

# Multi-Tier Priority Queues & 2-Tier Ladder Queue for Managing Pending Events

Julius D. Higiroy

Miami University

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# Overview

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# Introduction

- **Discrete Event Simulation (DES)** is used to simulate systems of interacting objects.
- The objects in the simulation are referred to as logical processes (LPs) and model objects in the real world.
- LPs interact by exchanging time stamped events and process events in priority order with event priorities determined by their time stamp.
- Events that have yet to be processed are called "**pending events**".
- Data structures for handling pending events follow a priority queue based implementation.

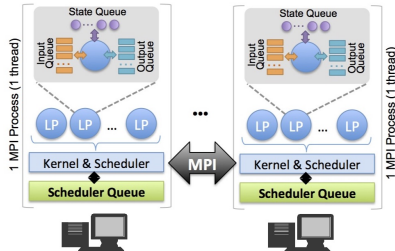
# Research Motivation

- Data structures for managing and prioritizing pending events play a critical role in ensuring efficient sequential and parallel simulations.
- The synchronization strategy in PDES can also impact the effectiveness of data structure because of the additional processing required during rollback recovery operations.
- A data structure that can effectively handle large number of concurrent events (**i.e. an average of one million events**).

# Research Proposal

- Our research proposes and explores multi-tier data structures for managing event list in sequential and optimistic parallel simulations.
- We aim to compare the effectiveness of our various data structures against the Ladder Queue pending event data structure. Ladder Queue has shown to outperform other pending event data structures in sequential DES with amortized  $O(1)$  time complexity.
- **Research Thesis:** Our multi-tier data structures (**2tLadderQ** and **3tHeap**) outperforms all other data structures in sequential and optimistically parallel simulations.

# Parallel Simulator Overview



- Assessment of the data structures will be conducted on MUSE.
- MUSE performs sequential and optimistically parallel simulations.
- MUSE uses Message Passing Interface (MPI) library for parallel processing.
- The kernel handles LP registration, event processing, state saving, synchronization and garbage collection.

# Parallel Simulator Overview

A scheduler queue is required to implement four key operations to manage pending events.

- ① **Enqueue one or more future events.**
- ② **Peek next event in priority order.**
- ③ **Dequeue events with the same time stamp for next LP.**
- ④ **Cancel pending events after a given time.**

# Scheduler Queues

- MUSE contains 6 scheduling queues for managing pending events.
- The queues are classified into two categories: single-tier and multi-tier queues.
- Single-tier queues use only a single data structure to implement the 4 key operations.
- Multi-tier queues organizes events into tiers.
- Each tier is implemented using different data structures.



# Binary Heap (**heap**)



## Time Complexity

**Enqueue:**  $\log(e \cdot l)$

**Dequeue:**  $\log(e \cdot l)$

**Cancel:**  $z \cdot \log(e \cdot l)$

**Legend:**

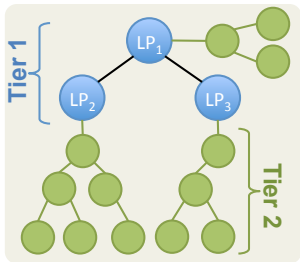
$l$ : #LPs

$e$ : #events / LP

$z$ : #canceled events

- It is a single-tier data structure that it is implemented as an array object.
- A `std::vector` is used as the backing container and C++11 algorithms (`std::push_heap`, `std::pop_heap`) are used to maintain the heap.
- The heap is prioritized based on time stamp with the lowest time stamp at the root of the heap.

