stability¹. The frequency of energy price variation is different for day-ahead and real time markets (Figure 1).

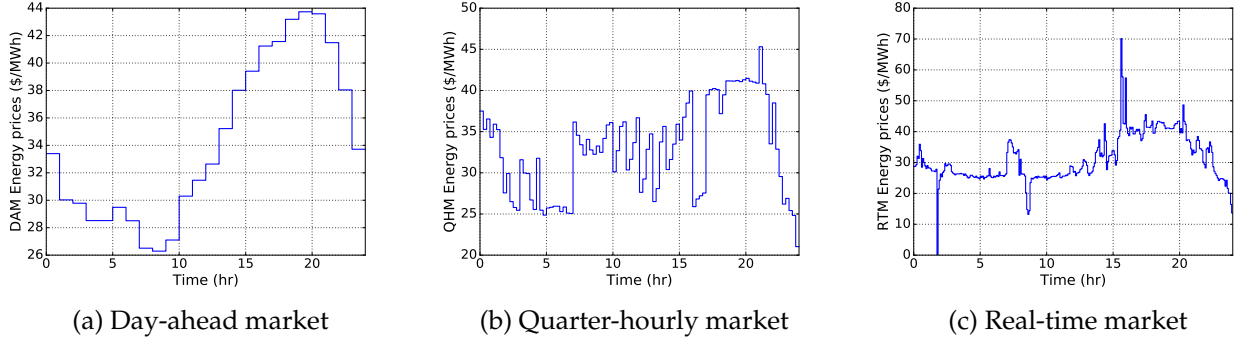


Figure 1: Energy prices for one day in the markets in California

Apart from price variations, the introduction of more renewable power sources in the grid such as wind and solar energy, there are greater variations and uncertainties in the net load as well. Since these sources depend on intermittent conditions such as weather, they introduce slow dynamics to the grid. Thus systems with faster dynamic responses such as battery and building systems are becoming increasingly important to balance these fluctuations and provide dynamic flexibility to the power grid. Also, factors such as transmission losses, generation cost and congestion affect the value of products (energy, regulation, spinning, non-spinning reserves) offered at different timescales. These fluctuations being inherently uncertain, determining the optimal participation policy requires analysis using stochastic optimization techniques.

2 Problem Definition and Decision-Making Setting

We consider a rechargeable Li-ion battery with a building that is inter-connected to the power grid for providing electricity services. Electricity services imply that batteries can provide power to or draw power from the grid. In our current setting, we do not consider participation in regulation or other ancillary services. The operator of the power grid (ISO) compensates the battery-owners for the electricity services provided. The goal for the battery-owners is to maximize the revenues generated by providing services to the grid and at the same time meeting the load demands from building. Any unmet load demand from the building is penalized with the corresponding electricity price in real time market.

We divide an annual dataset for electricity loads (available over 5-minute intervals) into 52 subsets of weekly load profiles, i.e 2016 intervals of 5-minute each. This division of data helps in capturing the different load profiles over the weekdays and the weekend. We then use these 52 weekly profiles to generate sample scenarios for our computational experiments (Section 4). Since the loads are correlated between time intervals, we formulate a multivariate normal distribution for weekly loads

¹<http://www.caiso.com/market/Pages/MarketProcesses.aspx>

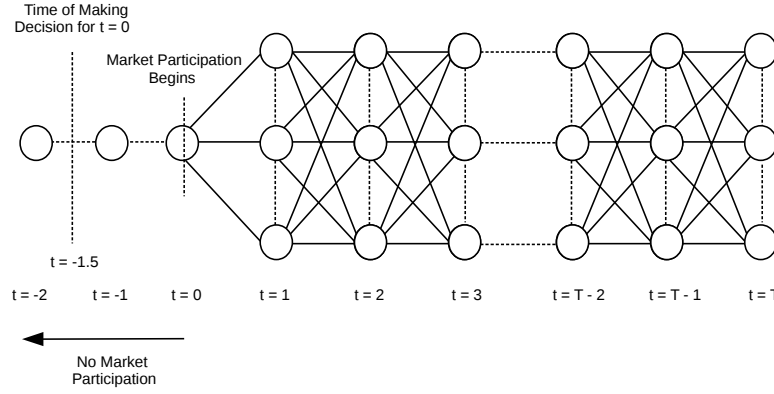


Figure 2: Scenario tree at the beginning of market participation

using a mean vector and a covariance matrix. The mean vector (of size 2016×1) is the mean of the 52 datasets, but the covariance matrix (of size 2016×2016) calculated directly from the 52 datasets cannot be used, since its rank can at most be 52. So we use the Ledoit-Wolf Covariance Estimator [1] (to tackle rank deficiency) for estimating a full rank covariance matrix. We generate 50 samples of load profiles (Figure 3) for a week using the mean and covariance matrix obtained.

