

CS & IT ENGINEERING

Operating Systems

Memory Management



Lecture No. 1



By- Dr. Khaleel Khan Sir

TOPICS TO BE COVERED

Abstract View of Memory

Loading vs Linking

Address Binding

Q.

Consider the following snapshot of a system running n processes. Process i is holding x_i instances of a resource R, for $1 \leq i \leq n$. Currently, all instances of R are occupied. Further, for all i, process i has placed a request for an additional y_i instances while holding the x_i instances it already has. There are exactly two processes p and q such that $y_p = y_q = 0$. Which one of the following can serve as a necessary condition to guarantee that the system is not approaching a deadlock?

A. $\min(x_p, x_q) < \max_{k \neq p, q} y_k$

→ if the request (Least)
of the Process is satisfiable

B. $x_p + x_q \geq \min_{k \neq p, q} y_k$ ✓

C. $\max(x_p, x_q) > 1$

D. $\min(x_p, x_q) > 1$

P_{id}	$\frac{Alloc}{R}$	$\frac{Req}{R}$	$\frac{Avail}{R}$
P_1	x_1	y_1	\circ
P_2	x_2	y_2	
P_3	x_3	y_3	
\vdots	\vdots	\vdots	
P_p	x_p	$\circ \times$	
P_q	x_q	$\circ \times$	
\vdots	\vdots	\vdots	
P_n	x_n	y_n	