## 2-tier Heap (2tHeap)



### Time Complexity

**Enqueue:**  $\log(e) + \log(l)$

**Dequeue:**  $\log(e) + \log(l)$

**Cancel:**  $z \cdot \log(e) + \log(l)$

**Legend:**

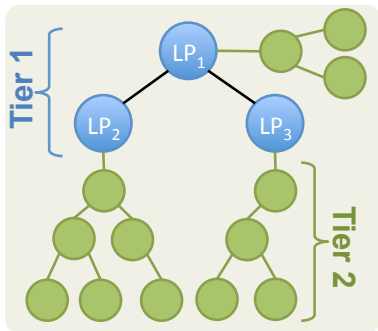
$l$ : #LPs

$e$ : #events / LP

$z$ : #canceled events

- 2tHeap was designed to reduced the time complexity of cancel operations by subdividing events into two distinct tiers.
- The first tier has containers for each local LP on an MPI-process.
- Each of the the tier-1 containers has a heap of events to be processed by a given LP.
- A `std::vector` is used as the backing container for both tiers and standard algorithms are used to maintain the min-heap property for both tiers after each operation.

# 2-tier Fibonacci Heap (fibHeap)



## Time Complexity

**Enqueue:**  $\log(e) + 1^*$

**Dequeue:**  $\log(e) + 1^*$

**Cancel:**  $z \cdot \log(e) + 1^*$

**Legend:**

$l$ : #LPs

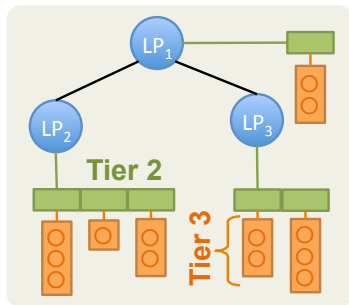
$e$ : #events / LP

$z$ : #canceled events

$1^*$ : amortized constant

- The fibHeap is an extension of the 2tHeap data structure. It uses a Fibonacci heap for scheduling LPs.
- The second tier is a binary heap data structure.

# 3-tier Heap (3tHeap)



## Time Complexity

**Enqueue:**  $\log(\frac{e}{c}) + \log(l)$

**Dequeue:**  $\log(l)$

**Cancel:**  $e + \log(l)$

**Legend:**

$l$ : #LPs

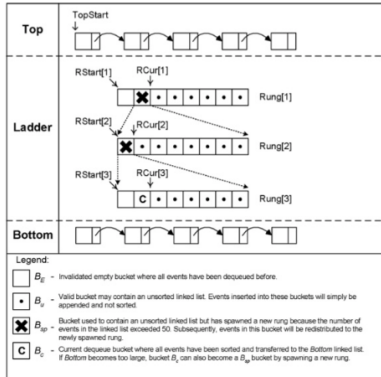
$e$ : #events / LP

$c$ : #concurrent events

$z$ : #canceled events

- The 3tHeap builds upon 2tHeap by further subdividing the second tier into two tiers.
- The binary heap implementation for the first tier that manages LPs for scheduling has been retained from 2tHeap.
- Assuming each LP has  $c$  concurrent events on an average, there are  $\frac{e}{c}$  tier-2 entries with each one having  $c$  pending events.

# Ladder Queue (ladderQ)



## Time Complexity

**Enqueue:**  $1^*$

**Dequeue:**  $1^*$

**Cancel:**  $e \cdot l$

**Legend:**

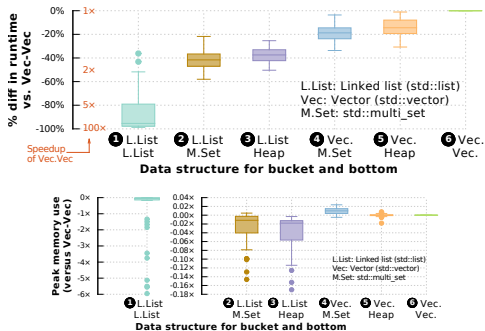
$l$ : #LPs

$e$ : #events / LP

$1^*$ : amortized constant

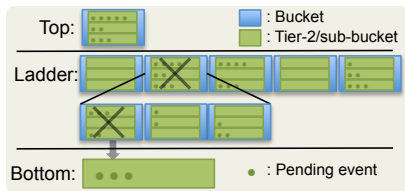
- Ladder Queue is a priority queue implementation proposed by Tang et al. with amortized constant time complexity.
- There are two key ideas underlying the Ladder Queue, namely: minimize the number of events to be sorted and delay sorting of events as much as possible.

