

Problem J

Sum Mod Pair of A

Jono likes arrays. Jono is quite interested in one particular type of operation on an array that he calls Sum Mod Pair of A, or SMPA for short.

Given an array of integers A (indexed from 0 to $N - 1$) and an integer M of a power of 2, the operation $\text{SMPA}(A, M)$ returns an array of size N^2 (indexed from 0 to $N^2 - 1$) where its i^{th} element is $(A_x + A_y) \bmod M$ with $x = \text{floor}(i/N)$ and $y = i \bmod N$.

For example, let $A_{0..2} = \{2, 4, 5\}$ and $M = 8$. Then,

$$\begin{aligned} \text{SMPA}(A, M) &= \{ (A_0 + A_0) \bmod M, (A_0 + A_1) \bmod M, (A_0 + A_2) \bmod M, \\ &\quad (A_1 + A_0) \bmod M, (A_1 + A_1) \bmod M, (A_1 + A_2) \bmod M, \\ &\quad (A_2 + A_0) \bmod M, (A_2 + A_1) \bmod M, (A_2 + A_2) \bmod M \} \\ &= \{ (2 + 2) \bmod 8, (2 + 4) \bmod 8, (2 + 5) \bmod 8, \\ &\quad (4 + 2) \bmod 8, (4 + 4) \bmod 8, (4 + 5) \bmod 8, \\ &\quad (5 + 2) \bmod 8, (5 + 4) \bmod 8, (5 + 5) \bmod 8 \} \\ &= \{4, 6, 7, 6, 0, 1, 7, 1, 2\} \end{aligned}$$

Jono is not satisfied with only one SMPA operation. He then introduces the following SMPA^K for a positive integer K .

$$\text{SMPA}^K(A, M) = \begin{cases} \text{SMPA}(A, M), & \text{if } K = 1 \\ \text{SMPA}^{K-1}(\text{SMPA}(A, M), M), & \text{otherwise} \end{cases}$$

For example, let $A_{0..1} = \{1, 2\}$ and $M = 8$.

- $\text{SMPA}^1(A, M) = \{2, 3, 3, 4\}$
- $\text{SMPA}^2(A, M) = \{4, 5, 5, 6, 5, 6, 6, 7, 5, 6, 6, 7, 6, 7, 7, 0\}$
- $\text{SMPA}^3(A, M) = \{0, 1, 1, 2, 1, 2, 2, 3, 1, 2, 2, 3, 2, 3, 3, 4, 1, 2, 2, 3, \dots\} \rightarrow (256 \text{ elements})$
- $\text{SMPA}^4(A, M) = \{0, 1, 1, 2, 1, 2, 2, 3, 1, 2, 2, 3, 2, 3, 3, 4, 1, 2, 2, 3, \dots\} \rightarrow (65536 \text{ elements})$

Jono would like to experiment with a large K but, as you might already notice, the array size grows exponentially. Therefore, he cannot simply print out the resulting array. Instead, he will be satisfied if he knows the sum of all elements in the resulting array. As this number can be very large as well, he decides to modulo the output by 998 244 353.

Your task in this problem is to compute the sum of all elements in the array produced by $\text{SMPA}^K(A, M)$. Output the non-negative remainder after being divided by 998 244 353.

Input

Input begins with a line containing three integers N M K ($1 \leq N \leq 100\,000$; $M \in \{2^0, 2^1, \dots, 2^{18}\}$; $1 \leq K \leq 10^9$) representing the size of array A , and the parameter M and K for the $\text{SMPA}^K(A, M)$ operation, respectively. The next line contains N integers A_i ($0 \leq A_i < M$) representing the array A .

Output

Output contains an integer in a line representing the non-negative remainder of the sum of all elements in $\text{SMPA}^K(A, M)$ after being divided by 998 244 353.

Sample Input #1

```
3 8 1
0 1 2
```

Sample Output #1

```
18
```

Explanation for the sample input/output #1

$\text{SMPA}^1(\{0, 1, 2\}, 8) = \{0, 1, 2, 1, 2, 3, 2, 3, 4\}$. The sum of all its elements is $0 + 1 + 2 + 1 + 2 + 3 + 2 + 3 + 4 = 18$.

Sample Input #2

```
3 8 2
0 1 2
```

Sample Output #2

```
316
```

Sample Input #3

```
5 8192 3
1000 2000 3000 4000 5000
```

Sample Output #3

```
577938879
```

Explanation for the sample input/output #3

The sum of all elements in the resulting array is 1 576 183 232. Its non-negative remainder after being divided by 998 244 353 is 577 938 879.