

CS & IT Engineering

Compiler Design

Intermediate Code & Code Optimization

Lecture: 4



Deva sir

Topics to be covered:

- Live Variable Analysis [Backward]
 - GEN & KILL Sets for each BB
 - IN & OUT Sets for each BB using Backward Analysis
- Reaching Definitions Analysis [Forward Analysis]
- Other topics: Code Generation
- Run Time Environments
- Assignment Questions.

Live Variable Analysis:

GEN (USE) Set

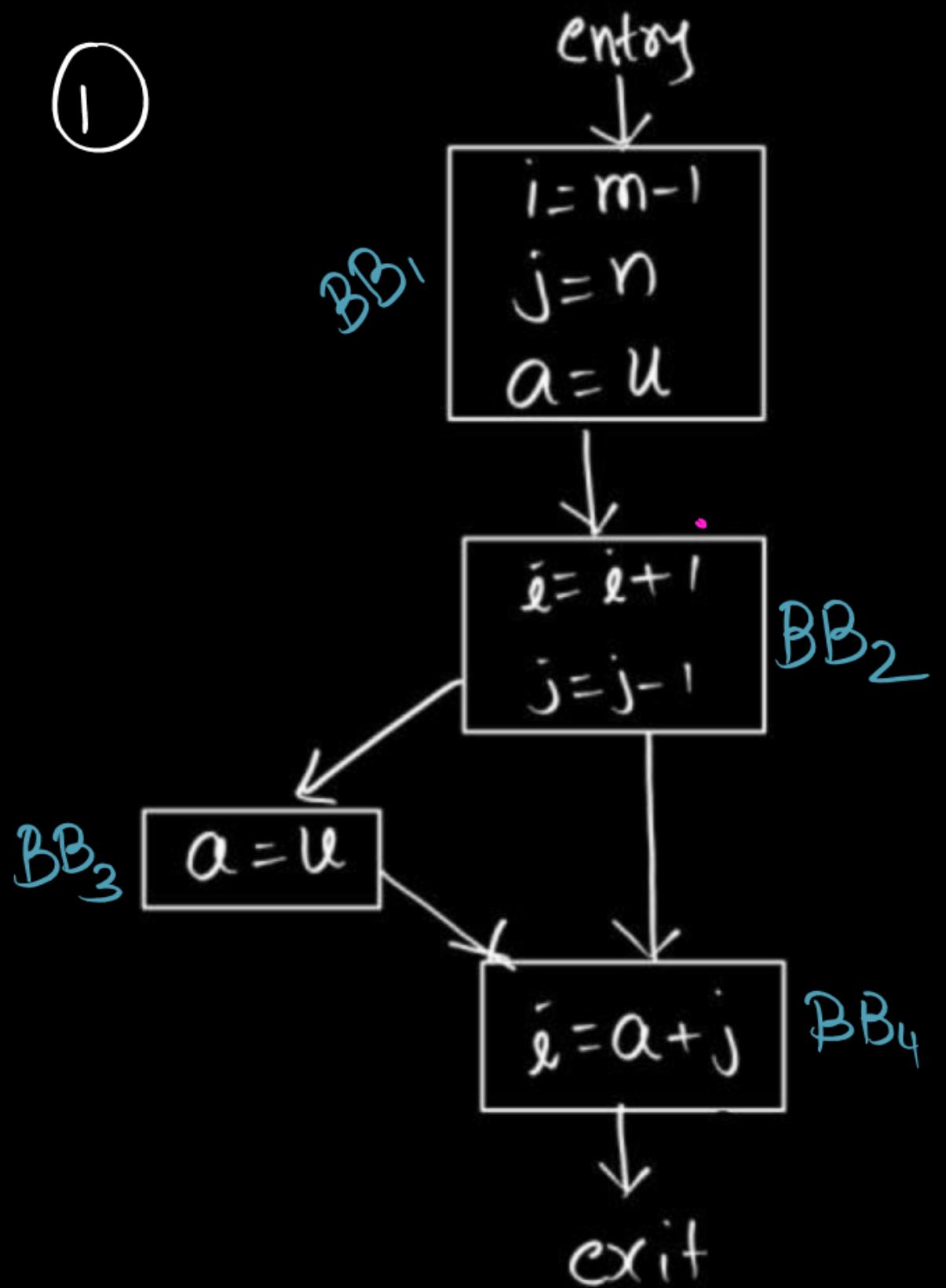
$$\boxed{\begin{array}{l} \bullet \\ x = a + b \\ y = \textcircled{2} * c \\ z = \textcircled{3} - d \end{array}}$$

KILL (DEF) Set

$$\begin{aligned} KILL_K &= \{x, y, z\} \\ &= \{v \mid v \text{ has definition} \\ &\quad \text{in } BB_K\} \end{aligned}$$

$GEN_K = \{a, b, c, d\}$
 $= \{l \mid l \text{ is used (read)} \text{ at some statement}$
 $\text{in } BB_K \text{ and}$
 $\text{no definition before the statement}\}$

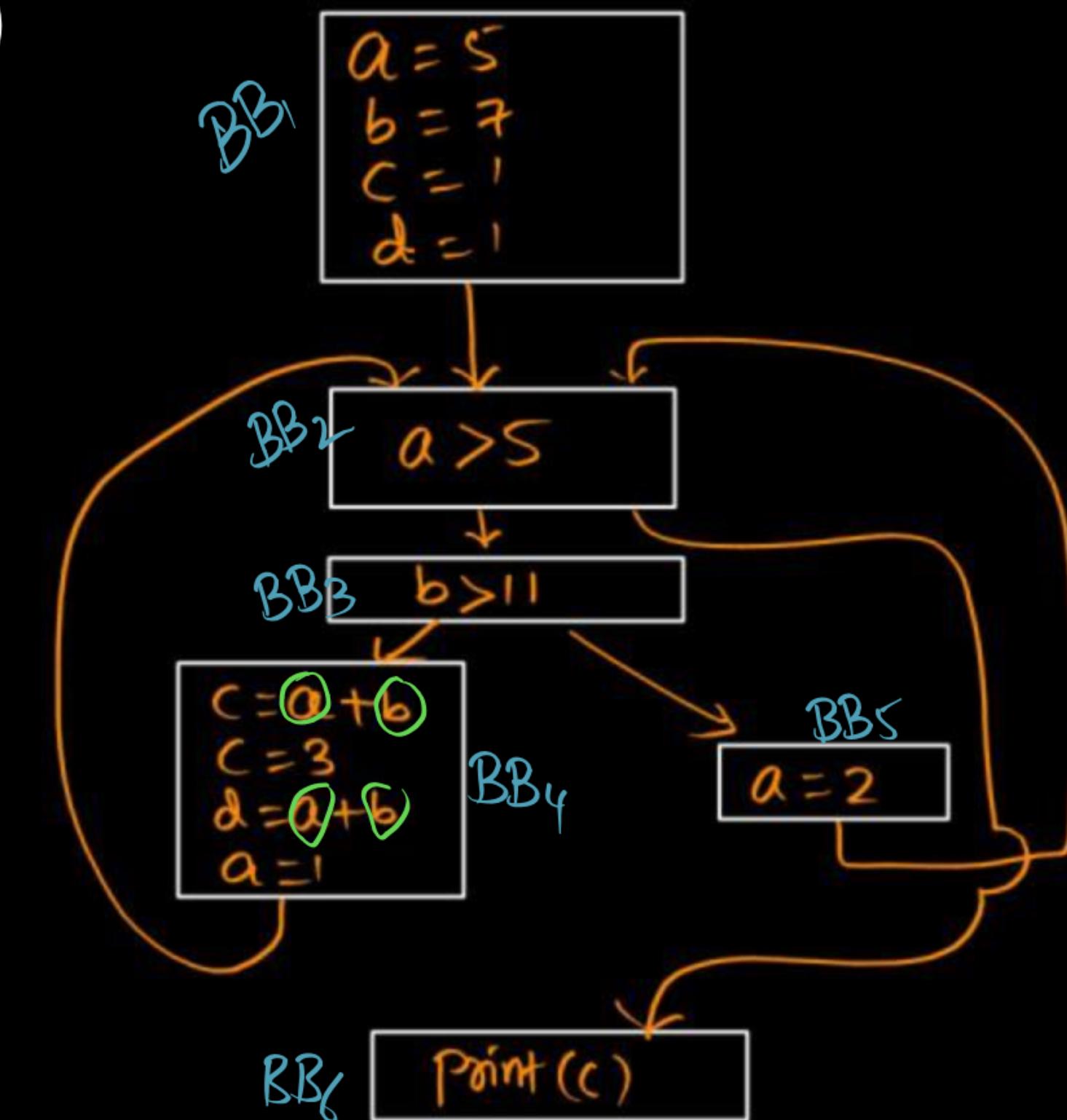
①



Compute GEN & KILL for each BB.

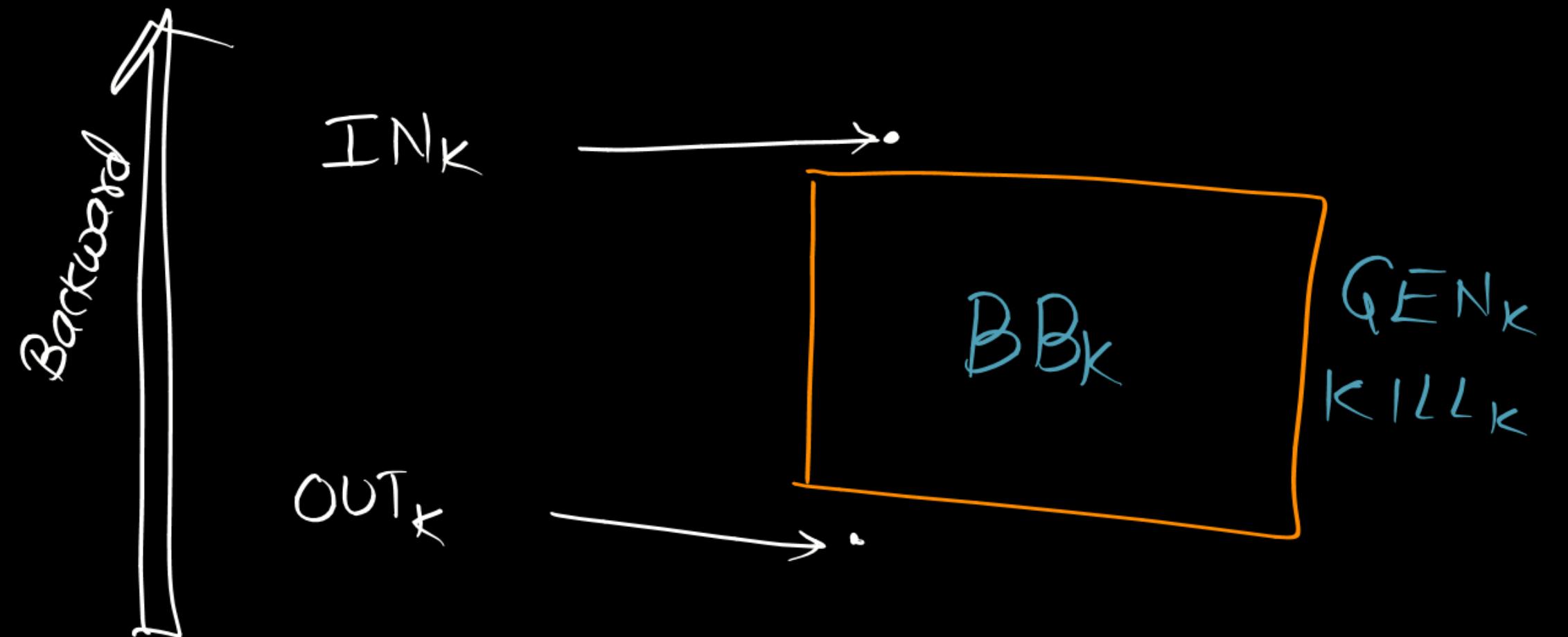
	GEN Set	KILL Set
BB ₁	{m,n,u}	{i,j,a}
BB ₂	{i,j}	{i,j}
BB ₃	{u}	{a}
BB ₄	{a,j}	{i}

②



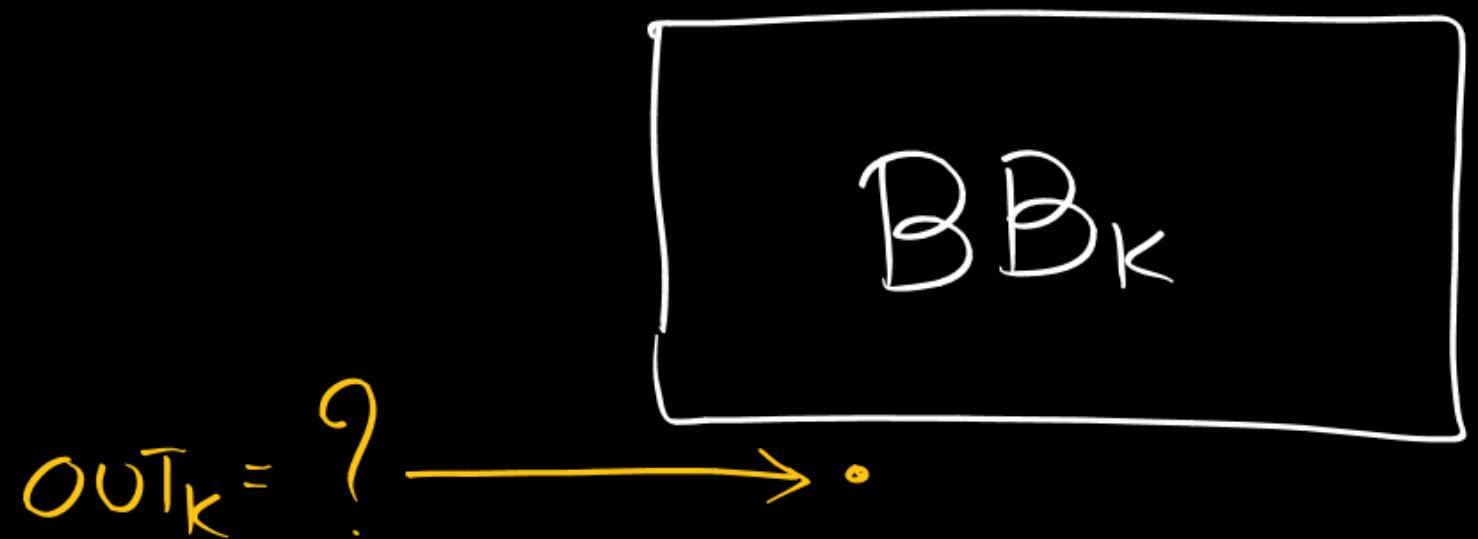
(USE) (DEF)

