

CS & IT ENGINEERING

Theory of Computation

Finite Automata



Lecture No. 20



By- DEVA Sir

TOPICS TO BE COVERED

01 Regulars & Non regulars

02 GATE PYQs & pending

03 Revision of all topics

04

05

(65)

 wwx

(66)

 wxw

(67)

 xww

(68)

 $ww^R x$

(69)

 wxw^R

(70)

 $xw\omega^R$ $w, x \in \{0, 1\}^*$

When you put w, e

 $= \infty$ $= (a+b)^*$

All are regular

- 三

$$\{wwx \mid w, x \in \{a, b\}^+ \}$$

- 72

{wxw
U T G}

- 73

۹۷

- 74

q w w x

Reg 75

- 76

$\{ xww^R$

$$\textcircled{71} \quad \{wwx \mid w, x \in \{a, b\}^+\}$$

$$\begin{matrix} w = a/b \\ \min w \end{matrix}$$

$$\boxed{aa(a+b)^+ \text{ OR } bb(a+b)^+}$$

1st form

2nd form some strings are missing in 1st

$$\boxed{\begin{array}{l} aaaax \\ ababx \rightarrow X \\ babax \\ bbbbx \end{array}}$$

2nd form

Not L(G)

2nd min

$$w = aa/ab/ba/bb$$

$$\textcircled{75} \quad \{wxw^R \mid w, x \in \{a, b\}^+\}$$

$$sx$$

$$w = a/b$$

$$\boxed{axa + bxb}$$

$$\boxed{\begin{array}{l} aaxaa \\ abxba \\ baxab \\ bbybb \end{array}}$$

all are covered

$$= a(a+b)^+a + b(a+b)^+b$$

Regula^a

$$w = aa/ab/ba/bb$$

75 $\{wxw^R \mid w, x \in \{a, b\}^+\}$

$\text{Ans} = \underline{a} \underline{(a+b)^+ a} + b (a+b)^+ b$

$$= \{wxw^R \mid w, x \in \{a, b\}^+, |w|=1\}$$

$$= \{w \mid w \in \{a, b\}^*, w \text{ starts \& ends with same i/p}, |w| \geq 3\}$$

Note: $L = \{w \mid w \in \{a, b\}^*, w \text{ starts and ends with same i/p symbol}\}$

$$= a + b + a(a+b)^*a + b(a+b)^*b$$

77

$$\{ \underbrace{wxwy}_{\text{before}} \mid w, x, y \in \{a, b\}^+ \} = \boxed{a(a+b)^+ a(a+b)^+ + b(a+b)^+ b(a+b)^+}$$

1st: $axay + bxyb$

2nd: $aazaay$

$abxyab$

$baxbay$

$bbyxby$

78

$$\{ \underbrace{xwyzw}_{\text{before before}} \mid w, x, y \in \{a, b\}^+ \}$$

1st: $xaya + xbyb$

2nd: $xaayaa$

$xabyab$

$xabayba$

$abbybab$

79

$$\{ \underbrace{xwyzwz}_{\text{before before}} \mid w, x, y, z \in \{a, b\}^+ \} = \boxed{xayaaz + xbybz}$$

80

$$\{ \underbrace{xww^Ry}_{\text{before before}} \mid w, x, y \in \{a, b\}^+ \} = \boxed{xaaay + xbbay}$$

ans:

$xaaaaay$

$xbbaaby$

$xabbay$

$xbbaaby$

$$\textcircled{81} \quad \{ w x w y \mid w, x, y \in \{a, b\}^* \}$$

$$\textcircled{82} \quad \{ x w y w \mid w, x, y \in \{a, b\}^* \}$$

$$\textcircled{83} \quad \{ x w y w z \mid w, x, y, z \in \{a, b\}^* \}$$

$$\textcircled{84} \quad \{ x w w^R y \mid w, x, y \in \{a, b\}^* \}$$

put w, y
 $x =$
 $= (a+b)^*$
all are regular

$$\{ \begin{matrix} w \\ wxwy \\ \text{UP} \\ \text{After} \end{matrix} \mid \begin{matrix} x,y \\ w,x,y \in \{a,b\}^+ \end{matrix} \}$$

Why we substitute only w ?

w is repeating.

To check dependence b/w w & symbols

⑧5

$$\{ \overbrace{xxwxw}^f \mid w, x \in \{a, b\}^+ \}$$

Not regular ✓

⑧6

$$\{ p \overbrace{x}^r \overbrace{w}^q \overbrace{x}^s \overbrace{s}^t \mid w, x \in \{a, b\}^+ \}$$

p, q, r, s

Result

⑧7

$$\{ p \boxed{x}^r q \boxed{x}^s r \boxed{w}^t s \boxed{w}^t \mid w, x \in \{a, b\}^+ \}$$

p, q, r, s, t

begin *begin* *after* *after*

⑧8 $\{ \boxed{x} w \boxed{x} \mid x, w \in \{a, b\}^+ \} \Rightarrow \text{Not reg}$

⑧9 $\{ \boxed{x} w \boxed{x} y \mid x, w, y \in \{a, b\}^+ \} = \text{away}^+ b w b y \Rightarrow \text{Regular}$

⑨0 $\{ \boxed{y} w \boxed{y} x \mid w, x, y \in \{a, b\}^+ \} = \text{away}^+ x w b x$

⑨1 $\{ w x y w \mid w, x, y \in \{a, b\}^+ \} \Rightarrow \text{Not regular}$

92

$\{ \boxed{ww} \# \boxed{ww} \mid w \in \{a,b\}^* \} \Rightarrow \text{Not regular}$

93

$\{ \cancel{ww} \cancel{x} \cancel{ww} \mid w, x \in \{a,b\}^* \} = (a+b)^* \Rightarrow \text{Reg}$

94

$\{ \cancel{w} \cancel{x} \cancel{w} \cancel{x} \cancel{w} \cancel{x} \cancel{y} \mid w, x, y \in \{a,b\}^* \}$

95

$\{ ww^R w w^R \mid w \in \alpha^* \} = \{ (a^*)^* \}$

$w w^R w w^R$

$w w^R w w^R$

$\Rightarrow \text{Regular over 1 symbol}$

$w = w^R$

⑨6 $\{ \omega \mid \omega \in \{0,1\}^*, n_0(\omega) = n_1(\omega) \}$

000000

⑨7 $\{ \omega \mid \omega \in \{0,1\}^*, n_{00}(\omega) = n_{11}(\omega) \}$

000000

~~Reg~~ ⑨8 $\{ \omega \mid \omega \in \{0,1\}^*, n_{01}(\omega) = n_{10}(\omega) \} \Rightarrow \text{Regular}$

⑨9 $\{ \omega \mid \omega \in \{0,1\}^*, n_{01}(\omega) = n_{00}(\omega) \}$

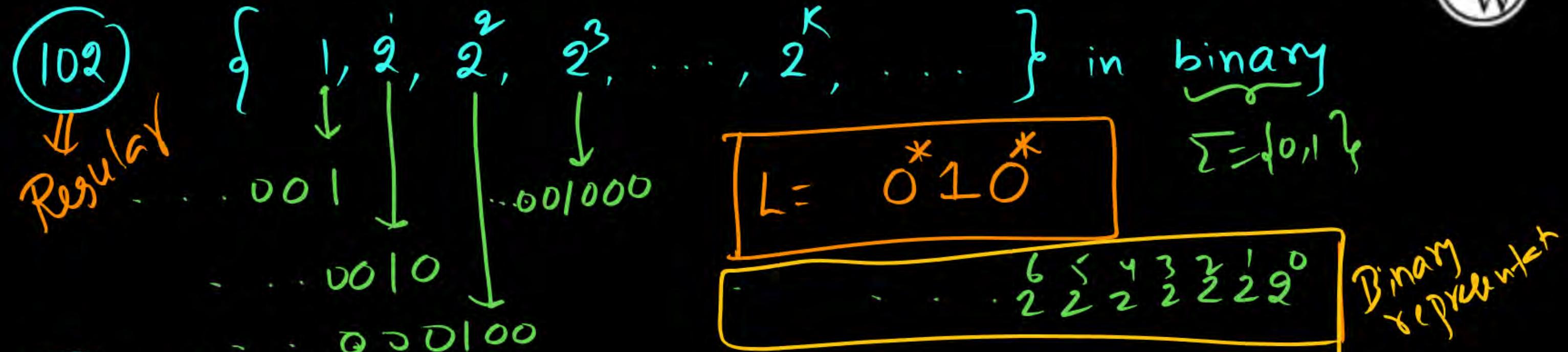
010101

⑩0 $\{ \omega \mid \omega \in \{0,1\}^*, n_{000}(\omega) = n_{111}(\omega) \}$

01010101

~~Reg~~ ⑩1 $\{ \omega \mid \omega \in \{0,1\}^*, n_{001}(\omega) = n_{100}(\omega) \} \Rightarrow \text{Regular}$

01001001



(103) $L = \{1, 2, 2^2, 2^3, \dots, 2^K, \dots\}$ in unary
 $= \{a^{2^n} \mid n \geq 0\} = \{b^{2^n} \mid n \geq 0\}$ over 1 symbol

⇒ Not regular

Q.9

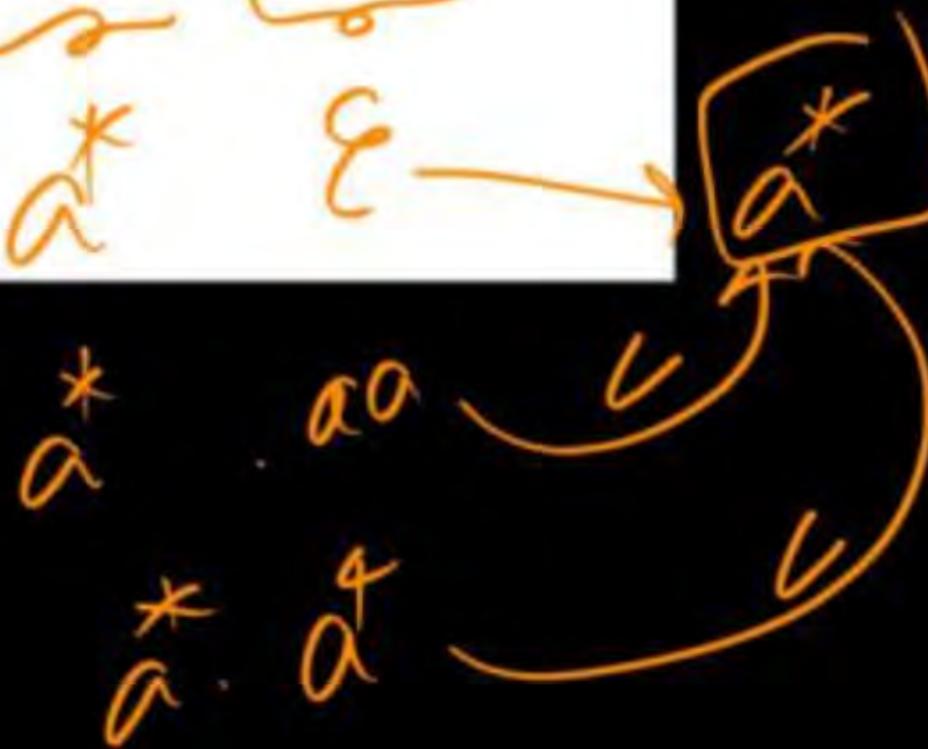
If $R1 = a^*$, and $R2 = (aa)^*$ then $R1.R2 = \underline{\quad}$

P
W

- A. $R1 = a^*$
- B. $R2.R1 = a^*$
- C. $R1+R2 = a^*$
- D. All of these

$$a^* \cdot (aa)^* = a^*$$

$\swarrow \quad \searrow$
 $a^* \quad \epsilon \rightarrow a^*$



②

If the regular set A is represented by $A = (01+1)^*$ and the regular set 'B' is represented by $B = ((01)^*1^*)^*$, which of the following is true? **(GATE - 98)**

- (a) $A \subset B$
- (b) $B \subset A$
- (c) A and B are incomparable
- (d) $A = B$

$$01 = x$$

$$1 = y$$

P
W

$$A = (x+y)^*$$

$$B = (x^*y^*)^*$$

$$\boxed{A = B}$$

$$(01+1)^* = (x+y)^*$$

$$((01)^*1^*)^* = (x^*y^*)^*$$

3

The string 1101 does not belong to the set represented by (GATE - 98)

- (a) 110^{*} (0+1)^{*} $\leftarrow 110 \in \Sigma^*$
- (b) 1(0+1)*101 $\leftarrow 1()^* 101$
- (c) (10)* (01)* (00+11)* $\leftarrow 110 \notin \Sigma^*$
- (d) (00+(11)* 0)* $\rightarrow 110110 \neq 1101$
- ↓
substry ↓
 word
 string

1101 is string  

$$\begin{aligned} 1101 &\in (a) \\ 1101 &\in (b) \end{aligned}$$

5
H.W.

Consider the set Σ^* of all strings over the alphabet $\Sigma = \{0, 1\}$.

Σ^* with the concatenation operator for strings (GATE - 03)

- (a) Does not form a group
- (b) Forms a non-commutative group
- (c) Does not have a right identity element
- (d) Forms a group if the empty string is removed from Σ^*

H.W.: Group 9

P
W

(Infix operators)

Group Theory

Closure ?

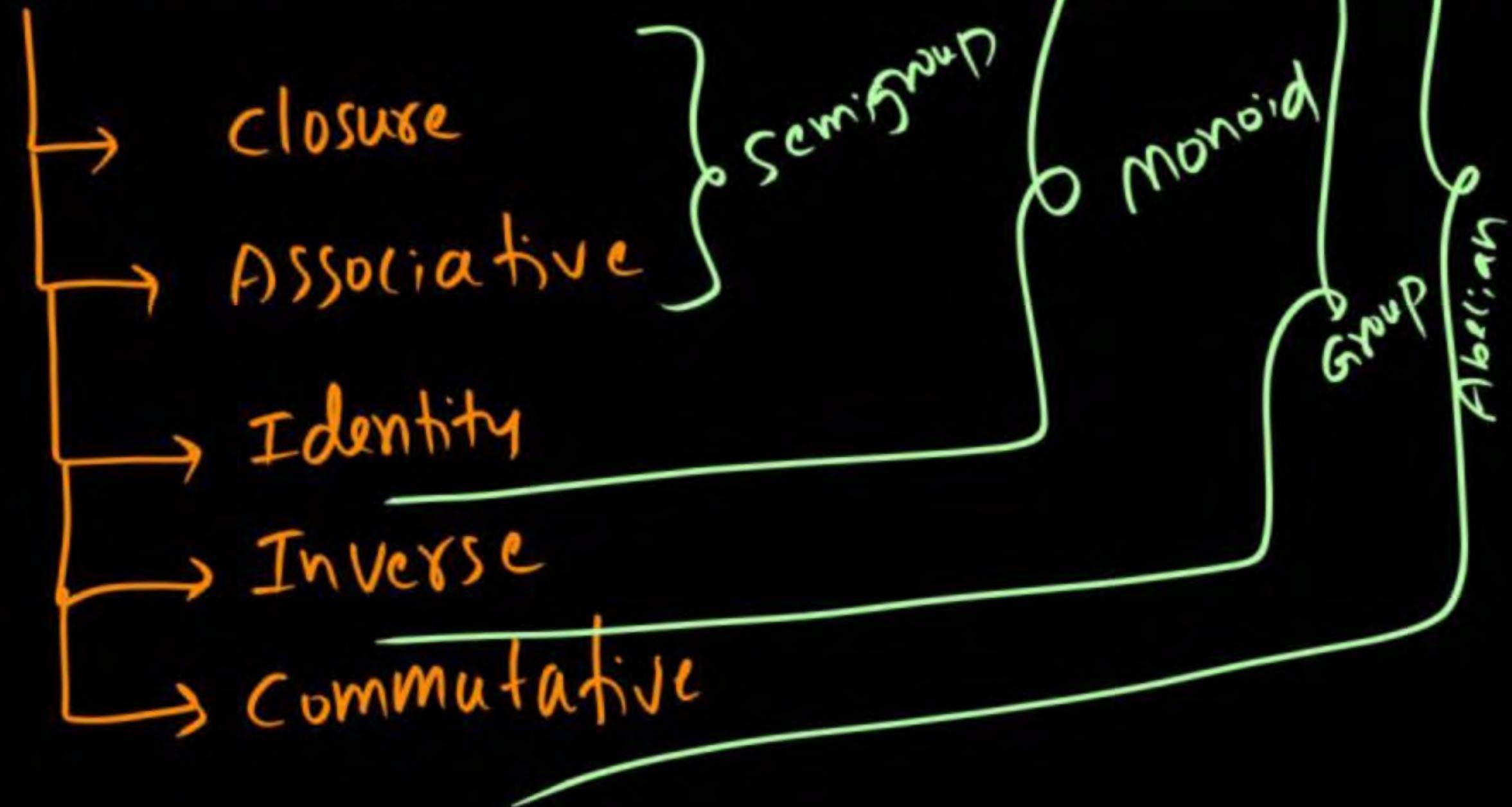
Associative ?

Identity ?

Inverse ?

Commutative ?

Group Theory



Model-6:

H.U.