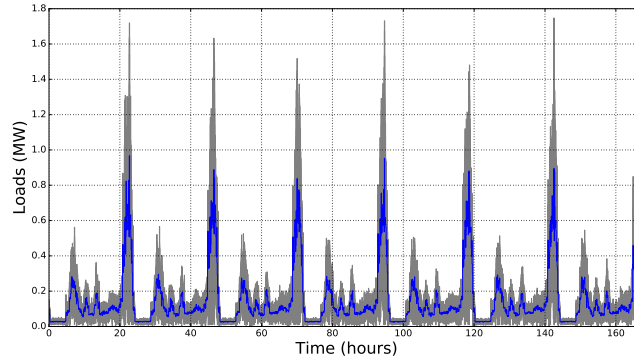


Figure 3: Load scenarios for a week

explain scenarios of loads, 12 between any two hours one scenario represents a profile of loads in 12 subintervals. participation begins at time $t = 0$ and we can take decision latest till 1.5 hours before any hour (according to market rule). so our decision making starts at -1.5 as shown in figure 2 and our participation begins at 0. so we consider battery and building as one system (building-battery system) just after goal. who try to min their total cost of operation and maximize the total revenue. under spikes figure - can use fast dynamic systems to capture the spikes to max the revenue potential. as seen from figure, dam is more smooth and less volatile. and average price is higher in dam.

Cosidering the price data for a full year to be known (deterministic) we can solve the optimization problem to maximize the annual revenues by operating a battery in the power grid for the whole year. In this work, we aim to solve this deterministic optimization problem with two approaches:

1. Simultaneous approach: In this approach, we formulate a single giant optimization problem for a full year and solve it to produce the optimal power and regulation capacities that the battery should operate with in each time interval in all the three markets.
2. Rolling (1 day) horizon approach: In this approach, we formulate an optimization problem for a day and solve it to produce the optimal power and regulation capacities for that day, then take the solutions at the end time-point of that day as the initial point for the next day, then formulate the optimization problem for the next day with those initial values and solve for the second day and sequentially we solve for the 365 days. It is called rolling horizon because in this approach we consider a horizon of 1 day and keep shifting the horizon to to the next day after solving the current day.

At the end, we will compare the two solutions and investigate the advantages and disadvantages of the two approaches.

investigate economic potential of various markets in stochastic setting i.e. compare expected revenue from different market and emphasize why participation in both is imp investigation of various solution methods subsection- sample avg approx of extensive form sussubset - upper and lower bound estimations stochastic dual dynamic programming receding horizon

In the U.S., generators/loads provide the hierarchical market structure with addition flexibility via *regulation* and *reserve* ancillary service products.

3 Optimization Model for Building-Battery System

3.1 Deterministic Setting

First, we formulate an optimization problem to minimize the cost (or maximize revenue) for the building-battery system operating in the electricity market in a deterministic setting assuming no uncertainty in any of the market and demand quantities. In this formulation, the building-battery system participates in the market at two timescales, hourly and 5-minute intervals. Since the price and load signals are discrete, real-time prices and loads available at 5-minute intervals and day-ahead prices at hourly intervals, we make the zero-order hold assumption, i.e. these time-varying signals are constant within an interval of corresponding duration of their timescale. We also assume that the energy stored in the battery before beginning of market participation is fixed at E_0 . With these assumptions, we develop the optimization problem formulation for the system is described below.

3.1.1 Sets used in the model

$$\begin{aligned}\mathcal{T}_{\mathcal{R}} &:= \{1, \dots, n_{\text{rtm}}\} \\ \mathcal{T}_{\mathcal{D}} &:= \{1, \dots, n_{\text{dam}}\}\end{aligned}$$

Here, $\mathcal{T}_{\mathcal{R}}$ is the set of time indices corresponding to each 5-minute subintervals in the real-time market within each hour, so $n_{\text{rtm}} = 12$. $\mathcal{T}_{\mathcal{D}}$ is the set of time indices corresponding to the hourly intervals of the day-ahead market. n_d can be chosen appropriately for any number of hours we plan to schedule the market participation policy for the building-battery system.

3.1.2 Time discretization used in the model

A time instance for a day-ahead market variable in the model is represented by only the index k ($k \in \mathcal{T}_D$) which corresponds to the interval between hours $k - 1$ and k . On the other hand, a time instance for a real-time variable in the model is represented by index (i, k) , where $i \in \mathcal{T}_R$ and $k \in \mathcal{T}_D$. The indices i and k in a time instance (i, k) for a real-time variable correspond to the end of the respective 5-minute interval. For example, the time instance $(5, 7)$ corresponds to the end of the interval between 4th and 5th 5-minute interval within the 7th hour.

So, if a variable or time-varying parameter is indexed by only one index k it implies that it varies at hourly intervals and belongs to the day-ahead market, whereas a variable or time-varying parameter indexed by (i, k) is a real-time variable.