# Ladder Queue (ladderQ - Fine Tuned)



- Comparison of execution time and peak memory using 6 different ladderQ configurations.
- L.List-L.List configuration was slowest and performed 85x slower than the Vec-Vec configuration.
- The increased performance of Vec-Vec comes at about a 6x increase in peak memory footprint when compared to L.List-L.List.

# 2-tier Ladder Queue (2tLadderQ)



## Time Complexity

**Enqueue:**  $1^*$

**Dequeue:**  $1^*$

**Cancel:**  $e \cdot l \div t_2 k$

**Legend:**

$l$ : #LPs

$e$ : #events / LP

$1^*$ : amortized constant

$t_2 k$ : parameter

- 2-tier Ladder Queue is the proposed alternative to Ladder Queue because the cost of event cancellation during rollbacks is reduced.
- 2tLadderQ retains the amortized constant time complexity of ladderQ with performance gains during event cancellation.

**Table:** Comparison of algorithmic time complexities of different data structures

Legend –  $l$ : #LPs,  $e$ : #events / LP,  $c$ : #concurrent events,  
 $z$ : # canceled events,  $t_2k$ : parameter,  $1^*$ : amortized constant

Name	Enqueue	Dequeue	Cancel
<b>heap</b>	$\log(e \cdot l)$	$\log(e \cdot l)$	$z \cdot \log(e \cdot l)$
<b>2tHeap</b>	$\log(e) + \log(l)$	$\log(e) + \log(l)$	$z \cdot \log(e) + \log(l)$
<b>fibHeap</b>	$\log(e) + 1^*$	$\log(e) + 1^*$	$z \cdot \log(e) + 1^*$
<b>3tHeap</b>	$\log(\frac{e}{c}) + \log(l)$	$\log(l)$	$e + \log(l)$
<b>ladderQ</b>	$1^*$	$1^*$	$e \cdot l$
<b>2tLadderQ</b>	$1^*$	$1^*$	$e \cdot l \div t_2k$

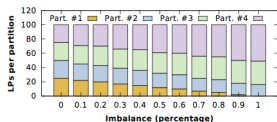


# Simulation Model

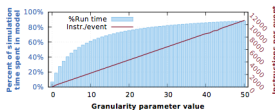
Table: Parameters in PHOLD benchmark

Parameter	Description
<b>rows</b>	Total number of rows in model.
<b>cols</b>	Total number of columns in model. $\#LPs = \mathbf{rows} \times \mathbf{cols}$
<b>eventsPerLP</b>	Initial number of events per LP.
<b>delay</b> or $\lambda$	Value used with distribution – Lambda ( $\lambda$ ) value for exponential distribution <i>i.e.</i> , $P(x \lambda) = \lambda e^{-\lambda x}$ .
<b>%selfEvents</b>	Fraction of events LPs send to self
<b>granularity</b>	Additional compute load per event.
<b>imbalance</b>	Fractional imbalance in partition to have more LPs on a MPI-process.
<b>simEndTime</b>	GVT when simulation logically ends.

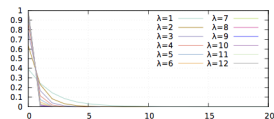
# Simulation Model - Key Parameters



(a) impact of imbalance



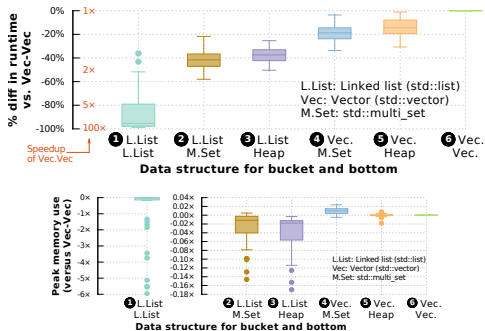
(b) impact of granularity



(c) impact of  $\lambda$  (delay)

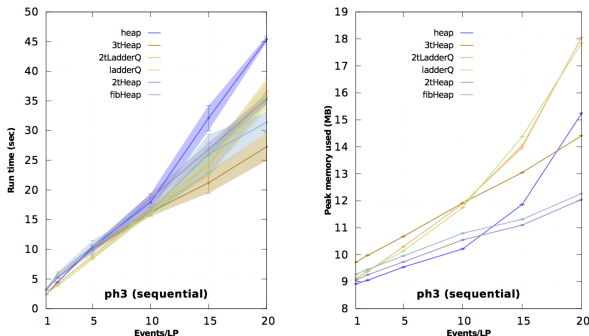
- Imbalance parameter influences the partition.
- Granularity impacts the processing time of events.
- $\lambda$  impacts the distribution of the time stamp values.