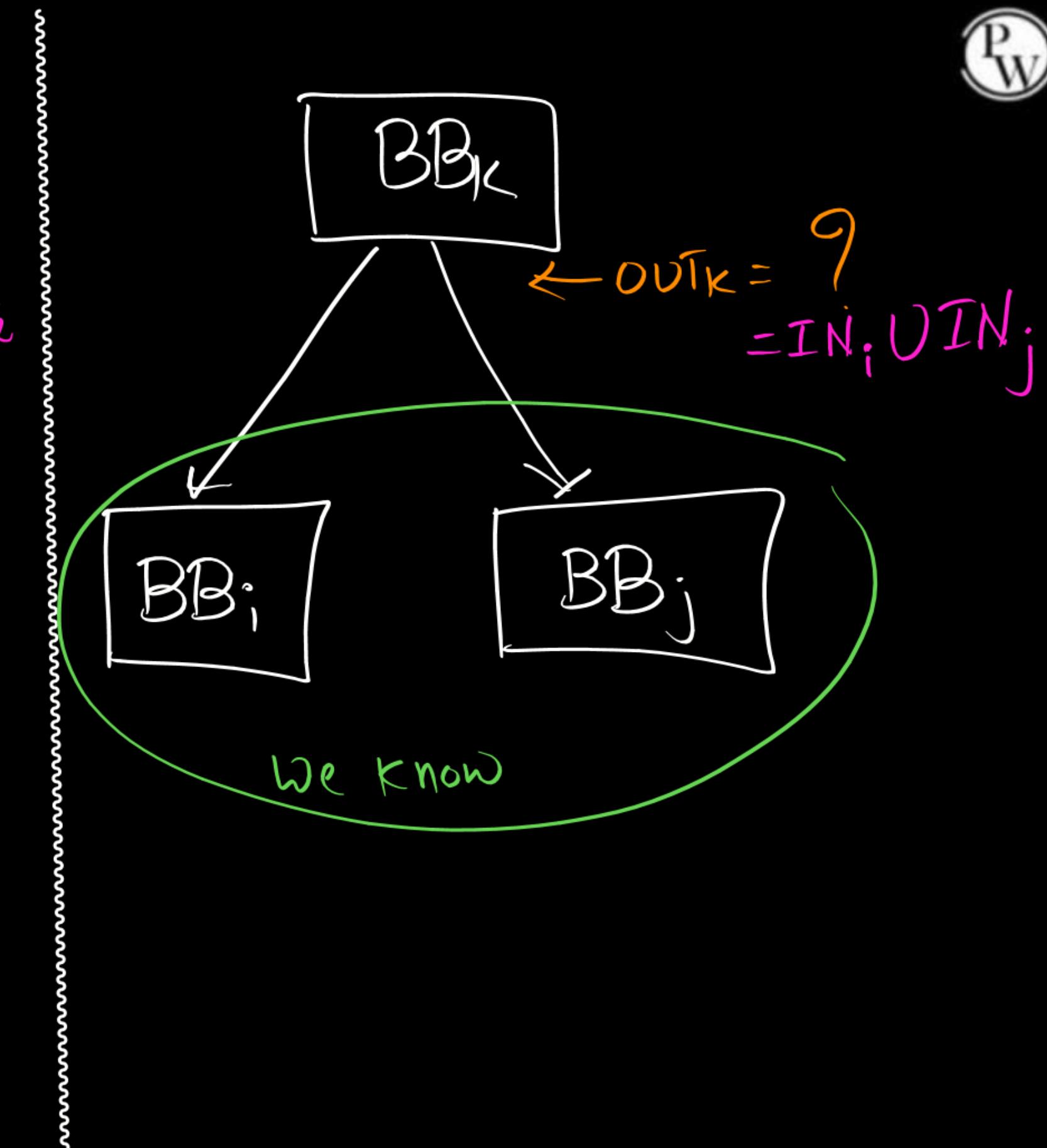
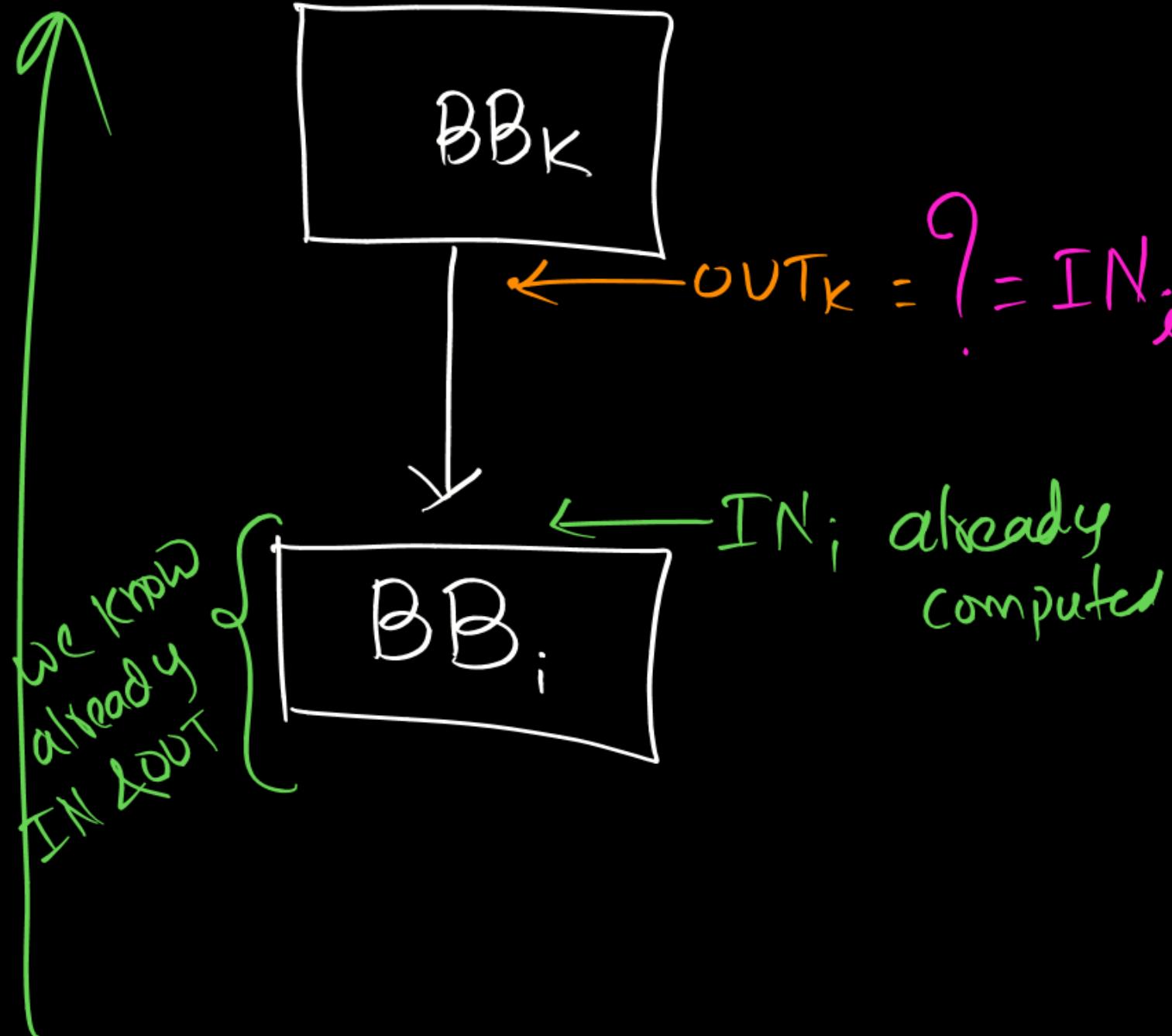
BB	GEN	KILL
1	ϕ	a, b, c, d
2	a	ϕ
3	b	ϕ
4	a, b	c, d, a
5	ϕ	a
6	c	ϕ



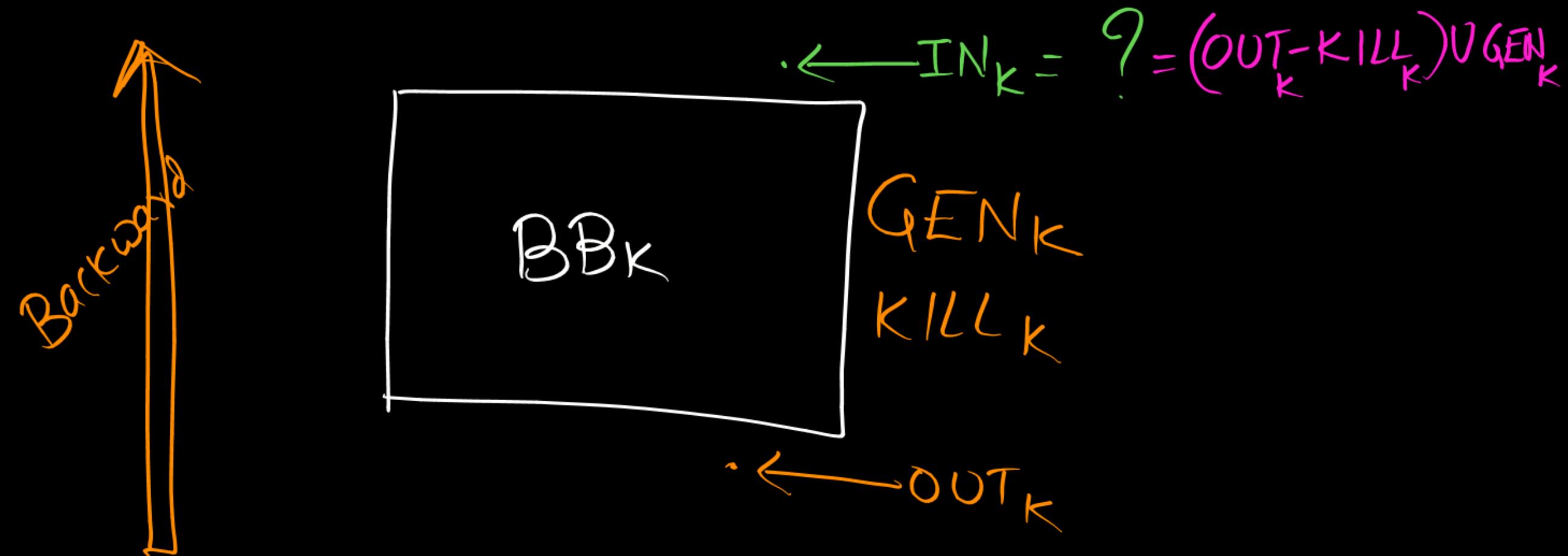
IN and OUT Sets Computation :

OUT_K for BB_K :