3.1.3 Parameters in the model:

- **Market parameters:**

- $\pi_k, \forall k \in \mathcal{T}_D$: Electricity price in day-ahead market in the interval between hour $k - 1$ to k
- $\pi_{i,k}, \forall i \in \mathcal{T}_R, k \in \mathcal{T}_D$: Electricity price in real-time market in the 5-minute interval between $(i - 1, k)$ and (i, k) within k^{th} hour
- Δt : Time interval (in unit of hours) in the real-time market (which is 5 minutes)

- **Battery parameters:**

- $E_{max} = 0.5$ MWh: Energy storage capacity of the battery
- $P_{max} = 0.5$ MW: Maximum discharging or charging rate of the battery
- $E_0 = E_{max}$: Energy stored in the battery before beginning of market participation

- **Building loads:**

- $L_{i,k}, \forall i \in \mathcal{T}_R, k \in \mathcal{T}_D$: Building loads in the 5-minute interval between $(i - 1, k)$ and (i, k) within k^{th} hour

3.1.4 Variables in the model:

- **Decision variables:**

- $P_k, \forall k \in \mathcal{T}_D$: Power committed by battery in day-ahead market in the interval between hour $k - 1$ to k
- $P_{i,k}, \forall i \in \mathcal{T}_R, k \in \mathcal{T}_D$: Power committed by battery in real-time market in the 5-minute interval between $(i - 1, k)$ and (i, k) within k^{th} hour
- $L_{s,i,k}, \forall i \in \mathcal{T}_R, k \in \mathcal{T}_D$: Power supplied by battery to the building in the 5-minute interval between $(i - 1, k)$ and (i, k) within k^{th} hour

- **State variables:**

- $E_{i,k}, \forall i \in \mathcal{T}_R, k \in \mathcal{T}_D$: Energy stored in the battery at time (i, k) (at the end of i^{th} 5-minute interval within k^{th} hour)

3.1.5 Constraints and objective function

- Net discharge (power) from the battery at any time:

$$P_{net_{i,k}} = P_i + P_{i,k} + L_{s_{i,k}} \quad (1)$$

- Balance on the energy stored in the battery at each time

$$E_{i,k} = E_{i-1,k} - P_{net_{i,k}} \Delta t_r, \quad \forall i \in \mathcal{T}_R, k \in \mathcal{T}_D \quad (2)$$

In 3.2.5, $E_{0,k} = E_0$ for $k \in \{1\}$ and $E_{0,k} = E_{n_{rtm}, k-1}$ for $k \in \mathcal{T}_R \setminus \{1\}$.

- Bounds on variables:

$$0 \leq E_{i,j,k} \leq E_{max}, \forall i \in \mathcal{T}_R, k \in \mathcal{T}_D \quad (3a)$$

$$-P_{max} \leq P_{i,k} \leq P_{max}, \forall i \in \mathcal{T}_R, k \in \mathcal{T}_D \quad (3b)$$

$$-P_{max} \leq P_k \leq P_{max}, \forall k \in \mathcal{T}_D \quad (3c)$$

$$(3d)$$

- Objective Function:

$$\min \quad - \sum_{i \in \mathcal{T}_R} \sum_{k \in \mathcal{T}_R} \pi_{i,k} P_{i,k} \Delta t_r - \sum_{k \in \mathcal{T}_D} \pi_k P_k \Delta t_r n_{rtm} + \sum_{i \in \mathcal{T}_R} \sum_{k \in \mathcal{T}_R} \pi_{i,k} (L_{i,k} - L_{s_{i,k}}) \Delta t_r \quad (4)$$

3.2 Optimization Under Uncertainty

Now, we consider uncertainty in the building loads and extend the optimization formulation in deterministic setting 3.1 to formulate an extensive form of stochastic optimization problem to minimize the expected cost (or maximize expected revenue) for the building-battery system. In the formulation of the problem under uncertainty, we assume all the the market participating conditions are same as in the deterministic setting except for the uncertainty in the loads. The extensive form of the stochastic optimization problem for the system is described below.

3.2.1 Sets used in the model

$$\mathcal{T}_R := \{1, \dots, n_{rtm}\}$$

$$\mathcal{T}_D := \{1, \dots, n_{dam}\}$$

Here, \mathcal{T}_R is the set of time indices corresponding to each 5-minute subintervals in the real-time market within each hour, so $n_{rtm} = 12$. \mathcal{T}_D is the set of time indices corresponding to the hourly intervals of the day-ahead market. n_d can be chosen appropriately for any number of hours we plan to schedule the market participation policy for the building-battery system.