⑤

$$L = b^* a^*$$

⑥

$$L = b^+ a^*$$

⑦

$$L = b^* a^+$$

⑧

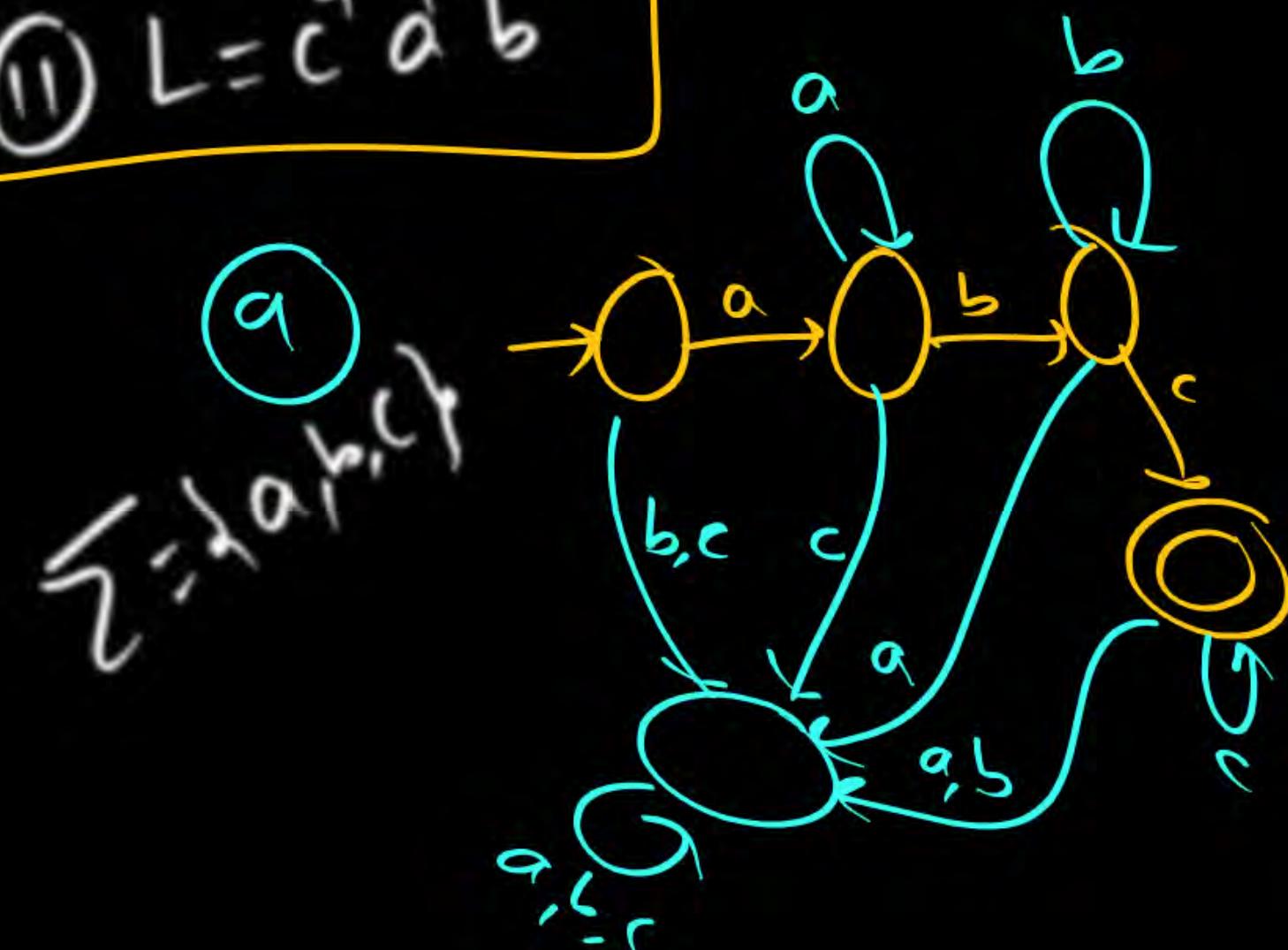
$$L = b^* a^*$$

$$L = \{a^m b^n c^p \mid m, n, p \geq 0\}$$

$$⑨ L = a^+ b^+ c^+$$

$$⑩ L = b^+ a^+ c^+$$

$$⑪ L = c^+ a^+ b^+$$

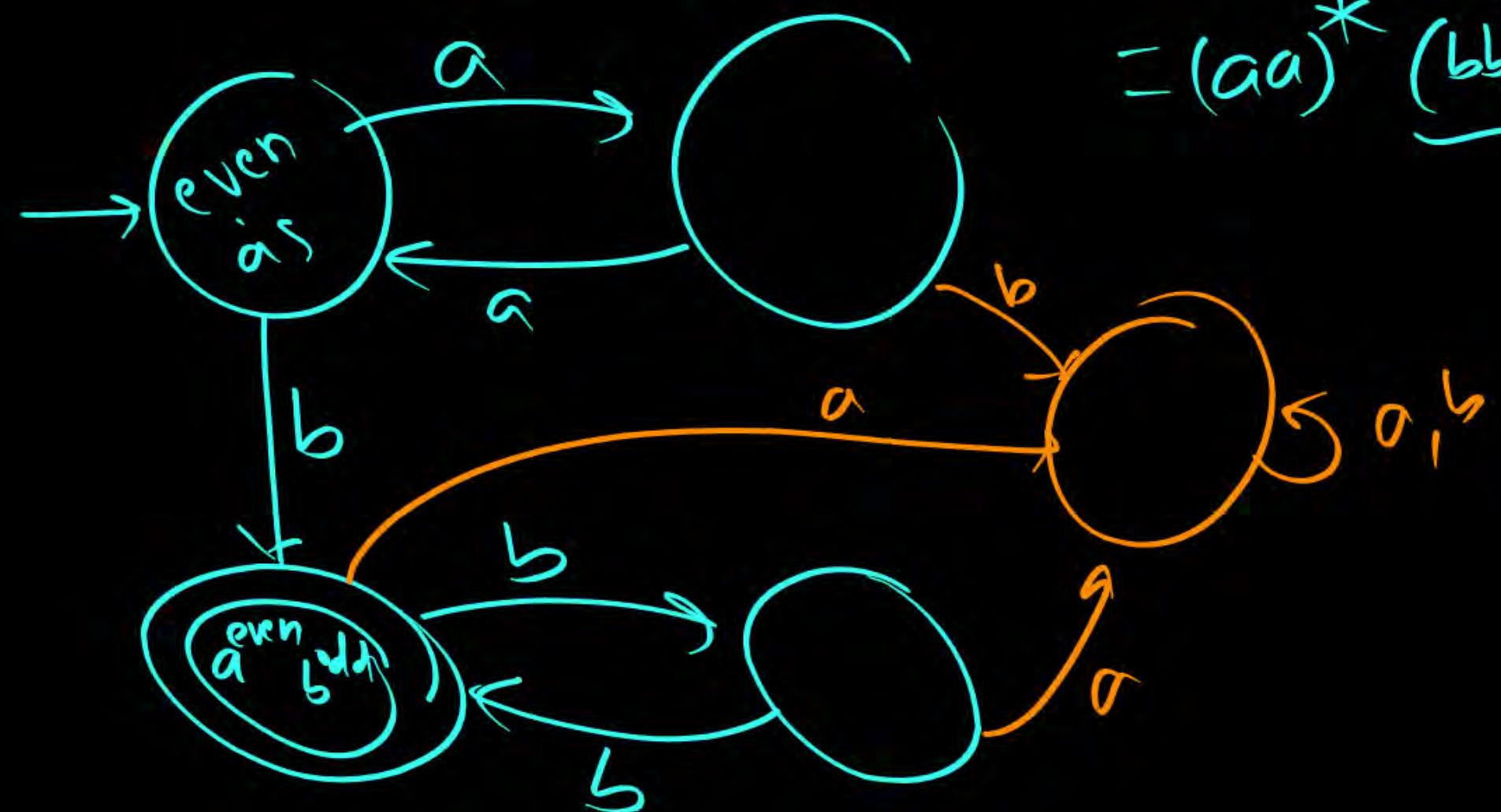


Model-7:

$$\textcircled{9} \quad \left| \tilde{\alpha}^m \tilde{\beta}^n \mid m=\text{even}, n=\text{odd} \right\rangle = \tilde{\alpha}^{\text{even}} \tilde{\beta}^{\text{odd}}$$

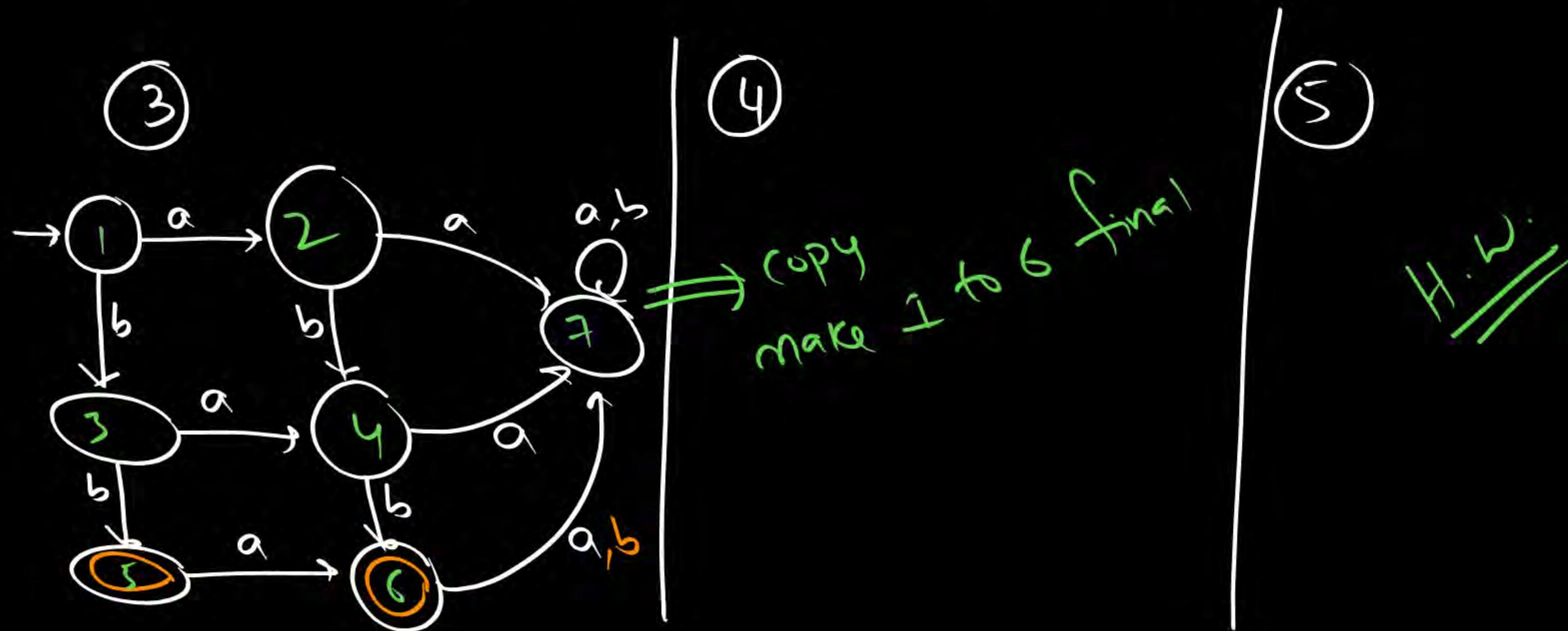
$$= (\tilde{\alpha}\tilde{\alpha})^* \tilde{\beta} (\tilde{\beta}\tilde{\beta})^*$$

$$= (\tilde{\alpha}\tilde{\alpha})^* (\tilde{\beta}\tilde{\beta})^* \tilde{\beta}$$



Model-8:

- ③ $\{\omega \mid \text{ " , } n_a(\omega) \leq 1, n_b(\omega) = 2\}$
④ $\{\omega \mid \text{ " , } n_b(\omega) \leq 1, n_b(\omega) \leq 2\}$,
⑤ $\{\omega \mid \text{ " , } n_a(\omega) \geq 1, n_b(\omega) \leq 2\}$



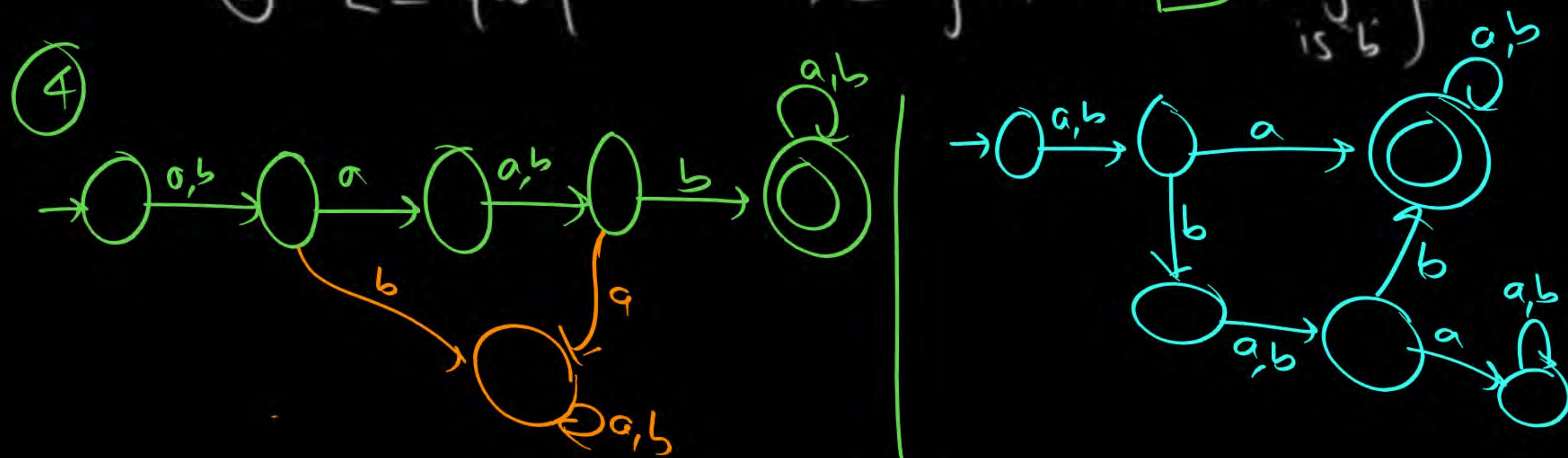
Model-12:

$$\textcircled{4} \quad L = \{ \omega \mid \text{ "}$$

, 2nd symbol is 'a' AND 4th symbol is 'b'

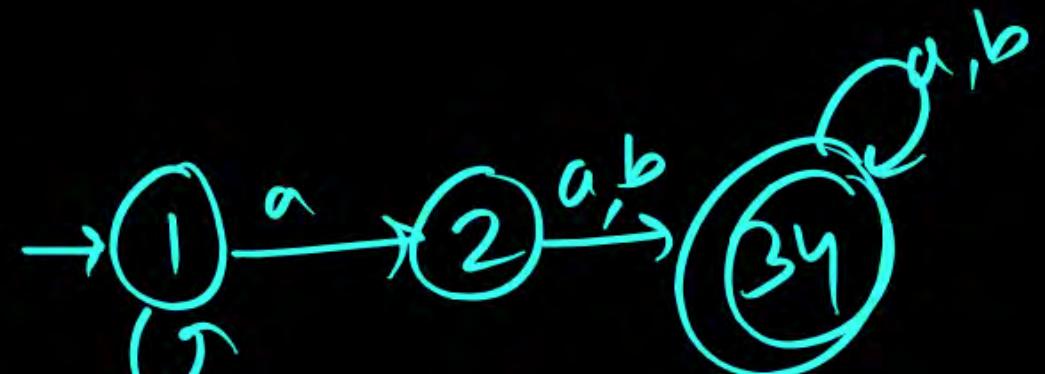
$$\textcircled{5} \quad L = \{ \omega \mid \text{ "}$$

, 2nd symbol is 'a' OR 4th symbol is 'b'

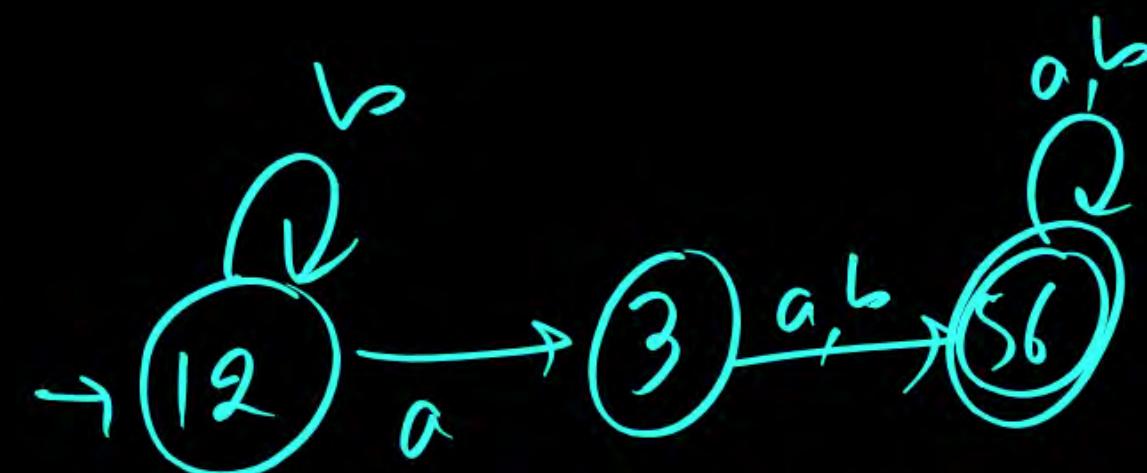
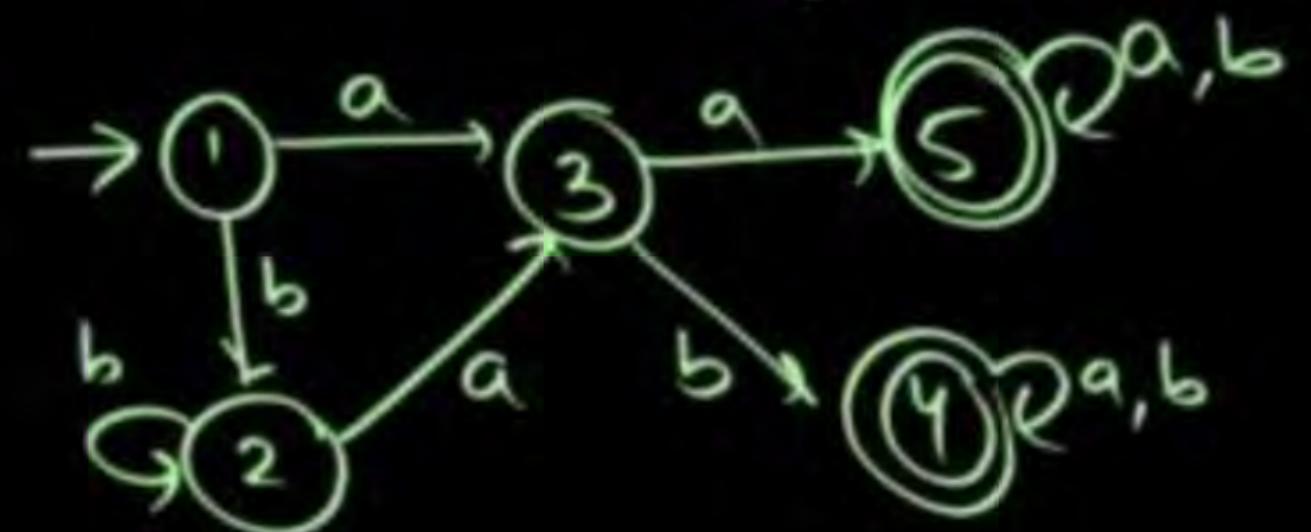