# Ladder Queue (ladderQ - Fine Tuned)



- Comparison of execution time and peak memory using 6 different ladderQ configurations.
- L.List-L.List configuration was slowest and performed 85x slower than the Vec-Vec configuration.
- The increased performance of Vec-Vec comes at about a 6x increase in peak memory footprint when compared to L.List-L.List.

# Preliminary Sequential Simulation Results

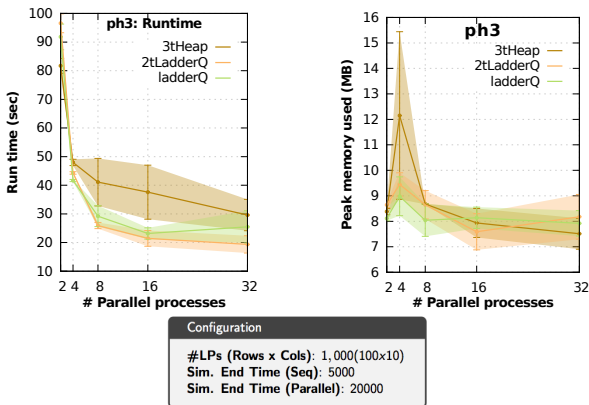


## Configuration

#LPs (Rows x Cols): 1,000(100x10)  
Sim. End Time (Seq): 5000  
Sim. End Time (Parallel): 20000

- Sequential simulation run time and peak memory usage statistics is shown with **%Self-events = 25%** and  $\lambda = 1$  at varied values for **eventsPerLP**.

# Preliminary Parallel Simulation Results



- Statistics from parallel simulation with **%Self-events** = 25%,  $\lambda = 10$  and **eventsPerLP** = 10.

# Experiment Design

- Assessments of the effectiveness of the six scheduler queues will be performed by running different configurations of the PHOLD benchmark in sequential and optimistically parallel simulations.
- Due to a large number of PHOLD parameters and combinations of their values. We will identify the most influential PHOLD parameters that impact performance of the scheduler queues using **Generalized Sensitivity Analysis**.
- The data to be collected and assessed consists of the following:
  - ① **simulation run time.**
  - ② **peak memory usage.**
  - ③ **# of rollbacks.**
  - ④ **characteristics of key queue operations.**
  - ⑤ **# of network messages exchanged.**

# Related Work

- Many investigations have explored the effectiveness of a wide variety of data structures for managing the pending event set.
- Tang et al., proposed a pending event set data structure named Ladder Queue as a priority queue based implementation of an event list that results in amortized  $O(1)$  performance. The authors, presented ladder queue as an improvement on existing priority queue based event lists data structures such as calendar queues.
- Franceschini et al., compared several priority-queue based pending event data structures to evaluate their performance in the context of sequential DEVS simulations. They found that Ladder Queue outperformed every other priority queue based pending event data structure such as Sorted List, Minimal List, Binary Heap, Splay Tree, and Calendar Queue.

## Related Work

- Dickman et al., compared event list data structures that consisted of Splay Tree, STL Multiset and Ladder Queue. However, the focus of their paper was in developing a framework for handling pending event set data structure in shared memory PDES. A central component of their study was the identification of an appropriate data structure and design for the shared pending event set.
- Gupta et al., extended their implementation of Ladder Queue for shared memory Time Warp based simulation environment, so that it supports lock-free access to events in the shared pending event set. The modification involved the use of an unsorted lock-free queue in the underlying Ladder Queue structure.
- Marotta et al., have contributed to the study of pending event set data structures in threaded PDES through the design of the Non-Blocking Priority Queue (NBPQ) data structure. A pending event set data structure that is closely related to Calendar Queues with constant time performance.