① 't': $(x_p + x_q) \geq \text{Min}(y_i)$
 $i \neq (p, q)$

② $(x_p + x_q) < \text{Min}(y_k)$
 $k \neq (p, q)$
deadlock

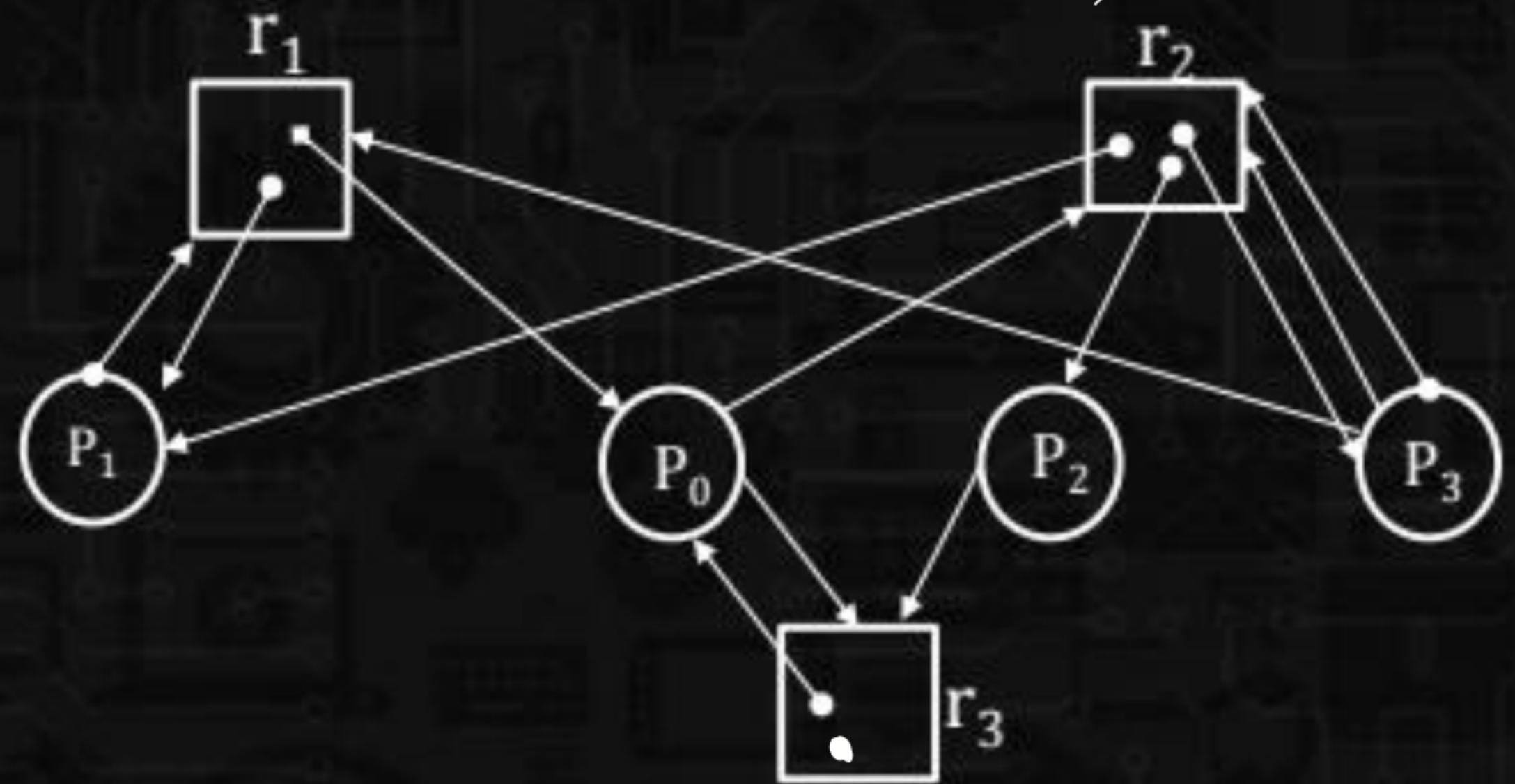
③ $(x_p + x_q) > \text{Max}(y_i)$

"Safe"

P
W

Q.

(Detection) (Which Algo)?
 Consider the Following Resource Allocation Graph. Find if the System is in (Deadlock State)



$(R.A.G \Rightarrow \text{Matrix form})$

	<u>Alloc</u>	<u>Req</u>	<u>Avail</u>