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A time instance for a day-ahead market variable in the model is represented by only the index k ($k \in \mathcal{T}_D$) which corresponds to the interval between hours $k - 1$ and k . On the other hand, a time instance for a real-time variable in the model is represented by index (i, k) , where $i \in \mathcal{T}_R$ and $k \in \mathcal{T}_D$. The indices i and k in a time instance (i, k) for a real-time variable correspond to the end of the respective 5-minute interval. For example, the time instance $(5, 7)$ corresponds to the end of the interval between 4th and 5th 5-minute interval within the 7th hour.

So, if a variable or time-varying parameter is indexed by only one index k it implies that it varies at hourly intervals and belongs to the day-ahead market, whereas a variable or time-varying parameter indexed by (i, k) is a real-time variable.

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- **Market parameters:**

- $\pi_k, \forall k \in \mathcal{T}_D$: Electricity price in day-ahead market in the interval between hour $k - 1$ to k
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- Δt : Time interval (in unit of hours) in the real-time market (which is 5 minutes)

- **Battery parameters:**

- $E_{max} = 0.5$ MWh: Energy storage capacity of the battery
- $P_{max} = 0.5$ MW: Maximum discharging or charging rate of the battery
- $E_0 = E_{max}$: Energy stored in the battery before beginning of market participation

- **Building loads:**

- $L_{i,k}, \forall i \in \mathcal{T}_R, k \in \mathcal{T}_D$: Building loads in the 5-minute interval between $(i - 1, k)$ and (i, k) within k^{th} hour

3.2.4 Variables in the model:

- **Decision variables:**

- $P_k, \forall k \in \mathcal{T}_D$: Power committed by battery in day-ahead market in the interval between hour $k - 1$ to k
- $P_{i,k}, \forall i \in \mathcal{T}_R, k \in \mathcal{T}_D$: Power committed by battery in real-time market in the 5-minute interval between $(i - 1, k)$ and (i, k) within k^{th} hour
- $L_{s_{i,k}}, \forall i \in \mathcal{T}_R, k \in \mathcal{T}_D$: Power supplied by battery to the building in the 5-minute interval between $(i - 1, k)$ and (i, k) within k^{th} hour

- **State variables:**

- $E_{i,k}, \forall i \in \mathcal{T}_R, k \in \mathcal{T}_D$: Energy stored in the battery at time (i, k) (at the end of i^{th} 5-minute interval within k^{th} hour)

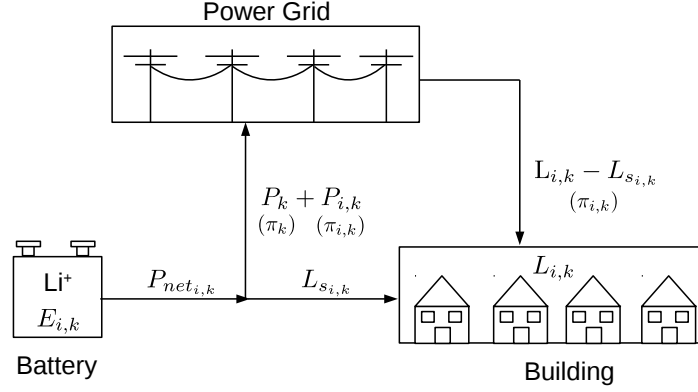


Figure 4: Illustration of Building-Battery System interconnected with Power Grid

3.2.5 Constraints and objective function

- Net discharge (power) from the battery at any time:

$$P_{net_{i,k}} = P_i + P_{i,k} + L_{s_{i,k}} \quad (5)$$

- Balance on the energy stored in the battery at each time

$$E_{i,k} = E_{i-1,k} - P_{net_{i,k}} \Delta t_r, \quad \forall i \in \mathcal{T}_R, k \in \mathcal{T}_D \quad (6)$$

In 3.2.5, $E_{0,k} = E_0$ for $k \in \{1\}$ and $E_{0,k} = E_{n_{rtm},k-1}$ for $k \in \mathcal{T}_R \setminus \{1\}$.

- Bounds on variables:

$$0 \leq E_{i,j,k} \leq E_{max}, \forall i \in \mathcal{T}_R, k \in \mathcal{T}_D \quad (7a)$$

$$-P_{max} \leq P_{i,k} \leq P_{max}, \forall i \in \mathcal{T}_R, k \in \mathcal{T}_D \quad (7b)$$

$$-P_{max} \leq P_k \leq P_{max}, \forall k \in \mathcal{T}_D \quad (7c)$$

$$(7d)$$

- Objective Function:

$$\min - \sum_{i \in \mathcal{T}_R} \sum_{k \in \mathcal{T}_R} \pi_{i,k} P_{i,k} \Delta t_r - \sum_{k \in \mathcal{T}_D} \pi_k P_k \Delta t_r n_{rtm} + \sum_{i \in \mathcal{T}_R} \sum_{k \in \mathcal{T}_R} \pi_{i,k} (L_{i,k} - L_{s_{i,k}}) \Delta t_r \quad (8)$$

