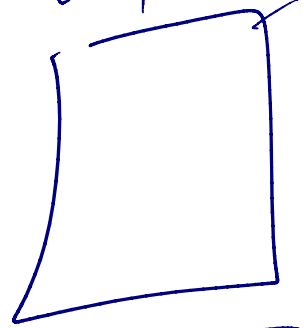


Decimal

$$\# = d_{n-1} \dots d_2 d_1 d_0$$

computer



$$\# = 123$$

$$\# = 1 \times 10^2 + 2 \times 10^1 + 3 \times 10^0$$



Base 10

0, ..., 9



$$\text{binary } \# = b_{n-1} \dots b_1 b_0$$

$\uparrow \quad \quad \quad \uparrow \quad \quad \uparrow$
 $2^{n-1} \quad \quad \quad 2^1 \quad \quad 2^0$

binary (unsigned) = 01101 the decimal equivalent

4	3	2	1	0
2^4	2^3	2^2	2^1	2^0
16	8	4	2	1

$\underbrace{8 + 4 + 1}_{= 13}$

$123_{10} \rightarrow \text{binary (base 2)}$

$128 \quad 64 \quad 32 \quad 16 \quad 8 \quad 4 \quad 2 \quad 1$

11_{10} $0 \quad 1 \quad 1 \quad 1 \quad 1 \quad 0 \quad 1 \quad 1$

$$\begin{array}{r}
 123 \\
 - 64 \\
 \hline
 59 \\
 32 \\
 \hline
 27 \\
 16 \\
 \hline
 11 \\
 8 \\
 \hline
 3
 \end{array}$$

$$\begin{array}{r}
 2 \overline{) 123} \\
 2 \overline{) 61} \\
 2 \overline{) 30} \\
 2 \overline{) 15} \\
 2 \overline{) 7} \\
 2 \overline{) 3} \\
 2 \overline{) 1} \\
 \hline
 0 \quad 1 \quad 1 \quad 0 \quad 1 \quad 1 \quad 1
 \end{array}$$

LSB

$(11111011)_2$

MSB

$173_{10} \rightarrow \text{binary}$

256	128	64	32	16	8	4	2	1
0	1	0	1	0	1	1	0	1

$$\begin{array}{r} 173 \\ - 128 \\ \hline 45 \\ 32 \\ \hline 13 \\ 8 \\ \hline 5 \end{array}$$

$(010101101)_2$

$2 \overline{) 173}$

010101101

32-17

hex (group 4 binary values)
for LSB \rightarrow msb

$(010101101)_2$

$(AD)_{16}$

$$\begin{array}{c} \downarrow \\ 16 \\ \hline 15 \end{array}$$

0 \rightarrow 15

0 \rightarrow 9, A, B, C, D, E, F

$$\begin{array}{c} 010101101 \\ \hline \quad \quad \quad A \quad \quad d \end{array}$$

$(AD)_{16}$ $(10101101)_2$ 04th (group 3 bits, from LSB \rightarrow MSB)

↓

0 \rightarrow 7
$$\begin{array}{cccc} 1 & 0 & 1 & 0 & 1 & 1 & 0 & 1 \\ \hline & & & & ? & & & \\ & & 2 & 5 & 5 & & & \end{array}$$

$$(AD)_{16} \stackrel{?}{=} (10101101)_2 \stackrel{?}{=} (255)_8$$

$$\begin{array}{ccc} 8^2 & 8^1 & 8^0 \\ \swarrow & | & \searrow \end{array}$$
Value of $(173)_8$ in decimal?

$$\begin{aligned} (173)_8 &= 1 \times 8^2 + 7 \times 8^1 + 3 \times 8^0 \\ &= 64 + 56 + 3 = (123)_{10} \end{aligned}$$

Value of $(7B)_{16}$ in decimal?

$$\begin{aligned}(7B)_{16} &= 7 \times 16^1 + B \times 16^0 \\ &= 112 + 11 \\ &= (123)_{10}\end{aligned}$$

Determine decimal value of

(a) $(011101110)_2 = (478)_{10}$

$$\begin{array}{r} 256 \\ 128 \\ 64 \\ 32 \\ 16 \\ 8 \\ 4 \\ 2 \\ \hline 80 \quad 14 \end{array}$$

$$\begin{array}{r} 256 \\ 128 \\ \hline 384 \\ 96 \\ \hline 480 \\ \hline \end{array}$$

decimal addition

$$\begin{array}{r}
 7 \\
 + 8 \\
 \hline
 15 \\
 \hline
 \hline
 \end{array}$$

Binary

$$\begin{array}{r}
 0 \\
 + 0 \\
 \hline
 0 \\
 \hline
 \hline
 \end{array}$$

$$\begin{array}{r}
 0 \\
 + 1 \\
 \hline
 1 \\
 \hline
 \hline
 \end{array}$$

$$\begin{array}{r}
 1 \\
 + 0 \\
 \hline
 1 \\
 \hline
 \hline
 \end{array}$$

$$\begin{array}{r}
 1 \\
 + 1 \\
 \hline
 10 \\
 \hline
 \hline
 \end{array}$$

2^1 2^0

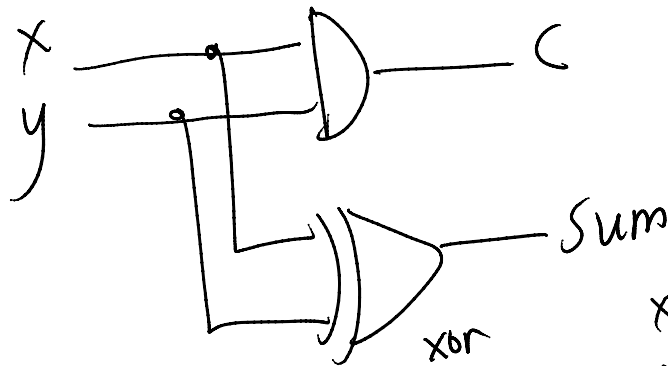
$$(10)_2 = 2_{10}$$

X	y	C	Sum
0	0	0	0
0	1	0	1
1	0	0	1
1	1	1	0

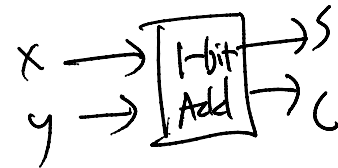
$$C = xy$$

$$\text{Sum} = \bar{x}y + x\bar{y}$$

$$= x \oplus y$$



1-bit
adder ✓



$$A = a_3 a_2 a_1 a_0$$

$$B = b_3 b_2 b_1 b_0$$

$$A + B$$