

A category has all finite limits iff it has finite products and equalizers.

Proof. Take a finite diagram

$$D : J \rightarrow C$$

Consider first the product

$$\prod_{i \in J_0} D_i$$

which has correct projections $p_j : \prod_{i \in J_0} D_i \rightarrow D_j$

□