



# COMPUTER SCIENCE

## Database Management System

### Query Language

Lecture\_1



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A graphic of a construction barrier with orange and white diagonal stripes and two yellow bollards at the top. It is positioned on the left side of the slide.

**TOPICS  
TO BE  
COVERED**

**01**

**Relational Algebra**

**02**

**Operators**

1 FD & Normalization

2 Transaction & Concurrency Control

3 ER MODEL & Conversion & Foreign key Concept

4 Query language

# Relational - Model (RDBMS)

E.F. Codd

Theoretical : RA, RC

Practical : SQL

Relational

## Query language

① Procedural  
Q.L

↳ Relational  
Algebra.

② Non Procedural  
Q.L

SQL  
XTRC  $\xrightarrow{RC \& DRC}$

# Query Language



## Procedural Query Language

- ↳ WHAT to Retrieve from DB
- ↳ HOW to Retrieve from DB

## Relational Algebra:

## Non Procedural Query Language

- ↳ WHAT to Retrieve from DB.
- SQL
- TRC

# Procedural Query Language and Non-procedural Query Language



## Procedural Query Language

Formulation of how to access data  
from the database table and what  
data required to retrieve from DB  
tables.

“Relational Algebra”

## Non-procedural Query Language

Formulation of what data retrieve  
from DB tables.

“Relational Calculus”  
“SQL”

## Relational Algebra.

The Basic Idea of Query language is Query  
executed On a DB Table (Relation) Table by Table (Step By  
One Tuple at a time Step)

## Difference b/w R.A & SQL.

RA  
↳ By default  
↳ Distinct  
↳ Output

SQL  
↳ By default  
↳ Duplicate Retain

# Relational Algebra



(Always generate distinct tuples)

Relational algebra refers to a procedural query language that takes relation instances as input and returns relation instances as output

Input : Relation (Table)

Output : Relation (Table)

# Relational Algebra

## Basic operators

- ① Selection [ $\sigma$ ]
- ② Projection [ $\pi$ ]
- ③ CROSS Product [ $\times$ ]
- ④ UNION [ $\cup$ ]
- ⑤ set Difference [ $-$ ]
- ⑥ Rename [ $\rho$ ]

## Derived operator

- ① JOIN ( $\bowtie$ ) & its type (using  $X, \sigma, \Pi$ )
- ② Division [ $\sqsupset$ ]
- ③ Intersection [ $\cap$ ]  
$$R \cap S = R - (R - S)$$

$$R \cap S = R - (R - S)$$

Q3)  $R : [1, 2, 3, 4, 5, 6]$

$$S : [4, 5, 6, 7, 8, 9, 10, 11]$$

$$R.H.S \Rightarrow [1, 2, 3]$$

$$R - (R - S) \Rightarrow [1, 2, 3, 4, 5, 6] - [1, 2, 3] = [4, 5, 6] \in R \cap S$$

L.H.S  
 $R \cap S = [4, 5, 6]$

# Relational Algebra



## Basic operators

- ①  $\pi$  : Projection operator
- ②  $\sigma$  : Selection operator
- ③  $\times$  : Cross-product operator
- ④  $U$  : Union
- ⑤  $-$  : Set difference MINUS
- ⑥  $\rho$  : Rename operator [ρ]

## Derived operators

- ①  $\cap$  : Intersection {using “ $-$ ”}
- ②  $\bowtie$  : Join {using  $X, \sigma$ } & its type
- ③ / or  $\div$  : Division {using  $\pi, x, -$ }

## Selection [ $\sigma$ ]:

It Select the Tuples | Based  
on Specified Condition.

### Syntax

$\sigma_{\text{Condition}}$  (Relation)

(e.g.)

$\sigma_{CGPA > 9}$  (Student)

$\sigma_{State = 'WB'}$  (Student)

Record | Row

## Projection [ $\Pi$ ]

It Select  
Field / Attribute / Attribute list  
from Relation.

### Syntax

$\Pi_{\text{Attribute}}$  |  $\Pi_{\text{Attribute or Attribute list}}$  (Relation)

(e.g.)  $\Pi_{\text{Sname}}$  (Student)

$\Pi_{\text{Sname Contact}}$  (Student)