	$\gamma_1 \gamma_2 \gamma_3$	$\gamma_1 \gamma_2 \gamma_3$	$\gamma_1 \gamma_2 \gamma_3$
P_0	1 0 1 - 0 1 1		0 0 1
P_1	1 1 0 - 1 0 0		$\langle 0 1 1 \rangle$
P_2	0 1 0 - 0 0 1		$\langle 1 1 2 \rangle$
P_3	0 1 0 - 1 2 0		$\langle 2 2 2 \rangle$
			$\langle P_2; P_0; P_1; P_3 \rangle$
			(SAPR)

$(1, 2, 3)$: deadlock can happen

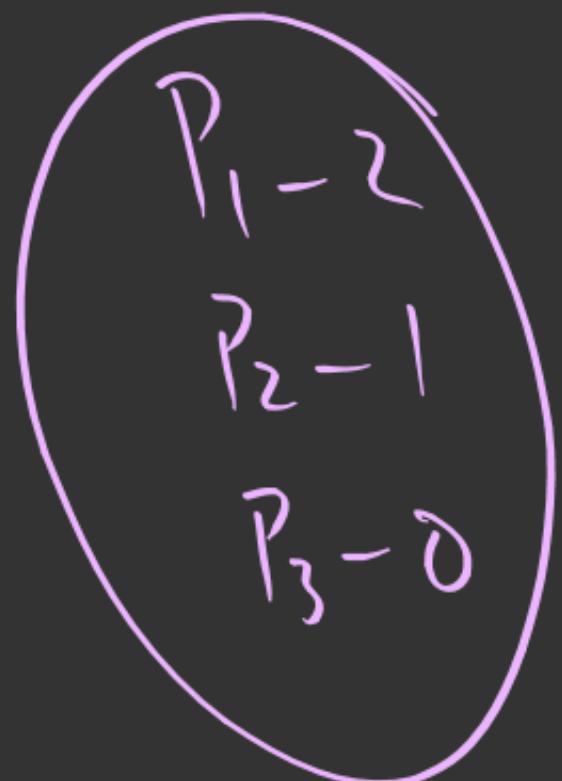
Dining Philosophers

$n = 3$ processes (P_1, P_2, P_3)