# Plan of Action & Milestones

- ① **Sequential & parallel simulation assessment:** Data will be collected to assess the effectiveness of the different data structures in sequential and parallel simulations. Data collection and analysis for sequential simulations will be completed by 14 March 2017. Data collection and analysis for parallel simulations will be completed by 22 March 2017.
- ② **Implement 2 additional simulation models:** We will extend the experimental analysis to include 2 additional models in order to evaluate performance of the data structures across different simulation models. The 2 simulation models will be implemented by 30 March 2017.

# Plan of Action & Milestones

- ③ **Assessment using additional simulation models:** The assessment of data structure performance using the models in sequential and optimistic parallel simulations will be completed by 28 April 2017.
- ④ **Record experimental results and analysis:** The research thesis writing will be completed by 19 May 2017 in preparation for the thesis defense.

# References



Dickman et al., (2013) Event Pool Structures for PDES on Many-core Beowulf Clusters. *In Proceedings of the 1st ACM SIGSIM Conference on Principles of Advanced Discrete Simulation* ACM, New York, NY, USA, 103-114.



Franceschini et al., (2015) A Comparative Study of Pending Event Set Implementations for PDEVS Simulation. *In Proceedings of the Symposium on Theory of Modeling and Simulation* Society for Computer Simulation International San Diego, CA, USA, 77-84.



Gupta et al., (2014) Lock-free Pending Event Set Management in Time Warp. *In Proceedings of the 2nd ACM SIGSIM Conference on Principles of Advanced Discrete Simulation* ACM, New York, NY, USA, 15-26.



Jafer et al., (2013) Synchronization methods in parallel and distributed discrete-event simulation *Simulation Modeling Practice and Theory* 30(2013), 54-73.



Marotta et al., (2016) A Non-Blocking Priority Queue for the Pending Event Set. *In Proceedings of the 9th EAI International Conference on Simulation Tools and Techniques ICST*, Brussels, Belgium, 46-55.



Tang et al., (2005) Ladder Queue: An  $O(1)$  Priority Queue Structure for Large-scale Discrete Event Simulation. *ACM Trans. Model. Comput. Simul.* 15, 3(July 2005), 175-204.

# The End

# Intro to Discrete Event Simulation (DES)

**Discrete Event Simulation (DES)** is a framework for simulating the behavior of real or imagined systems.

## Simulation properties

- an **entity** that is an object of interest in the simulated system.
- a **state** that is represented by a set of variables that describe the system at a particular point in time.
- an **event** that is an instantaneous occurrence that can change the state of the simulated system.
- a virtual simulation **clock** that indicates the time of the last event occurrence that has been simulated.
- an **evolution** of the modeled system that is given by a chronologically ordered sequence of events.

$s_0, (e_0, t_0), s_1, (e_1, t_1), s_2, (e_2, t_2), \dots, s_n, (e_n, t_n)$

# Intro to Discrete Event Simulation (DES)

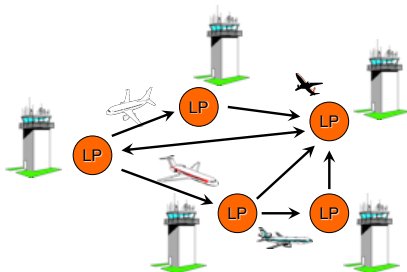
## Simulation application

- The model of the real or imagined system.
- The collection of state variables.
- The collection of event handlers.