①  $\Pi_{\text{RollNo}}(\text{Student})$

OP  $\rightarrow$

RollNo
1
2
3
4
5
6
7

②  $\Pi_{\text{Name}}(\text{STUDENT})$

OP  $\rightarrow$

Abhay
Priyanshu
Shivansh
Sourav
Tarun

STUDENT

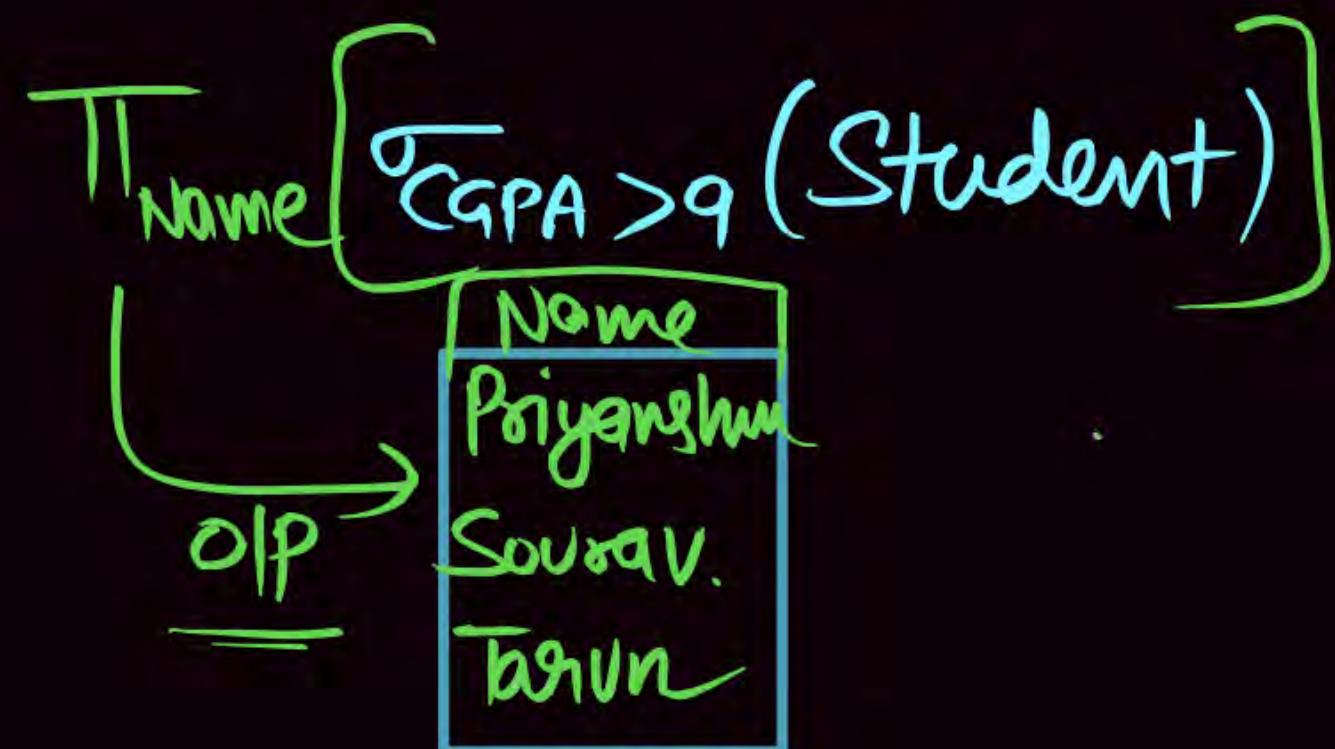
RollNo	Name	GPA
1	Abhay	9
2	Priyanshu	10
3	Shivansh	9
4	Sourav.	10
5	Priyanshu	9
6	Tarun	10
7	Abhay	9

①

$\sigma_{CGPA > 9} (\text{Student})$

RollNo	Name	CGPA
2	Priyanshu	10
4	Sourav	10
6	Tarun	10

②



## STUDENT

RollNo	Name	GPA
1	Abhay	9
2	Priyanshu	10
3	Shivansh	9
4	Sourav.	10
5	Priyanshu	9
6	Tarun	10
7	Abhay	9

# Relational Algebra



## Basic operators

### I. $\pi$ : Projection [ $\Pi$ ]

- $\pi_{\text{Attribute name}} (R)$ : It is used to project required attribute from relation R.
- $\sigma_{\text{Condition}(P)} (R)$ : It is used to select records from relation R, those satisfied the condition (P).

Condition(R)

field | column

tuple | Row

⑧ W.A.Q (Write a Query) to find  
Pname of Red Color parts ?

Soln

$\Pi_{\text{Pname}} \left[ \text{Color} = \text{Red} \text{ (Parts)} \right]$

Pname	Ans
A	
C	

Parts

Pid	Pname	Color
1	A	Red
2	B	Green
3	C	Red
4	D	Green
5	A	yellow
6	C	Blue.

# Example:

$\textcircled{R}$

R	A	B	C
A	8	4	5
B	2	4	5
C	7	4	6
D	3	5	5

$\pi_{B,C}(R)$  

①  $\pi_{B,C}(R)$ :

B	C
4	5
4	6
5	5

②  $\sigma_{A>S}(R)$ :

A	B	C
8	4	5
7	4	6

**① Reserves ( $R_1$ )**

<u>Sid</u>	<u>Bid</u>	<u>day</u>
22	101	10/10/96
58	103	11/12/96

**②**
**Sailors( $S_1$ )**

<u>Sid</u>	<u>Sname</u>	<u>Rating</u>	<u>age</u>
22	dustin	7	45.0
31	lubber	8	55.5
58	rusty	10	35.0

**③**
**Sailors( $S_2$ )**

<u>Sid</u>	<u>Sname</u>	<u>Rating</u>	<u>age</u>
28	yuppy	9	35.0
31	lubber	8	55.5
44	guppy	5	35.0
58	rusty	10	35.0

## Selection ( $\sigma$ )

R.A  $\Rightarrow$  Maintain the Order.

P  
W

Q.1  $\sigma_{\text{rating} > 8} (S_2)$

Sid	Sname	Rating	Age
28	yuppy	9	35.0
58	Rusty	10	35.0

Sailors ( $S_2$ )

Sid	Sname	Rating	age
28	yuppy	9	35.0
31	lubber	8	55.5
44	guppy	5	35.0
58	rusty	10	35.0

# Selection ( $\sigma$ )

Ans.1

$\sigma_{\text{rating} > 8} (S_2)$

Output:

Sid	Sname	Rating	age
28	yuppy	9	35.0
58	rusty	10	35.0

Sailors ( $R_2$ )

Sid	Sname	Rating	age
28	yuppy	9	35.0
31	lubber	8	55.5
44	guppy	5	35.0
58	rusty	10	35.0

Q.