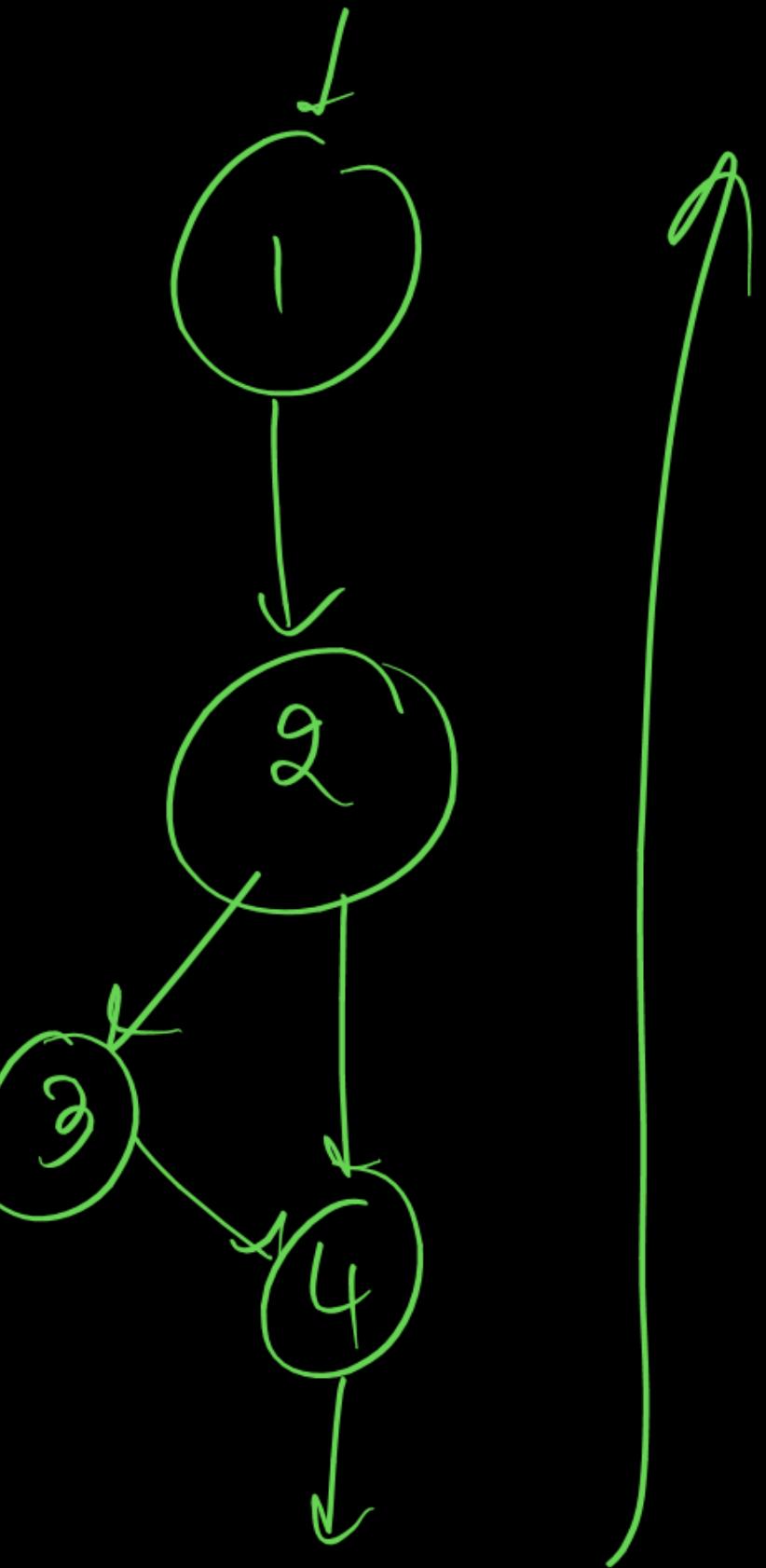
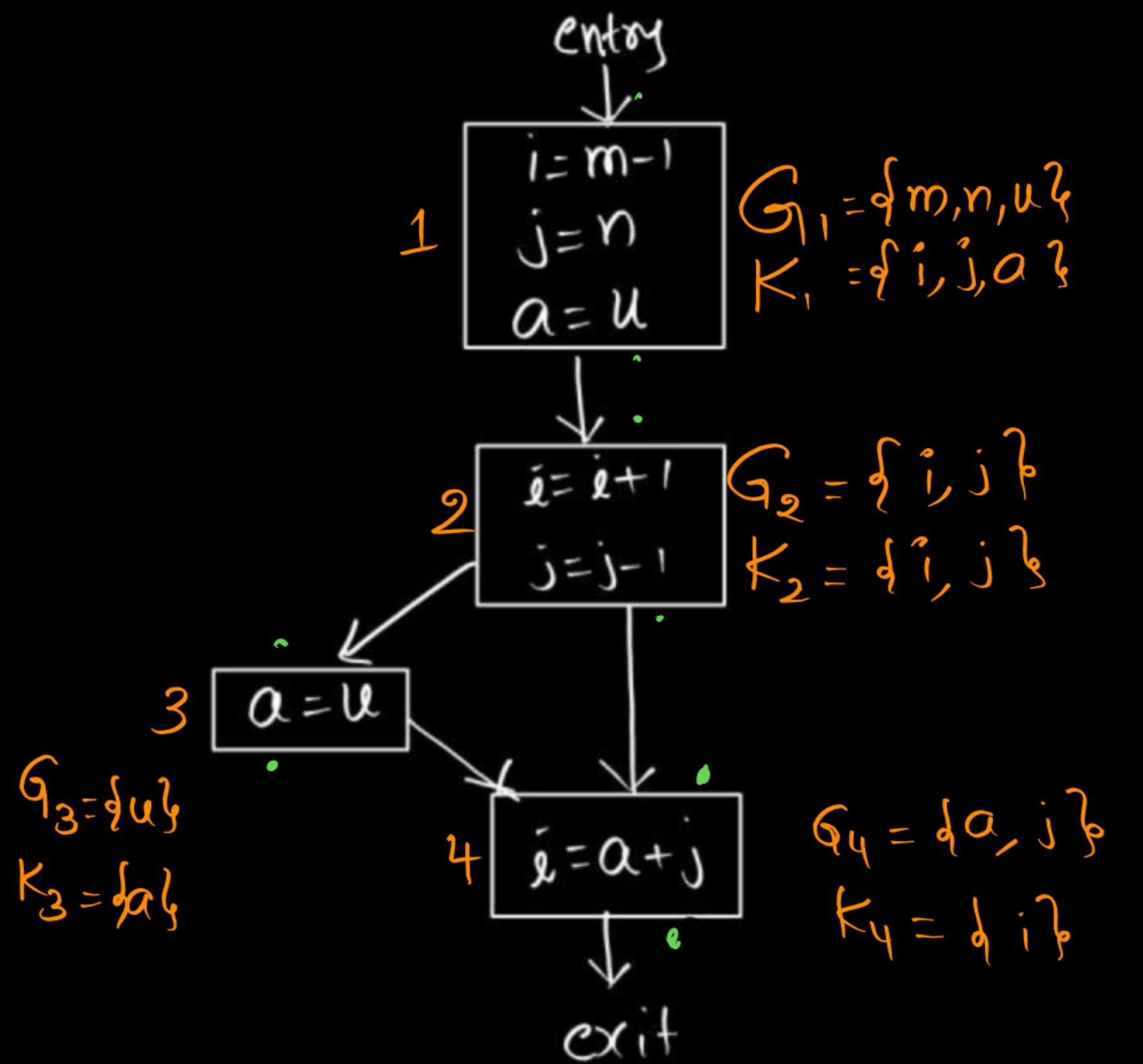


