

$$R \rightarrow XRX \mid S$$

$$S \rightarrow aTb \mid bTa$$

$$T \rightarrow XTX \mid X \mid \varepsilon$$

$$X \rightarrow a \mid b$$

1.1) What are the variables of G?

- R,S,T,X

1.2) What are the terminals of G?

- a,b

1.3) Which is the start variable of G?

- R

1.4) Give three strings in L(G)

- Abba
- Baaabb
- Aaabbaaa

1.5) Give three strings NOT in L(G)

- Abbaa
- Babab
- Ababab

1.6) For the following derivations, circle True or False.

- $T \Rightarrow aba$ **True**
- $T \Rightarrow^* aba$ **True**
- $T \Rightarrow T$ **True**
- $XXX \Rightarrow^* aba$ **False**
- $X \Rightarrow^* aba$ **False**
- $T \Rightarrow^* XX$ **True**
- $T \Rightarrow^* XXX$ **True**
- $S \Rightarrow^* \varepsilon$ **True**

2. [5 pts] Give context free grammars that generate the following languages. Alphabet $\Sigma = \{0, 1\}$.

2.1) $L = \{\omega \mid \omega \text{ contains at least three } 1s\}$

$$S \rightarrow 0S1 \mid \varepsilon$$

2.2) $L = \{\omega \mid \omega \text{ starts and ends with the same symbol}\}$

$$S \rightarrow 0S0 \mid 1S1 \mid \varepsilon$$

2.3) $L = \{\omega \mid \text{the length of } \omega \text{ is odd}\}$

$$S \rightarrow 0S0 \mid 1S1 \mid \varepsilon$$

2.4) $L = \{\omega \mid \text{the length of } \omega \text{ is odd and its middle is a } 0\}$

$$S \rightarrow 0S0 \mid 1S1 \mid \varepsilon$$

$$A \rightarrow 0A \mid 1A$$

2.5) $L = \{\omega \mid \omega = \omega R, \text{ that } \omega \text{ is a palindrome}\}$

$$S \rightarrow aSa \mid bSb \mid \varepsilon$$

3. [5 pts] Give CFG that generates the language $A = \{aibjck \mid i = j \text{ or } j = k \text{ where } i, j, k \geq 0\}$. Is your grammar ambiguous? Why or why not?

$S \rightarrow XcY \mid aSc \mid \epsilon$

$X \rightarrow aXb \mid \epsilon$

$Y \rightarrow cYb \mid \epsilon$

This CFG generates strings where the counts of 'a's, 'b's, and 'c's are equal. It is not ambiguous because there is only one way to derive each string, and the rules are unambiguous. The CFG ensures that for each 'a' added, there is a corresponding 'b', and for each 'b' added, there is a corresponding 'c', making it impossible for ambiguity to occur.