 $\pi_{\text{sname, rating}} (\sigma_{\text{rating} > 8} (S_2))$ P  
W

Output:

Sname	Rating
yuppy	9
rusty	10

Sailors( $S_2$ )

Sid	Sname	Rating	age
28	yuppy	9	35.0
31	lubber	8	55.5
44	guppy	5	35.0
58	rusty	10	35.0

Q.

$$\pi_{\text{sname, rating}}(\sigma_{\text{rating} > 8}(S_2))$$
Π<sup>nd</sup>σ<sup>st</sup>

Output:

Sname	Rating
yuppy	9
rusty	10

Sailors( $S_2$ )

Sid	Sname	Rating	age
28	yuppy	9	35.0
31	lubber	8	55.5
44	guppy	5	35.0
58	rusty	10	35.0

# Projection( $\pi$ )

Q.2

 $\pi_{age}(S_2)$ 

Age
35.0
55.5

Sailors ( $R_2$ )

Sid	Sname	Rating	age
28	yuppy	9	35.0
31	lubber	8	55.5
44	guppy	5	35.0
58	rusty	10	35.0

# Projection ( $\pi$ )

Ans.2  $\pi_{age}(S_2)$

Output:

age
35.0
55.5

⑧

$\pi_{Sname Rating}(S_2)$

Sailors ( $S_2$ )

<u>Sid</u>	<u>Sname</u>	<u>Rating</u>	<u>age</u>
28	<u>yuppy</u>	9	35.0
31	<u>lubber</u>	8	55.5
44	<u>guppy</u>	5	35.0
58	<u>rusty</u>	10	35.0

Q.

 $\pi_{\text{sname, rating}}(S_2)$ **Output:**

Sname	Rating
yuppy	9
lubber	8
guppy	5
rusty	10

## Some Important Points / Conclusion .

① Reserves ( $R_1$ )

<u>Sid</u>	<u>Bid</u>	<u>day</u>
22	101	10/10/96
58	103	11/12/96

②

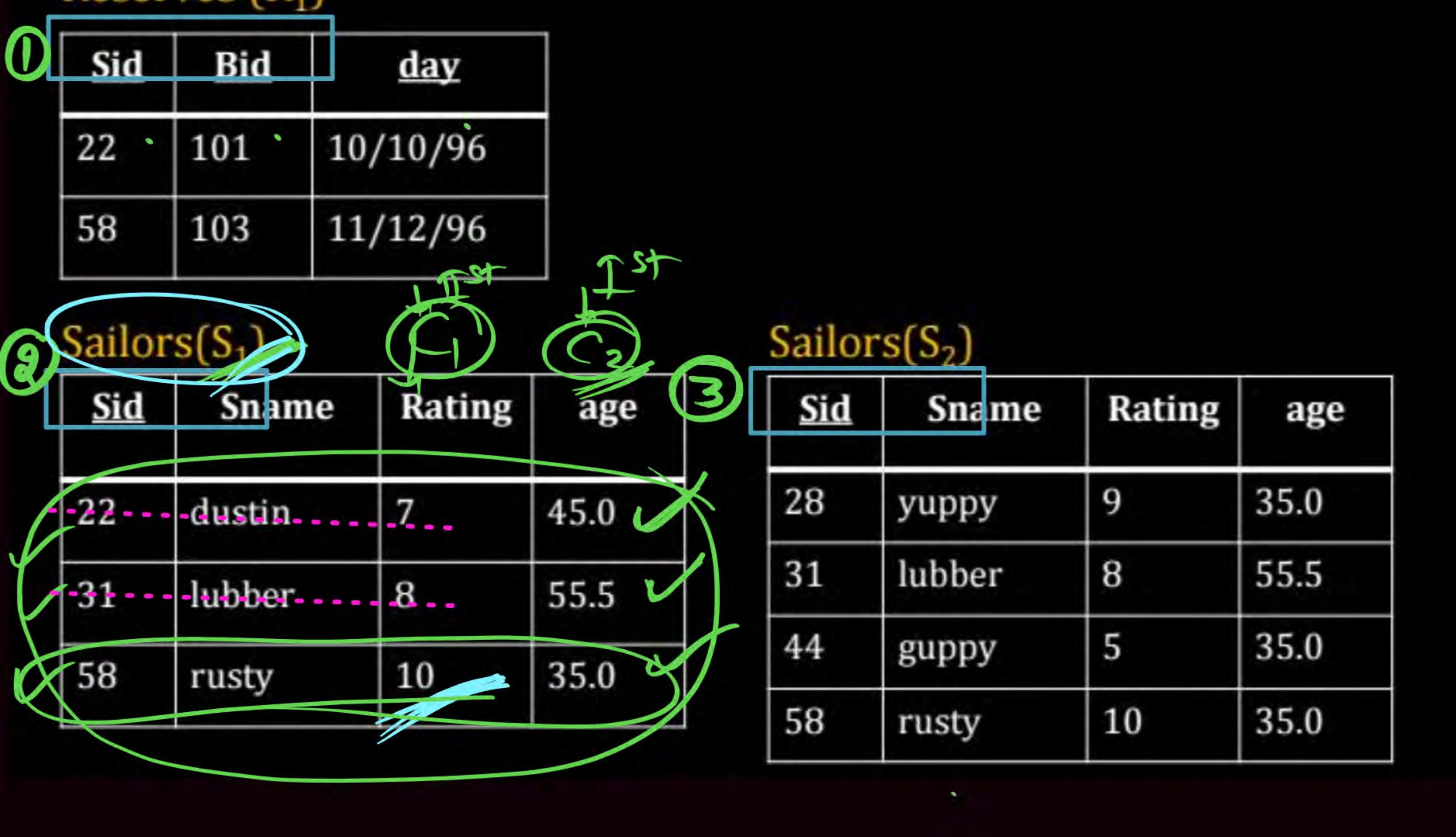
Sailors( $S_1$ )

<u>Sid</u>	<u>Sname</u>	<u>Rating</u>	<u>age</u>
22	dustin	7	45.0
31	lubber	8	55.5
58	rusty	10	35.0

③

Sailors( $S_2$ )

<u>Sid</u>	<u>Sname</u>	<u>Rating</u>	<u>age</u>
28	yuppy	9	35.0
31	lubber	8	55.5
44	guppy	5	35.0
58	rusty	10	35.0



$$\circ_{C_3}(\circ_{C_2}(\circ_{C_1}(R))) \equiv \circ_{C_2}(\circ_{C_1}(\circ_{C_3}(R)))$$