4 Computational Experiments

4.1 Full Problem

In this case study, we sample 50 scenario paths (out of the 50^{168} possibilities) for a week's time period. We then construct a full model for for this week and use real price signals from 01/01/2015 to 01/07/2015 in California ISO ². For every 1 hour interval in the model, we sample a scenario, and use the load data corresponding to that scenario for the 12 intervals (5 minutes each) in that hour. This helps to reduce the size of scenario tree (from $50^{168 \times 12}$ to 50^{168}). We solve this model (with 50 sampled paths) 100 times to get a confidence interval on the expected revenue. We then compare this expected revenue (obtained by participating in both real time and day-ahead market) to the cases when the battery participates only in either real time or day-ahead market alone. Highest revenue is

Table 1: Revenue Breakup from Participation in Different Markets

Market Participated	Total Revenue (\$)	Unmet Load Cost (\$)	DAM Revenue (\$)	RTM Revenue (\$)
DAM + RTM	739.73	-8.75	815.74	-84.76
DAM	-921.61	76.93	-844.68	N/A
RTM	70.03	-9.10	N/A	60.93
None	-10,293.23	10,293.23	N/A	N/A

earned when the battery participates in both the real time and day-ahead markets (Table 1). Whereas, if it participates in just day-ahead or real time market alone, the revenue is much less or even negative (results in loss). Consider the case when it participates in only day ahead market. It is evident from Figure 9 and 10 that the battery needs to charge itself (buy energy from the grid) in order to meet the building load demands. The price of energy is on average higher in day-ahead market than that in real time markets. Thus with no participation in real time market in does not have the flexibility to buy energy from the real-time market at lower prices and sell to day-ahead market (at a higher price) to make profits. The building loads need to be met in real-time (at every 5-minute interval) while the battery has the opportunity to buy or sell energy from the grid only at every hour. Thus the battery is forced to store enough energy to meet the building requirement for an hour by buying energy in hourly intervals from the day-ahead market. Whenever it has slightly excess energy available it tries to sell that energy to the day-ahead market to minimize the overall cost.

On the other hand, when it participates in both day-ahead and real-time markets, it has the flexibility to buy from the real-time market and sell to the day-ahead market while saving sufficient energy to meet the building requirement in real-time. This is possible because the real-time electricity prices are slightly lower than the day-ahead market prices on average. The real-time prices also fall below the day-ahead market prices very often (Figures 6a and 6b) and because of its fast dynamics, the battery can capture these moments by buying from real-time market and selling in day-ahead market to make profit.

