A category has all finite limits iff it has finite products and equalizers.

Proof. Take a finite diagram
$$D : J \to C$$
.

Consider first the product
$$\prod_{i \in J_0} D_i$$
which has correct projections $p_j : \prod_{i \in J_0} D_i \to D_j$ $\square$