$C_1$ : Rating > 9

$C_2$ : Age  $\geq 35$

$$\circ_{C_1}(\circ_{C_2}(S_L)) \Rightarrow \circ_{Rating > 9} \left( \circ_{Age \geq 35}(S_L) \right)$$

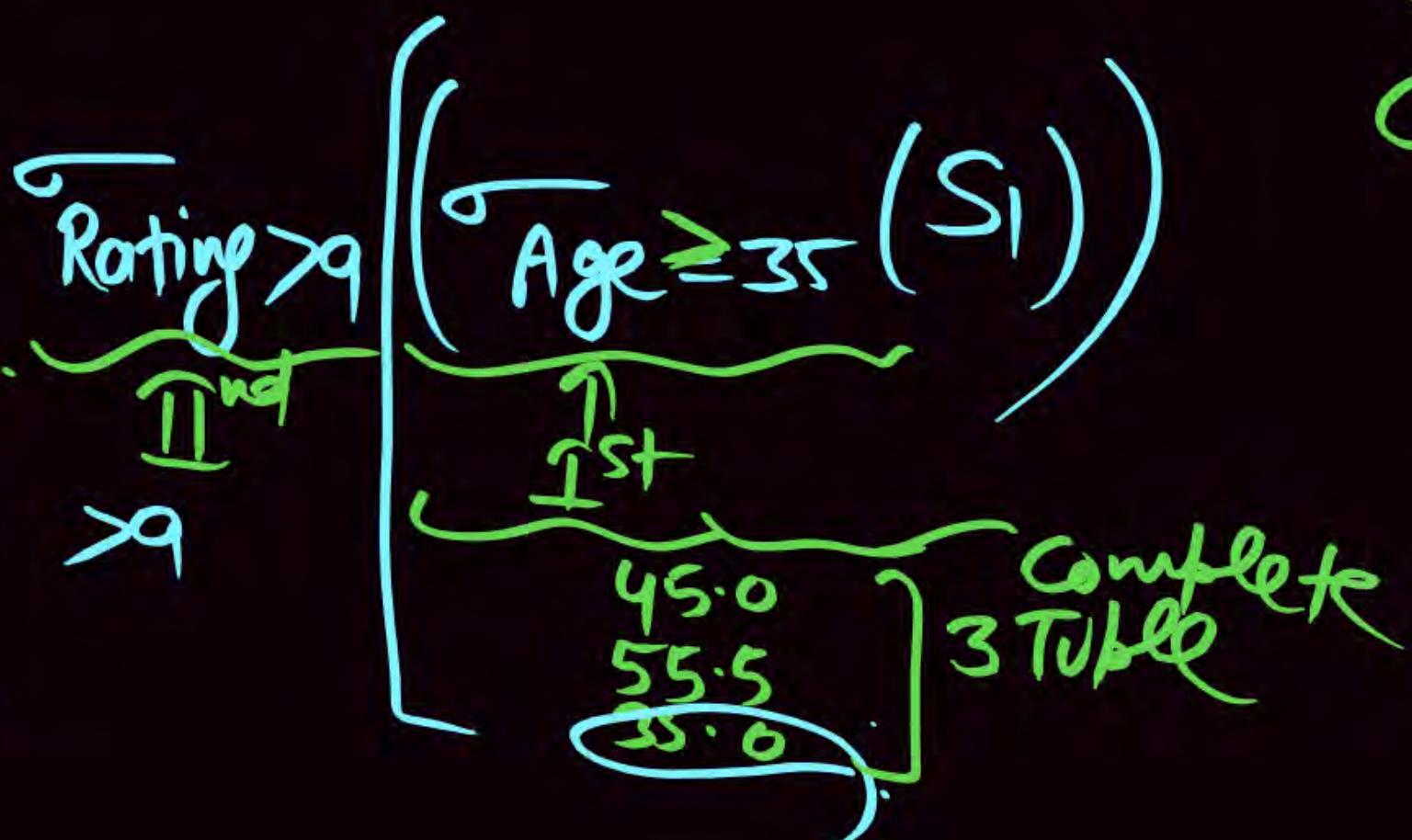
QOP

58	Rusty	10	35.0
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$C_1$ : Condition 1

$C_2$ : Condition 2

$C_3$ : Condition 3



① Reserves ( $R_1$ )

<u>Sid</u>	<u>Bid</u>	<u>day</u>
22	101	10/10/96
58	103	11/12/96

②

Sailors( $S_1$ )

<u>Sid</u>	<u>Sname</u>	<u>Rating</u>	<u>age</u>
22	dustin	7	45.0
31	lubber	8	55.5
58	rusty	10	35.0

③

④

Sailors( $S_2$ )

<u>Sid</u>	<u>Sname</u>	<u>Rating</u>	<u>age</u>
28	yuppy	9	35.0
31	lubber	8	55.5
44	guppy	5	35.0
58	rusty	10	35.0

$$\sigma_{C_3}(\sigma_{C_2}(\sigma_{C_1}(R))) \equiv \sigma_{C_2}(\sigma_{C_1}(\sigma_{C_3}(R)))$$

$C_1$ : Rating > 9

$C_2$ : Age  $\geq 35$ .

$$\sigma_{C_2}(\sigma_{C_1}(R)) \Rightarrow \underbrace{\text{Age} \geq 35}_{\text{2nd}} \left( \underbrace{\text{Rating} > 9}_{\text{1st}} (S_L) \right)$$

(OLP)

58	Rusty	10	35.0
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$C_1$ : Condition 1

$C_2$ : Condition 2

$C_3$ : Condition 3.

$$\textcircled{1} \quad \widehat{\sigma}_{C_2}(\widehat{\sigma}_{C_1}(R)) \equiv \widehat{\sigma}_{C_1}(\widehat{\sigma}_{C_2}(R))$$

Selection ( $\widehat{\sigma}$ ) is commutative.

