

Quantum Information and Computation

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All course materials downloadable from <http://www.qi.damtp.cam.ac.uk/node/272>.

Some foci of the course: why do we need *quantum* computation and information? What is information? Classical information is presented by bits – boolean variable with values 0,1, and bit strings for more alternative messages. Also, what is computation? In the classical sense it is updating bit strings by prescribed sequence of steps called "program". It uses basic elementary Boolean operations/gates, e.g. AND, OR, NOT, SWAP acting on 1 or 2 bits.

Now if information consists of bits, then what is a bit? It is not abstract maths but two distinguishable state of a physical system.

Computation (info processing) must correspond to a physical evolution of the system representing the bits. So possibilities if info storage/communicating/processing must all rest on laws of physics and cannot be determined by abstract thought/mathematics alone.

Some benefits/issues of quantum vs classical physics:

(a) Computing power (computational complexity). A quantum computer cannot compute anything that's not computable *in principle* on a classical computer. However, computational hardness, or amount of resources needed, matters. If it's too high then the problem is uncomputable *in practice*.

Example. Task: given an integer N ($n = O(\log N)$ digits), we have an input size n . We wish to find a polynomial time algorithm, which runs in number of steps bounded by polynomials in n . Such an algorithm is feasible in practice. Algorithms needing exponential time are not feasible in practice, for example, trial division, which requires $O(\sqrt{N}) = O(2^{n/2})$ steps. The best known classical factoring algorithm runs in $2^{O(n^{1/3}(\log n)^{1/3})}$ which is not feasible. However, there is a quantum algorithm (Shor's Algorithm) that runs in polynomial time, and is in fact only $O(n^3)$.

(b) Communication/security benefits:

- Provably secure communication possible with quantum effects, which is impossible classically;
- Novel kinds of communicator, e.g. quantum teleportation, etc.

(c) Technological issues: Moore's law: miniaturisation of classical computing components (since 1965, factor of 4 every 3.5 years). Now at atomic scale where classical physics fails!

However, building a quantum computer seems to be very difficult now, and is beyond human's capability at this point. In 2018 (this year) we expect to have a working quantum computer of size 50 qubits.