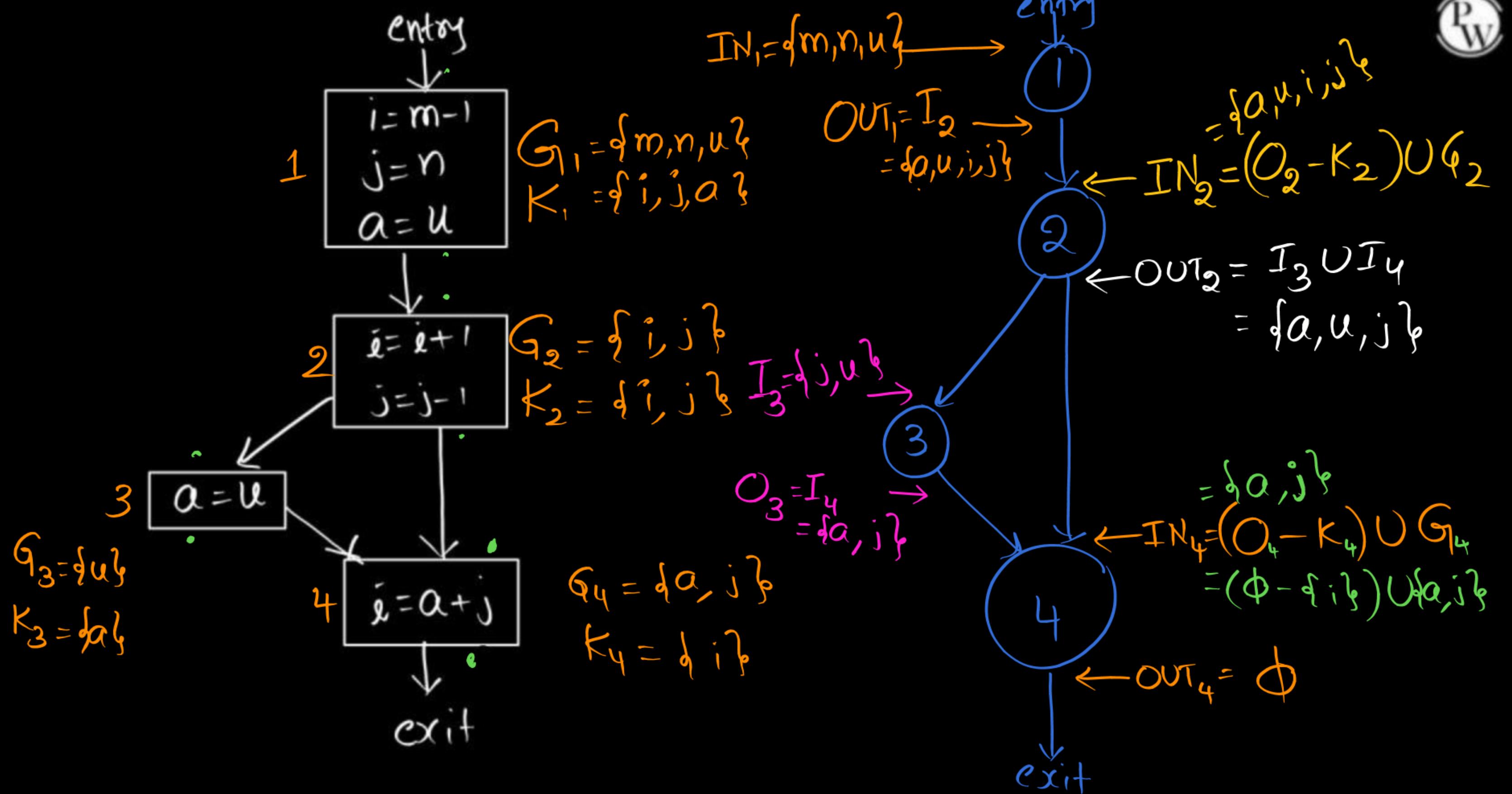


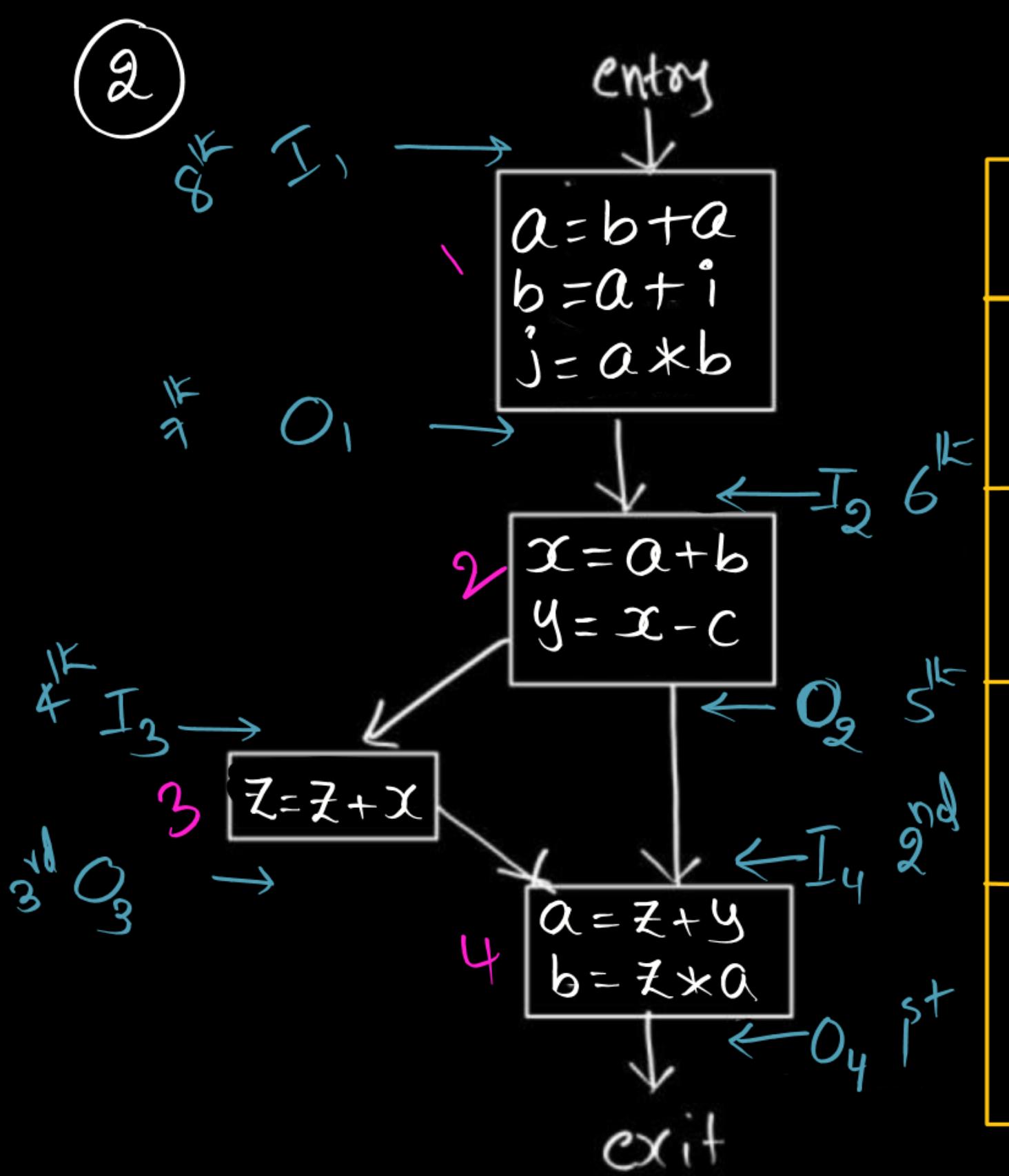
IN_K for BB_K





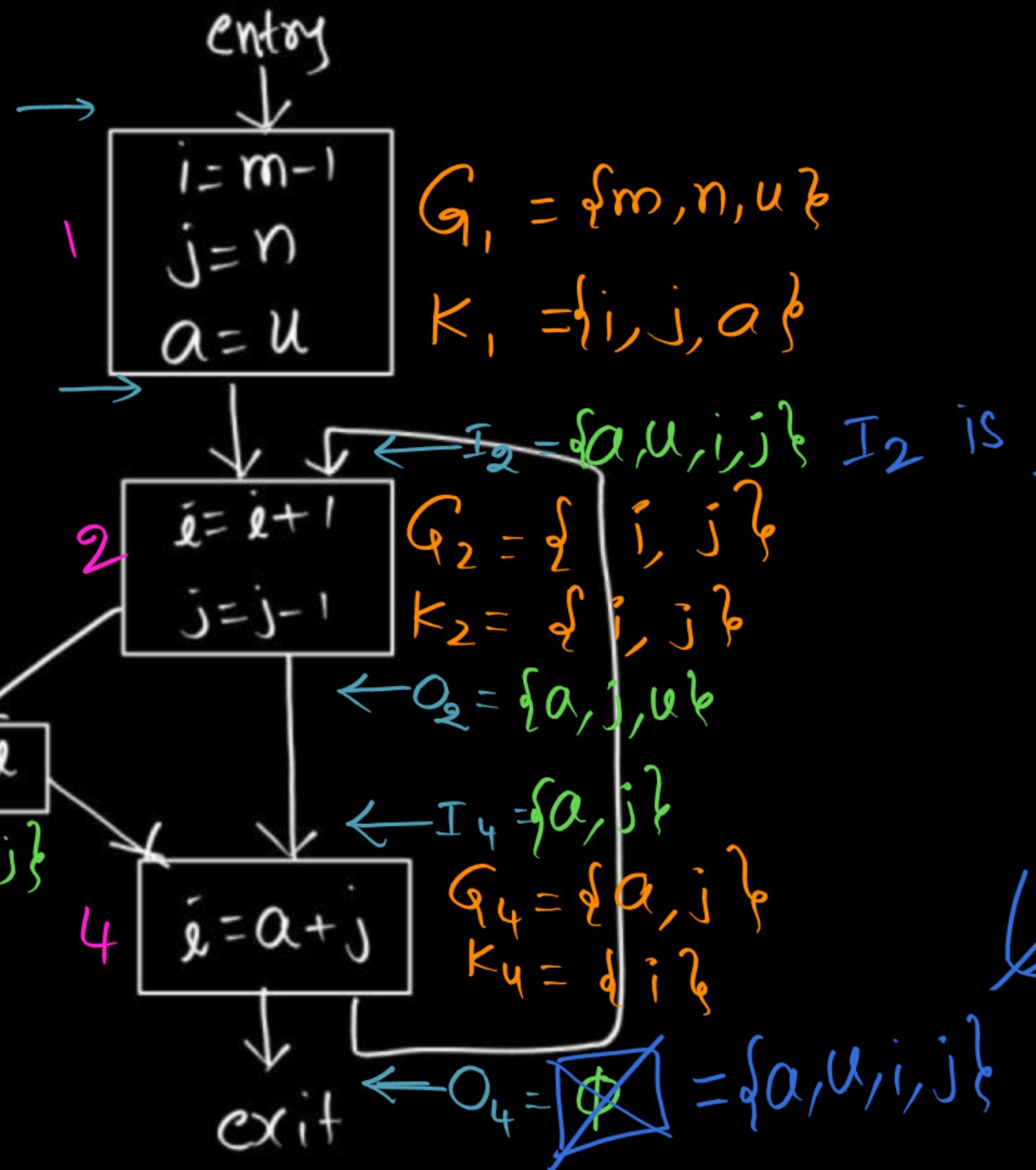






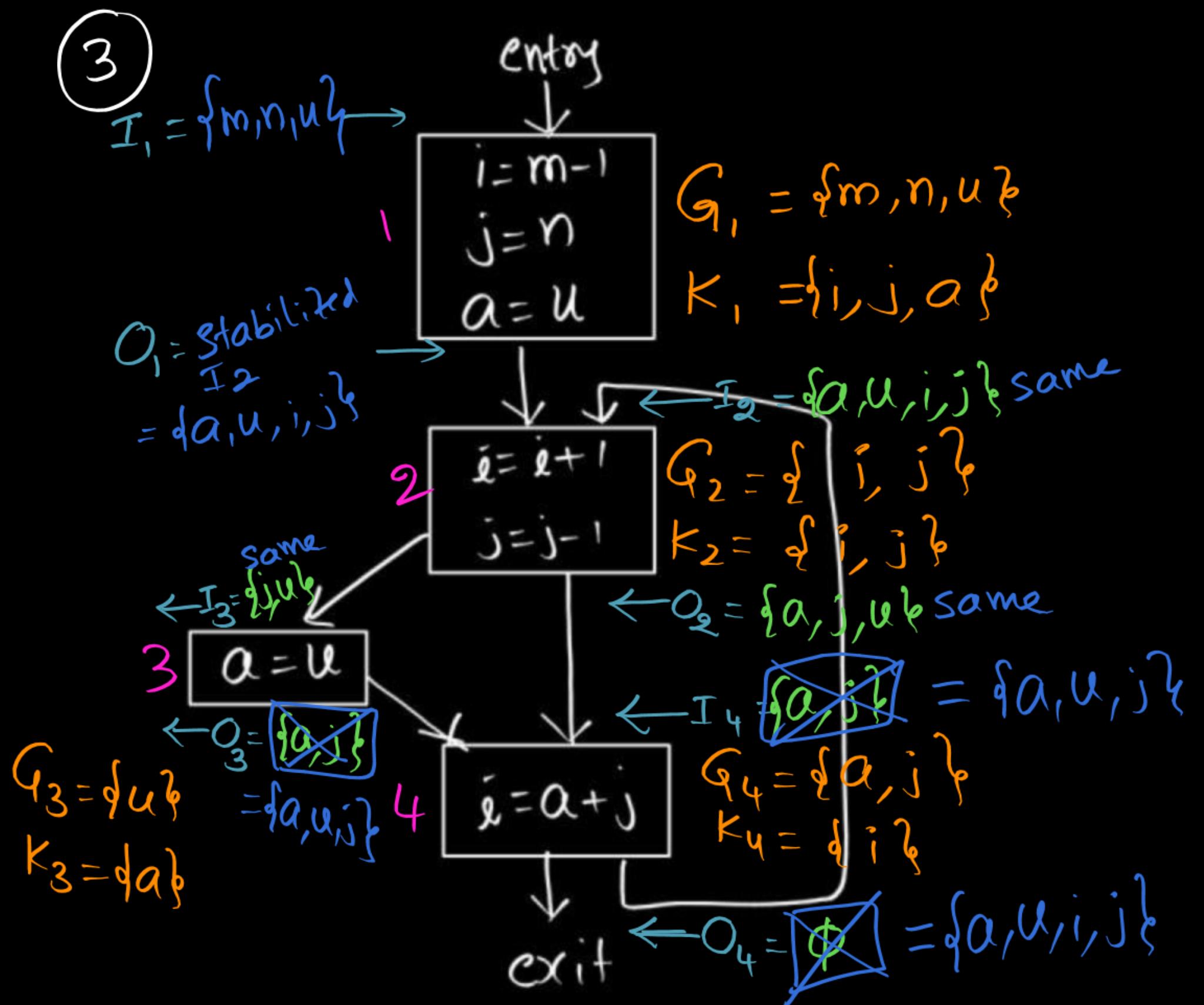
BB	GEN	KILL	OUT	IN
1	a, b, i	a, b, j	a, b, c, z	a, b, i, c, z
2	a, b, c	x, y	x, y, z	a, b, c, z
3	x, z	z	$I_4 = z, y$	x, y, z
4	z, y	a, b	\emptyset	z, y