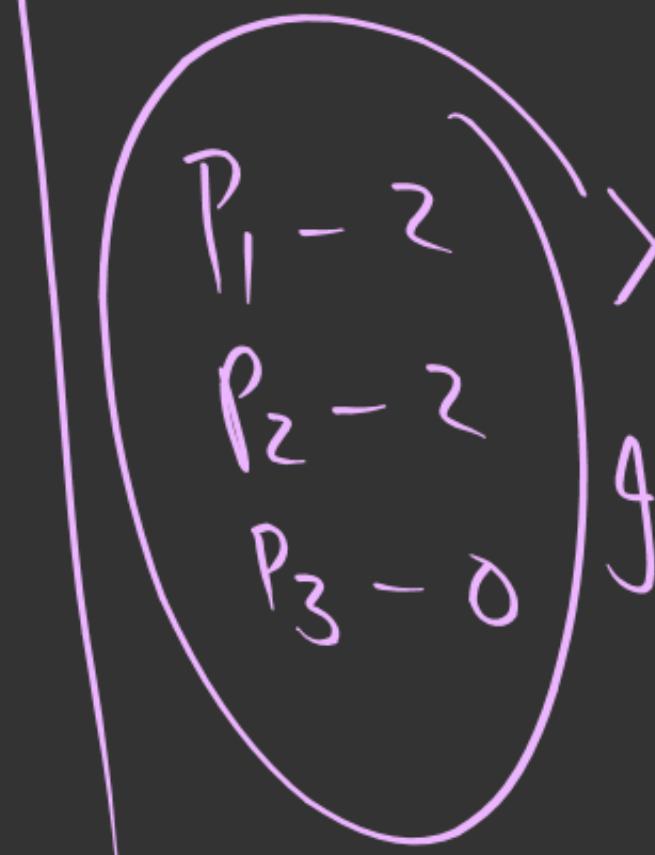
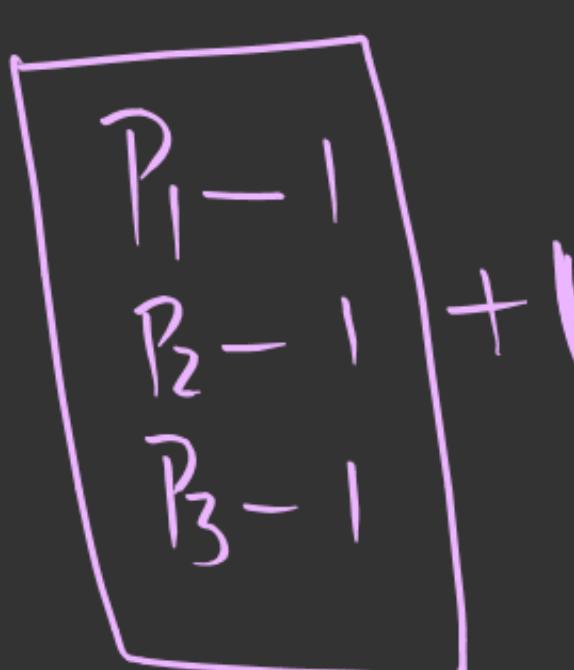
$$R = 4$$