$$\textcircled{2} \quad \widehat{\sigma}_{C_2}(\widehat{\sigma}_{C_1}(R)) \equiv \widehat{\sigma}_{C_1 \wedge C_2}(R)$$

↑  
'AND'

$$\textcircled{3} \quad \widehat{\sigma}_{\text{Age} \geq 35}(\widehat{\sigma}_{\text{Rating} > 9}(S_L)) \equiv \widehat{\sigma}_{\text{Age} \geq 35 \wedge \text{Rating} > 9}(S_L)$$

① Reserves ( $R_1$ )

<u>Sid</u>	<u>Bid</u>	<u>day</u>
22	101	10/10/96
58	103	11/12/96

②

Sailors( $S_1$ )

<u>Sid</u>	<u>Sname</u>	<u>Rating</u>	<u>age</u>
22	dustin	7	45.0
31	lubber	8	55.5
58	rusty	10	35.0

③

Sailors( $S_2$ )

<u>Sid</u>	<u>Sname</u>	<u>Rating</u>	<u>age</u>
28	yuppy	9	35.0
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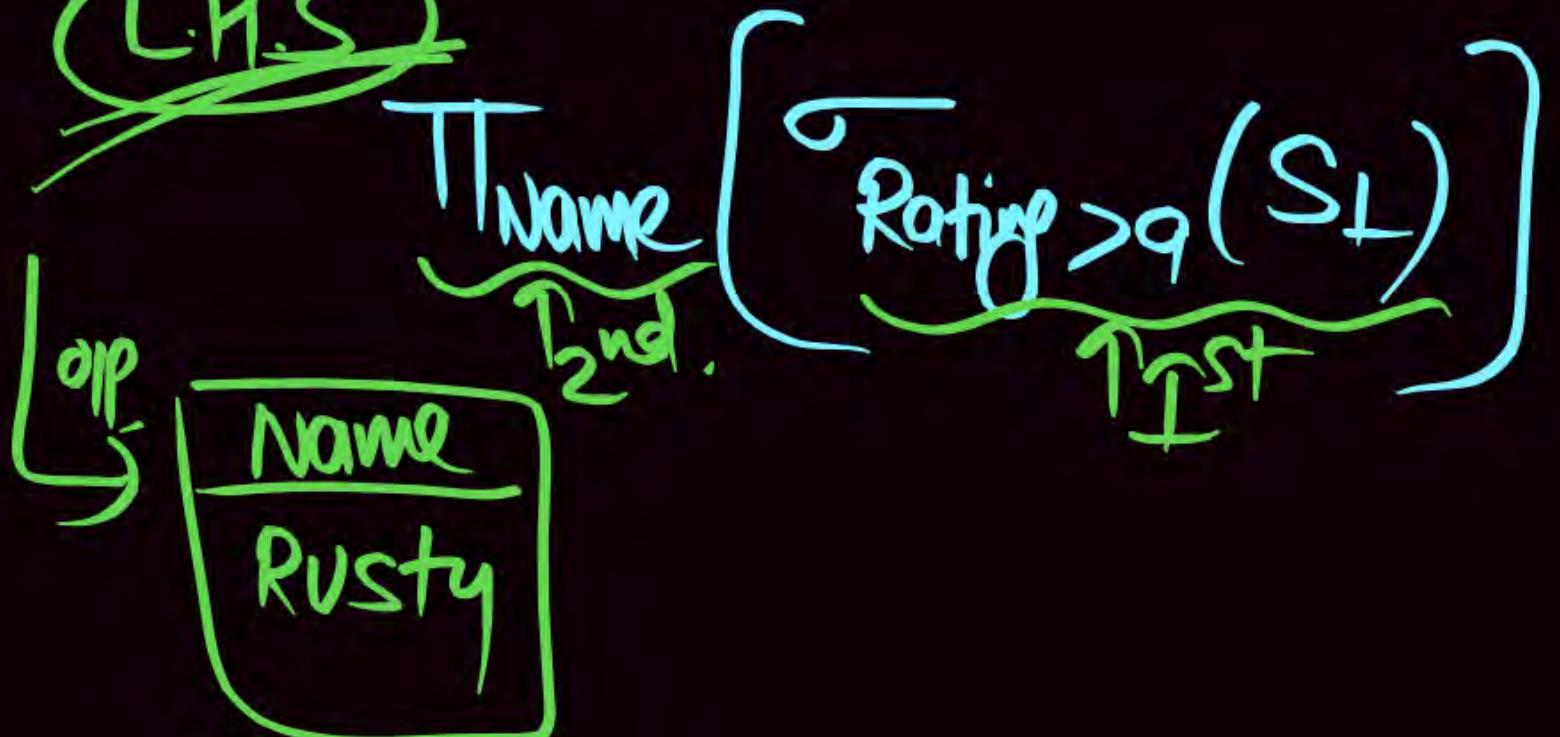
③