DFA Minimization

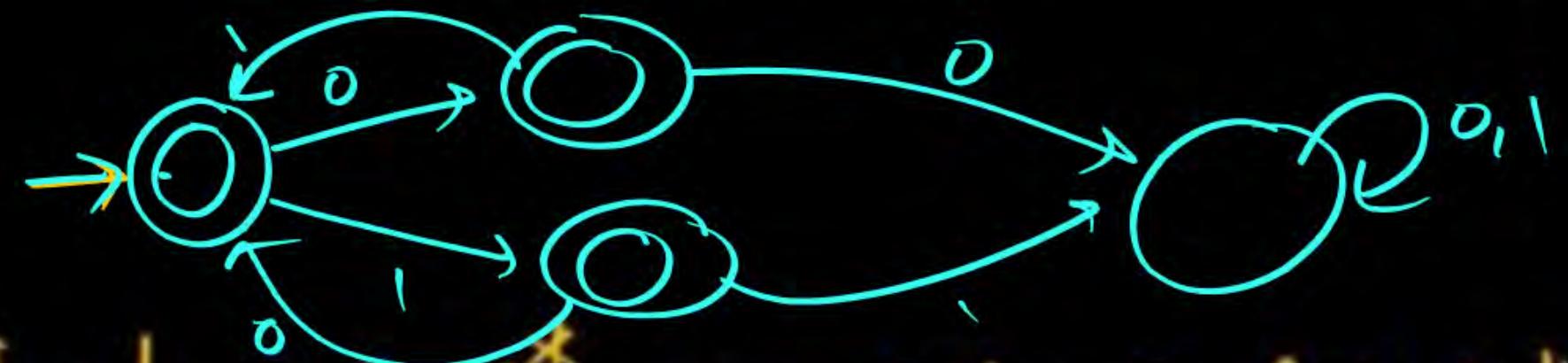
1)



2)



Model-13:

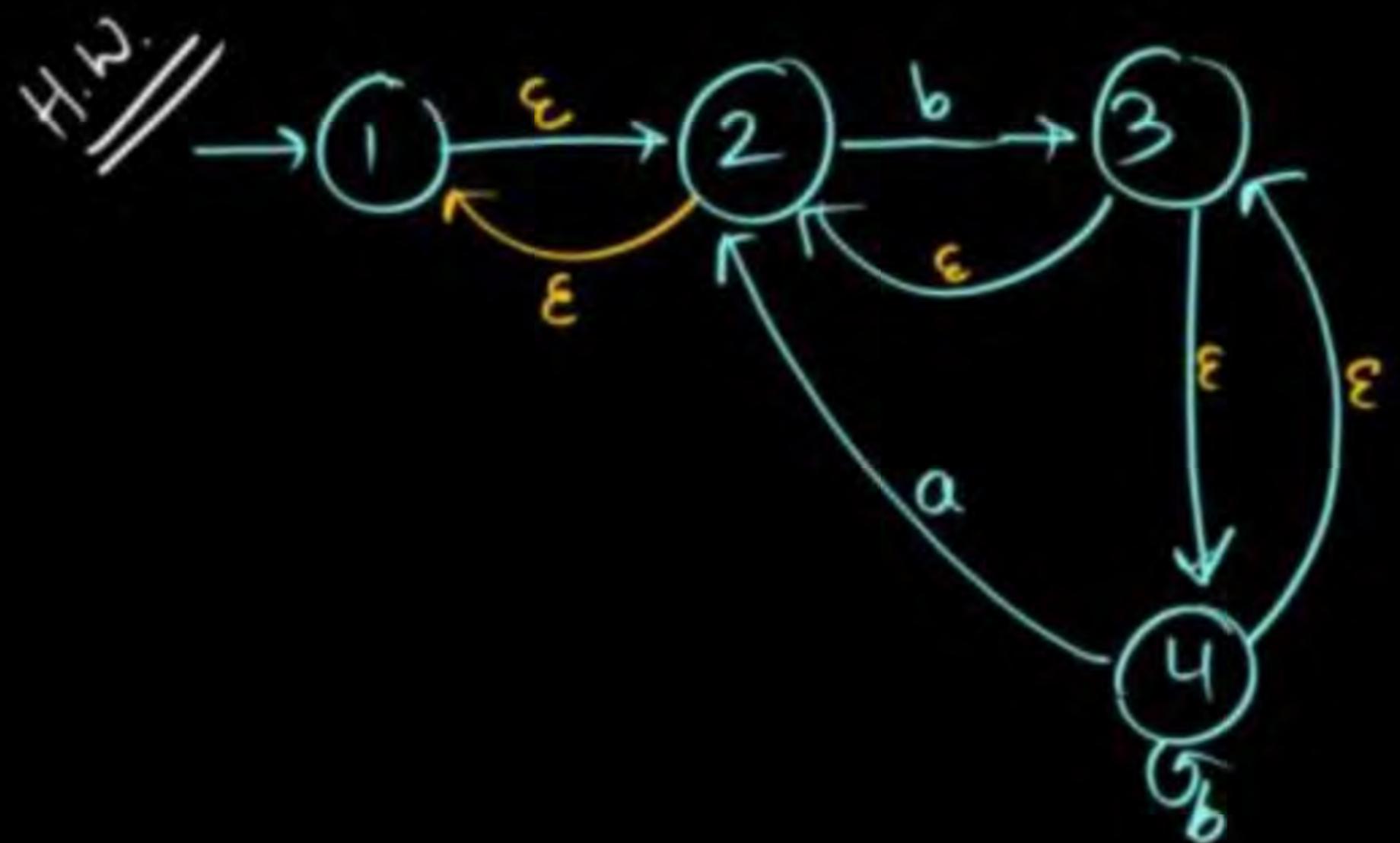


P
W

Prf ③ $L = \{w \mid w \in \{0,1\}^*\}$, every Prefix P of w satisfies

$$L = \{\epsilon, 0, 1, 00, 01, 10, 11, \dots \mid |n_0(P) - n_1(P)| \leq 1\}$$

w	ϵ	0	1	00	01	10	11
Prefixes(w)	ϵ	ϵ	ϵ	ϵ	ϵ	ϵ	ϵ
	$ 0-0 =0$	$ 1-0 \leq 1$	$ 1-1 =0$	$ 2-0 \neq 1$	$ 2-1 \neq 1$	$ 1-0 =1$	$ 2-1 \neq 1$
				$\boxed{00}$	$\boxed{01}$	$\boxed{10}$	$\boxed{11}$
							$\boxed{000}$



$$\hat{\delta}(1, \underline{aab}) = \phi$$

$$\hat{\delta}(2, bb) = \{3, 2, 1, 4\}$$

$$\hat{\delta}(3, bab) = \{3, 2, 1, 4\}$$

$$\hat{\delta}(4, ab) = \{1, 2, 3, 4\}$$

Let L be the language represented by the regular expression $\Sigma^*0011\Sigma^*$ where $\Sigma=\{0,1\}$. What is the minimum number of states in a DFA that recognizes \bar{L} (complement of L)?

(GATE - 15 - SET3)

- (a) 4
- (b) 5**
- (c) 6
- (d) 8

min \Rightarrow 0011

↓
5 states

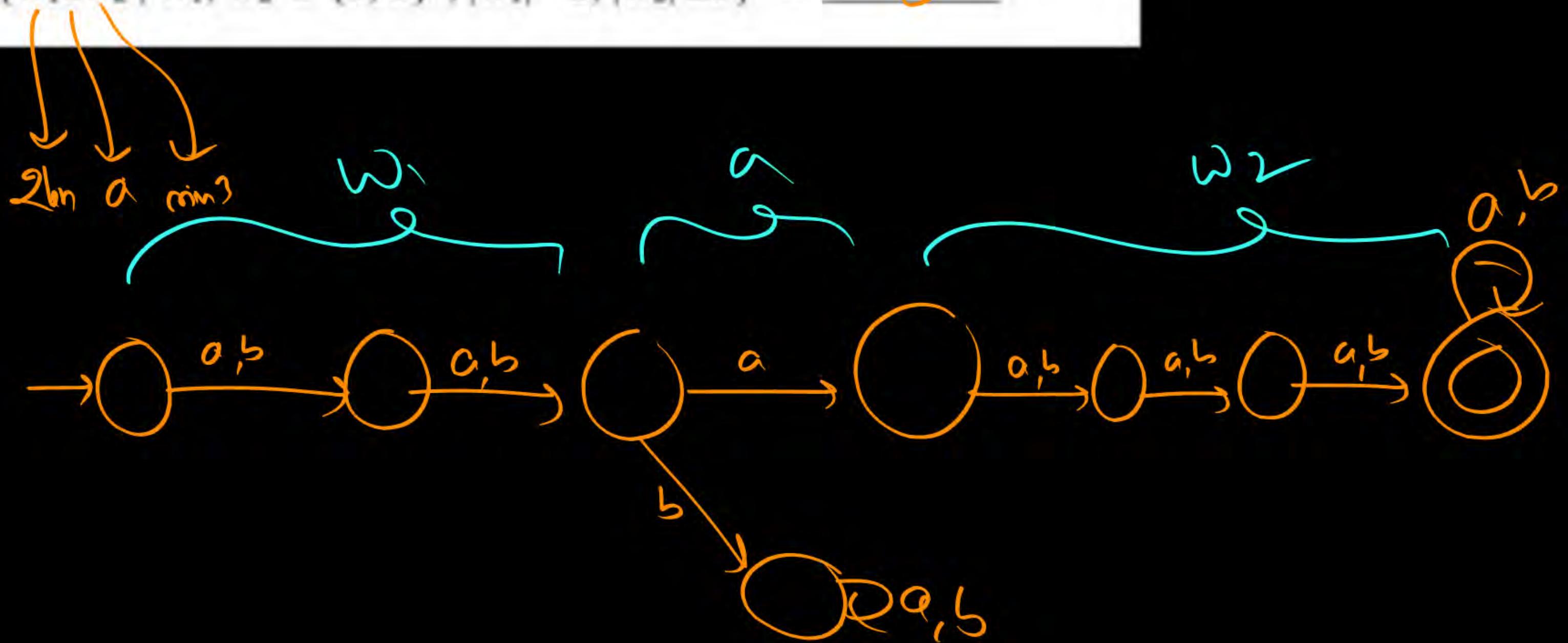
Consider the language L given by the regular expression $(a+b)^*b(a+b)$ over the alphabet $\{a, b\}$. The smallest number of states needed in a deterministic finite-state automaton (DFA) accepting L is 4. (GATE - 17 - SET1)

k^{th} symbol from end is 'b'

2^k states

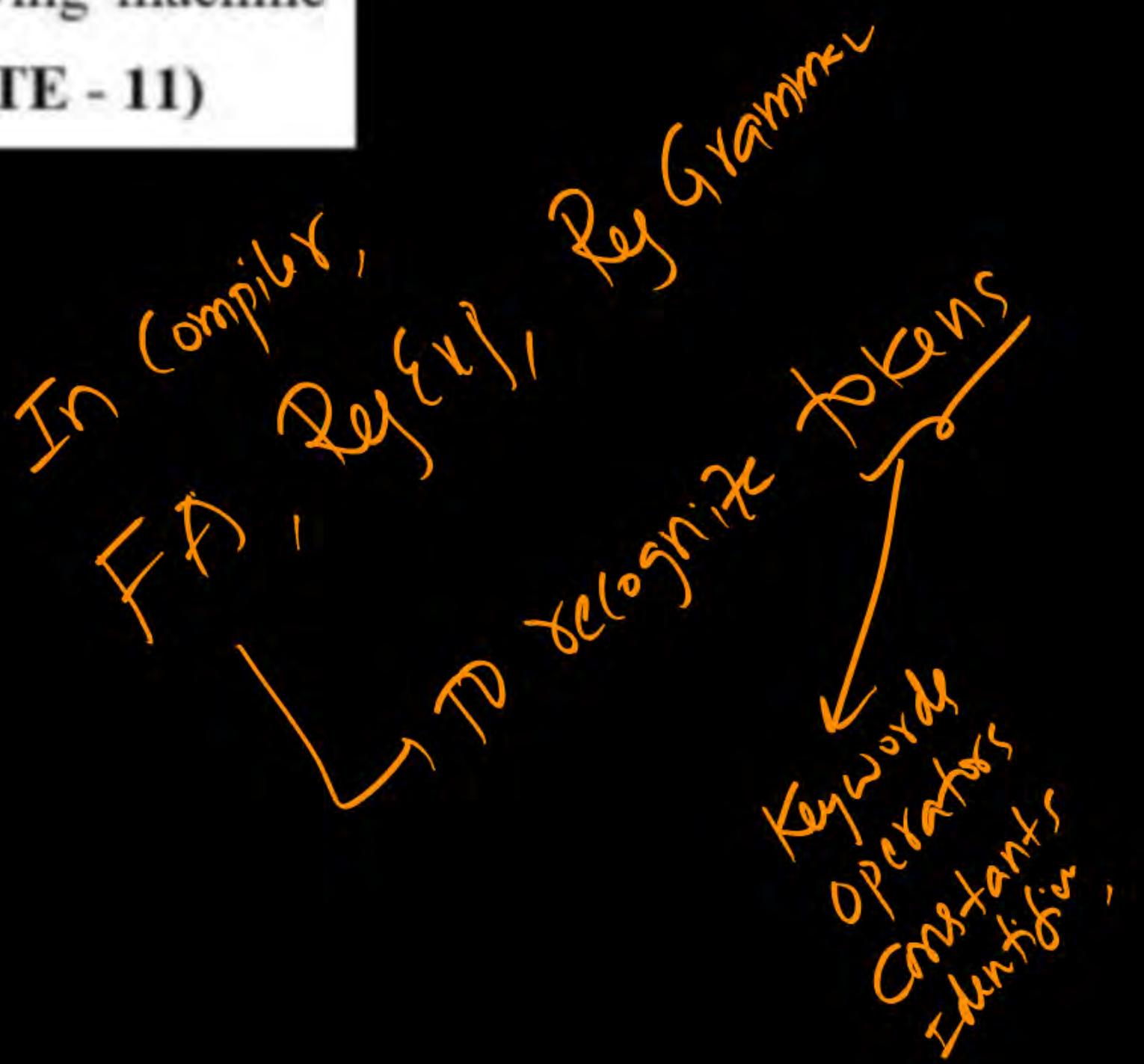
The minimum possible number of states of a deterministic finite automaton that accepts the regular language (GATE – 17 – SET2)

$L = \{w_1 a w_2 \mid w_1, w_2 \in \{a, b\}^*, |w_1| = 2, |w_2| \geq 3\}$ is 8.



The lexical analysis for a modern computer language such as java needs the power of which one of the following machine models in a necessary and sufficient sense? **(GATE - 11)**

- (a) Finite state automata
- (b) Deterministic pushdown automata
- (c) Non-deterministic pushdown automata
- (d) Turing machine



The number of substrings (of all lengths inclusive) that can be formed from a character string of length n is (GATE - 89 & 94)

(a) n

(c) $\frac{n(n-1)}{2}$

(b) n^2

(d) $\frac{n(n+1)}{2} + 1$

No option

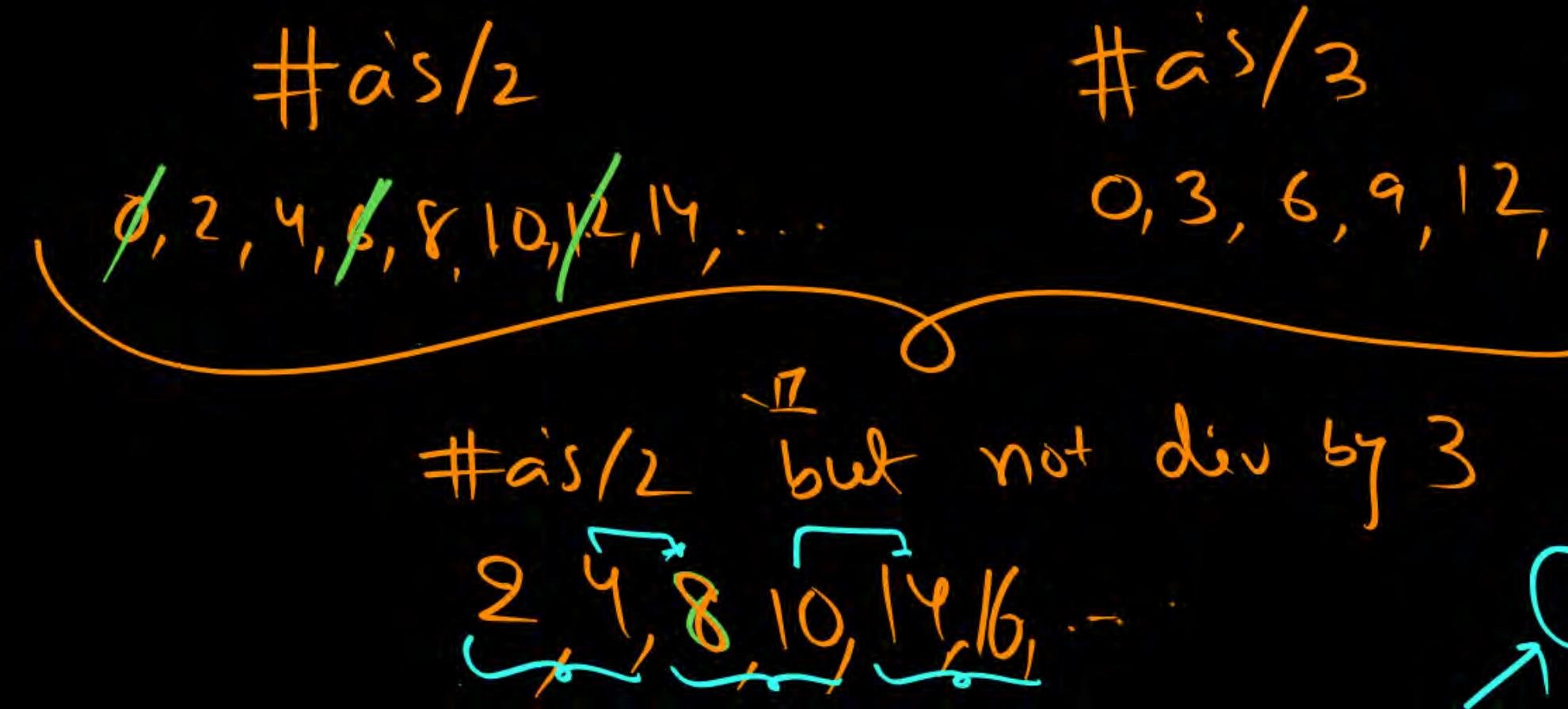
$$n+1 \leq \text{No. of substrings} \leq \frac{n(n+1)}{2} + 1$$

Consider the following language.

$$L = \{x \in \{a, b\}^* \mid \text{number of } a's \text{ in } x \text{ divisible by 2 but not divisible by 3}\}$$

The minimum number of states in DFA that accepts L is 6

6 ✓



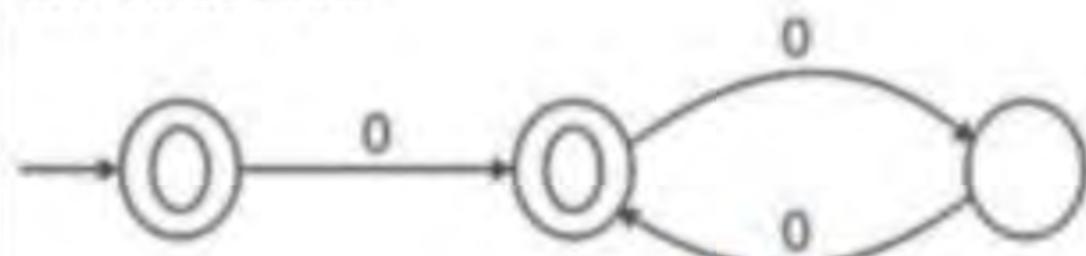
Given a language L , define L^i as follows:

$$L^0 = \epsilon$$

$$L^i = L^{i-1} \cdot L \text{ For all } i > 0$$

The order of a language is defined as the smallest such that $L^k = L^{k+1}$.