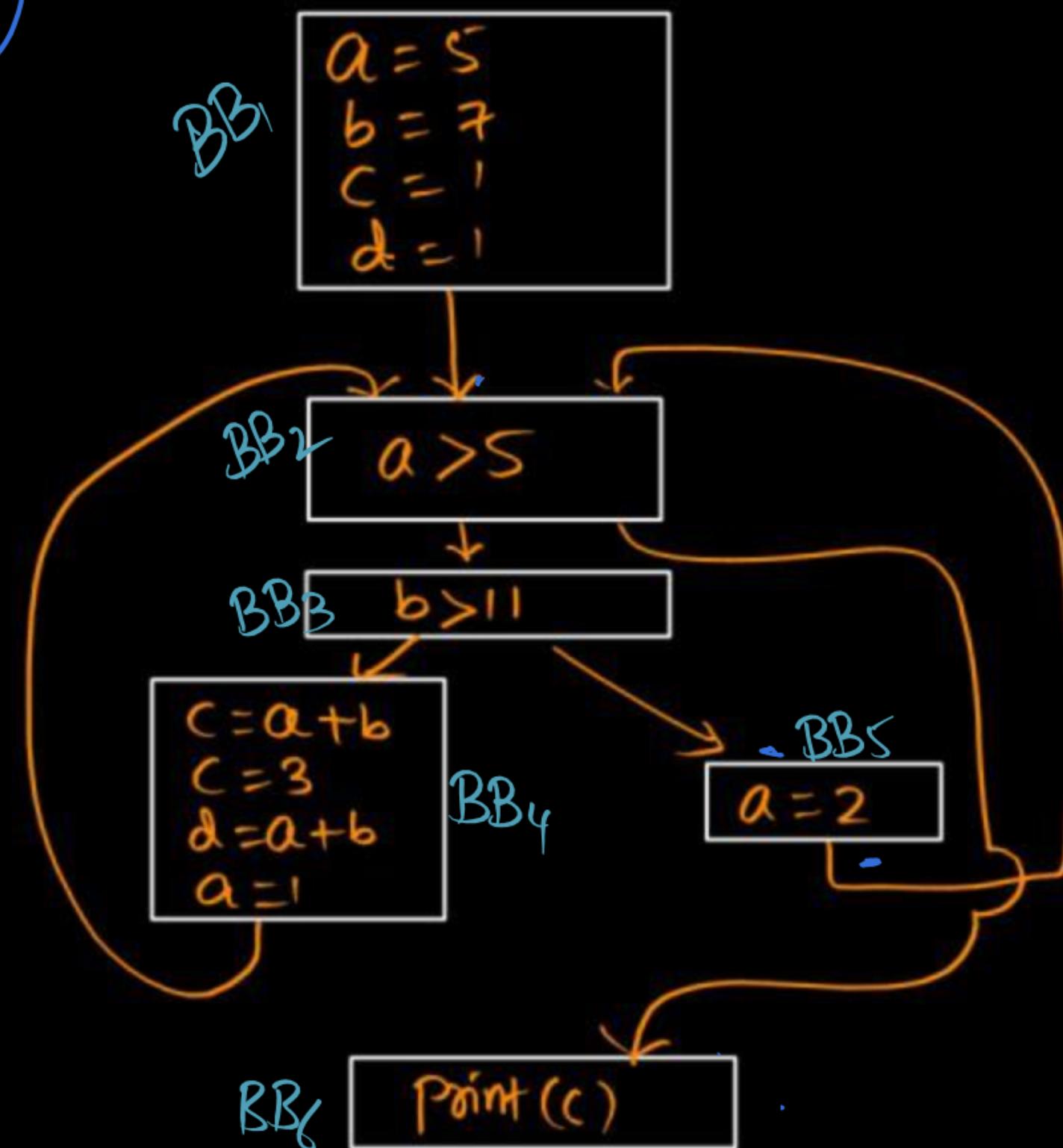
③

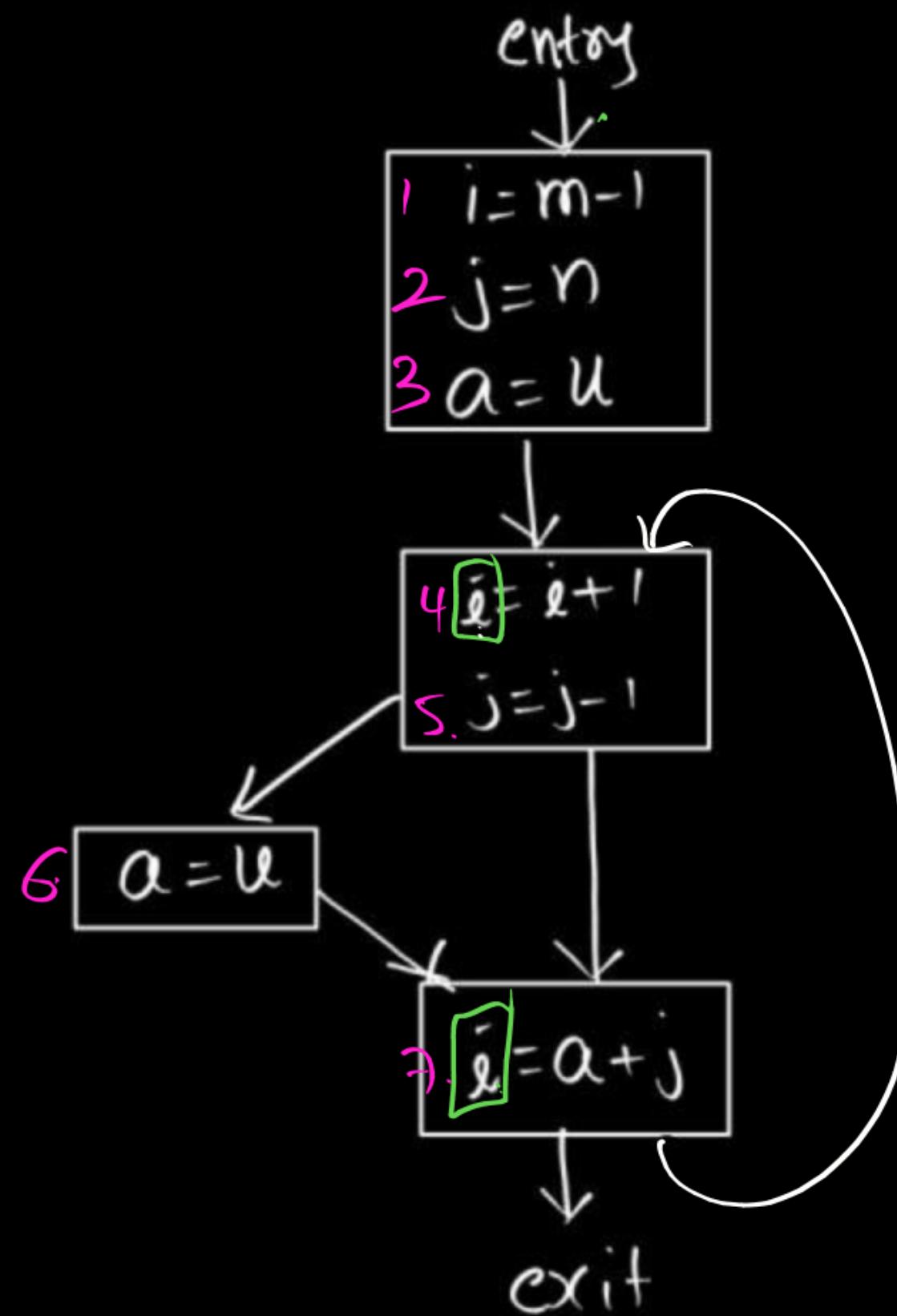
 $I_1 =$ 

I_2 is computed, now O_4 gets new values

③



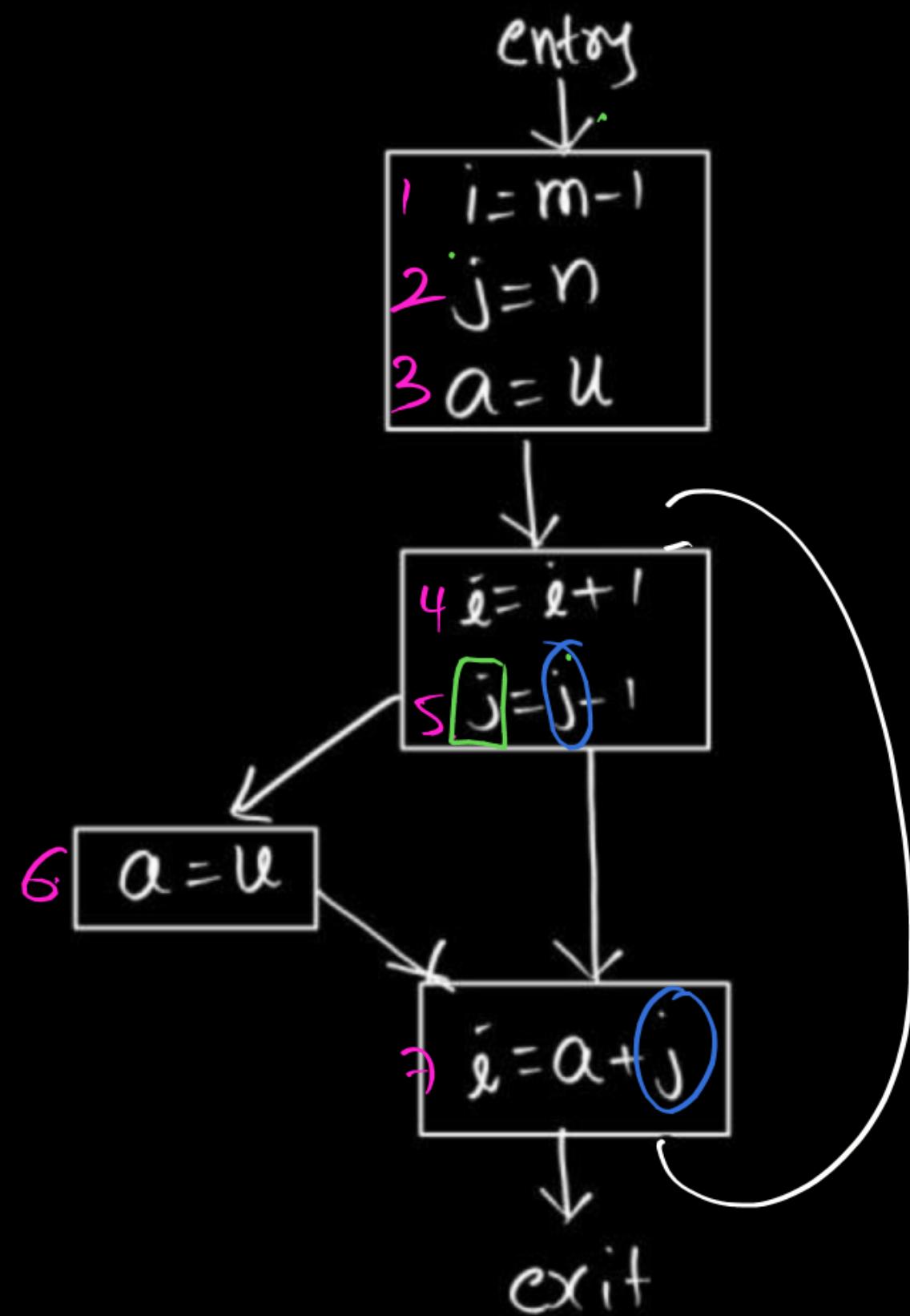
H.W
④



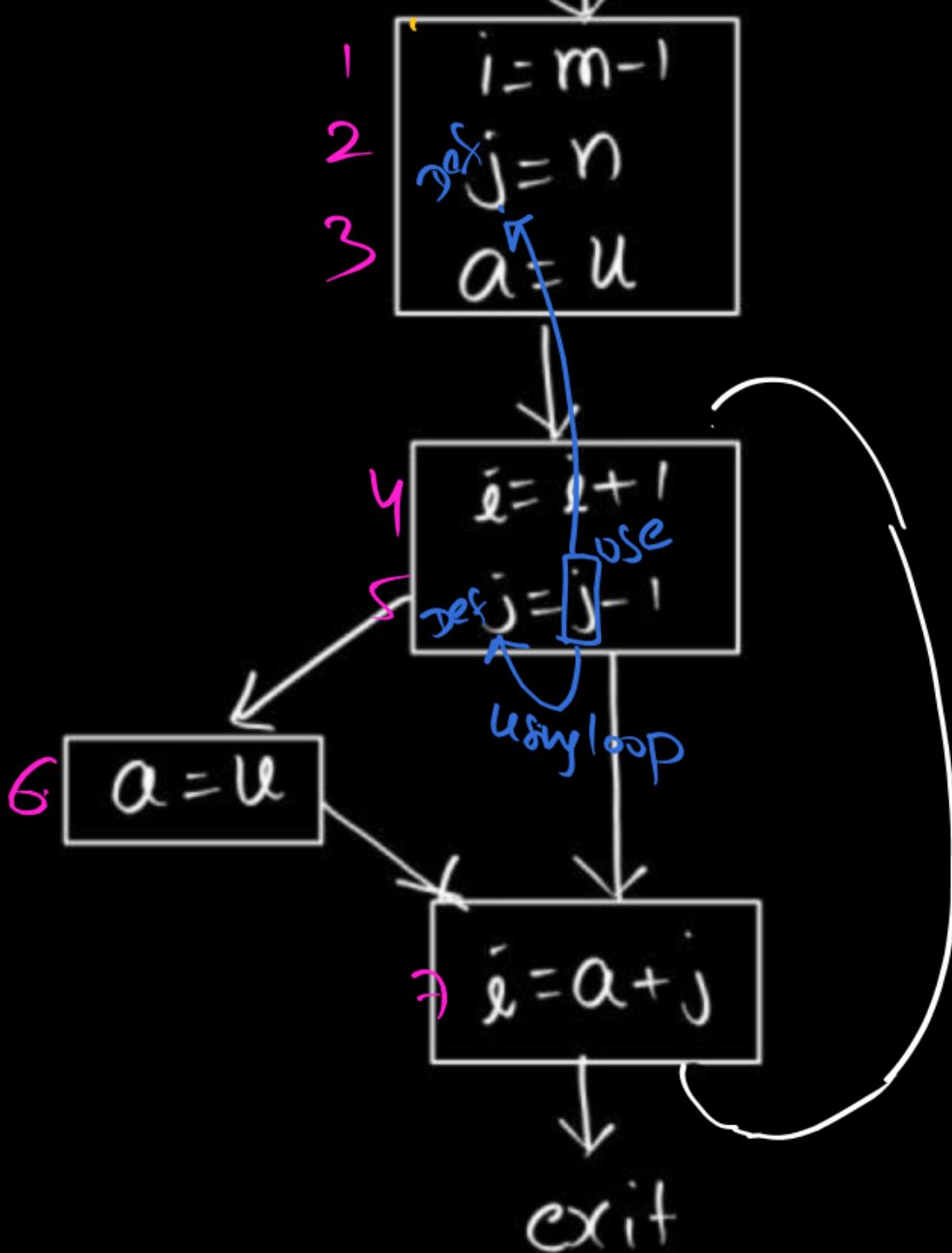
At statement 1 : Live Range(i) = ?
 $1 \rightarrow 2 \rightarrow 3 \rightarrow 4$

At statement 4 : Live Range(i) = ?
Nil

At statement 7 : Live Range(i) = ?
 $7 \rightarrow 4$



Reaching Definitions: entry



I) USE - DEF chains

At statement $\overset{\text{for } j}{S}$: S

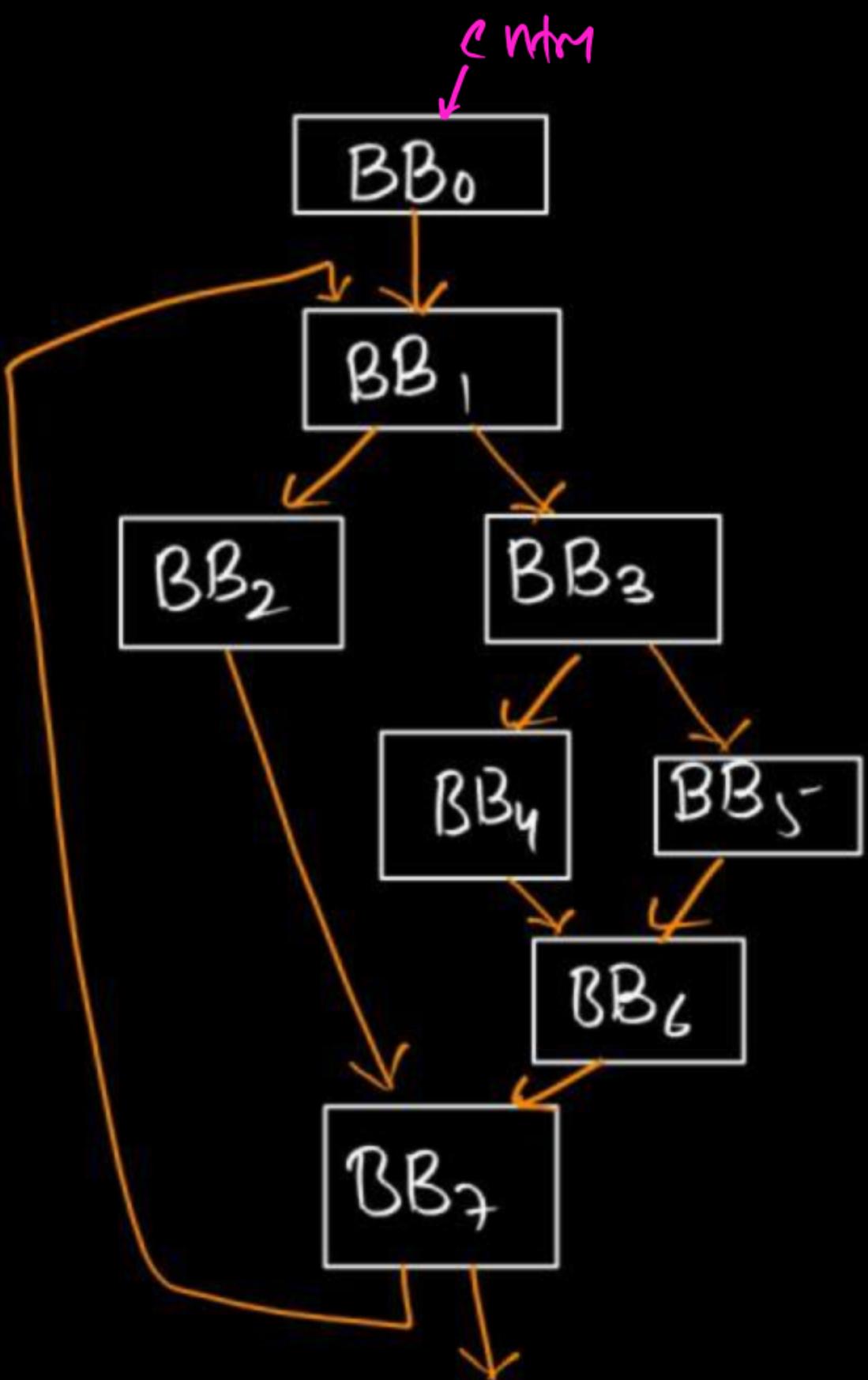
$$\begin{array}{c} \text{source} \\ S \rightarrow 2 \\ S \rightarrow 5 \end{array}$$