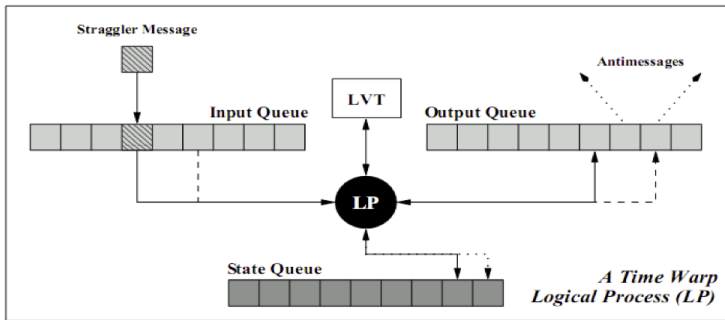
## Simulator

- The environment that manages and executes the simulation.
- Maintains an event list for handling events.
- Manages forward progress of simulation time.

# Implementation of DES

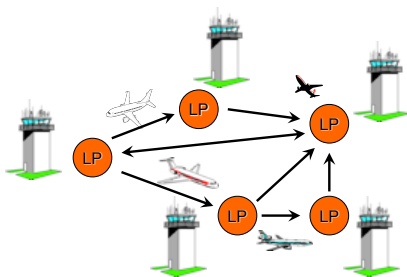


- DES is implemented as a set of logical processes (LPs).
- LPs map to physical processes in the simulated system.
- Each LP has the following components:
  - state queue:** maintains saved states of the LP.
  - input queue:** maintains events received from other LPs.
  - output queue:** maintains events sent to other LPs.
  - local clock:** time of last event processed.



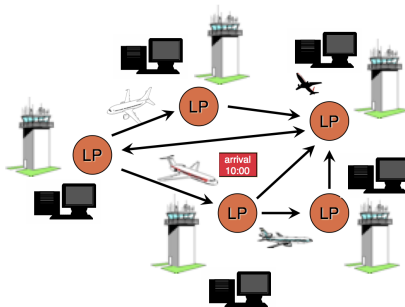


# Implementation of DES



- LPs interact with each other by exchanging and processing time stamped events.
- Events that are yet to be processed are called **pending events**.
- LPs process these events in time stamp order order and generate new events that are transmitted to other LPs.

# Parallelism in DES



- Parallel computing simulates DES models on parallel computers.
- In parallel DES (PDES), LPs exchange time stamped events using message passing.
- Processing events concurrently on different processors is hard.
- **Synchronization problem:** since the simulation runs in parallel, all LPs have their own internal clock, so each LP may be at different points in time relative to each other.

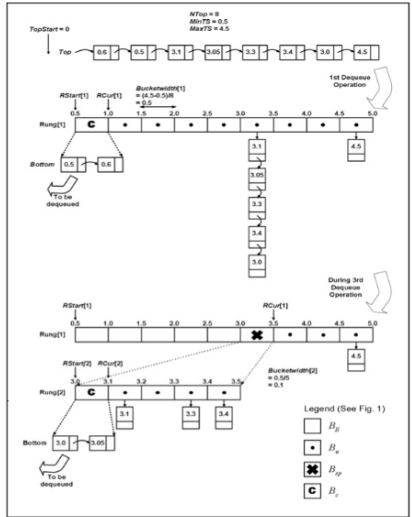
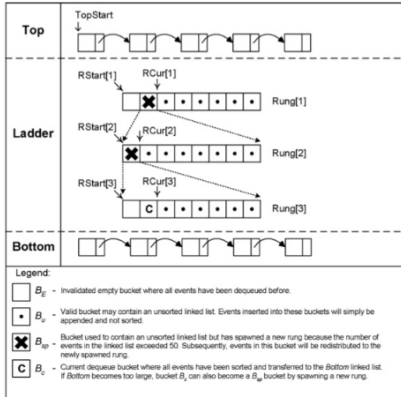
## Conservative approach to PDES

- Causality errors are not allowed to occur.
- Strategy required to determine when it is safe to process an event.

## Optimistic approach to PDES

- Allows causality errors to occur.
- When a causality error is detected, rollback mechanism is invoked.