Condition

$C_1$ : Rating > 9

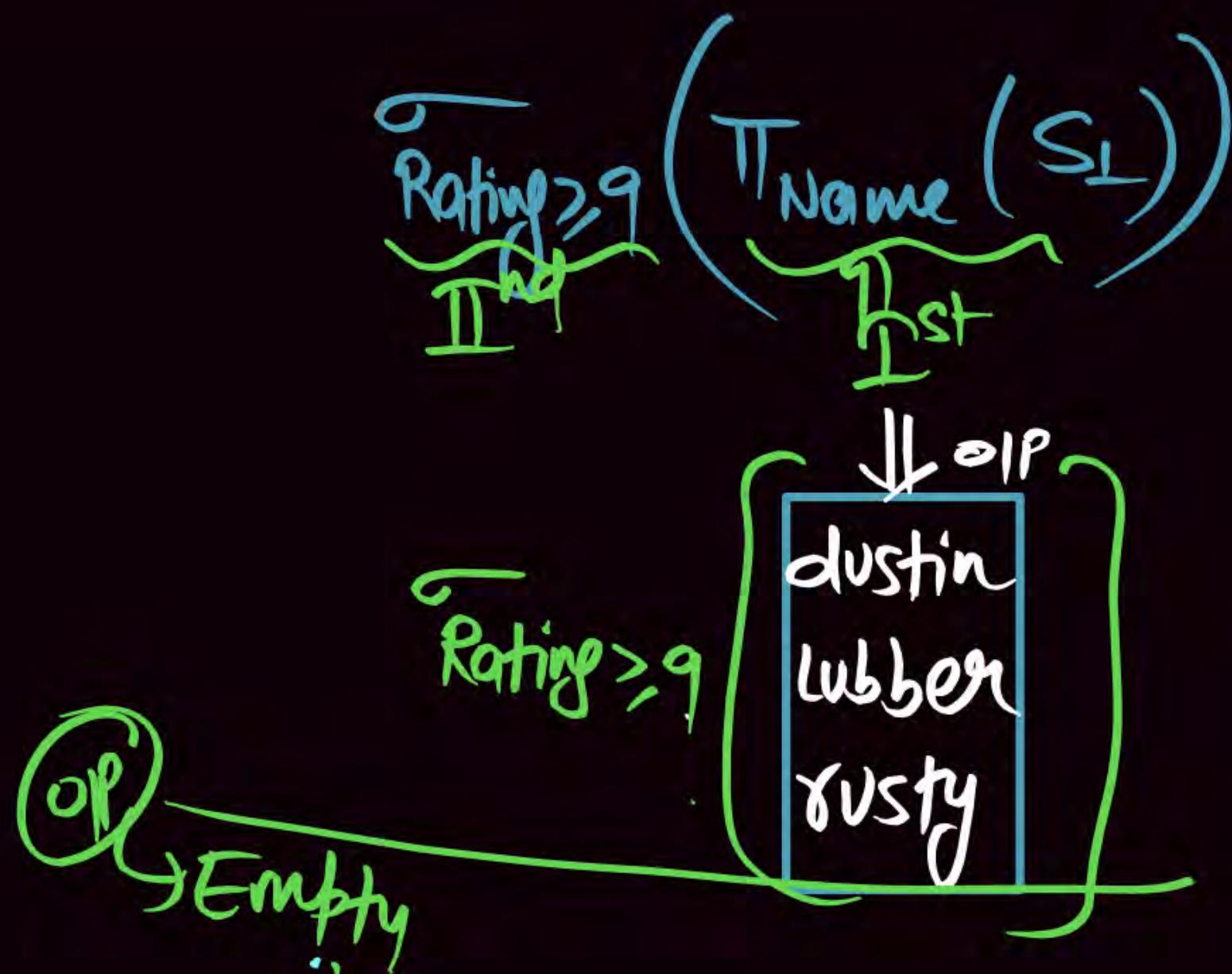
$A_L$  (Attribute) : Name

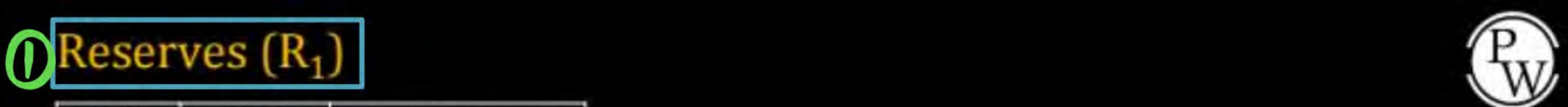
L.H.S



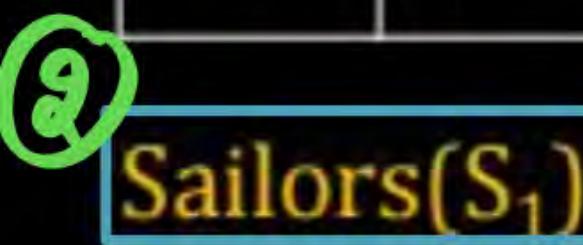
R.H.S

$$\text{L.H.S} \quad \boxed{\Pi_{A_L} [\Sigma_L(R)]} \neq \Sigma_L [\Pi_{A_L}(R)] \quad \text{R.H.S}$$





<u>Sid</u>	<u>Bid</u>	<u>day</u>
22	101	10/10/96
58	103	11/12/96



<u>Sid</u>	<u>Sname</u>	<u>Rating</u>	<u>age</u>
22	dustin	7	45.0
31	lubber	8	55.5
58	rusty	10	35.0



<u>Sid</u>	<u>Sname</u>	<u>Rating</u>	<u>age</u>
28	yuppy	9	35.0
31	lubber	8	55.5
44	guppy	5	35.0
58	rusty	10	35.0

⑧ In this L.H.S Can be Replaced/ Transformed by R.H.S

⑨

$$\underset{\text{(L.H.S)}}{C_L} \left[ T_{A_1}(R) \right] \xrightarrow{\text{YES}} T_{A_1} \left[ \underset{\text{(R.H.S)}}{C_L}(R) \right]$$

In this (L.H.S Parts) firstly Attribute  $A_1$  is selected  
then Condition  $C_L$  is Applied on Attribute  $A_1$

⑩

$A_1$  (Attribute) : Rating

$C_L$  (Condition) Rating  $\geq 9$

LHS

$$\begin{array}{c} \text{L.H.S} \\ \text{L.H.S} \end{array} \xrightarrow{\text{Rating}} \boxed{\frac{9}{10}}$$

$$\begin{array}{c} \text{L.H.S} \left[ T_{A_1}(R) \right] \\ \xrightarrow{\text{Rating} \geq 9} \left[ T_{\text{Rating}}(S_2) \right] \xrightarrow{\frac{9}{10}} \end{array}$$