At statement $\overset{\text{for } j}{\gamma}$: $\gamma \rightarrow S$

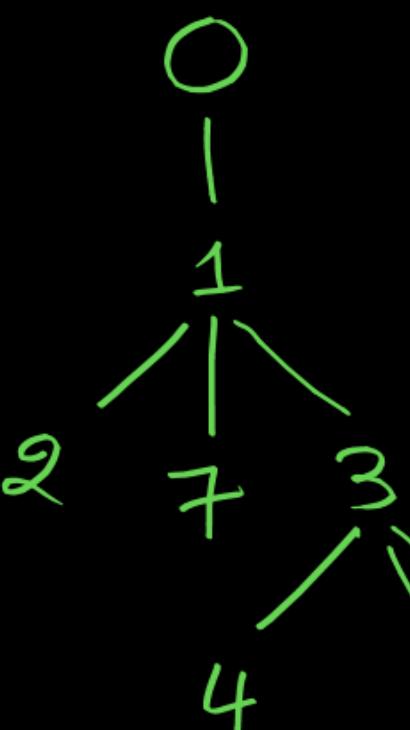
II) DEF - USE chains

At statement S : $S \rightarrow \gamma$
 $S \rightarrow S$

At statement $\overset{\text{for } j}{L}$: $L \rightarrow S$



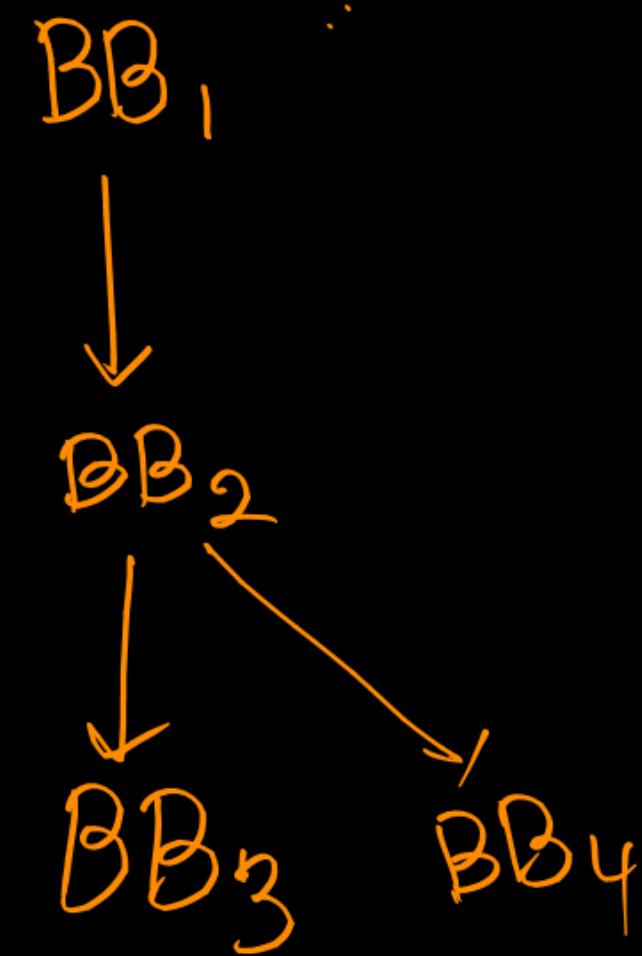
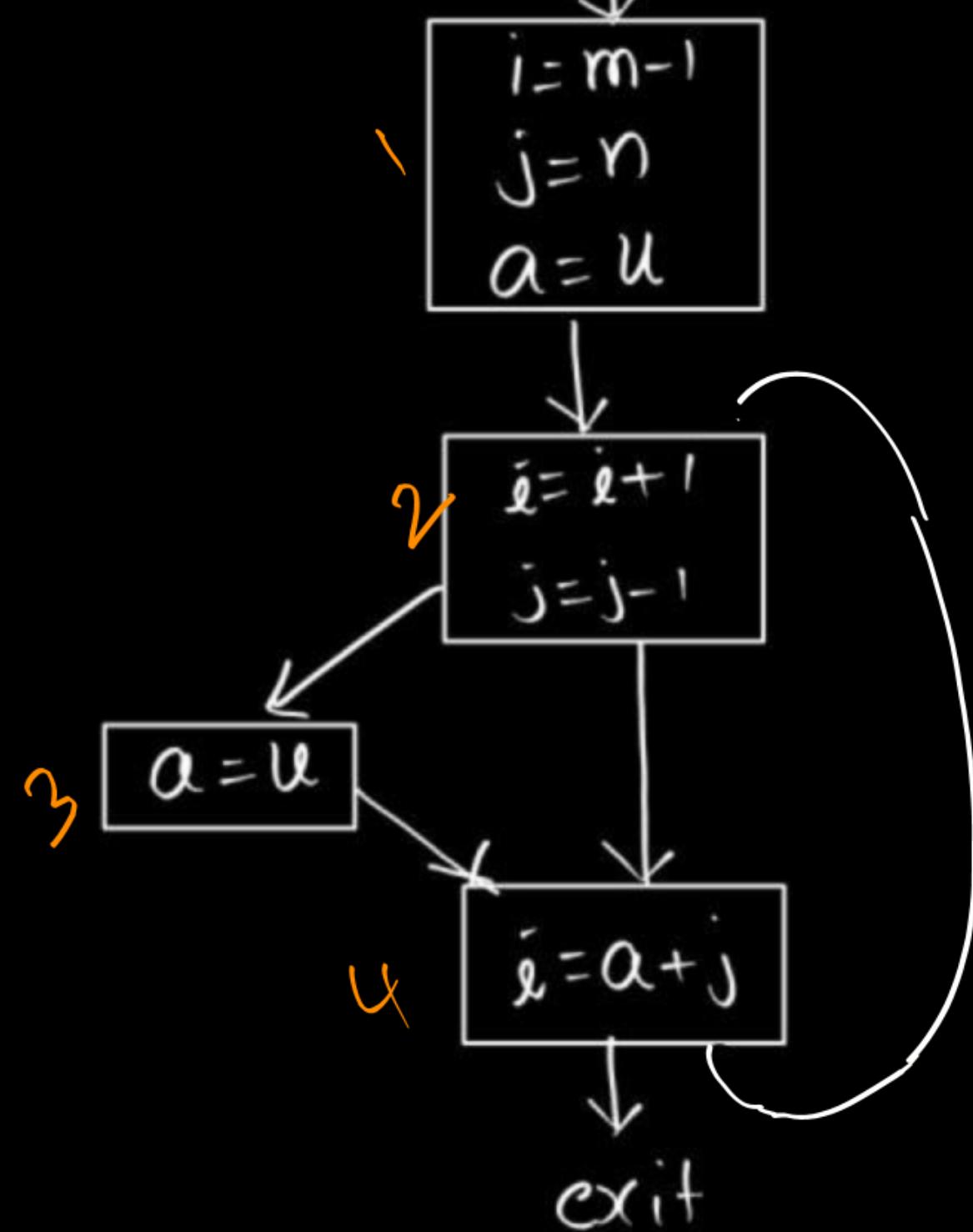
Dominator Tree



BB	Dominated by
0	0
1	0, 1
2	0, 1, 2
3	0, 1, 3
4	0, 1, 3, 4
5	0, 1, 3, 5
6	0, 1, 3, 6
7	0, 1, 7

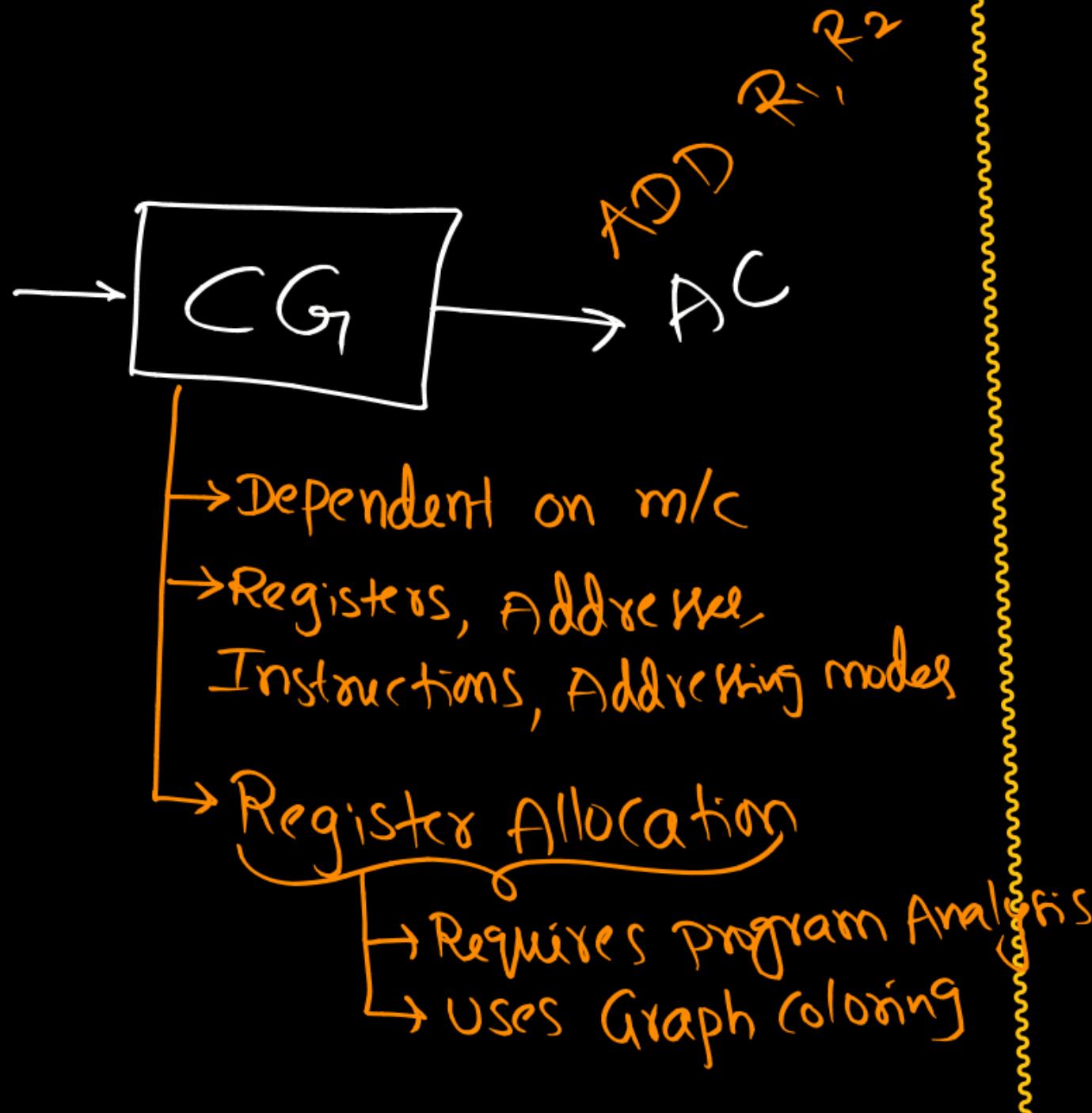
Reaching Definitions: entry

PW



Code Generation

$x-y+x$
 yc



Run Time Environment

- Parameter passing
 - [Call by value
 - [Call by Reference]
- Memory Allocation
 - Static
 - Stack
 - Dynamic
 - Heap
- Activation Record

Static Memory Allocation \Rightarrow Doesn't Support Recursion

Stack Memory Allocation \Rightarrow Supports Recursion

Control Flow Graph

```
s := 0  
i := 1  
L1: if i > n goto L2  
    t := i * i  
    s := s + t  
    i := i + 1  
    goto L1  
L2: return s
```

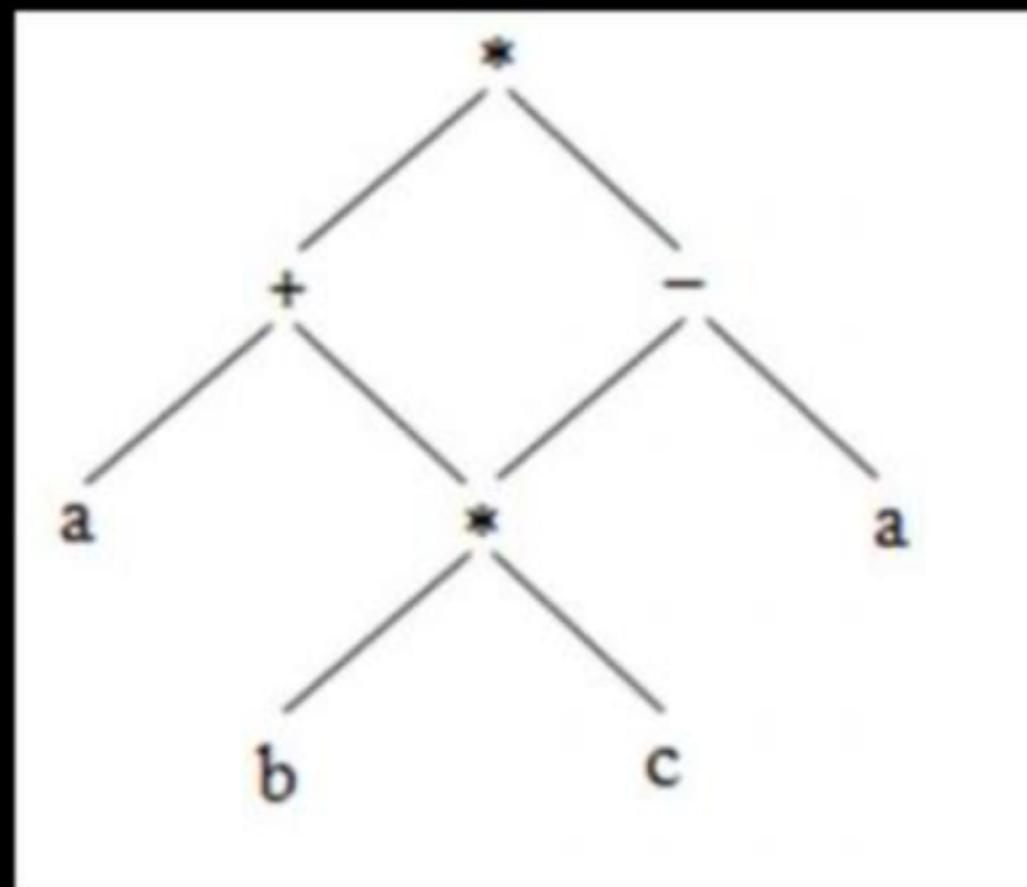
H.W.

- Q1) Draw CFG
- Q2) GEN, KILL, IN, OUT Sets for each BB
- Q3) Dominator Tree
- Q4)
 - Every use of i , find definitions of i
 - Every def of i , find uses of i
- Q5) Find live variables at every statement

Control Flow Graph

```
1  receive m (val)
2  f0 ← 0
3  f1 ← 1
4  if m <= 1 goto L3
5  i ← 2
6  L1: if i <= m goto L2
7  return f2
8  L2: f2 ← f0 + f1
9  f0 ← f1
10 f1 ← f2
11 i ← i + 1
12 goto L1
13 L3: return m
```

Q1 Find equivalent expression for the following syntax tree.