$$P_i \rightarrow 2(R)$$

No deadlock



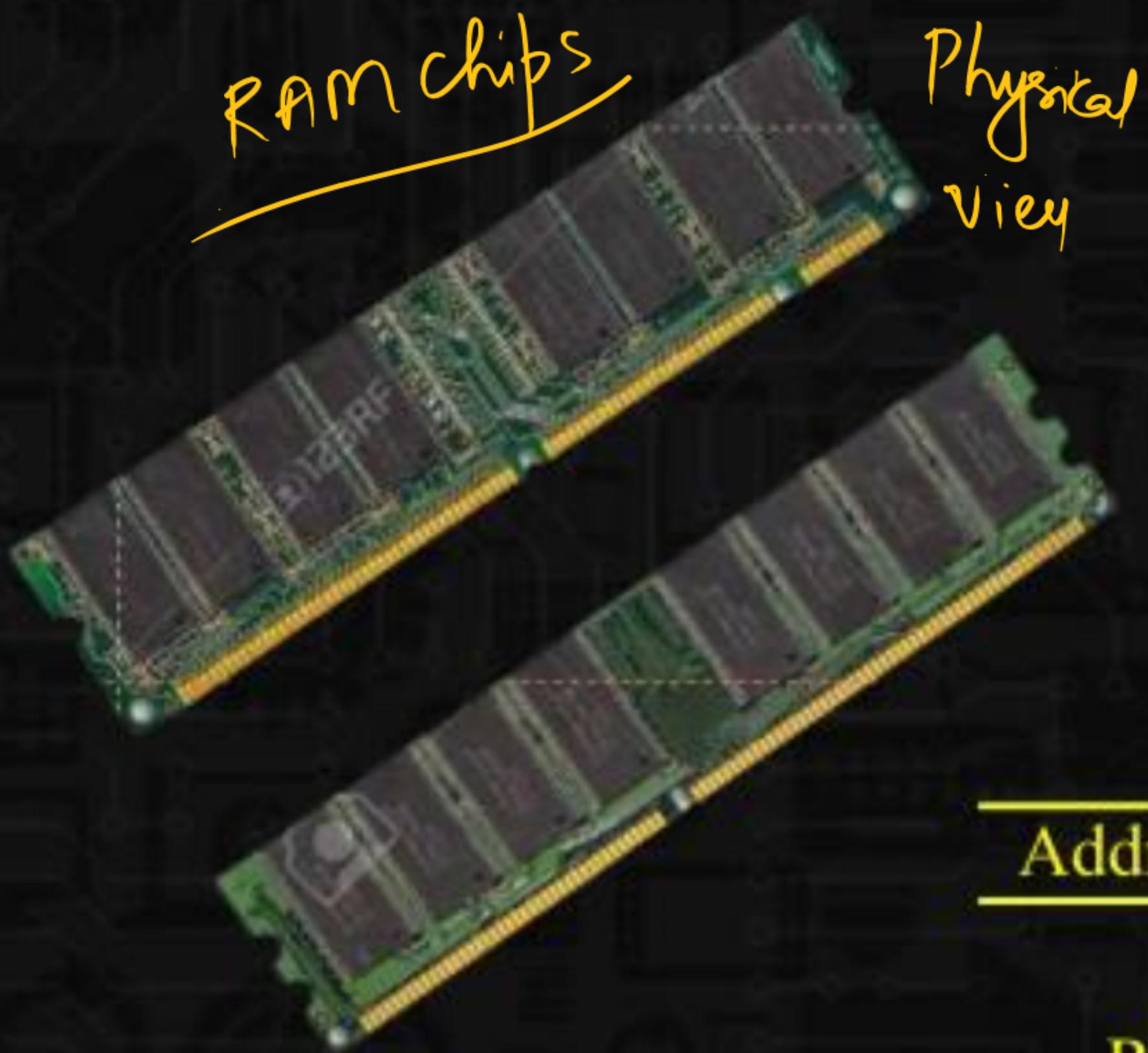
Deadlock



Is this deadlock?

a) Max(R) to cause deadlock

b) Min(R) for deadlock freedom



Memory Management

Primary (Main)

