

## 0.1 Representable Functors

Let  $\mathcal{C}$  be a locally small category,  $C \in \text{obj}(\mathcal{C})$  then  $\text{Hom}_{\mathcal{C}}(C, -) : \mathcal{C} \rightarrow \text{Set}$  is the set of representable functors. This functor is faithful if the object  $C$  has the property that for any objects  $X$  and  $Y$  and arrows  $f, g : X \rightarrow Y$  if  $f \neq g$  there is an arrow  $x : C \rightarrow X$  such that  $fx \neq gx$ . That is, the arrows in the category are distinguished by their effect on generalized elements based at  $C$ . Such an object  $C$  is called a generator for  $\mathcal{C}$ .

Contravariant of a representable functor  $\text{Hom}_{\mathcal{C}}(-, C) : \mathcal{C}^{op} \rightarrow \text{Set}$

Ring of continuous functions  $C(X)$  -wow-  $f : X \rightarrow \mathbb{R}$  | *discontinuous*