Consider the language L_1 (over alphabet 0) accepted by the following automaton:



The order of L_1 is 9

Note: If $L^k = L^{k+1}$ then $L^k = L$

$$L = \epsilon + 0(00)^*$$

$$L^2 = L \cdot L$$

$$= 0^* \cdot L = 0^*$$

$$\boxed{L^3 = L^2}$$

$$L^0 = \epsilon \rightarrow \textcircled{1}$$

$$L^1 = L^{0+1}, L = L^0 \cdot L = L = \epsilon + 0(00)^*$$

$$\boxed{L^1 \neq L^0}$$

$$L^2 = L^1 \cdot L = (\epsilon + 0(00)^*) \cdot (\epsilon + 0(00)^*) = 0^*$$

$$\boxed{L^2 \neq L^1}$$

$$L^0 = \checkmark$$

$$L^1 = L^0 \Rightarrow O(L) = 0$$

$$L^2 = L^1 \Rightarrow O(L) = 1$$

$$L^3 = L^2 \Rightarrow O(L) = 2$$

$$L^4 = L^3 \Rightarrow O(L) = 3$$

$$L^5 = L^4 \Rightarrow O(L) = 4$$

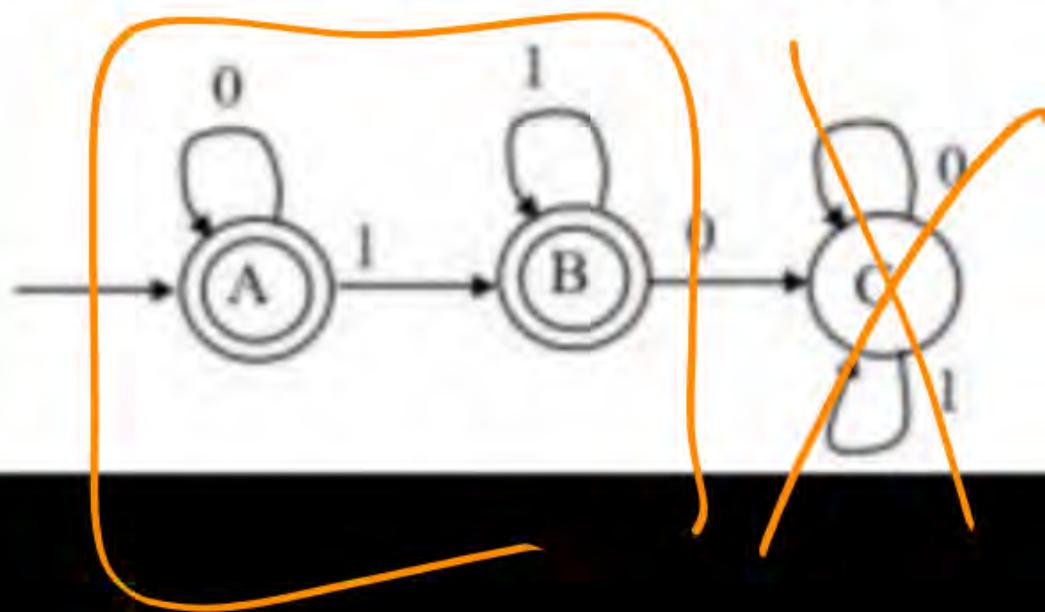
$$L^6 = L^5 \Rightarrow O(L) = 5$$

$$L^7 = L^6 \Rightarrow O(L) = 6$$

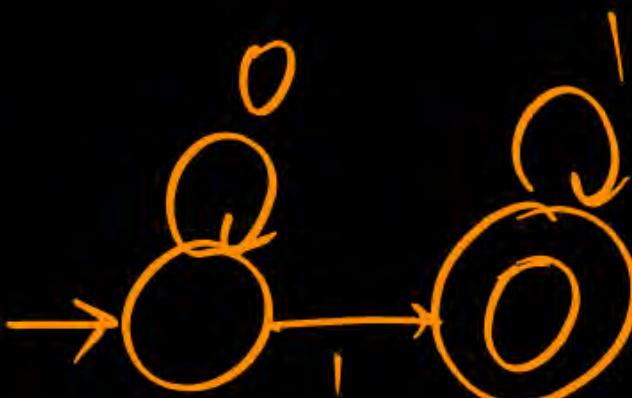
$$L^8 = L^7 \Rightarrow O(L) = 7$$

$$L^9 = L^8 \Rightarrow O(L) = 8$$

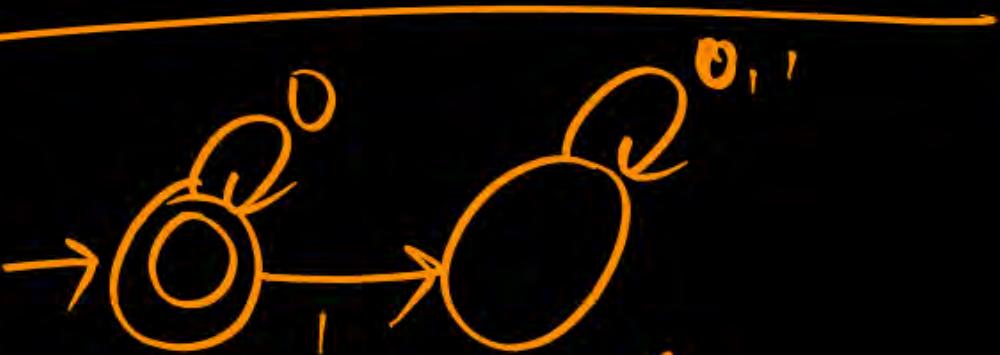
The regular expression for the language recognized by the finite state automation of the below figure is _____ (GATE - 94)



$$L = \bar{0}^* \bar{1}^*$$



$$L = \bar{0}^* 1^* = \bar{0}^* 1^+$$



$$L = \bar{0}^*$$

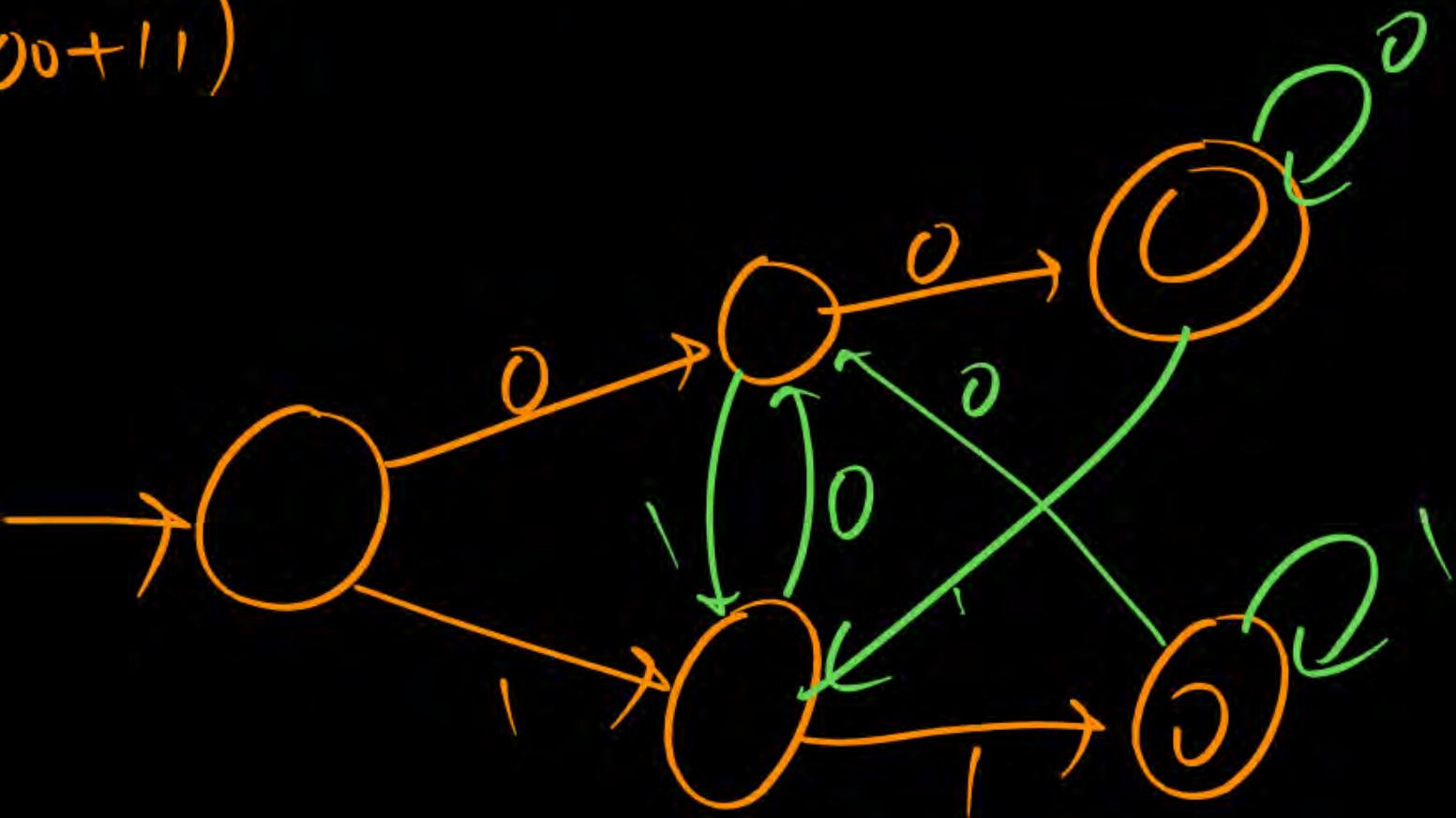
Let L be the set of all binary strings whose last two symbols are the same .The number of states in the minimum state deterministic finite-state automaton accepting L is

(GATE - 98)

→ 5 states

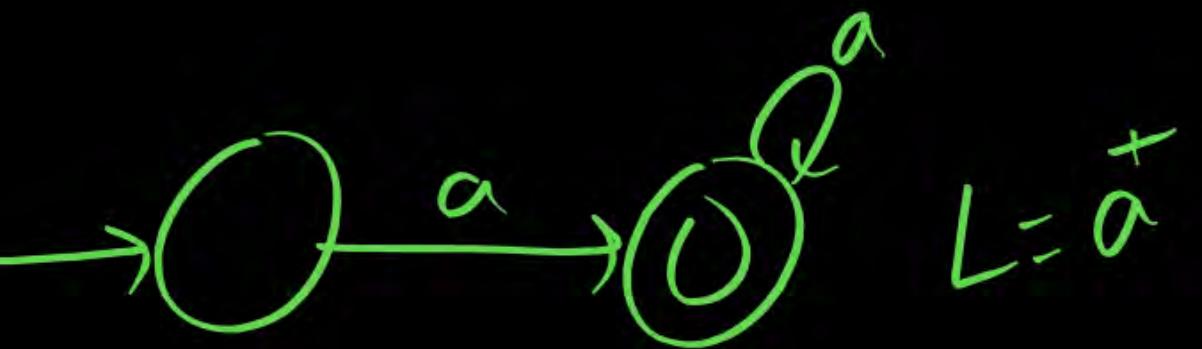
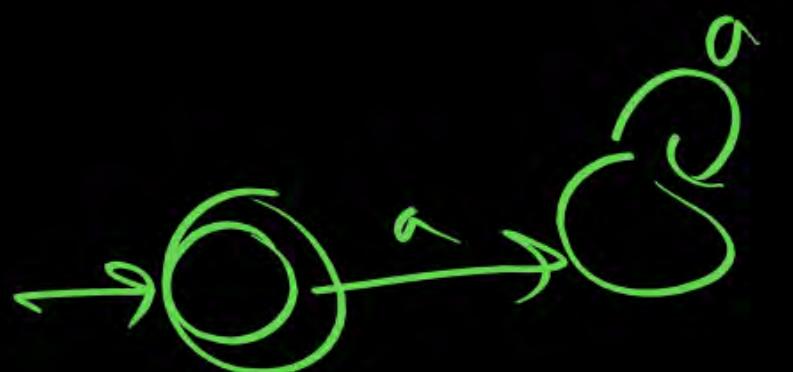
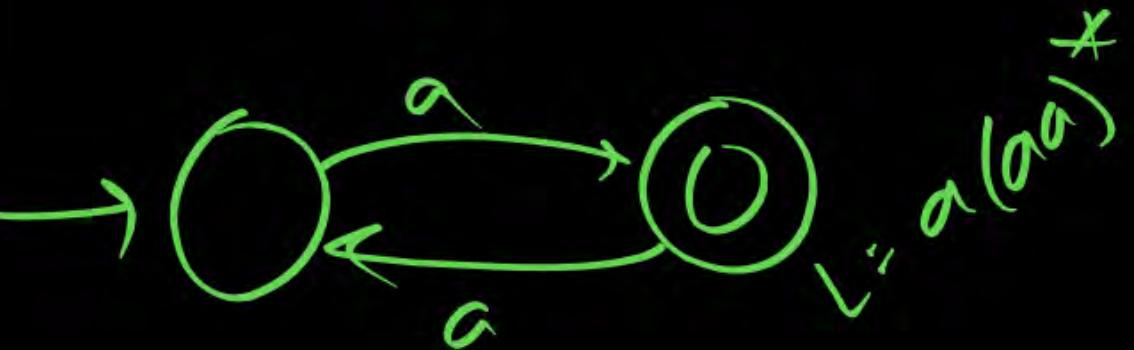
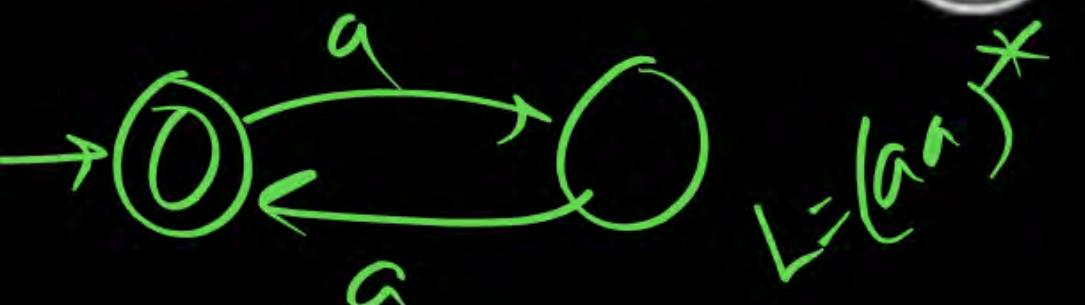
$$\Sigma = \{0, 1\}$$

$$L = (0+1)^* (00+11)$$



What can be said about a regular language L over $\{a\}$ whose minimal finite state automaton has two states? (GATE - 2000)

- (a) L must be $\{a^n \mid n \text{ is odd}\}$
- (b) L must be $\{a^n \mid n \text{ is even}\}$
- (c) L must be $\{a^n \mid n \geq 0\}$
- (d) Either L must be $\{a^n \mid n \text{ is odd}\}$ or L must be $\{a^n \mid n \text{ is even}\}$



Consider a DFA over $\Sigma = \{a, b\}$ accepting all strings which have number of a's divisible by 6 and number of b's divisible by 8.

What is the minimum number of states that the DFA will have?

(GATE - 01)

- (a) 8
- (b) 14
- (c) 15
- (d) 48

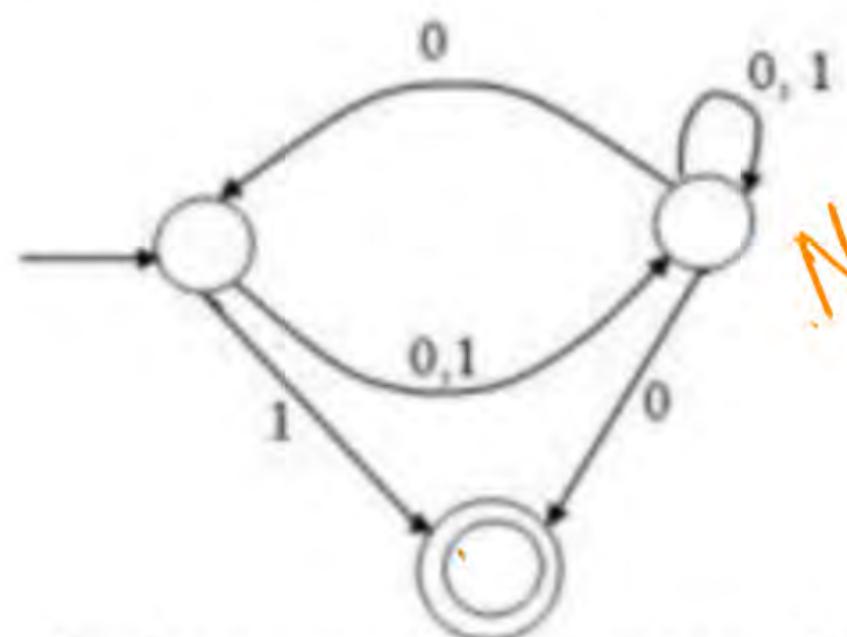
The smallest finite automation which accepts the language

$L = \{x \mid \text{length of } x \text{ is divisible by 3}\}$ has

(GATE - 02)

- (a) 2 states
- (b) 3 states
- (c) 4 states
- (d) 5 states

Consider the NFA M shown below.