① Reserves ( $R_1$ ) P  
W

<u>Sid</u>	<u>Bid</u>	<u>day</u>
22	101	10/10/96
58	103	11/12/96

②

Sailors( $S_1$ )

<u>Sid</u>	<u>Sname</u>	<u>Rating</u>	<u>age</u>
22	dustin	7	45.0
31	lubber	8	55.5
58	rusty	10	35.0

③

Sailors( $S_2$ )

<u>Sid</u>	<u>Sname</u>	<u>Rating</u>	<u>age</u>
28	yuppy	9	35.0
31	lubber	8	55.5
44	guppy	5	35.0
58	rusty	10	35.0

In this L.H.S Can be Replaced/ Transformed by R.H.S

④

$$\underset{(L.H.S)}{\overline{C_L} \left[ T_{A_1}(R) \right]} \rightarrow \underset{(R.H.S)}{T_{A_1} \left[ \overline{C_L}(R) \right]}$$

YES ✓

In this (L.H.S parts) firstly Attribute  $A_1$  is selected  
then Condition  $C_L$  is Applied on Attribute  $A_1$ .

⑤

$A_1$  (Attribute) : Rating

$C_L$  (Condition) Rating  $\geq 9$

R.H.S

	$T_{A_1} \left[ \overline{C_L}(R) \right]$	$T_{Rating} \left[ \overline{Rating \geq 9(S_2)} \right]$	
	$\begin{array}{ c c } \hline \text{Rating} & \\ \hline 9 & \\ \hline 10 & \\ \hline \end{array}$	$\begin{array}{ c c } \hline \text{Rating} & \\ \hline 9 & \\ \hline 10 & \\ \hline \end{array}$	$\begin{array}{ c c } \hline \text{Rating} & \\ \hline 9 & \\ \hline 10 & \\ \hline \end{array}$

⑤

$$\underline{\underline{\pi_A}}(\underline{\underline{\pi_{AB}(R)}}) \equiv \underline{\underline{\pi_A}}(R)$$

⑥

$$\underline{\underline{\pi_a}}(R) \equiv \underline{\underline{\pi_a}}(\underline{\underline{\pi_b}}(R))$$

if  $a \subseteq b$

⑦

$$\underline{\underline{\pi_{sid}}}(\text{student}) \equiv \underline{\underline{\pi_{sid}}} \left( \begin{matrix} \underline{\underline{\pi_{sid\_sname}}} \\ b \end{matrix} (\text{student}) \right)$$

⑦

$$\boxed{\pi_a(R) \neq \pi_b(R)}$$

a: (attribute) Name

⑧

$$\pi_{\text{name}}(S_1) \neq \pi_{\text{bid}}(S_1)$$

b: bid

# Set operator

U: Union operator

- : Except or minus

$\cap$  : Intersection operator

- ❑ To apply set operations relations must be union compatible.
- ❑ R and S relations are union compatible
- ❑ If and only if-
  - (i) Arity of R equal to Arity of S and
  - (ii) Domain of attributes of R must be same as domain of attributes of s respectively.

**Example**

Example 1:

$$\pi_{Sid\ Sname}(\dots\dots\dots) \cap \pi_{Sid}(\dots\dots\dots)$$

{Arity not same so, set operation not allowed}

Example 2:

$$\pi_{Sid\ Sname}(\dots\dots\dots) \cap \pi_{Sid\ Marks}(\dots\dots\dots)$$

{Arity same but Sname domain is different from marks so, not allowed}

## Example

$$\pi_{\text{Sid Sname}}(\dots \dots \dots) \cap \pi_{\text{Stud ID, Stud name}}(\dots \dots \dots)$$

{Arity and domains are same so, allowed for set operation}

1. Set operation on relation:

R	A	S	B
	2		2
	2		2
	2		4
	3		

$$R \cup S : \{x / x \in R \vee x \in S\} =$$

A
2
3
4

$$R - S : \{x / x \in R \wedge x \notin S\} =$$

A
3

$$R \cap S : \{x / x \in R \wedge x \in S\} =$$

A
2

Assume Relation R & Relation S consist M & N Tuple Respectively

- (1) Range of tuples in  $R \cup S = \max(M, N)$  to  $M + N$
- (2) Range of tuples in  $R \cap S = \phi$  to  $\min(M, N)$
- (3) Range of tuples in  $R - S = \phi$  to  $M$
- (4) Range of tuples in  $S - R = \phi$  to  $N$

# Union Operation

- ❑ Notation:  $r \cup s$
- ❑ Defined as :

$$r \cup s = \{t | t \in r \text{ or } t \in s\}$$

- ❑ For  $r \cup s$  to be valid.
  1.  $r, s$  must have the same arity (same number of attributes)
  2. The attribute domains must be compatible (example: 2<sup>nd</sup> column of  $r$  deals with the same type of values as does the 2<sup>nd</sup> column of  $s$ )

## Example:

To find all courses taught in the Fall 2009 semester, or in the Spring 2010 semester, or in both.

$$\pi_{\text{course\_id}}(\sigma_{\text{semester} = \text{"Fall"} \wedge \text{year} = 2009} (\text{section})) \cup \\ \pi_{\text{course\_id}}(\sigma_{\text{semester} = \text{"Spring"} \wedge \text{year} = 2010} (\text{section}))$$

# Set Difference Operation

- ❑ Notation:  $r - s$
- ❑ Defined as :

$$r - s = \{t \mid t \in r \text{ and } t \notin s\}$$

- ❑ Set differences must be taken between compatible relations.
  - ❖  $r$  and  $s$  must have the same arity
  - ❖ attribute domains of  $r$  and  $s$  must be compatible

## Example:

Example: to find all courses taught in the Fall 2009 semester, but not in the Spring 2010 semester

$$\pi_{\text{course\_id}}(\sigma_{\text{semester} = \text{"Fall"} \wedge \text{year} = 2009}(\text{section})) - \\ \pi_{\text{course\_id}}(\sigma_{\text{semester} = \text{"Spring"} \wedge \text{year} = 2010}(\text{section}))$$