- (a) $((a + b) * c) * (b * (c - a))$
- (b) $a + (b * c - a)$
- (c) $(a + (b * c)) * ((b * c) - a)$
- (d) $a * (a + b * c) - a$

Q2

Find Equivalent Three Address code

$$X=((a*a)+(a*b))-(a*b)$$

Q3

Find SSA Code

$$t_1 = b * c$$

$$t_2 = a + t_1$$

$$t_3 = b * c$$

$$t_4 = d * t_3$$

$$t_5 = t_2 + t_4$$

Q4

Finding minimum number of variables in 3AC and SSA

$$t_1 = a * b$$

$$t_2 = f / t_1$$

$$t_3 = a * t_2$$

$$t_4 = b * t_3$$

$$t_5 = t_4 + e$$

Q5

Finding minimum number of variables in 3AC and SSA

$$t_1 = (a + b)$$

$$t_2 = (c + d)$$

$$t_3 = t_1 + t_2$$

$$t_4 = t_1 + e$$

$$t_5 = t_4 + d$$

Q6

Finding minimum number of variables in 3AC and SSA

$$p = q + r$$

$$s = p + 1$$

$$t = q + r$$

$$u = s + t$$

$$v = t + u$$

Q7

Finding minimum number of nodes in DAG

$$p = q + r$$

$$s = p + 1$$

$$t = q + r$$

$$u = s + t$$

$$v = t + u$$

Three address codes can be implemented by

- (a) indirect triples
- (b) direct triples
- (c) quadruples
- (d) none of the above

An array $a[n]$ is used in the following Pseudo code and each element of array is size of 8 bytes.

```
do
  i=i+1;
  while (a[i]>v);
```

Which of the following is equivalent 3-address code for above program.

(a) L: $t_1 = i+1$
 $i = t_1$
 $t_2 = i*8$
 $t_3 = a[t_2]$
if $t_3 > v$ goto L

(b) L: $t_1 = i+1$
 $t_2 = i*8$
 $t_3 = a[t_2]$
if $t_3 < v$ goto L

(c) L: $t_1 = i+1$
 $t_2 = i*8$
 $t_3 = a[t_2]$
if $t_3 > v$ goto L

(d) L: $t_1 = i+1$
 $i = t_1$
 $t_2 = i*8$
 $t_3 = a[t_2]$
if $t_3 < v$ goto L

Q10

Consider the following code segment.

$x = u - t;$

$y = x * v;$

$x = y + w;$

$y = t - z;$

$y = x * y;$

The minimum number of total variables required to convert the above code segment to static single assignment form is _____.

(GATE – 16 – SET1)

Q11

Consider the following intermediate program
in three address code

$$p = a - b$$

$$q = p * c$$

$$p = u * v$$

$$q = p + q$$

Which one of the following corresponds to a static single assignment form of the above code?

(GATE – 17- SET1)

(a) $p_1 = a - b$

$$q_1 = p_1 * c$$

$$p_1 = u * v$$

$$q_1 = p_1 + q_1$$

(b) $p_3 = a - b$

$$q_4 = p_3 * c$$

$$p_4 = u * v$$

$$q_5 = p_4 + q_4$$

(c) $p_1 = a - b$

$$q_1 = p_2 * c$$

$$p_3 = u * v$$

$$q_2 = p_4 + q_3$$

(d) $p_1 = a - b$

$$q_1 = p * c$$

$$p_2 = u * v$$

$$q_2 = p + q$$

Q12

For a C program accessing $X[i][j][k]$, the following intermediate code is generated by a compiler. Assume that the size of an integer is 32 bits and the size of character is 8 bits.

$$t_0 = i * 1024$$

$$t_1 = j * 32$$

$$t_2 = k * 4$$

$$t_3 = t_1 + t_0$$

$$t_4 = t_3 + t_2$$

$$t_5 = X[t_4]$$

Which one of the following statements about the source code for the C program is CORRECT?

(GATE - 14 - SET2)

- (a) X is declared as “int $X[32][32][8]$ ”
- (b) X is declared as “int $X[4][1024][32]$ ”
- (c) X is declared as “char $X[4][32][8]$ ”
- (d) X is declared as “char $X[32][16][2]$ ”

Q13

The program below uses six temporary variables a, b, c, d, e, f.

a = 1

b = 10

c = 20

d = a + b

e = c + d

f = c + e

b = c + e

e = b + f

d = 5 + e

return d + f

Assuming that all operations take their operands from registers, what is the minimum number of registers needed to execute this program without spilling?

(GATE - 10)

(a) 2

(b) 3

(c) 4

(d) 6

Q14

Consider the basic block given below.

$$a = b + c$$

$$c = a + d$$

$$d = b + c$$

$$e = d - b$$

$$a = e + b$$

The minimum number of nodes and edges present in the DAG representation of the above basic block respectively are

(GATE – 14 – SET3)

- (a) 6 and 6
- (b) 8 and 10
- (c) 9 and 12
- (d) 4 and 4

Find number of nodes and edges in CFG.

Q15

- (1) $X := 20$
- (2) if $X \geq 10$ goto (8)
- (3) $X := X - 1$
- (4) $A[X] := 10$
- (5) if $X < 4$ goto (7)
- (6) $X := X - 2$
- (7) goto (2)
- (8) $Y := X + 5$

MCQ



Consider the following grammar G.

$$S \rightarrow F \mid H$$

$$F \rightarrow p \mid c$$

$$H \rightarrow d \mid c$$

Where S, F and H are non-terminal symbols, p, d and c are terminal symbols.

Which of the following statements(s) is/are correct?

S1: LL(1) can parse all strings that are generated using grammar G.

S2: LR(1) can parse all strings that are generated using grammar G.

- A Only S1
- B Only S2
- C Both S1 and S2
- D Neither S1 and S2

[GATE-2015-CS: 2M]

MCQ

Among simple LR (SLR), canonical LR, and look-ahead LR (LALR), which of the following pairs identify the method that is very easy to implement and the method that is the most powerful, in that order?

[GATE-2015-CS: 1M]

- A SLR, LALR
- B Canonical LR, LALR
- C SLR, canonical LR
- D LALR, canonical LR

MCQ

Which one of the following is TRUE at any valid state in shift-reduce parsing?

[GATE-2015-CS: 1M]

- A Viable prefixes appear only at the bottom of the stack and not inside
- B Viable prefixes appear only at the top of the stack and not inside
- C The stack contains only a set of viable prefixes
- D The stack never contains viable prefixes

MCQ

Consider the grammar defined by the following production rules, with two operators * and +

$$S \rightarrow T * P$$

$$T \rightarrow U \mid T * U$$

$$P \rightarrow Q + P \mid Q$$

$$Q \rightarrow Id$$

$$U \rightarrow Id$$

Which one of the following is TRUE?

[GATE-2014-CS: 1M]

- A + is left associative, while * is right associative
- B + is right associative, while * is left associative
- C Both + and * are right associative
- D Both + and * are left associative

MCQ

A canonical set of items is given below

$$S \rightarrow L. > R$$

$$Q \rightarrow R.$$

On input symbol $>$ the set has

[GATE-2014-CS: 1M]

- A a shift-reduce conflict and a reduce-reduce conflict.
- B a shift-reduce conflict but not a reduce-reduce conflict.
- C a reduce-reduce conflict but not a shift-reduce conflict.
- D neither a shift-reduce nor a reduce-reduce conflict.

MCQ

Consider the following two sets of LR(1) items of LR(1) grammar.

$$X \rightarrow c.X, c/d$$

$$X \rightarrow c.X, \$$$

$$X \rightarrow .cX, c/d$$

$$X \rightarrow .cX, \$$$

$$X \rightarrow .d, c/d$$

$$X \rightarrow .d, \$$$

Which of the following statement related to merging of the two sets in the corresponding LALR parser is/are FALSE?

1. Cannot be merged since look aheads are different.
2. Can be merged but will result in S-R conflict.
3. Can be merged but will result in R-R conflict.
4. Cannot be merged since goto on c will lead to two different sets.

A 1 only

B 2 only

[GATE-2015-CS: 2M]

C 1 and 4 only

D 1, 2, 3 and 4

MCQ

What is the maximum number of reduces moves that can be taken by a bottom up parser for a grammar with no epsilon and unit productions (i.e. of type $A \rightarrow \epsilon$ and $A \rightarrow a$) to parse a string with n tokens?

- A n/2
- B n-1
- C 2^{n-1}
- D 2^n

[GATE-2013-CS: 1M]

MCQ

The grammar $S \rightarrow aSa \mid bS \mid c$ is

[GATE-2010-CS: 2M]

- A LL(1) but not LR(1)
- B LR(1) but not LL(1)
- C Both LL(1) and LR(1)
- D Neither LL(1) nor LR(1)

MCQ

An LALR(1) parser for a grammar G can have shift-reduce (S-R) conflicts if and only if [GATE-2008-CS: 2M]

- A The SLR(1) parser for G has S-R conflicts
- B The LR(1) parser for G has S-R conflicts
- C The LR(0) parser for G has S-R conflicts
- D The LALR(1) parser for G has reduce-reduce conflicts.

MCQ

Which of the following describes a handle (as applicable to LR-parsing) appropriately? [GATE-2008-CS: 1M]

- A It is the position in a sentential form where the next shift or reduce operation will occur.
- B It is non-terminal whose production will be used for reduction in the next step
- C It is a production that may be used for reduction in a future step along with a position in the sentential form where the next shift or reduce operation will occur.
- D It is the production p that will be used for reduction in the next step along with a position in the sentential form where the right-hand side of the production may be found.

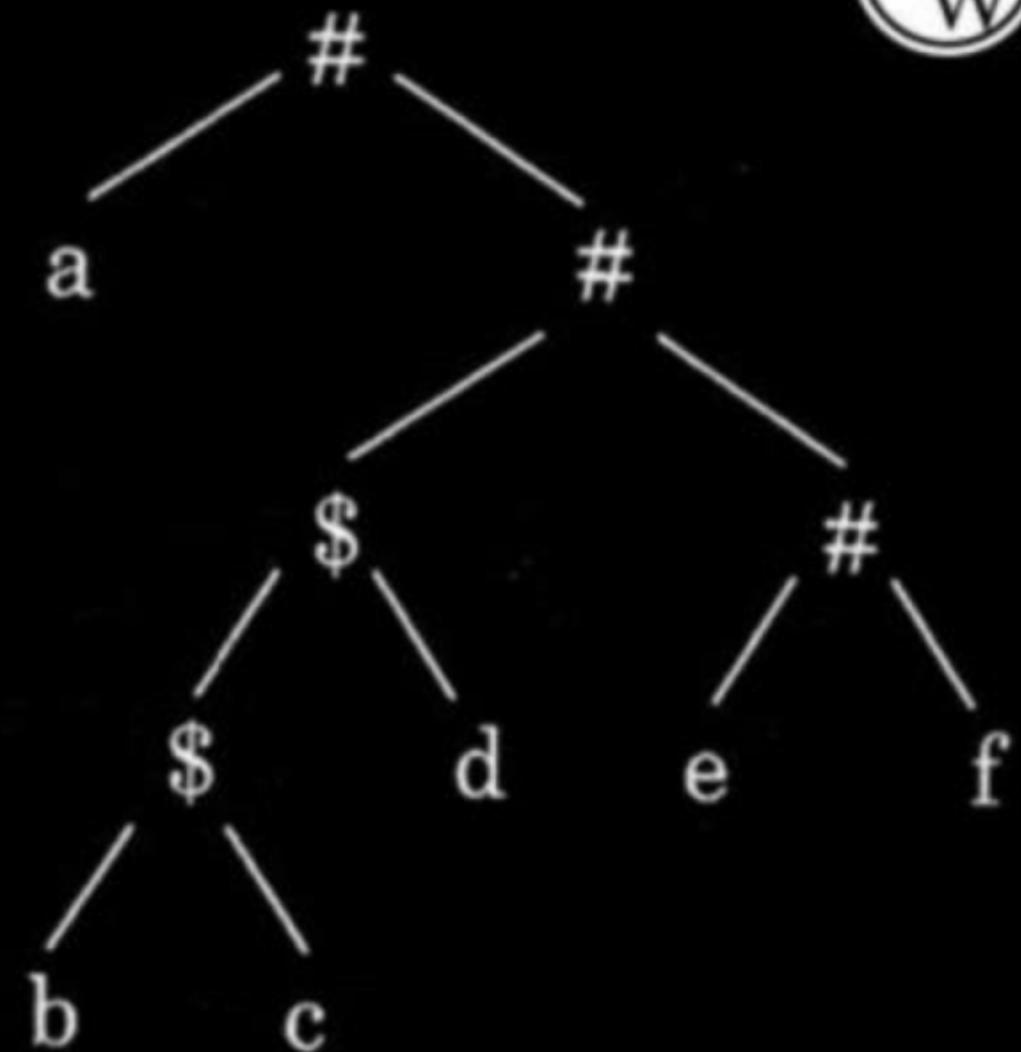
MCQ

Consider the following parse tree for the expression

$a \# b \$ c \$ d \# e \# f$,

involving two binary operators $\$$ and $\#$.

Which one of the following is correct for
the given parse tree? [GATE-2018-CS: 2M]



- A \$ has higher precedence and is left associative; # is right associative
- B # has higher precedence and is left associative; \$ is right associative
- C \$ has higher precedence and is left associative; # is left associative
- D # has higher precedence and is right associative; \$ is left associative.

MCQ

Which one of the following statements is FALSE? [GATE-2018-CS: 1M]

- A Context-free grammar can be used to specify both lexical and syntax rules.
- B Type checking is done before parsing.
- C High-level language programs can be translated to different Intermediate Representations.
- D Arguments to a function can be passed using the program stack

NAT

The attribute of three arithmetic operators in some programming language are given below.