NFA

$$= L \subset \Sigma^*$$

Let the language accepted by M be L. Let L_1 be the language accepted by the NFA, M_1 obtained by changing the accepting state of M to a non-accepting state and by changing the non-accepting state of M to accepting states. Which of the following statements is true?

(a) $L_1 = \{0, 1\}^* - L$

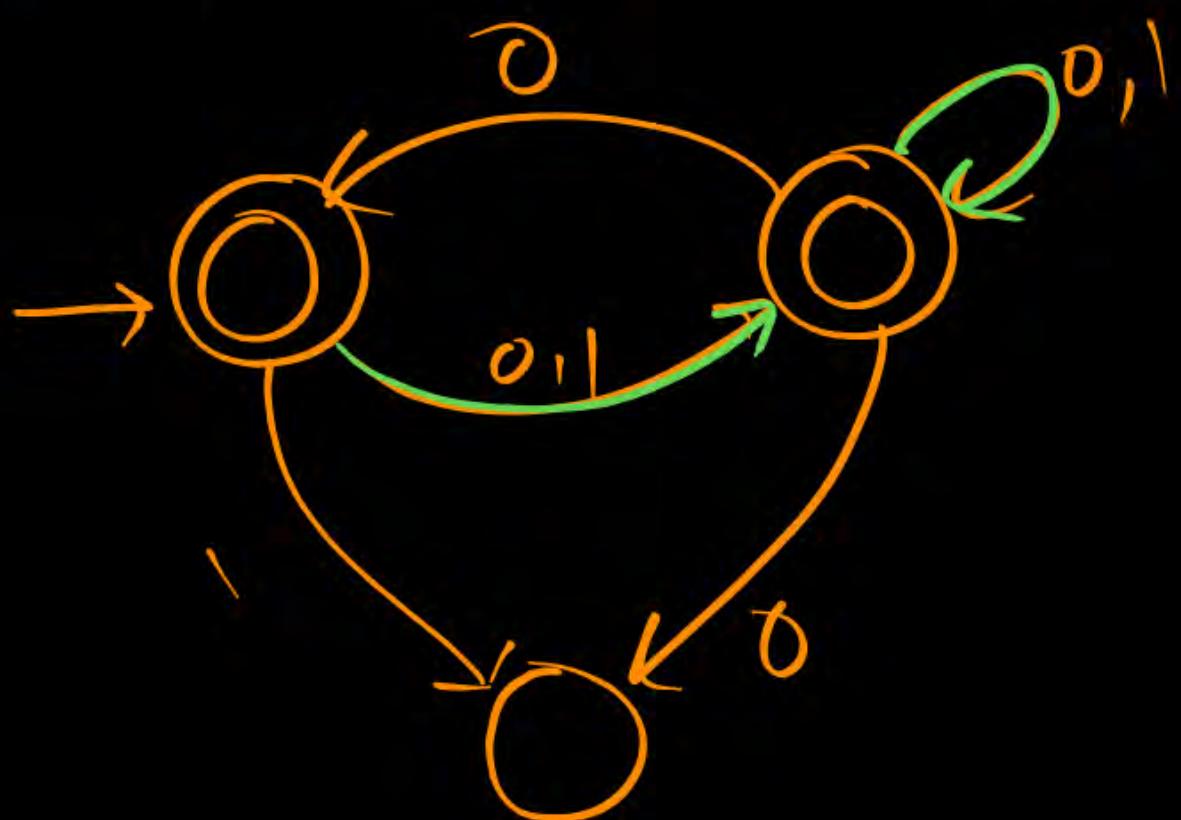
(c) $L_1 \subseteq L$

✓✓✓✓+

(b) $L_1 = \{0, 1\}^*$

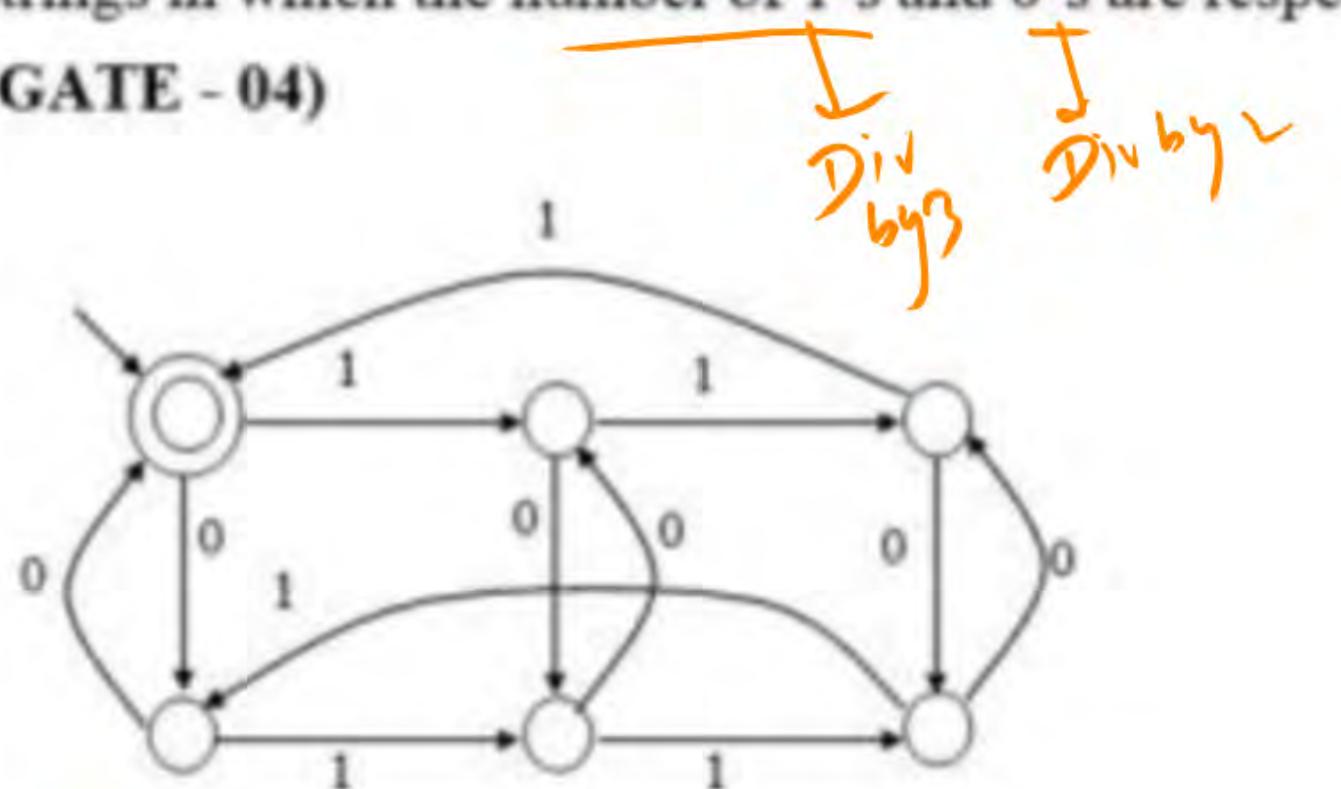
(d) $L_1 = L$

$$L_1 = (0+1)^*$$



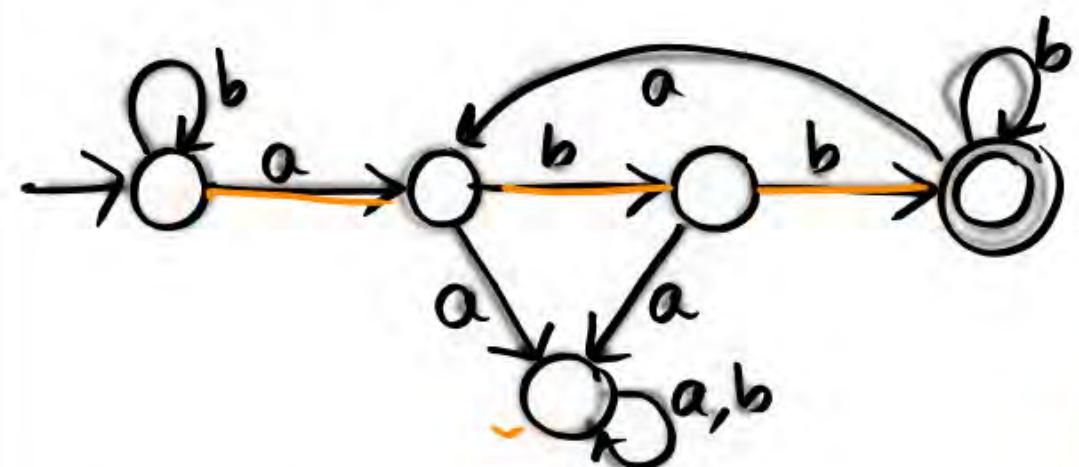
The following finite state machine accepts all those binary strings in which the number of 1's and 0's are respectively

(GATE - 04)



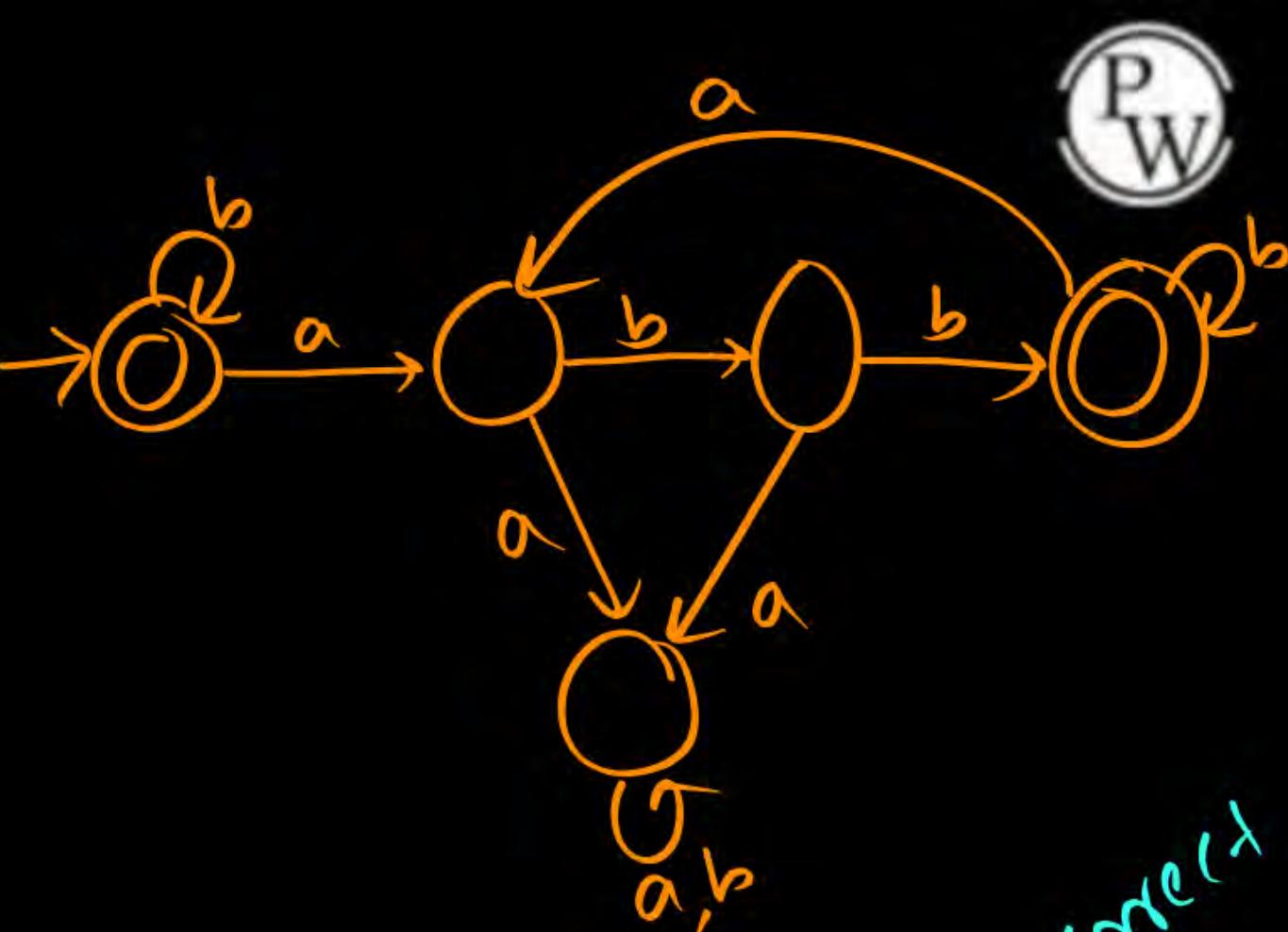
- (a) Divisible by 3 and 2
- (b) Odd and even
- (c) Even and odd
- (d) Divisible by 2 and 3

Consider the machine M:



(GATE - 05)

- The language recognized by M is:
- (a) $\{w \in \{a,b\}^*\mid$ every a in w is followed by exactly two b's $\}$
 - (b) $\{w \in \{a,b\}^*\mid$ every a in w is followed by at least two b's $\}$
 - (c) $\{w \in \{a,b\}^*\mid$ w contains the substring 'abb' $\}$ = Set of all strings containing abb.
 - (d) $\{w \in \{a,b\}^*\mid$ w does not contain 'aa' as a substring $\}$



Option (b) is correct
J Option (b) is correct

If s is a string over $(0+1)^*$ then let $n_0(s)$ denote the number of 0's in s and $n_1(s)$ the number of 1's in s . Which one of the following languages is not regular?

(GATE - 06)

- (a) $L = \{s \in (0+1)^* \mid n_0(s) \text{ is a } \underbrace{\text{3-digit prime}}_{2,3,5,7} \}$ $\Rightarrow \text{Reg}$
- (b) $L = \{s \in (0+1)^* \mid \text{for every prefix } s' \text{ of } s, |n_0(s') - n_1(s')| \leq 2\}$ $\Rightarrow \text{Reg}$
- (c) $L = \{s \in (0+1)^* \mid |n_0(s) - n_1(s)| \leq 4\} \Rightarrow \text{Not Reg}$
- (d) $L = \{s \in (0+1)^* \mid n_0(s) \bmod 7 = n_1(s) \bmod 5 = 0\} \Rightarrow \text{Reg}$

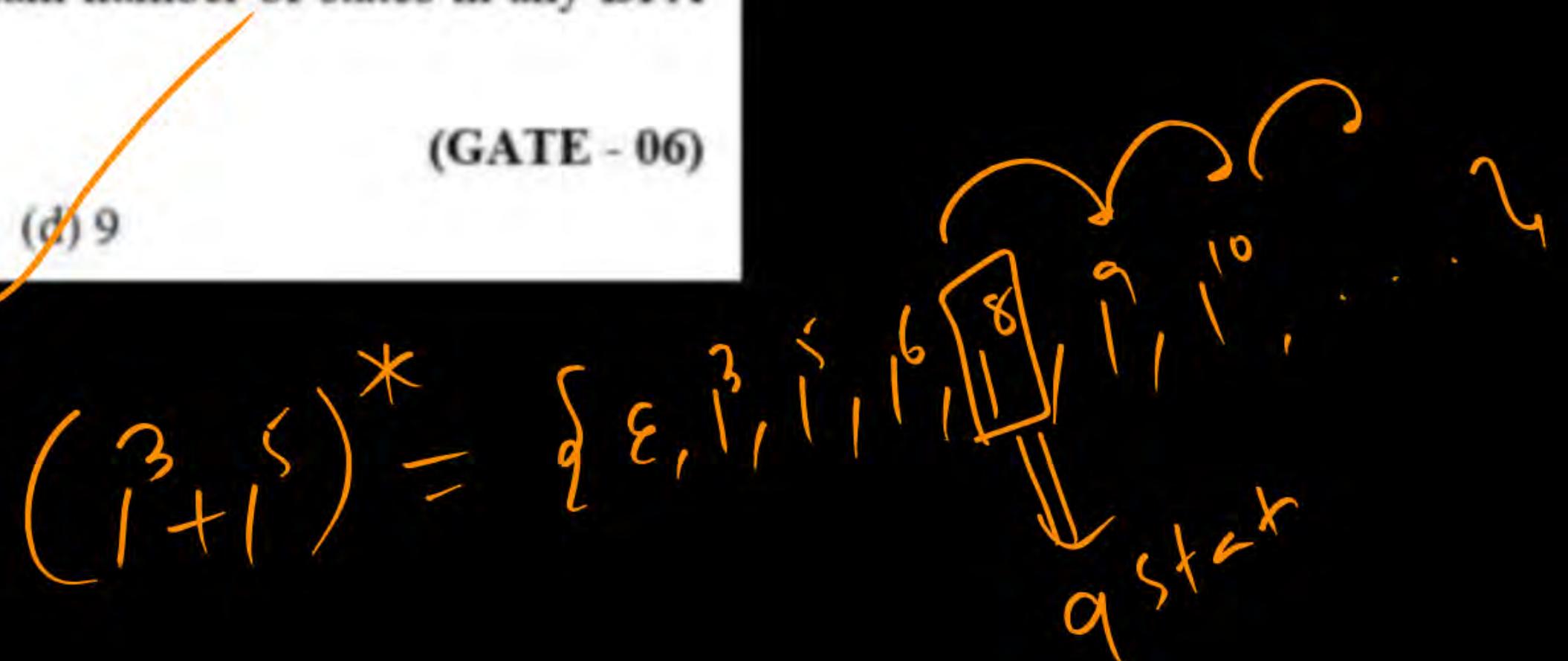
35 states

Consider the regular language

$L = (111+11111)^*$. The minimum number of states in any DFA accepting this language is

- (a) 3 (b) 5 (c) 8

(GATE - 06)



A minimum state deterministic finite automaton accepting the language

$L = \{w \mid w \in \{0, 1\}^*, \text{number of } 0\text{'s and } 1\text{'s in } w \text{ are divisible by } 3 \text{ and } 5, \text{ respectively}\}$ has