## Ladder Queue (**ladderQ**)



# 3-tier Heap (3tHeap) - Enqueue Operation

```
void
ThreeTierHeapEventQueue::enqueueEvent(xxxx::Agent* agent, xxxx::Event* event) {
    ASSERT(agent != NULL);
    ASSERT(event != NULL);
    ASSERT( agent->tier2 != NULL );
    ASSERT(getIndex(agent) < agentList.size());
    // A convenience reference to tier2 list of buckets
    Tier2List& tier2 = *agent->tier2;
    // Use binary search O(log n) to find match or insert position
    agentBktCount += tier2.size();
    Tier2List::iterator iter =
        std::lower_bound(tier2.begin(), tier2.end(), event, lessThanPtr);
    // There are 3 cases: 1. we found matching bucket, 2: iterator
    // to bucket with higher rcvTime, or 3: tier2.end().
    if (iter == tier2.end()) {
        tier2.emplace_back(makeTier2Entry(event)); // add new entry to end.
    } else if ((*iter)->getReceiveTime() == event->getReceiveTime()) {
        // We found an existing bucket. Append this event to this
        // existing bucket.
        (*iter)->updateContainer(event);
    } else {
        // If there is no bucket with a matching receive time in Tier2
        // vector, then insert an instance of HOETier2Entry (aka
        // bucket) into the vector at the appropriate position.
        ASSERT((*iter)->getReceiveTime() > event->getReceiveTime());
        tier2.emplace(iter, makeTier2Entry(event));
    }
    // ASSERT(std::is_sorted(tier2.begin(), tier2.end()));
}

void
ThreeTierHeapEventQueue::enqueue(xxxx::Agent* agent,
                                  xxxx::EventContainer& events) {
    ASSERT(agent != NULL);
    // Note: events container may be empty!
    ASSERT(getIndex(agent) < agentList.size());
    // Add all events to tier2 entries appropriately.
    for (xxx::Event* event : events) {
        // Enqueue event but don't waste time fixing-up heap yet for
        // this agent. We will do it at the end after all events are
        // added. However, we don't increase reference counts in this
        // API.
        enqueueEvent(agent, event);
    }
    // Clear out all the events in the incoming container
    events.clear();
    // Update the location of this agent on the heap as needed.
    updateHeap(agent);
}
```



# 2-tier Ladder Queue (2tLadderQ) Cancel Operation

```
// Method to cancel all events in the 2-tier heap.
int
xxx::TwoTierLadderQueue::eraseAfter(xxxx::Agent* dest,
    const xxx::AgentID sender,
    const xxx::Time sendTime) {
    UNUSED_PARAM(dest);
    return remove_after(sender, sendTime); ★

int
xxx::TwoTierLadderQueue::remove_after(xxxx::AgentID sender,
    const Time sendTime) {
    // Check and cancel entries in top rung.
    int numRemoved = top.remove_after(sender, sendTime
        LQ2T_STATS(COMMA ceScanTop)); ★
    LQ2T_STATS(ceTop += numRemoved);
    // Cancel out events in each rung of the ladder.
    for (size_t rung = 0; (rung < nRung); rung++) {
        const int rungEvtRemoved =
            ladder[rung].remove_after(sender, sendTime
                LQ2T_STATS(COMMA ceScanLadder));
        ladderEventCount -= rungEvtRemoved;
        numRemoved += rungEvtRemoved;
        LQ2T_STATS(ceLadder += rungEvtRemoved);
    }
    // Clear out the rungs in ladder that are now empty after event
    // cancellations.
    while (nRung > 0 && ladder[nRung - 1].empty()) {
        LQ2T_STATS(ladder[nRung - 1].updateStats(avgBktCnt));
        nRung--; // Logically remove rung from ladder
    }
    // Save original size of bottom to track stats.
    LQ2T_STATS(const size_t botSize = bottom.size());
    // Cancel events from bottom.
    const int botRemoved = bottom.remove_after(sender, sendTime); ★
    if (botRemoved > -1) {
        numRemoved += botRemoved;
        // Update statistics counters
        LQ2T_STATS(ceBot += botRemoved);
        LQ2T_STATS(ceScanBot += botSize);
        LQ2T_STATS((botRemoved == 0) ? (ceNoCanScanBot += botSize) : 0);
    }
    return numRemoved;
}
```