

using f from previous lecture,
→ with 2-level implementation
if delay in each gate is $2ns$
total delay = $4ns$

→ after factoring
total delay = $6ns$
(critical path) longest path

factoring may reduce the cost of
an implementation, but may cause longer
delay

Functional Decomposition

$$f = \bar{x}_1 x_2 x_3 + x_1 \bar{x}_2 x_3 + x_1 x_2 x_4 + \bar{x}_1 \bar{x}_2 x_4$$

$$= (\bar{x}_1 x_2 + x_1 \bar{x}_2) x_3 + (x_1 x_2 + \bar{x}_1 \bar{x}_2) x_4$$

$$\downarrow \Rightarrow g = \bar{x}_1 x_2 + x_1 \bar{x}_2$$

$$= g x_3 + \bar{g} x_4$$

$$\begin{aligned} g &= \bar{x}_1 x_2 + x_1 \bar{x}_2 \\ \bar{g} &= \overline{\bar{x}_1 x_2 + x_1 \bar{x}_2} \\ &= (\bar{x}_1 + \bar{x}_2)(\bar{x}_1 + x_2) \\ &= \bar{x}_1 \bar{x}_1 + \bar{x}_1 x_2 + \bar{x}_1 \bar{x}_2 + \bar{x}_1 x_2 \\ &= \bar{x}_1 x_2 + \bar{x}_1 \bar{x}_2 \end{aligned}$$

$$f = \bar{x}_1 x_2 x_3 + x_1 \bar{x}_2 x_3 + x_1 x_2 x_4 + \bar{x}_1 \bar{x}_2 x_4$$

calculate cost (Need the inputs):

$$2 \text{ inputs} = 2$$

$$4 \text{ 3-input AND} = 12$$

$$1 \text{ 4-input OR} = 4$$

$$\begin{array}{r} \text{inputs} = 18 \\ \hline \end{array}$$

$$\begin{array}{r} \text{gates} = 7 \\ \hline \text{total cost} = 25 \end{array}$$

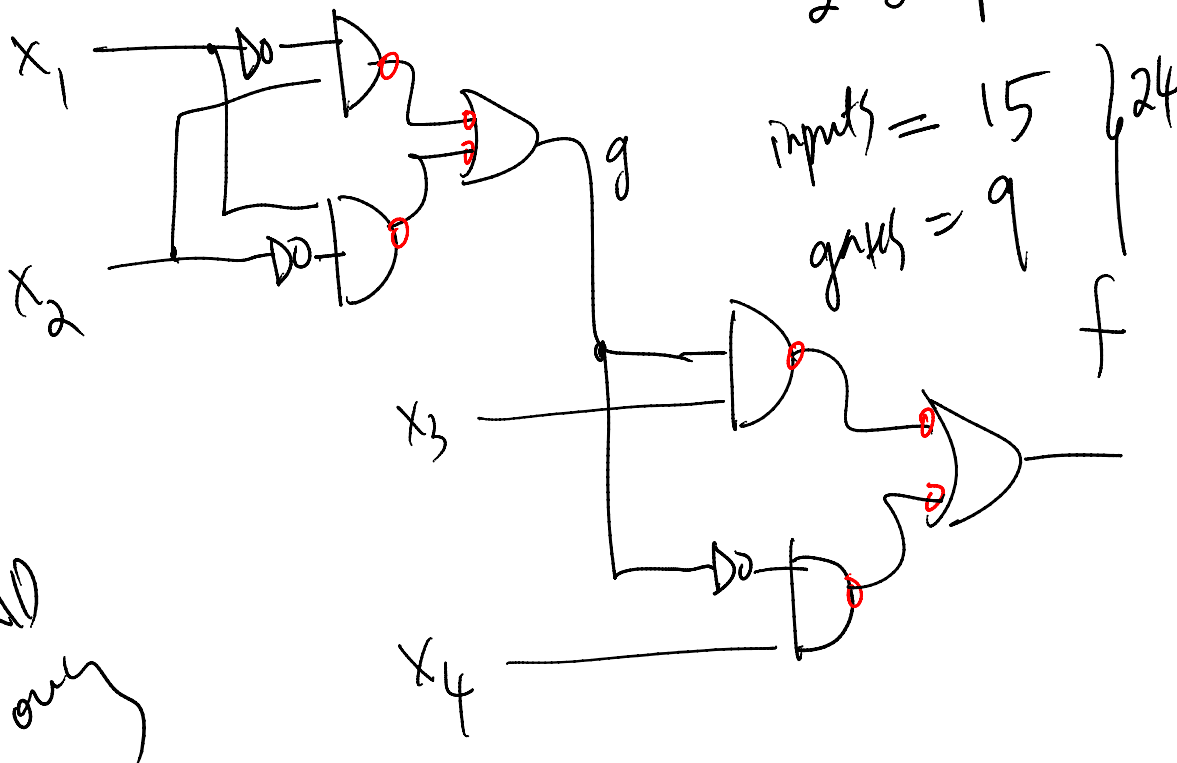
$$f = g x_3 + \bar{g} x_4$$

$$g = \bar{x}_1 x_2 + x_1 \bar{x}_2$$

3 inverters = 3

4 2-input AND = 8

2 2-input OR = 4



NAND only