**Example:****Sailors ( $S_1$ )**

<u>Sid</u>	Sname	Rating	age
22	dustin	7	45.0
31	lubber	8	55.5
58	rusty	10	35.0

**Sailors ( $S_2$ )**

<u>Sid</u>	Sname	Rating	age
28	Yuppy	9	35.0
31	Lubber	8	55.5
44	Guppy	5	35.0
58	rusty	10	35.0

(1) Union  $S_1 \cup S_2$

## (1) Union

Sid	Sname	Rating	age
22	dustin	7	45.0
31	lubber	8	55.5
58	rusty	10	35.0
44	guppy	5	35.0
28	yuppy	9	35.0

 $S1 \cup S2$

## (2) Set Difference

Sid	Sname	Rating	age
22	dustin	7	45.0

S1 - S2

### (3) Intersection

Sid	Sname	Rating	age
31	lubber	8	55.5
58	rusty	10	35.0

$S1 \cap S2$

## Basic operators

### II. Cross product ( $\times$ ):

- ❑  $R \times S$ : It result all attributes of R followed by all attributes of S, and each record of R paired with every record of S.
- ❑  $\text{Degree}(R \times S) = \text{Degree}(R) + \text{Degree}(S)$
- ❑  $|(R \times S)| = |R| \times |S|$

## NOTE:

- Relation R with n tuples and
- Relation S with 0 tuples then
- number of tuples in  $R \times S = 0$  tuples

# Join ( $\bowtie$ )

## I. Natural join ( $\bowtie$ )

$R \bowtie S \equiv \pi_{\text{distinct attributes}}(\sigma_{\text{equality between common attributes of } R \text{ and } S} (R \times S))$

Example:

- $T_1$  (ABC) and  $T_2$  (BCDE)

$$\therefore T_1 \bowtie T_2 = \pi_{ABCDE} \left( \begin{array}{l} \sigma_{T_1 \cdot B = T_2 \cdot B} (T_1 \times T_2) \\ \cap T_1 \cdot C = T_2 \cdot C \end{array} \right)$$

- $T_1$  (AB) and  $T_2$  (CD)

$$\therefore T_1 \bowtie T_2 \equiv T_1 \times T_2 = \pi_{ABCD} (T_1 \times T_2)$$

**NOTE:**

Natural join equal to cross-product if join condition is empty.

**Join ( $\bowtie$ )****II. Conditional Join ( $\bowtie_c$ )**

- ❑  $R \bowtie_c S \equiv \sigma_c (R \times S)$

# Join ( $\bowtie$ )

## III. Outer Joins:

### (a) LEFT OUTER JOIN

$R \bowtie S$  : It produces

$(R \bowtie S) \cup \{Records\ of\ R\ those\ are\ failed\ join\ condition\ with\ remaining\ attributes\ null\}$

### (b) RIGHT OUTER JOIN ( $\bowtie\leftarrow$ )

$R \bowtie\leftarrow S$  : It produces

$(R \bowtie S) \cup \{Records\ of\ S\ those\ are\ failed\ join\ condition\ with\ remaining\ attributes\ null\}$

### (C) FULL OUTER JOIN ( $\bowtie\leftrightarrow$ )

$R \bowtie\leftrightarrow S = (R \bowtie S) \cup (R \bowtie\leftarrow S)$

# Natural Join $\bowtie$

**R**

A	B	C
1	2	4
3	2	6

**S**

B	C	D
2	4	8
2	7	4

 **$R \times S =$** 

R.A	R.B	R.C	S.B	S.C	S.D
1	2	4	2	4	8
1	2	4	2	7	4
3	2	6	2	4	8
3	2	6	2	7	4

$$R \bowtie S = \pi_{ABCD} \left\{ \begin{array}{l} \sigma_{RB} = S.B \wedge^{(R \times S)} \\ R.C = S.C \end{array} \right\}$$

$$R \bowtie S = \begin{array}{|c|c|c|c|} \hline & A & B & C & D \\ \hline 1 & 2 & 4 & 8 & \\ \hline \end{array}$$

# Left Outer Join [ $\bowtie$ ]

 $(R \bowtie S)$  $R$ 

A	B	C
1	2	4
3	2	6

 $S$ 

B	C	D
2	4	8
2	7	4

 $(R \bowtie S) =$ 

A	B	C	D
1	2	4	8

 $R \bowtie S =$ 

A	B	C	D
1	2	4	8
3	2	6	Null

# Right Outer Join [ $\bowtie$ ]

$$R \bowtie S =$$

	A	B	C	D
1	2	4	8	
Null	2	7	4	

# Full Outer Join [ $\bowtie$ ]

Full outer join = Left outer join Union Right outer join

$$R \bowtie S = R \bowtie S \cup R \bowtie S$$

A	B	C	D
1	2	4	8
3	2	6	Null

U

A	B	C	D
1	2	4	8
Null	2	7	4

$$R \bowtie S =$$

A	B	C	D
1	2	4	8
3	2	6	Null
Null	2	7	4

**Q.**

Let R and S be two relations with the following schema

R(P, Q, R1, R2, R3)

S(P, Q, S1, S2)

Where {P, Q} is the key for both schemas. Which of the following queries are equivalent?

- I.  $\pi_P(R \bowtie S)$
- II.  $\pi_P(R) \bowtie \pi_P(S)$
- III.  $\pi_P(\pi_{P,Q}(R) \cap \pi_{P,Q}(S))$
- IV.  $\pi_P(\pi_{P,Q}(R) - (\pi_{P,Q}(R) - \pi_{P,Q}(S)))$

**A**

Only I and II

**B**

Only I and III

**C**

Only I, II and III

**D**

Only I, III and IV

P  
W

**THANK  
YOU!**