²<http://oasis.caiso.com/mrioasis/logon.do>

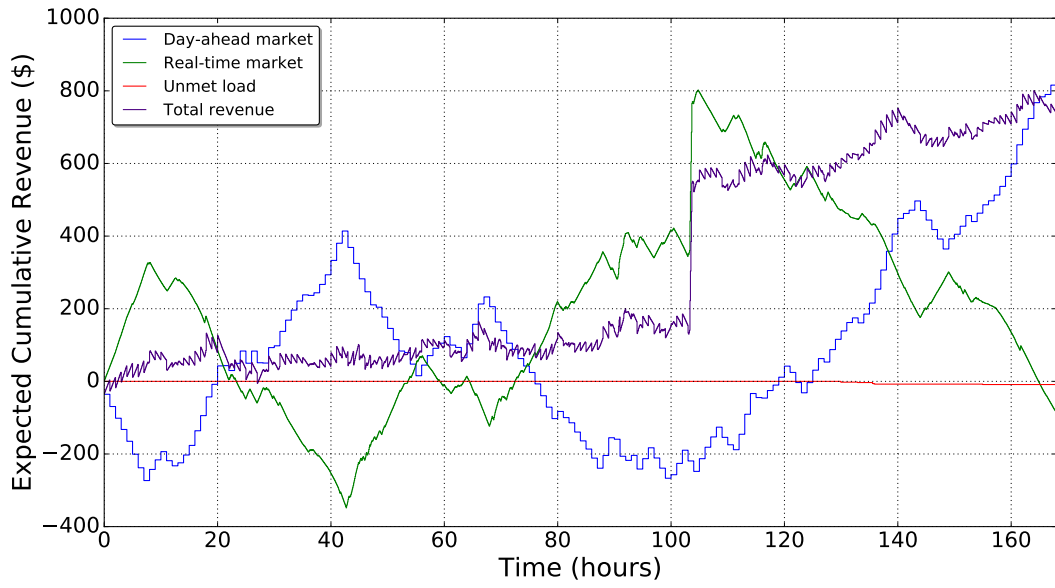
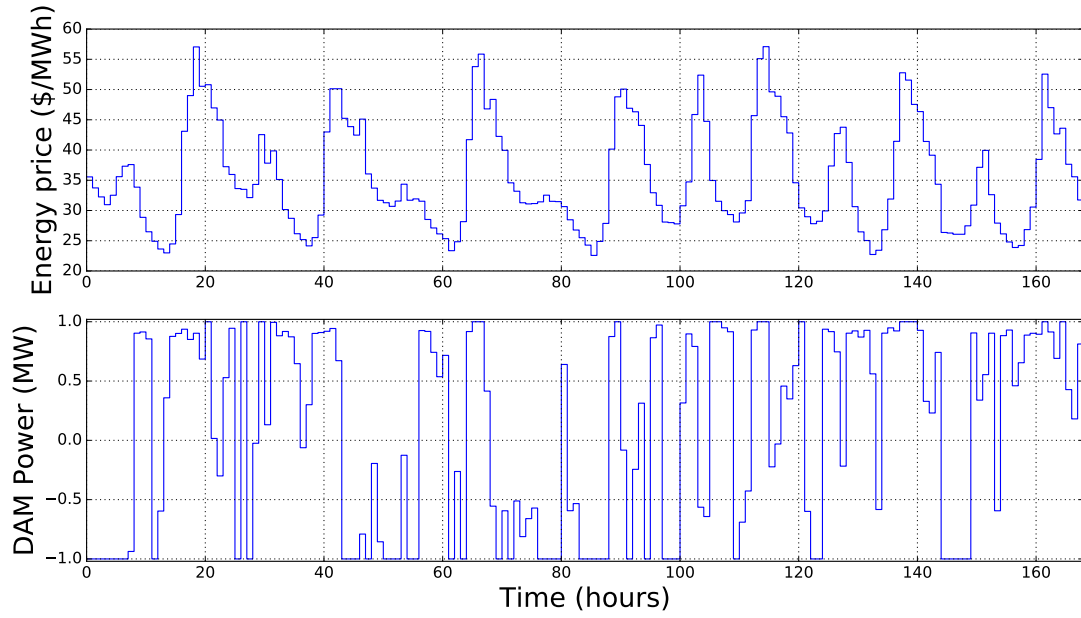
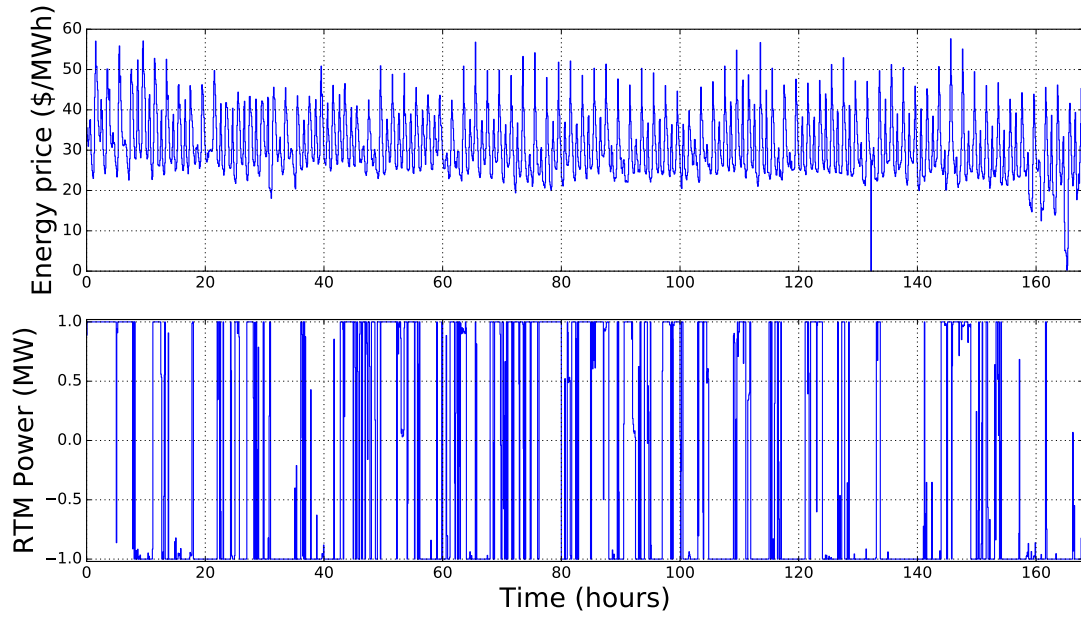


Figure 5: Trajectory of cumulative revenues when battery participates in both day-ahead and real-time markets



(a) Day-ahead market



(b) Real-time market

Figure 6: Energy participation policy when battery participates in both day-ahead and real-time markets