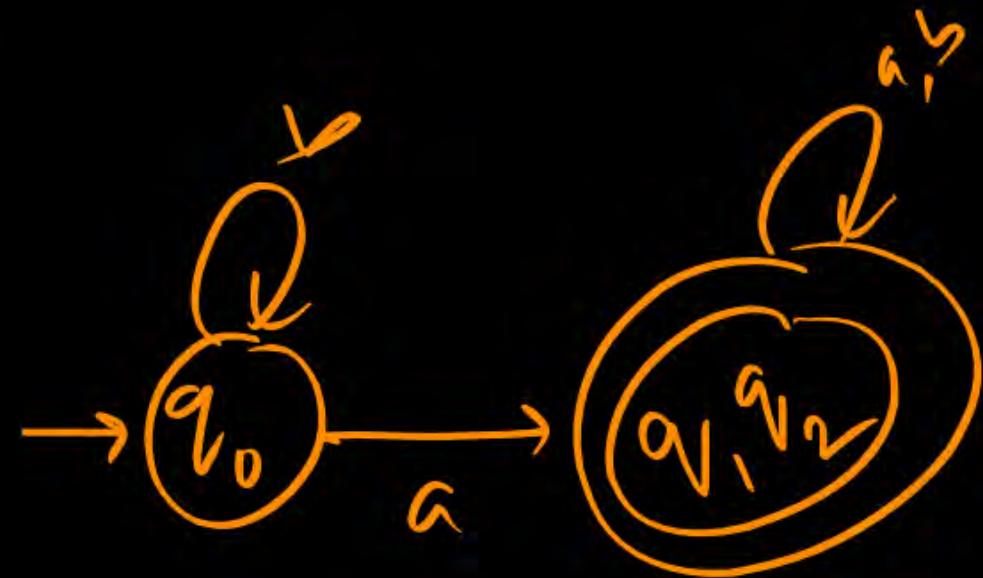
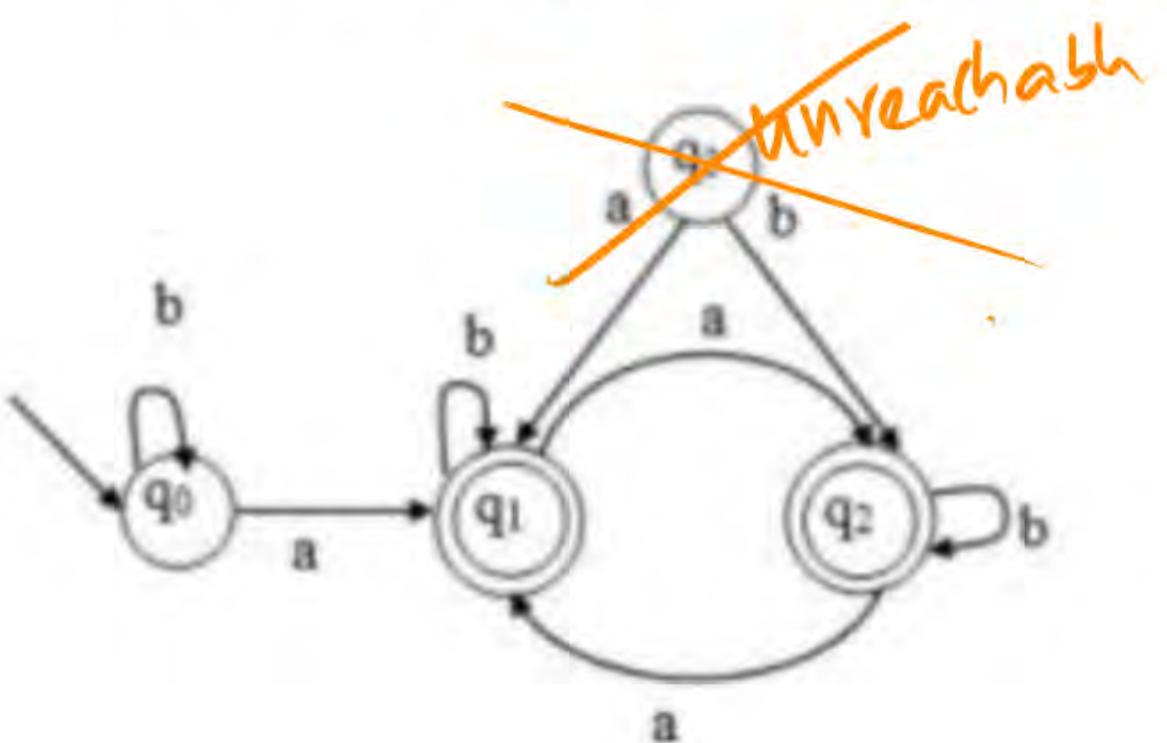
(GATE - 07)

- (a) 15 states
- (b) 11 states
- (c) 10 states
- (d) 9 states

$3 \times 5 = 15$

Consider the following finite state automaton

(GATE - 07)

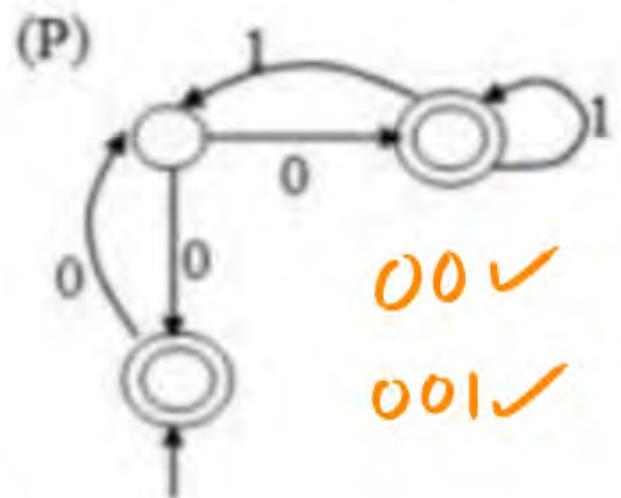


The language accepted by this automaton is given by the regular expression

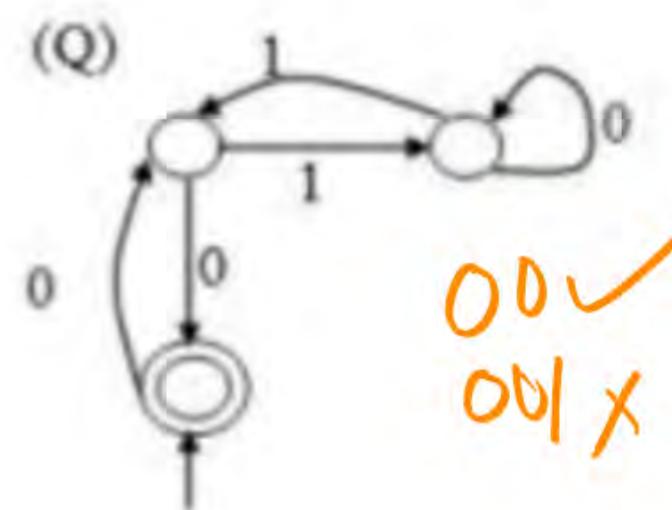
- (a) $b^*ab^*ab^*$
- (b) $(a+b)^*$
- (c) $b^*a(a+b)^*$
- (d) $b^*ab^* ab^*$

$b^* a (a+b)^*$
 $(a+b)^* a (a+b)^*$

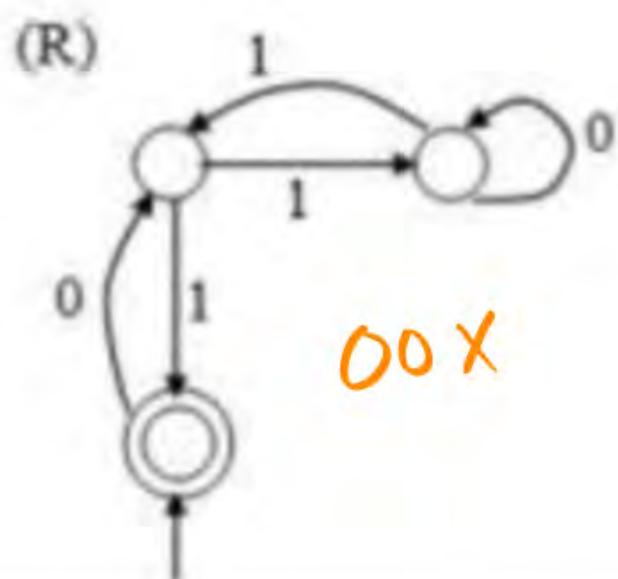
Match the following NFAs with the regular expressions they correspond to



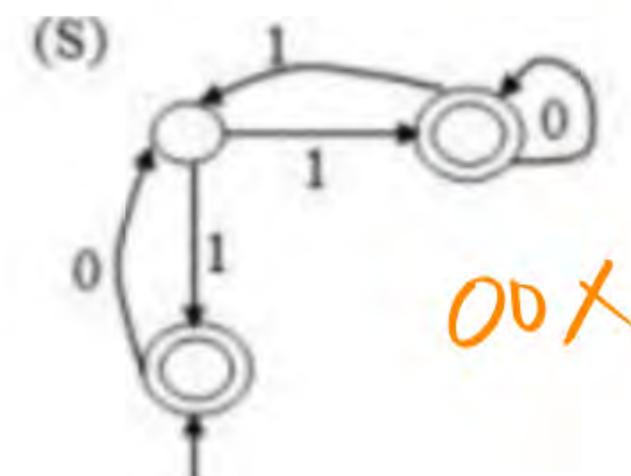
00 ✓
001 ✓



00 ✓
001 ✗



oox



oox

(GATE - 0)

(GATE - 08) L = ϵ + $0(01^* 1 + 00)^* 01^*$

$$2. \quad \varepsilon + 0(10^* 1 + 00)^* 0$$

$$P,Q \in \{3, \varepsilon + 0(10^* 1 + 10)^* 1\}$$

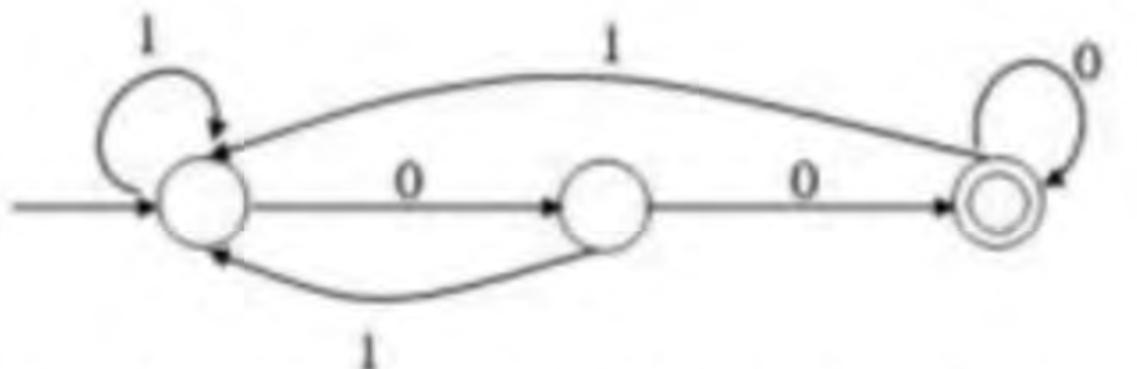
4. $\varepsilon + 0(10 * 1 + 10) * 10 *$

P.0

RS

- (a) P-2, Q-1, R-3, S-4
 - (b) P-1, Q-3, R-2, S-4
 - (c) P-1, Q-2, R-3, S-4
 - (d) P-3, Q-2, R-1, S-4





The above DFA accepts the set of all strings over $\{0, 1\}$ that

(GATE - 09)

- (a) Begins either with 0 or 1
- (b) End with 0
- (c) End with 00
- (d) Contains the substring 00.

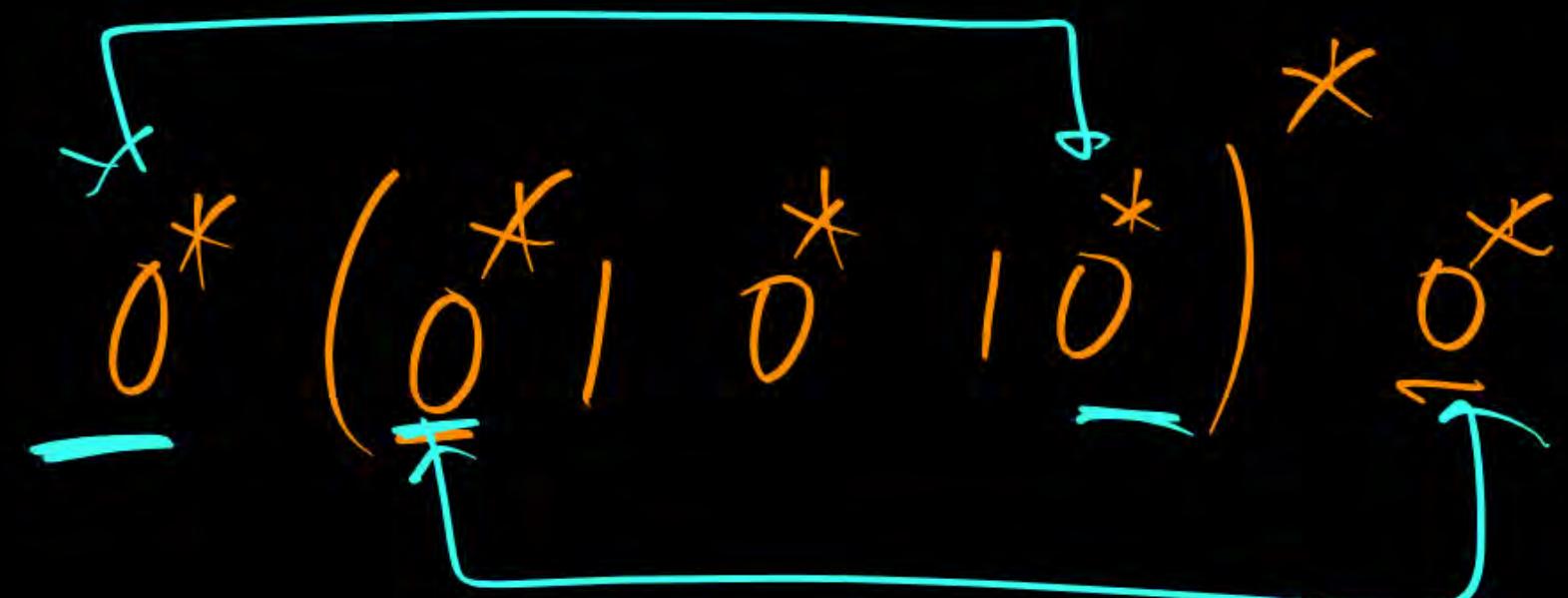
Let $L = \{w \in (0+1)^* \mid w \text{ has even number of 1's}\}$, i.e L is the set of all bit strings with even number of 1's. Which one of the regular expressions below represents L ?

(a) $(0^* 1 0^*)^*$ $\xrightarrow{0} 11011$
(c) $0^* (1 0^* 1)^* 0^*$ $\xrightarrow{\epsilon} 11011$

(b) $0^* (1 0^* 1 0^*)^*$ $\xrightarrow{0} 11011$
(d) $0^* 1 (1 0^* 1)^* 1 0^*$ $\xrightarrow{\epsilon} 11011$

(GATE - 10)

$\overbrace{(11011)}^{(1010)(1010)}$
 $\overbrace{(1010)(1010)(\epsilon|\epsilon)}^{(1\epsilon|0)(1\epsilon|0)}$
 $\overbrace{(1\epsilon|0)(1\epsilon|0)(11011)}^{(11011)}$

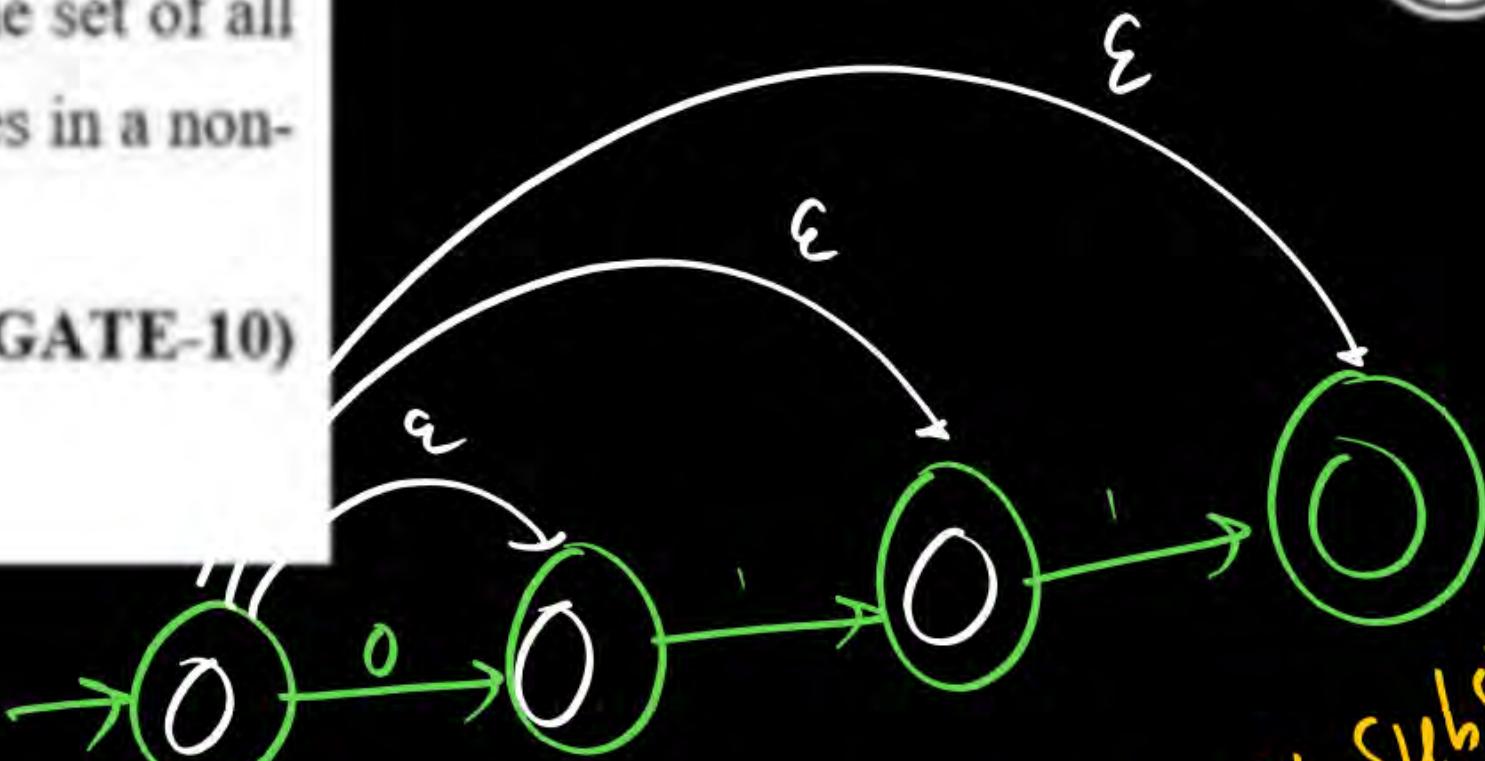




Let w be any string of length n in $\{0, 1\}^*$. Let L be the set of all substrings of w . What is the minimum number of states in a non-deterministic finite automation that accepts L ?