RAM + ROM

R/W Memory

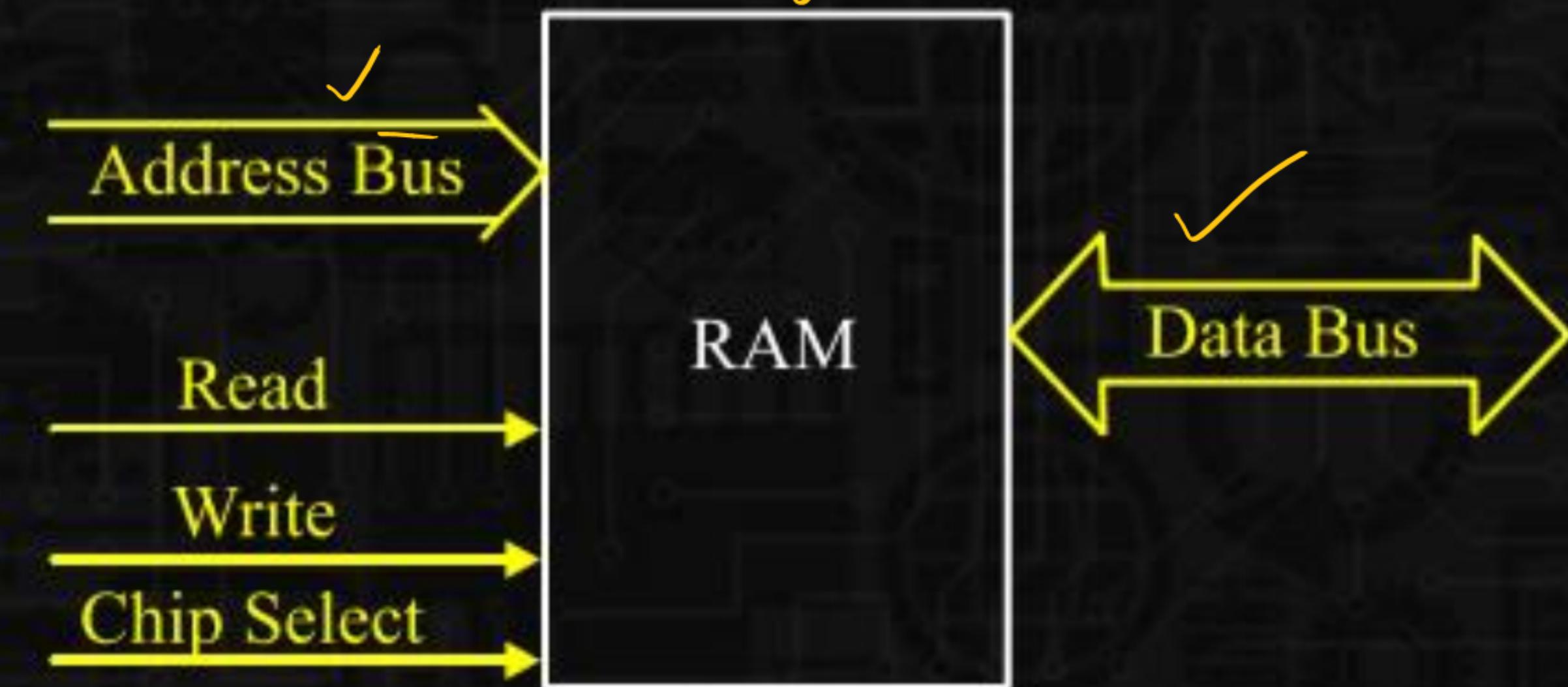
FileSystem

P
W

+ Cache +

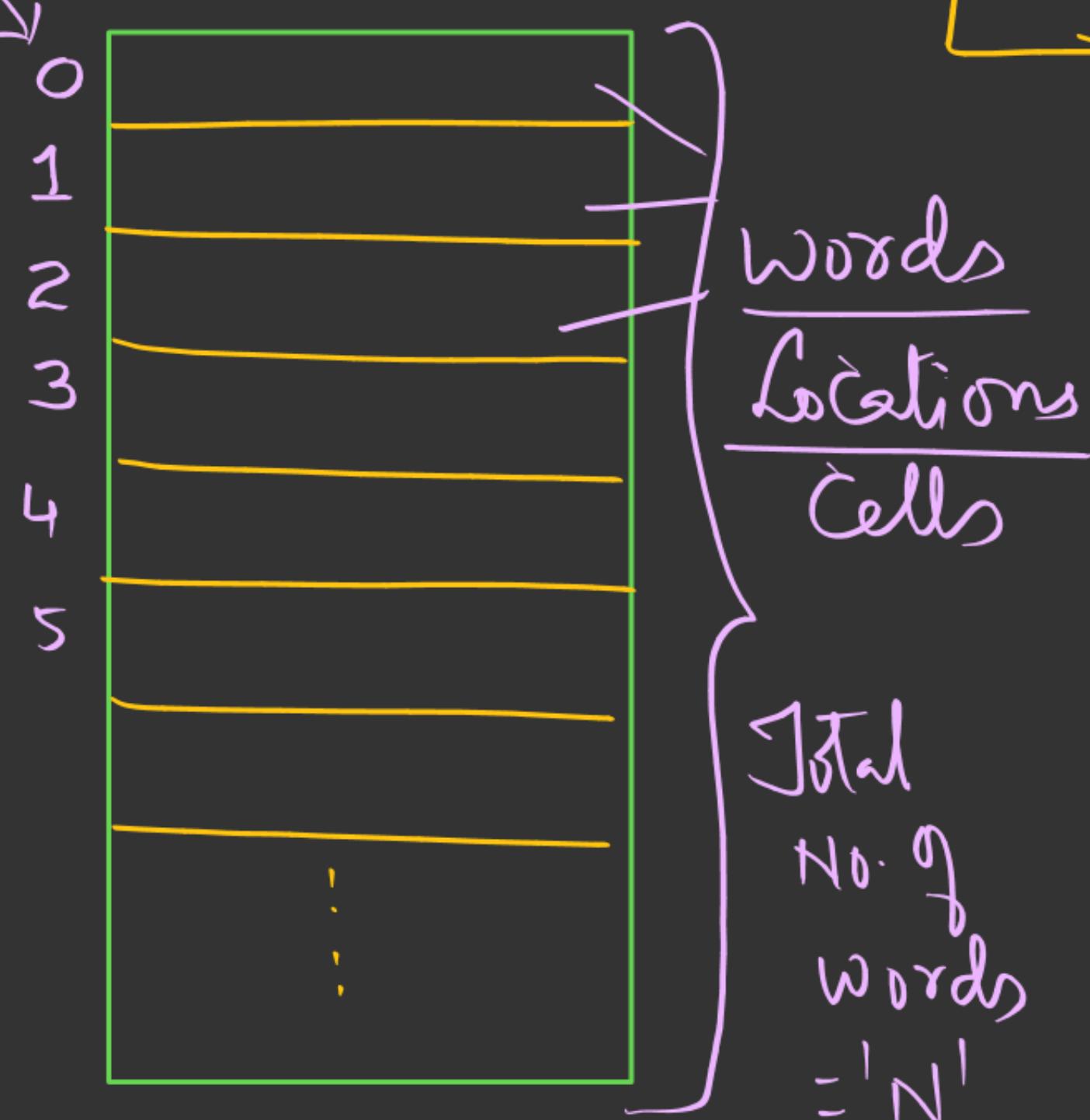
{Registers}

Block Diagram



Address

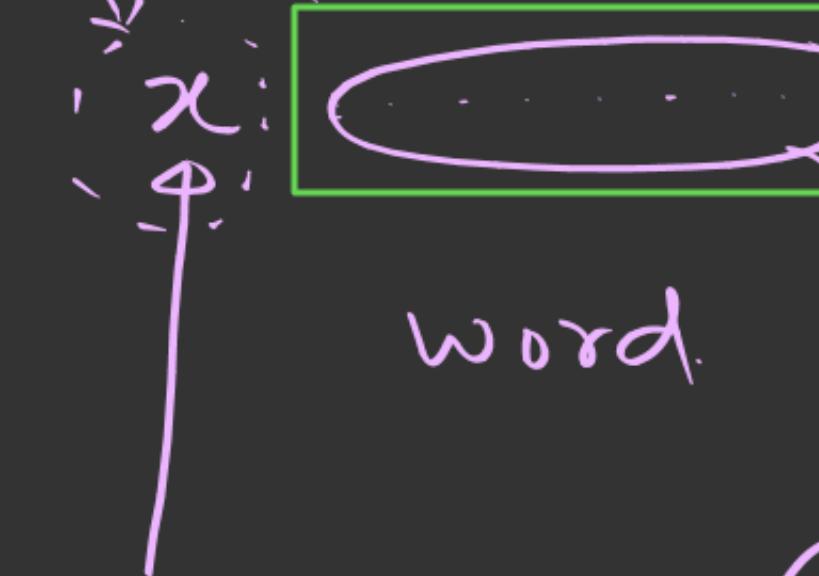
Linear - 1-dimensional view of Memory (Abstract view)



→ Array of words

m-bit

word length/width of word
(m) bit
Bytes



fixed length
Address (bit)

Instm + Data

1 Byte = 8 bit

1 Nibble = 4 bit

⇒ Memory Capacity

Mem is Specified: $\frac{\text{No. of words} \times \text{width of word}}{(N \times m)}$

i. Relation b/w N & n:

→ Binary bits: (0, 1)

→ Using 3 binary bits, How many combinations are possible (2^3)

4 bits \Rightarrow 16 (2^4)