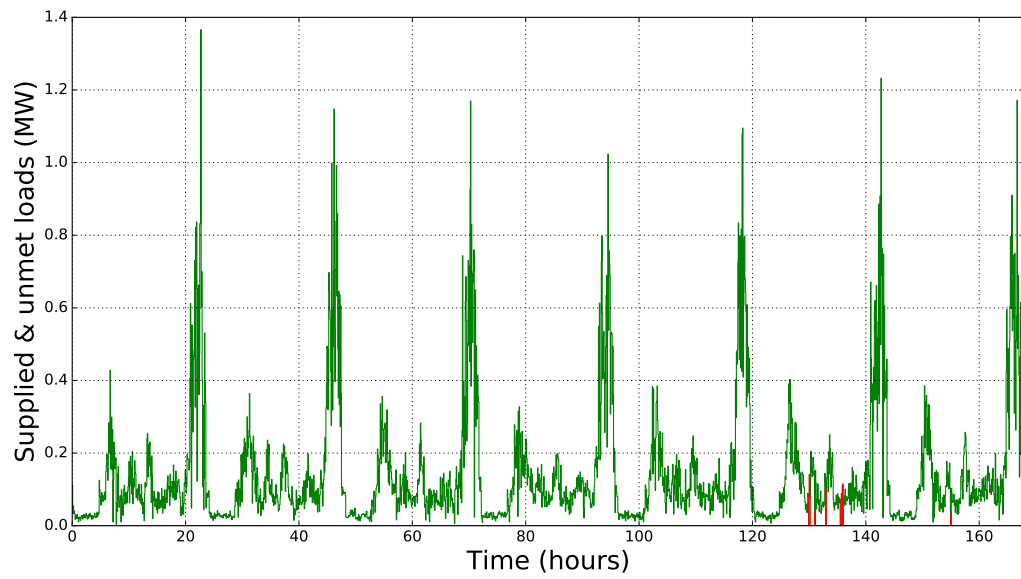
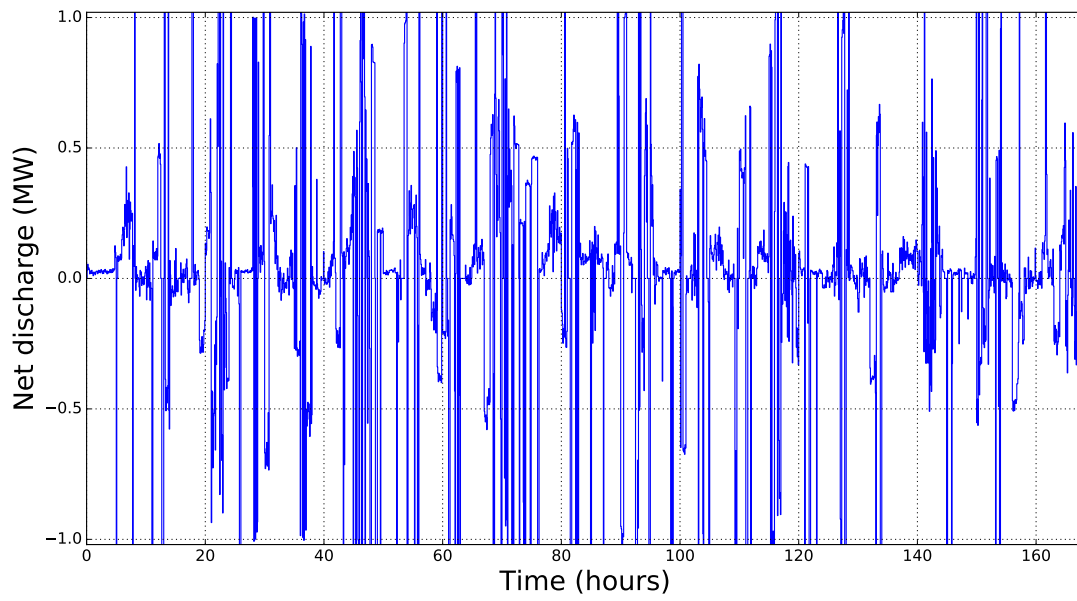
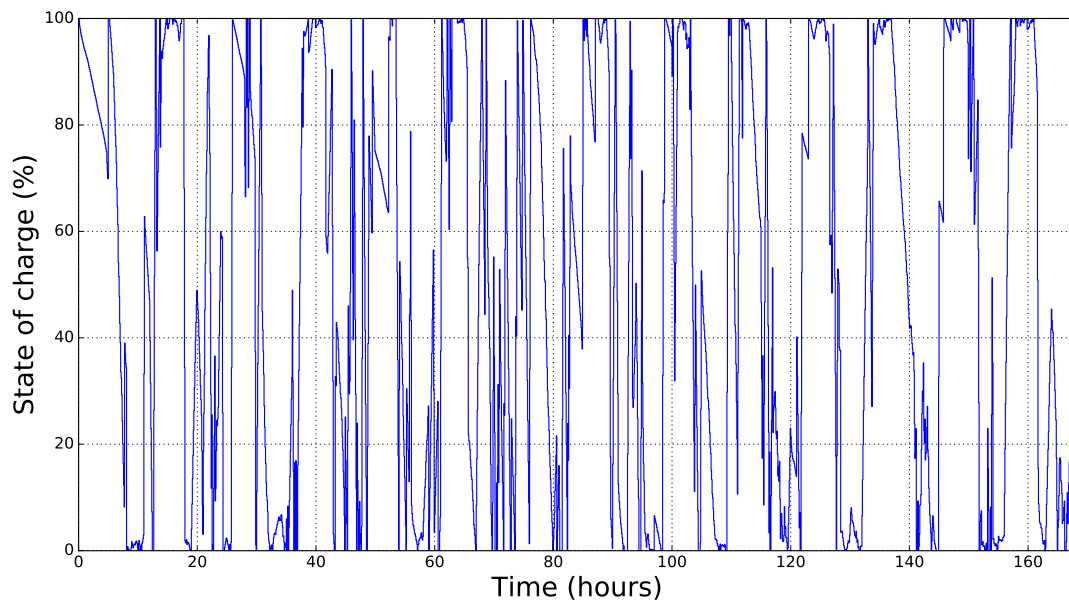