- (a) $n - 1$
- (b) n
- (c) $n+1$
- (d) 2^{n-1}

(GATE-10)



$$w = \overrightarrow{011} \quad \text{with } n=3$$

$$L = \{ \epsilon, 0, 1, 01, 11, 011 \} = \text{Set of all substrings of } w$$

$n+1$ states

Definition of the language L with alphabet {a} is given as following.

$$L = \{a^{nk} \mid k > 0, \text{ and } n \text{ is a positive integer constant}\}$$

What is the minimum number of states needed in a DFA to recognize L?

(GATE - 11)

- (a) $k + 1$
- ~~(b) $n + 1$~~
- (c) 2^{n+1}
- (d) 2^{k+1}

$n = \text{constant}$

$k > 0$

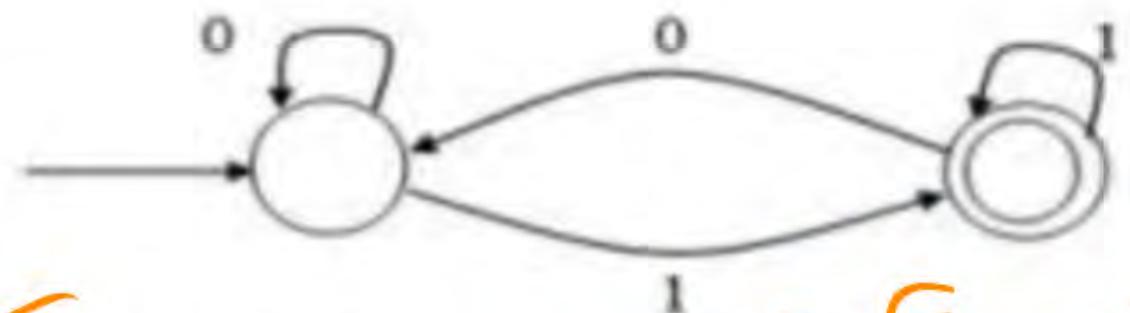
$$L = \{a^n \mid n > 0\}$$

$$n=1 \Rightarrow \{a^k \mid k > 0\} = a^+ \Rightarrow 2 \text{ states}$$



Which of the regular expression given below represent the following DFA?

(GATE – 14-SET1)



Ends with 1

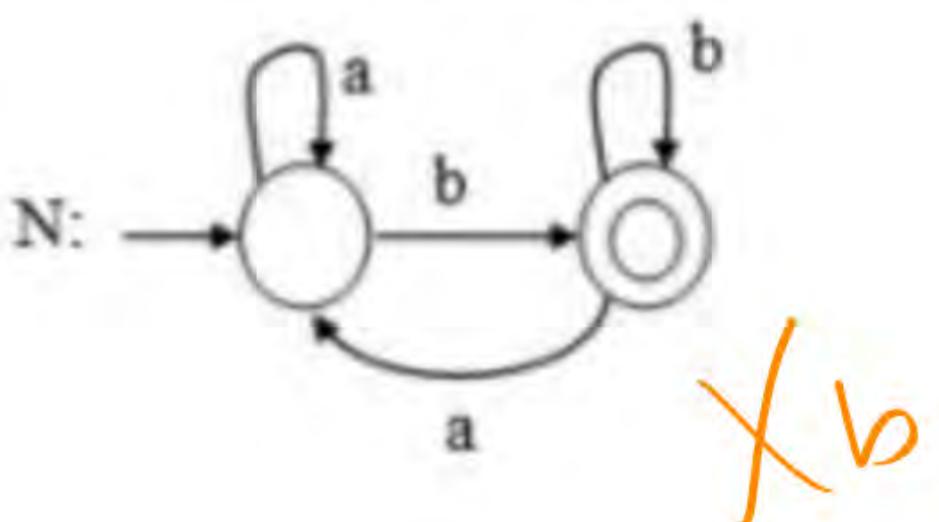
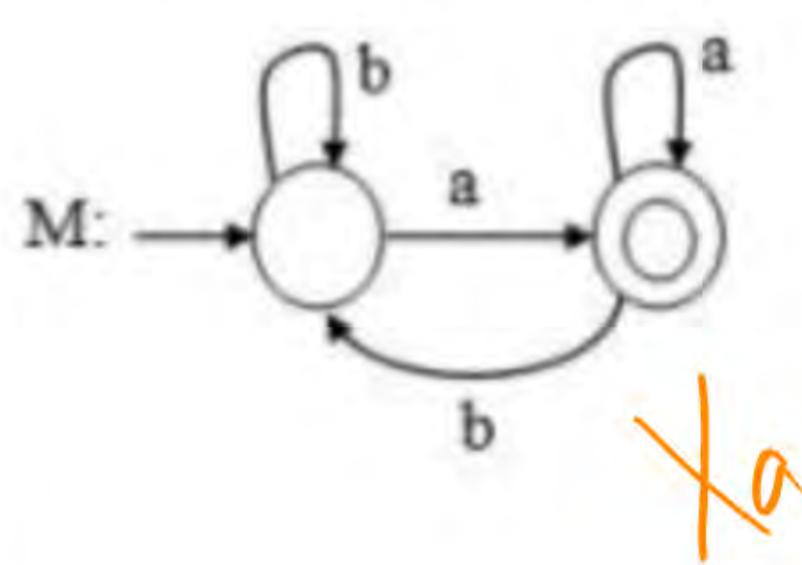
I. $0^*1(1+00^*1)^*$ $\rightarrow 0^*1[(\epsilon+00^*)1]^*$

II. $0^*1^*0+11^*0^*0$ $\rightarrow 0^*1[\sigma^*1]^* = (\sigma^*1)^+$

III. $(0+1)^*1$

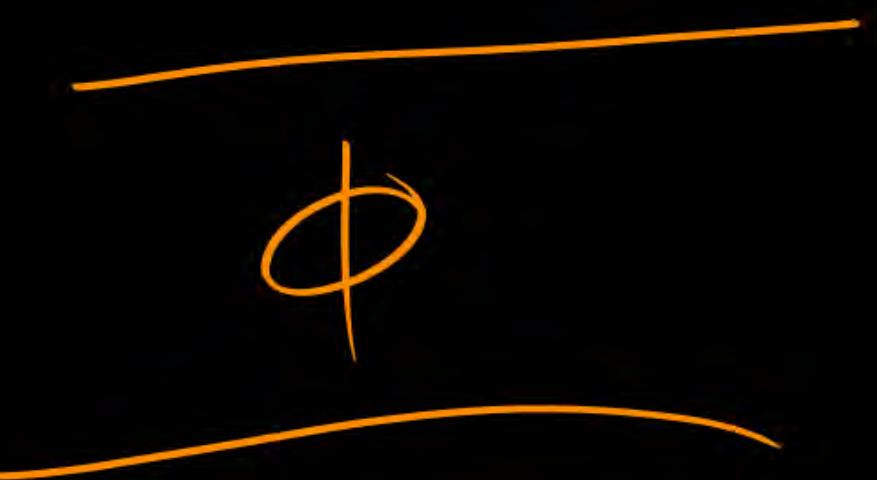
- (a) I and II only
(c) II and III only

- (b) I and III only
(d) I, II, and III



Consider the DFAs M and N given above. The number of states in a minimal DFA that accepts the languages $L(M) \cap L(N)$ is 2.

(GATE – 15 – SET1)



X_a

1

X_b

1

Consider the alphabet $\Sigma = \{0, 1\}$, the null/empty string λ , and the set of strings X_0 , X_1 , and X_2 generated by the corresponding non-terminals of a regular grammar. X_0 , X_1 , and X_2 are related as follows.

$$X_0 = 1 X_1$$

$$X_1 = 0 X_1 + 1 X_2$$

$$X_2 = 0 X_1 + \{\lambda\}$$

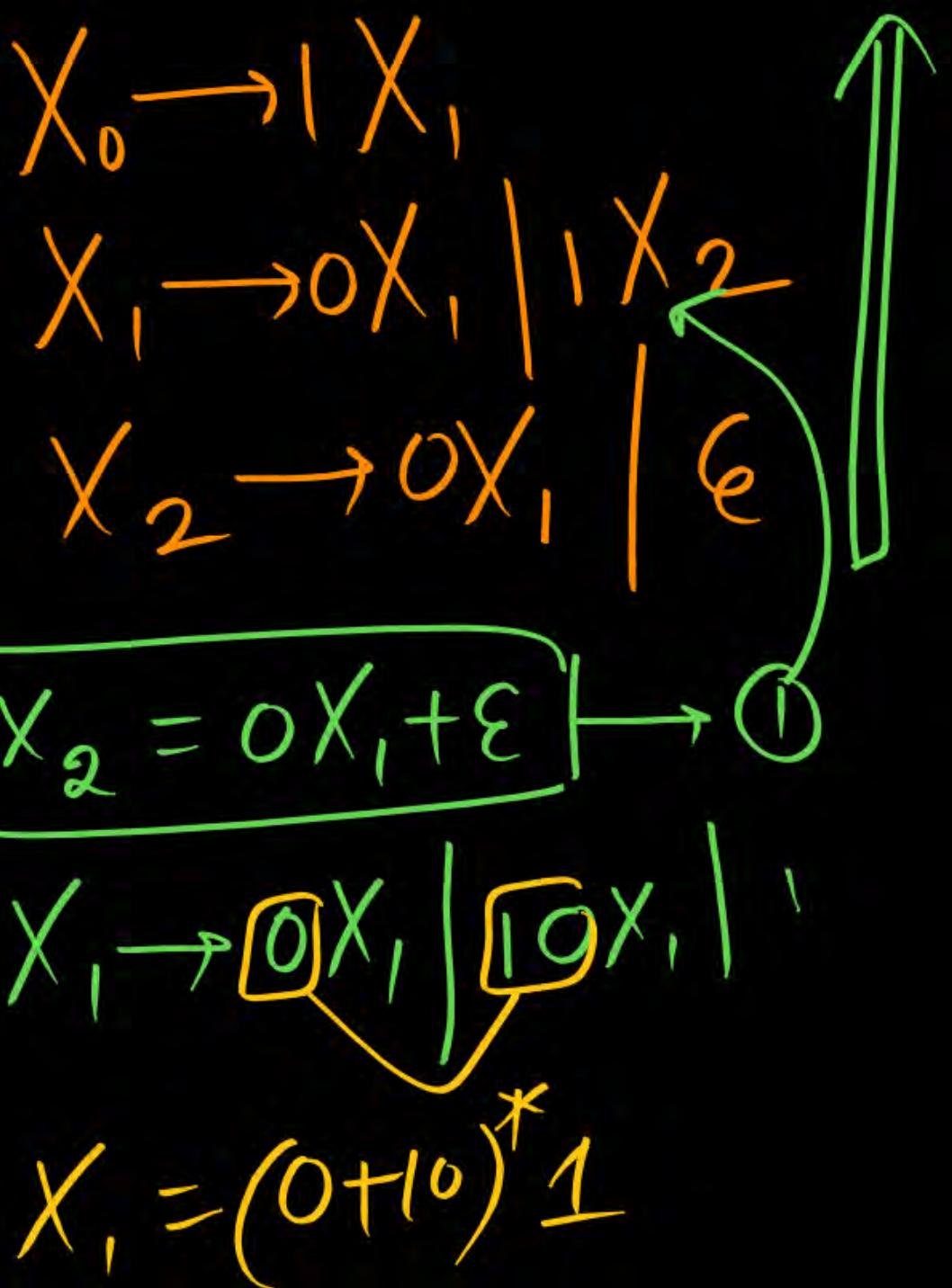
Which one of the following choices precisely represents the strings in X_0 ?

(GATE - 15- SET2)

- (a) $10(0^*+(10)^*)1$
- (b) $10(0^*+(10^*))^*1$
- (c) $1(0+10)^*1$
- (d) $10(0+10)^*1 + 110(0+10)^*1$

$$X_0 = 1 (0+10)^* 1$$

$$X_0 = ?$$



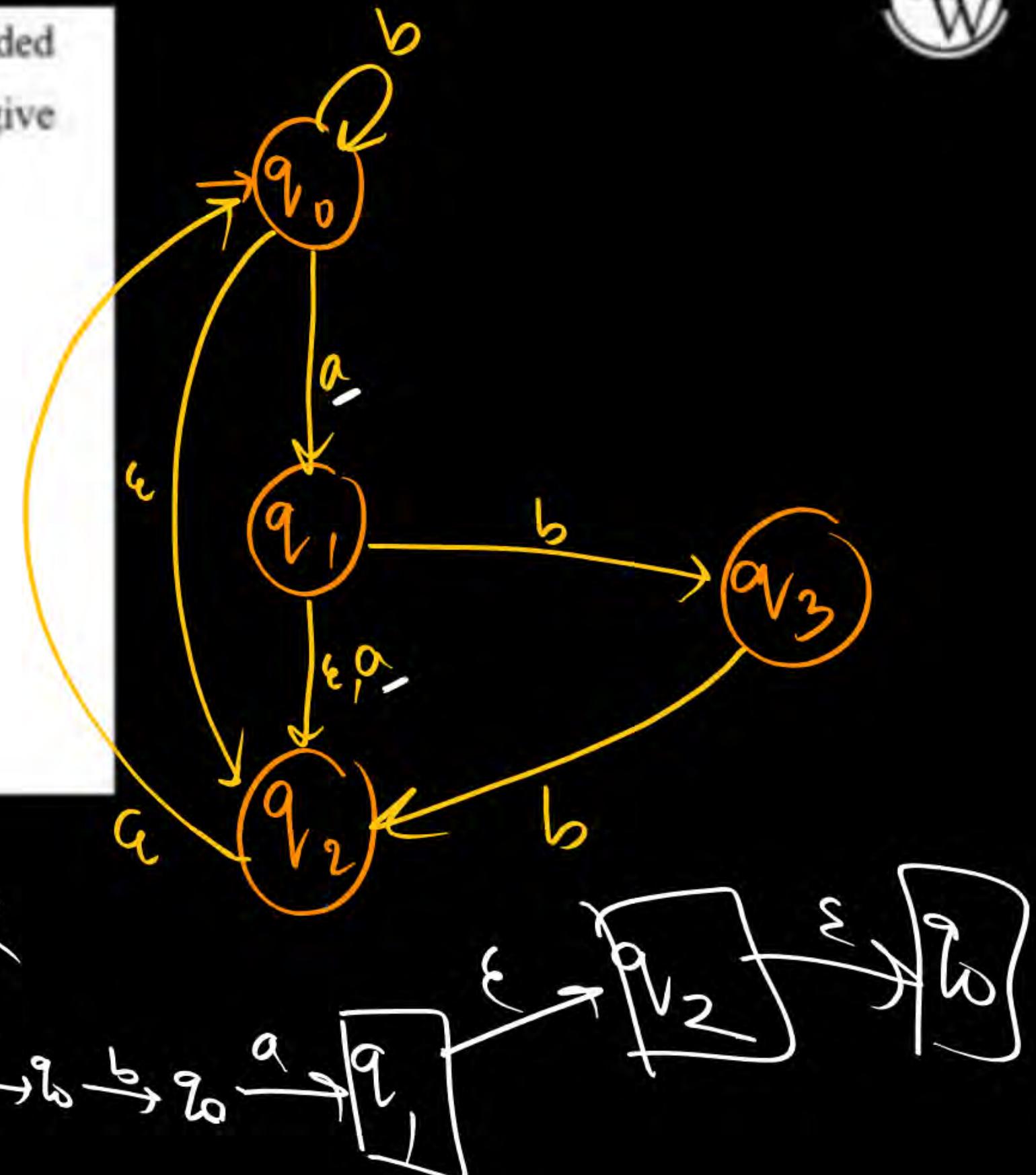
Let δ denote the transition function and $\hat{\delta}$ denote the extended transition function of the ϵ -NFA whose transition table is given below:

δ	ϵ	a	b
$\rightarrow q_0$	$\{q_2\}$	$\{q_1\}$	$\{q_0\}$
q_1	$\{q_2\}$	$\{q_2\}$	$\{q_3\}$
q_2	$\{q_0\}$	\emptyset	\emptyset
q_3	\emptyset	\emptyset	$\{q_2\}$