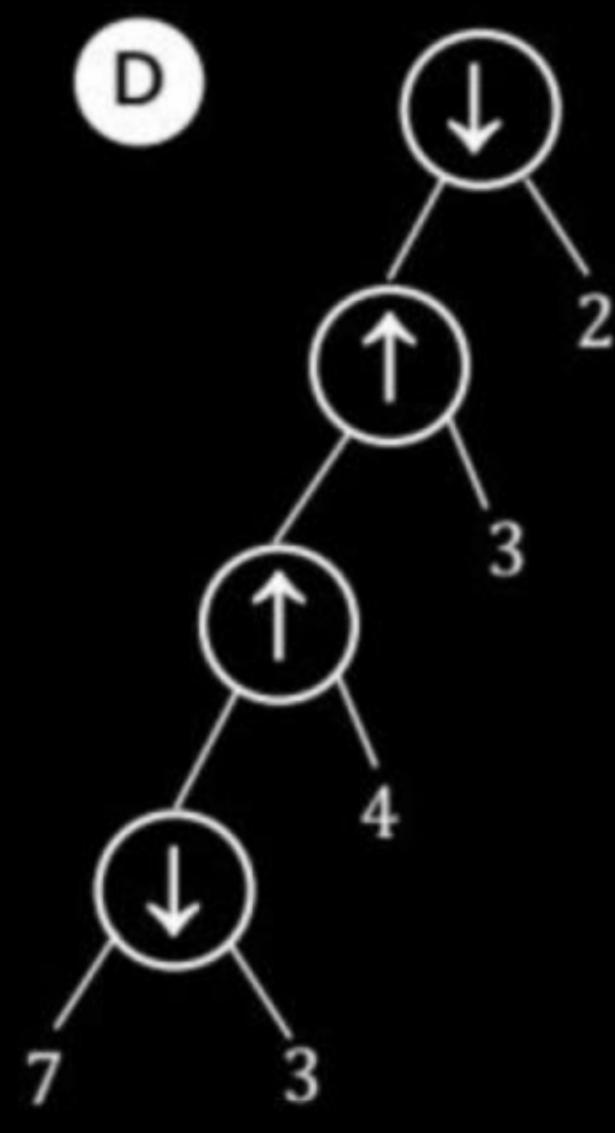
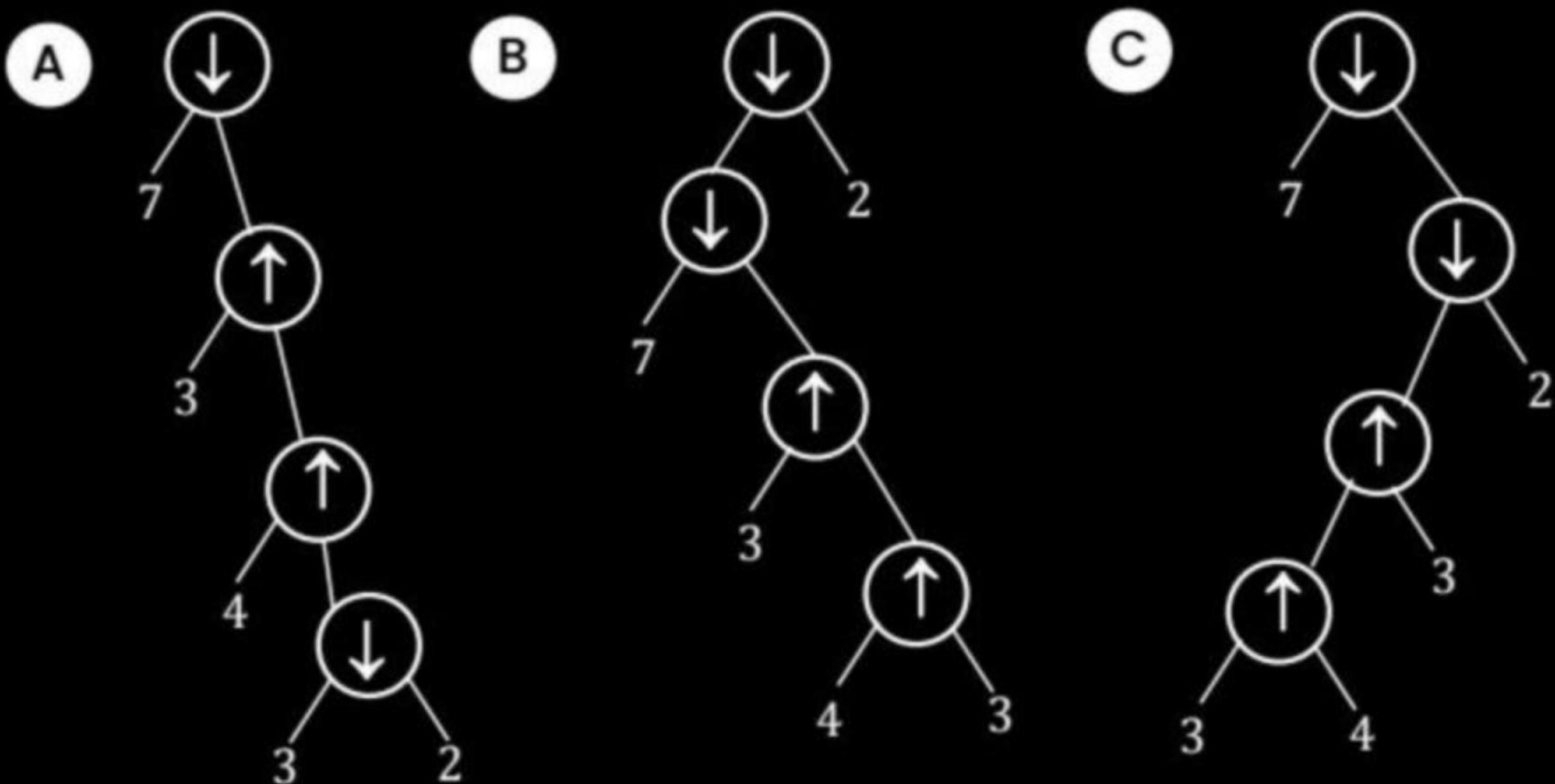
OPERATOR	PRECEDENCE	ASSOCIATIVITY	ARITY
+	High	Left	Binary
-	Medium	Right	Binary
*	Low	Left	Binary

The value of the expression $2 - 5 + 1 - 7 * 3$ in this language is _____.

[GATE-2016-CS: 2M]

MCQ

Consider two binary operators ' \uparrow ' and ' \downarrow ' with the precedence of operator \downarrow being lower than that of the operator \uparrow . Operator \uparrow is right associative while operator \downarrow is left associative. Which one of the following represents the parse tree for expression $(7 \downarrow 3 \uparrow 4 \uparrow 3 \downarrow 2)$ [GATE-2011-CS: 2M]



MCQ

A student wrote two context-free grammars G1 and G2 for generating a single C-like array declaration. The dimension of the array is at least one. For example,
`int a[10][3];`

The grammars use D as the start symbol, and use six terminal symbols `int; id [] num.`

Grammar G1

$$D \rightarrow \text{int } L;$$

$$L \rightarrow \text{id } [E]$$

$$E \rightarrow \text{num}]$$

$$E \rightarrow \text{num}][E]$$

Grammar G2

$$D \rightarrow \text{int } L;$$

$$L \rightarrow \text{id } E$$

$$E \rightarrow E[\text{num}]$$

$$E \rightarrow [\text{num}]$$

Which of the grammars correctly generate the declaration mentioned above?

A Both G1 and G2

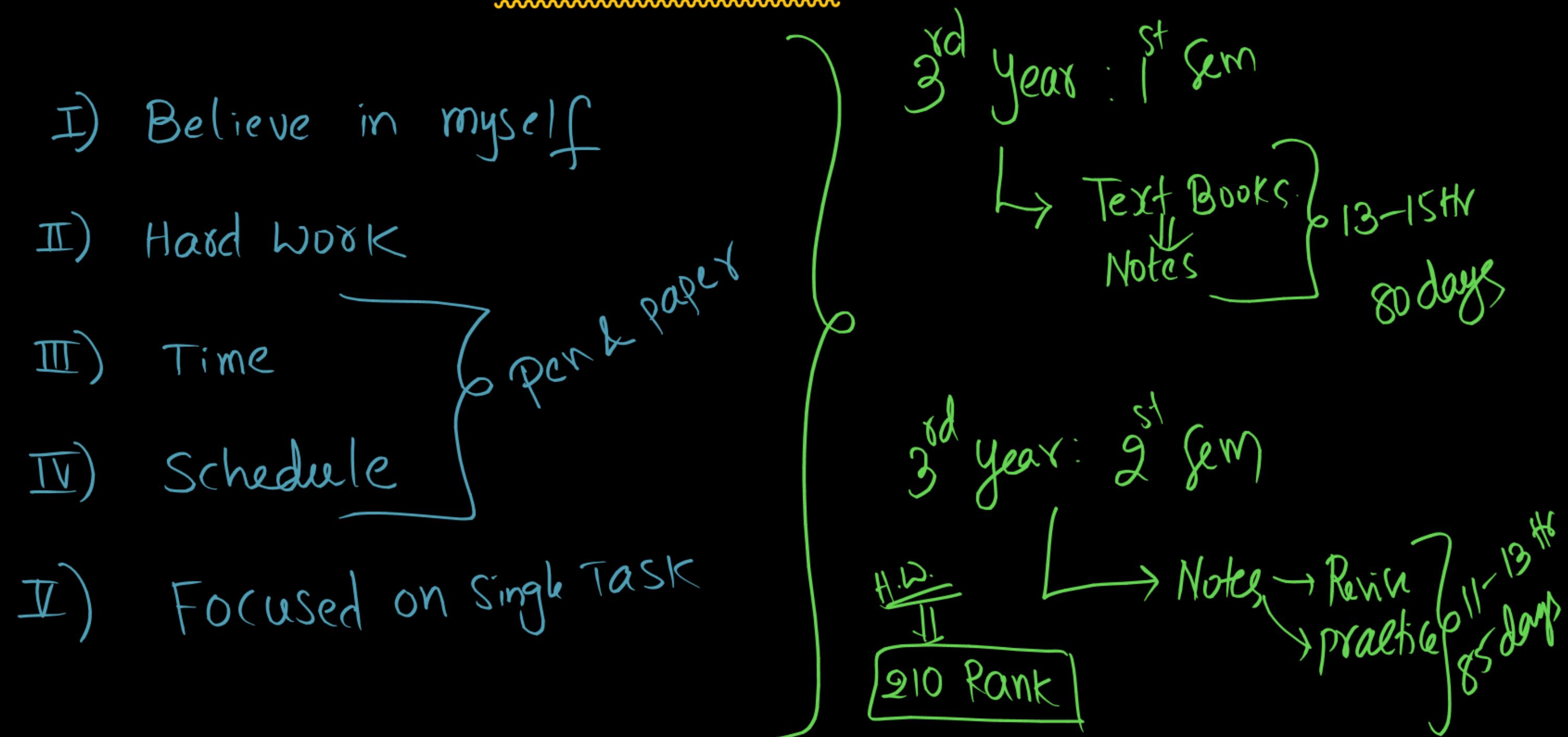
B Only G1

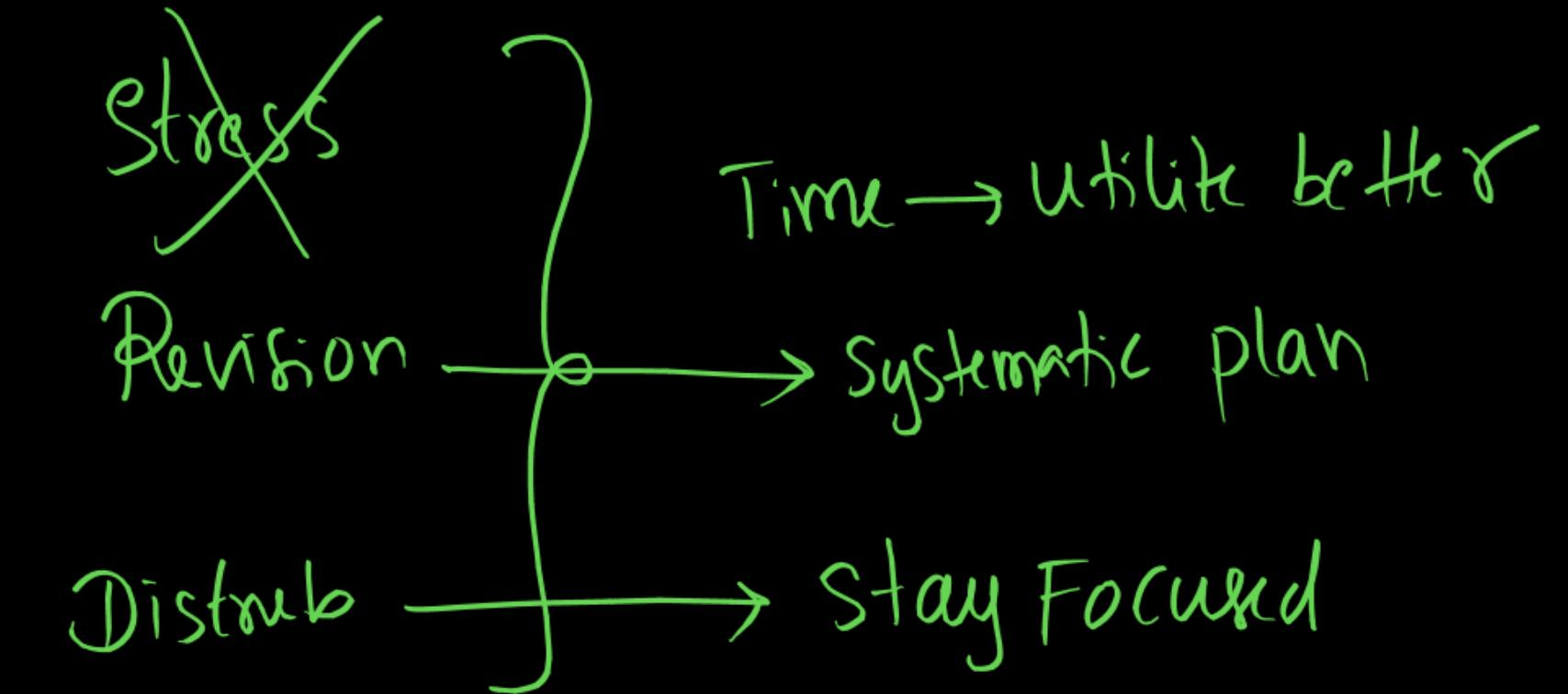
[GATE-2016-CS: 2M]

C Only G2

D Neither G1 nor G2

GATE Journey :





13 hrs
my time

Ambiguous CFG
↓
10 hrs

6 hrs
your time

Amb CFG
↓
2 hrs

Understand → First



Apply (practise) → Next

If

Review

Summary

DEVA SIR PKI

Telegram group

Thank you
PW
Soldiers

