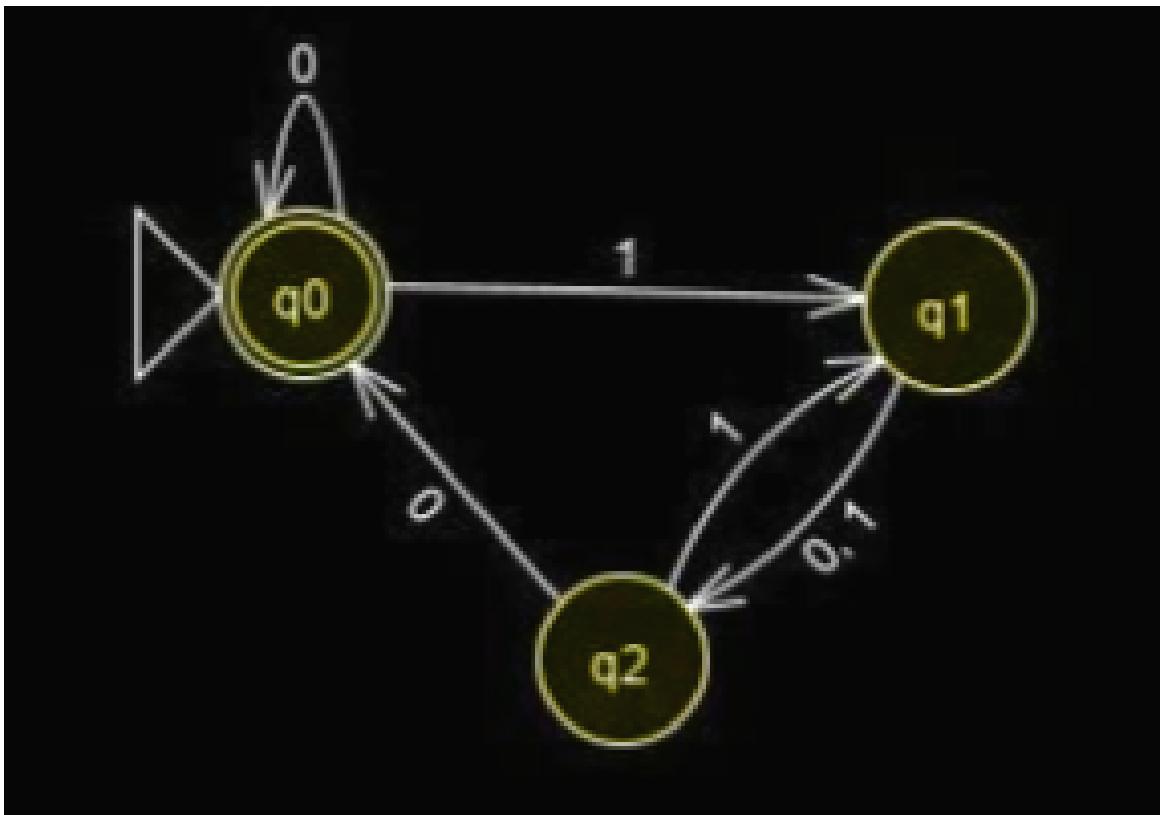


1. [6 pts] Answer questions for the following DFA M and give reasons for your answers.



1.1) Is  $\langle M, 0100 \rangle \in ADFA$ ? (Note:  $ADFA$  represents the acceptance problem of DFA)

- Yes, because if you plug in 0100 into the above DFA, the path taking is as follows:  
 $q0 > q0 > q1 > q2 > q0 >$  accepted.

1.2) Is  $\langle M, 011 \rangle \in ADFA$ ?

- No, because if you plug in the input string 011 into the above DFA, the path taking is as follows  $q0 > q0 > q1 > q2 >$  rejected.

1.3) Is  $\langle M \rangle \in ADFA$ ?

- No, because nothing is passed into the above DFA. The input should be  $\langle M, w \rangle$  where  $w$  is some input string

1.4) Is  $\langle M, 0100 \rangle \in AREX$ ?

- No, because M is in DFA form which is not in the correct form for AREX.

1.5) Is  $\langle M \rangle \in EDFA$ ?

- No, because M is a DFA that is not empty so it is not in the set of EDFA

1.6) Is  $\langle M, M \rangle \in EQDFA$ ?

- Yes, because the two DFAs are passed into the EQdfa and  $M = M$ .

2. [7 pts] Assume  $\Sigma = \{0, 1\}$ . Given a DFA  $C$ , does there exist an algorithm to decide whether  $L(C) = \Sigma^*$ ? Express this problem as a language denoted as  $ALLDFA$  and prove that  $ALLDFA$  is decidable (Hints: build a Turing decider).

**The language for the above problem is  $M = \{\langle C \rangle \mid C \text{ is a DFA and } L(C) = \Sigma^*\}$ .  $M$  is decidable. We can use proof by constructions to determine this. TM F “on input  $\langle C \rangle$ ”**

1. We can build a DFA  $D$  that accepts  $\Sigma^*$
2. We can run TM E (EQ DFA) on  $\langle C, D \rangle$  and we will get the following
  - a. If E accepts, F is accepted
  - b. If E rejects, F is rejected

3. [7 pts] Given two DFAs  $A$  and  $B$ , we consider the problem of deciding whether  $L(A)$  (language of  $A$ ) is a subset of  $L(B)$ . Express this problem as a language denoted as  $SUBDFA$  and prove that  $SUBDFA$  is decidable.

**If  $L(A)$  is in the subset  $L(B)$ , the following must also be true:  $L(A)$  intersected with  $!L(B)$  must be empty. This is true because if  $L(A)$  is in  $!L(B)$  that means that it is not in  $L(B)$  which makes  $L(A)$  not in the subset of  $L(B)$ . We can make a language  $V = \{\text{“On input } \langle A, B \rangle \text{ where } A \text{ and } B \text{ are regular expressions”}\}$**

1. We can construct a DFA  $M$  such that  $L(M) = !L(B)$  intersected with  $L(A)$
2. We must run TM T on input W, where T decides EmptyDFA
3. If T accepts, then it is accepted and if T rejects, then it is rejected.