Then $\hat{\delta}(q_2, aba)$ is

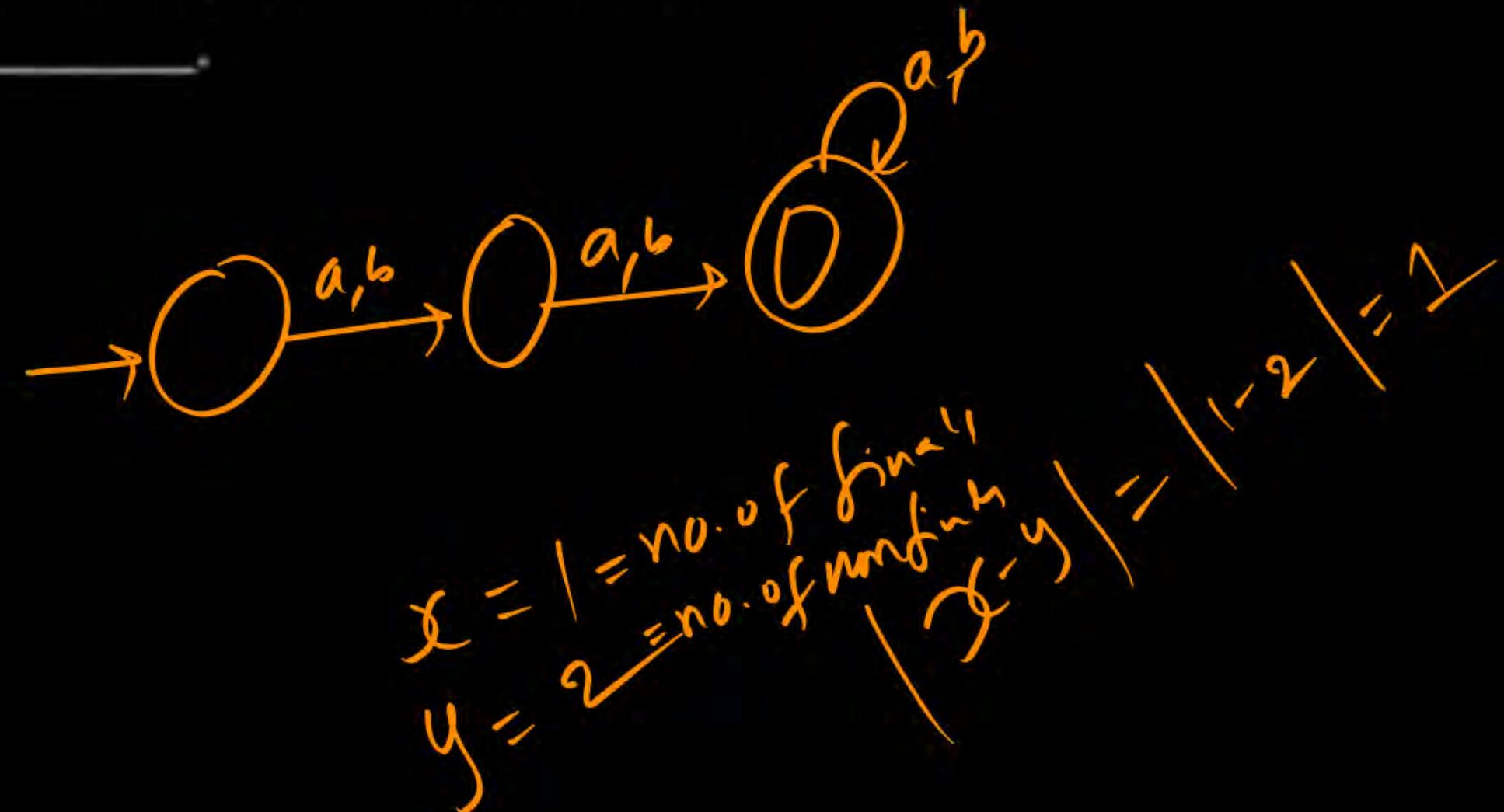
(GATE - 17 - SET2)

- (a) \emptyset
- (b) $\{q_0, q_1, q_3\}$
- (c) $\{q_0, q_1, q_2\}$
- (d) $\{q_0, q_2, q_3\}$



Let $L = (a+b)(a+b)(a+b)^*$ over alphabet $\Sigma = \{a, b\}$. [NAT]

If x is total number of final states and y is total number of non-final states, then $|x-y| = \underline{\hspace{2cm}}$.



If x and y are number of equivalence classes for L_1 and L_2 respectively then $L_1 + L_2 = \underline{\hspace{2cm}} 0$.

$$L_1 = aa(a+b)^*$$

$$L_2 = (a+b)^* aa$$

• GATE 1998

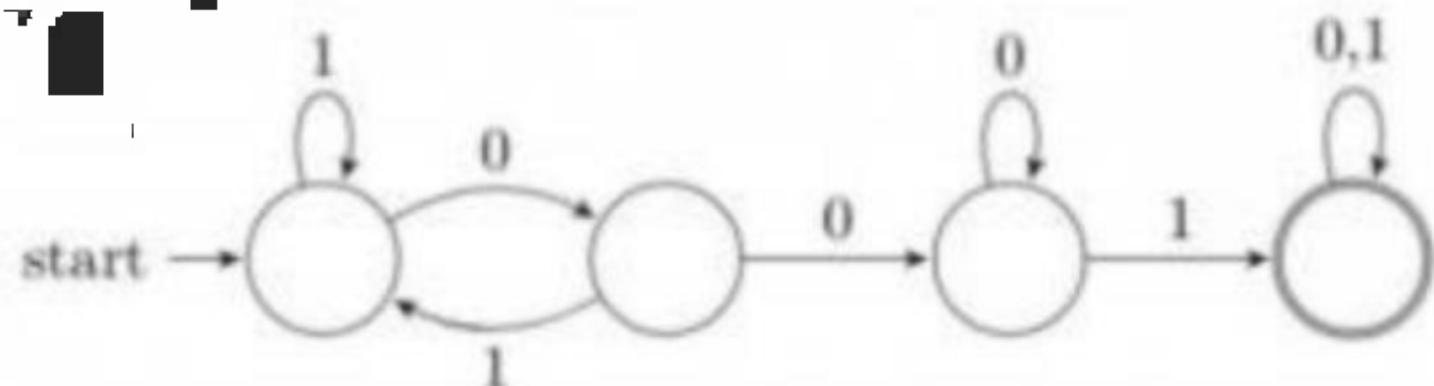
Which of the following set can be recognized by a Deterministic Finite state Automaton?

- A. The numbers $1, 2, 4, 8, \dots, 2^n, \dots$ written in binary
- B. The numbers $1, 2, 4, 8, \dots, 2^n, \dots$ written in unary
- C. The set of binary string in which the number of zeros is the same as the number of ones.
- D. The set $\{1, 101, 11011, 1110111, \dots\}$

Consider a DFA over $\Sigma = \{a, b\}$ accepting all strings which have number of a's divisible by 6 and number of b's divisible by 8. What is the minimum number of states that the DFA will have?

- A. 8
- B. 14
- C. 15
- D. 48

Consider the following deterministic finite state automaton M.



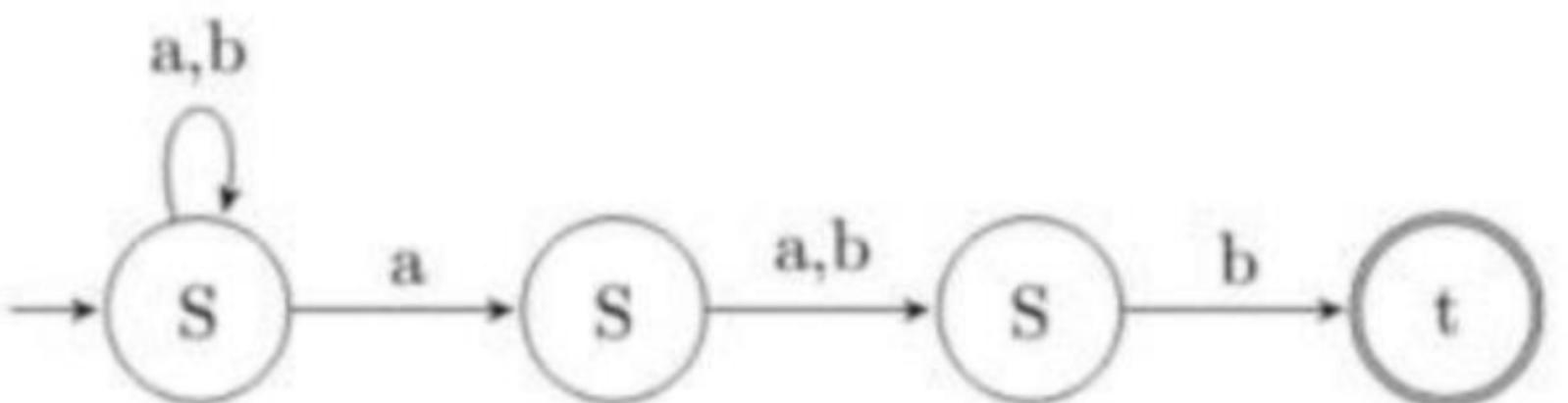
Let S denote the set of seven bit binary strings in which the first, the fourth, and the last bits are 1. The number of strings in S that are accepted by M is

- A. 1
- B. 5
- C. 7
- D. 8

Which one of the following regular expressions is NOT equivalent to the regular expression $(a+b+c)^*$?

- A. $(a^*+b^*+c^*)^*$
- B. $(a^*b^*c^*)^*$
- C. $((ab)^*+c^*)^*$
- D. $(a^*b^*+c^*)^*$

Which regular expression best describes the language accepted by the non-deterministic automaton below?



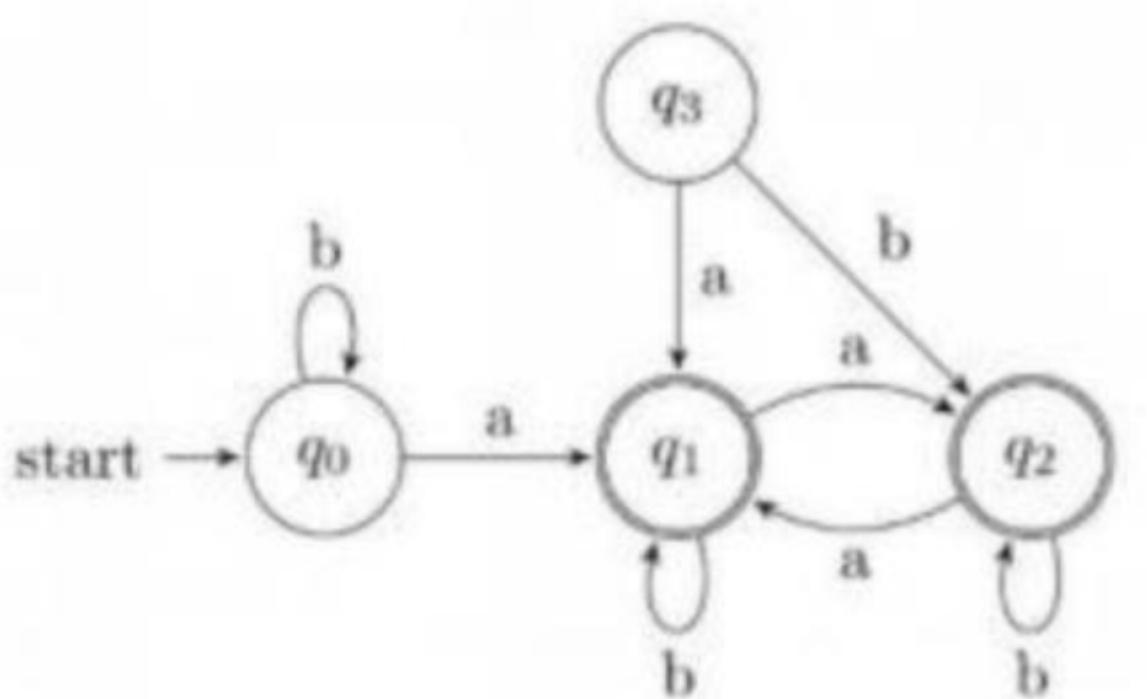
- A. $(a+b)^* a(a+b)b$
- B. $(abb)^*$
- C. $(a+b)^* a(a+b)^* b(a+b)^*$
- D. $(a+b)^*$

A minimum state deterministic finite automaton accepting the language

$L = \{w | w \in \{0,1\}^*, \text{ number of } 0\text{s and } 1\text{s in } w \text{ are divisible by } 3 \text{ and } 5, \text{ respectively } \}$ has

- A. 15 states
- B. 11 states
- C. 10 states
- D. 9 states

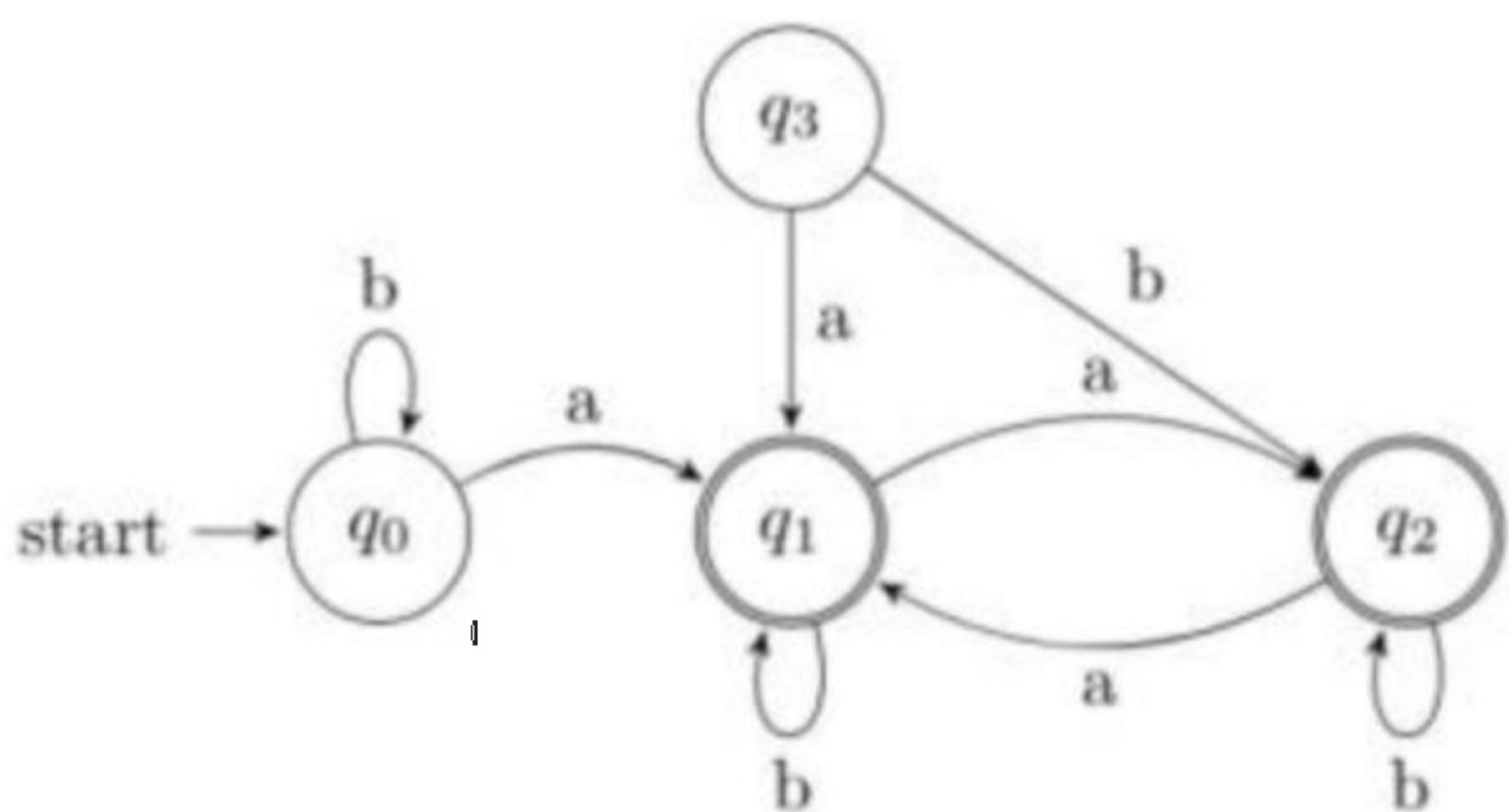
Consider the following Finite State Automaton:



The language accepted by this automaton is given by the regular expression

- A. $b^*ab^*ab^*ab^*$
- B. $(a+b)^*$
- C. $b^*a(a+b)^*$
- D. $b^*ab^*ab^*$

Consider the following Finite State Automaton:



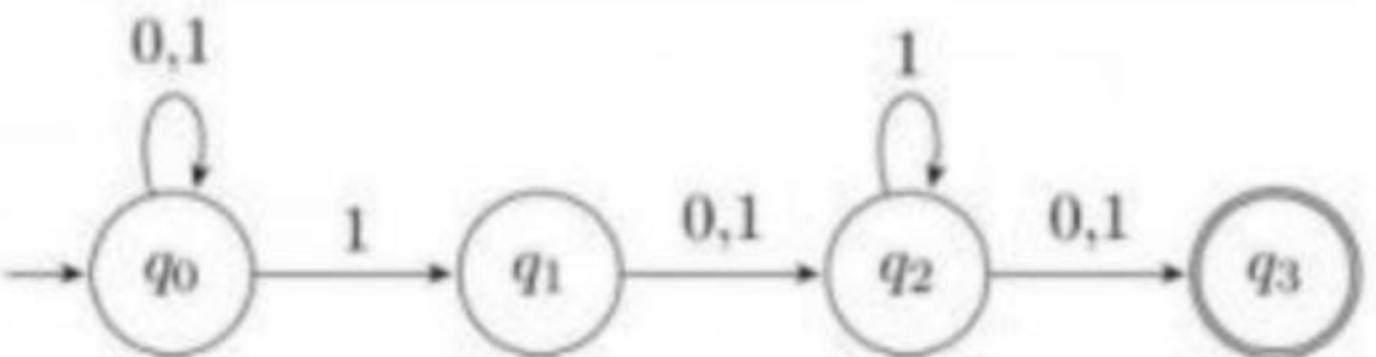
The minimum state automaton equivalent to the above FSA has the following number of states:

- A. 1
- B. 2
- C. 3
- D. 4

What is the complement of the language accepted by the NFA shown below?
Assume $\Sigma = \{a\}$ and ϵ is the empty string.



- A. \emptyset
- B. $\{\epsilon\}$
- C. a^*
- D. $\{a, \epsilon\}$



What is the set of reachable states for the input string 0011?

- A. {q0,q1,q2}
- B. {q0,q1}
- C. {q0,q1,q2,q3}
- D. {q3}

The number of states in the minimal deterministic finite automaton corresponding to the regular expression $(0+1)^*(10)$ is ____.

The number of states in the minimum sized DFA that accepts the language defined by the regular expression.

$(0+1)^*(0+1)(0+1)^*$ is _____.

Let Σ be the set of all bijections from $\{1, \dots, 5\}$ to $\{1, \dots, 5\}$, where id denotes the identity function, i.e. $\text{id}(j) = j$, $\forall j$. Let \circ denote composition on functions. For a string $x = x_1 x_2 \dots x_n \in \Sigma^n$, $n \geq 0$, let $\pi(x) = x_1 \circ x_2 \circ \dots \circ x_n$.

Consider the language $L = \{x \in \Sigma^* \mid \pi(x) = \text{id}\}$. The minimum number of states in any DFA accepting L is _____.

Bijection function? ^{Marks}
Identity function? ^{PC}