Figure 7: Power supplied to building and unmet load when battery participates in both day-ahead and real-time markets



(a) Net battery discharge



(b) State of charge trajectory

Figure 8: Operating condition of battery when participating in both day-ahead and real-time markets

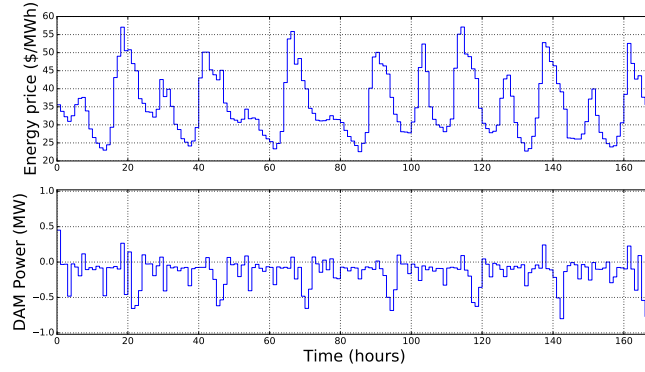


Figure 9: Energy participation policy when battery participates only in day-ahead market.

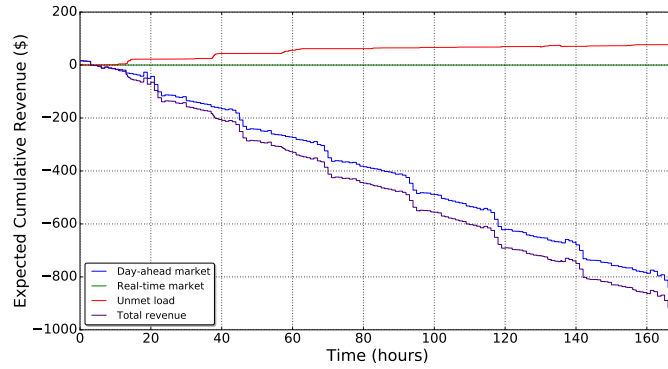


Figure 10: Trajectory of cumulative revenue when battery participates only in day-ahead market

4.1.1 Upper Bound from Mean Value Problem

4.1.2 Estimating Bounds with Perfect Information

4.1.3 Estimating Bounds with Two-Stage Approximation: Restriction

4.2 Receding Horizon Heuristic

We sample 50 paths upto next 24 hours horizon

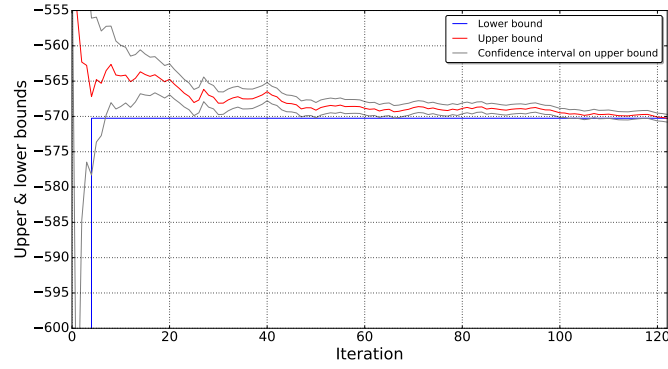


Figure 11: Trajectory of the lower and upper bounds obtained at every iteration of stochastic dual dynamic programming

4.3 Stochastic Dual Dynamic Programming

5 Conclusions

6 Future Work

6.1 Price Uncertainty

6.2 Three Layer Markets

References

- [1] Olivier Ledoit and Michael Wolf. A well-conditioned estimator for large-dimensional covariance matrices. *Journal of multivariate analysis*, 88(2):365–411, 2004.