'n' bits $\Rightarrow 2^n$

Binary	Decimal
000	0
001	1
010	2
011	3
100	4
101	5
110	6
111	7

n: Size of Address in bits
 m: word length
 width word
 N: Total # of words

$$N = \frac{8 \text{ words}}{\underline{\underline{n}}}$$

000	0	
001	1	
010	2	
011	3	
100	4	
101	5	
110	6	
111	7	

$$2^{10} \sim 10^3 = 1T$$

$$2^{30} \sim 10^9 = 1P$$

$$n = \frac{3 \text{ bits}}{\underline{\underline{1}}}$$

$$2^3 = 8W$$

$$2^5 = 32W$$

$$2^6 = 64W$$

$$\overset{?}{2} = 128W$$

$$2^8 = 256W$$

$$2^9 = 512W$$

$$\boxed{\frac{N = 2^n W}{n = \log_2 N \text{ bits}}}$$

$$2) N = \underline{\underline{256}}$$

$$n = \log_2 256 = \log_2 8 \\ = 8 \text{ bits}$$

$$3) N = \underline{\underline{512}}$$

$$n = 9 \text{ bits}$$

$$4) n = 6 \text{ bits}$$

$$N = 2^6 = 64W$$

$$5) N = \underline{\underline{8KB}}$$

$$n = 3 + 10 = \underline{\underline{13 \text{ bits}}}$$

$$6) n = 15 \text{ bits}$$

$$N = 2^{15} = 2^5 \times 2^{10} \\ = 32KB$$

$$7) N = 16GB$$

$$n = 4 + 30 \\ = 34 \text{ bits}$$

K = Kilo
B = Bytes

$$1) \quad N = \underline{500 \text{ GB}}$$

$N = 2^n$
 $n = \log_2 N \text{ bits}$

$$n = 9 + 30 = \underline{\underline{39 \text{ bits}}}$$

$$2) \quad N = \underline{\underline{1000 \text{ KB}}}$$

$$n = 10 + 10 = \underline{\underline{20 \text{ bits}}}$$

$$3) \quad N = \underline{\underline{\log_2 M \text{ Bytes}}}$$

$$n = \underline{\underline{\log_2(\log_2 M) \text{ bits}}}$$

$$4) \quad n = 31 \text{ bits}$$

$$N = 2^{31} = \underline{\underline{2 \text{ GB}}}$$

$$5) \quad \underline{n = 23 \text{ bits}}$$

$$N = 2^{23} = \underline{\underline{8 \text{ MB}}}$$

$$= 2^3 \times 2^{20} = \underline{\underline{8 \text{ MB}}}$$

$$6) \quad n = x \text{ bits}$$

$$N = 2^x \text{ B}$$

$$7) \quad n = \underline{\underline{\log_2 3 \text{ bits}}}$$

$$\begin{aligned} N &= 2^{\log_2 3} \\ &= 3^{\log_2 2} \\ &= \boxed{N = 3 \text{ Bytes}} \end{aligned}$$

$$n = \underline{\underline{\log_2 3 \text{ bits}}}$$

$$1) \quad \begin{aligned} n &= \underline{13 \text{ bits}} \\ m &= \underline{8 \text{ bits}} \quad \checkmark \\ N &= 8 \text{ K W} \\ &= 8 \text{ K B} \end{aligned}$$

$$\boxed{1W = 1B}$$

$$II. \quad \frac{N \propto n \propto m}{}$$

is used to select one word of size 16 bits

$$2) \quad \begin{aligned} n &= \underline{18 \text{ bits}} \\ m &= \underline{16 \text{ bits}} \\ N &= 256 \text{ KW} = \text{Word view} \\ &= 512 \text{ KB} = \text{Byte view} \end{aligned}$$

$$3) \quad \begin{aligned} n &= 33 \text{ bits} = 2^{33} \\ m &= 64 \text{ bits} \Rightarrow 1W = 8B \end{aligned}$$

$$\begin{aligned} N &= 8G \text{ W} \quad \checkmark \\ &= 64G \text{ B} \quad \checkmark \end{aligned}$$



$$3) N = \underline{\underline{64KB}}$$

$$m = \underline{\underline{4B}}$$

$$N = \frac{64KB}{4B} W$$

$$= \underline{\underline{(16KW)}}$$

$$n = 14\text{bit}(W)$$

$$\underline{\underline{n = 16\text{bit}(B)}}$$

$$= 8B \Rightarrow n = 3\text{bit}$$

$$N \sim \frac{\text{Words}}{\text{Bytes}}$$

$$m \sim \text{bit/Bytes}$$

$$n \sim \text{bit}$$

(B1)	(B2)
(B3)	(B4)
(B5)	(B6)
(B7)	(B8)

$$1W = 2B$$

$$N = \frac{8B}{2B} = \underline{\underline{4W}} (2\text{bit})$$

$$1W = 4B$$

$$3) \quad m = \frac{23 \text{ bit}}{(m = \frac{32 \text{ bit}}{4B})}$$
$$N = 2^{23} = 2^{3 \cdot 2^0} = 8MW$$
$$N = 8M \times 4B$$
$$= \underline{\underline{32MB}}$$

$$N = 2^n W$$
$$n = \log_2 N \text{ bit}$$

$$4) \quad \underline{\underline{N = 256MB}}$$
$$m = \underline{128B}$$

$$N = \underline{\underline{2MW}}$$

$$m = 21 \text{ bit (W)}$$
$$m = 28 \text{ bit (B)}$$

$$\frac{2}{\cancel{256MB}} \\ \cancel{128B}$$

Last Twist

$$N = \frac{8G\text{ bits}}{64\text{ bits}}$$

$$m = \underline{64\text{ bits}}$$

$$\frac{8G\text{ bits}}{64\text{ bits}}$$

$$= \frac{2^{33}}{2^6} = 2^{27}$$

$$N = 2^{27} = \underline{\underline{128MW}} \checkmark$$

$$N = \frac{8G\text{ bits}}{8\text{ bits}} = \underline{\underline{1GB}} \checkmark$$

Memory



$$lw = \underline{\underline{2\text{ bits}}}$$

$$\frac{16\text{ bits}}{2\text{ bits}}$$

$$= \underline{\underline{8W}}$$

