Estimates of COVID-19 Cases Across Four Canadian Provinces

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Abstract

This paper estimates population infection rates from coronavirus disease 2019 (COVID-19) across four Canadian provinces from late March to early May 2020. The analysis combines daily data on the numbers of conducted tests and diagnosed cases with a methodology that corrects for non-random testing. We estimate the relationship between daily changes in the number of conducted tests and the fraction of positive cases in the non-random sample (typically less than one percent of the population), and apply this gradient to extrapolate the predicted fraction of positive cases if testing were expanded to the entire population. The estimated population infection rates were 1.7 - 2.6 percent in Quebec, 0.7 - 1.4 in Ontario, 0.5 - 1.2 percent in Alberta, and 0.2 - 0.4 percent in B.C. over the sample period. In each province, these estimates are substantially below the average positive case rate, consistent with non-random testing of higher risk populations. The results also imply widespread undiagnosed COVID-19 infection. For each identified case by mid-April, we estimate that there were roughly 12 population infections.

Keywords: COVID-19, Population Infection Rates, Non-random Testing

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1 Introduction

The first cases of coronavirus disease 2019 (COVID-19) in Canada were documented in late January, 2020, and by May 5 more than 63,000 cases had been reported (CSSE, 2020). Because testing has been limited to a small fraction of the population and infected individuals with mild or no symptoms may not seek testing, however, there is potential for widespread undocumented infections.¹

This paper estimates population infection rates for COVID-19 across four Canadian provinces – Quebec, Ontario, Alberta, and B.C. – from late March to early May. The analysis is based on the methodology developed in Benatia, Godefroy and Lewis (2020) that corrects observed infection rates among tested individuals for non-random sampling to calculate infection rates in the overall population.² To implement the procedure, we estimate the relationship between the number of tests and the share of positive tests. This gradient is informative for the severity of selection bias. For example, a negative slope indicates positive selection bias, since individuals who are most frequently tested have the highest probability of infection. If the functional form of this relationship can be consistently estimated, we can compute the population infection rate as a combination of the observed sample infection rate and the estimated selection gradient, which corrects for non-random testing.

In practice, our approach faces two main empirical challenges. First, there is concern that the supply of testing may respond endogenously to underlying disease prevalence. For example, if policymakers expand testing in response to increases in underlying disease prevalence, our estimation strategy would underestimate the selection bias gra-

¹See Dong et al. (2020); Lu et al. (2020); Hoehl et al. (2020); Pan et al. (2020); Bai et al. (2020).

²There is a large body of research in economics devoted to the issue of non-random sampling. See Heckman (1976); Heckman (1979); Heckman, Lalonde and Smith (1999); Blundell and Costa Dias (2002); Das, Newey and Vella (2003); Newey (2009). Epidemiologists have also devoted considerable attention to the issue of sample "representativeness" (for a detailed discussion see the International Journal of Epidemiology volume 42, issue 4).

dient and thus overestimate total population infections. To address this concern, we focus on high frequency day-to-day changes in the number of completed tests across U.S. states and all Canadian provinces.³ Because there is little scope for evolution in disease prevalence from one day to the next, daily changes in testing should be orthogonal to changes in population infection rates. To further validate this assumption, we estimate models that control for province and state fixed effects, thereby allowing for daily exponential growth in disease prevalence that is specific to each jurisdiction.

The second empirical challenge stems from uncertainty regarding the true functional relationship between the positive test rate and the size of the tested sample. In the empirical implementation, we specify a flexible functional relationship that appears to fit the data well. Nevertheless, the results ultimately depend on an untested assumption that the estimated relationship – based on data from the sample of tested individuals who typically comprise less than one percent of the population – can be extrapolated to the rest of the population. Despite this limitation, we believe the approach offers significant advantages over existing methods use to estimate population infection rates (see below). In ongoing work, we hope to refine the estimation procedure to address this functional form concern.

We find wide cross-province differences in both the levels of population infection rates and their trends. Average population infection rates that ranged from 0.3 percent in B.C. to 3 percent in Quebec. Infection rates in B.C. declined modestly over the sample period. In Ontario, infection rates rose from early to mid-April and subsequently declined. Meanwhile, Quebec and Alberta experienced increases in population infection rates over the month of April. These trends need not reflect increases in the number of newly infected individuals, since our population infection rates capture

³To improve the precision of the estimates, we include all Canadian provinces with U.S. states to estimate the selection bias gradient. Once this gradient has been estimated, however, our estimates of underlying prevalence rely solely on the shares of positive cases across the four Canadian provinces we study.

both newly infected individuals and those with continued detectable viral load over the sample period.⁴

Our results also suggest widespread undetected COVID-19 infection across Canadian provinces. We calculate that for every diagnosed case there were 12 population infections in mid-April. These ratios range from 8.6 in B.C. to 14.8 in Ontario. These estimates are comparable to recent evidence on the rates of undetected infection in the United States and internationally (Perkins et al., 2020; Johndrow, Lum and Ball, 2020; Verity et al., 2020; Ferguson et al., 2020). For example, Aspelund et al. (2020) estimate that 80 to 90 percent of COVID-19 cases went undiagnosed in Iceland from late March to early April. Benatia, Godefroy and Lewis (2020) estimate a ratio of 12 population infections per diagnosed case in the U.S. by early April. More recently, the CDC reported results based on seroprevalence that suggest total infections were 10 times higher than the number of confirmed cases (CDC, 2020).

This paper provides new evidence on overall population infection rates for COVID-19 in Canada. Our findings complement evidence for COVID-19 prevalence, nation-wide. Using survey results for COVID-19 symptoms, Reid (2020) finds that more than 100,000 households reported COVID-like symptoms after adjusting for seasonal influenza rates. The results do not account for potentially large numbers of asymptomatic infections. Meanwhile, Verity et al. (2020) combines assumptions regarding the age-adjusted case fatality rate with COVID-related deaths to estimate total population infections in Canada on March 31. These estimates indicate that case detection rate was just 5 percent through March. Our analysis provides the first provincial-level estimates. Given wide cross-provinces differences in per capita testing, official case

⁴There is an extended period over which individuals may test positive for COVID-19. PCR testing has identified cases days before symptom onset and detected continued viral RNA presence more than three weeks after symptom onset (Huang et al., 2020; Cai et al., 2020; Zhou et al., 2020). Often times these positive cases occur among individuals who are no longer symptomatic, and it is believed that they reflect lingering viral material that no longer poses a risk of transmission.

counts may mask important geographic differences in the severity of the outbreak. Indeed, whereas the official case count in Quebec was 55 percent higher than Ontario, our results show that gap in total cases was less than 20 percent.

Our empirical framework complements existing methods used to estimate population infection rates in the United States and internationally (Ferguson et al., 2020; Perkins et al., 2020; Li et al., 2020b; Riou et al., 2020a; Johndrow, Lum and Ball, 2020; Javan, Fox and Meyers, 2020; Verity et al., 2020). One approach has been based on the Susceptible Infectious Removed (SIR) epidemiological model, which calibrates parameters to the specific characteristics of the SARS-CoV-2 pandemic to estimate current and future infections. A challenge for this approach is the large uncertainty regarding the relevant parameter values for the virus, and the fact that the parameter values will evolve as societies take different measures to reduce transmission. Other research has relied on Bayesian modelling to infer past disease prevalence from observed COVID-19 deaths. While, these models require fewer assumptions regarding the underlying parameter values, because they 'scale up' observed deaths to estimate population infections, small differences in the assumed case fatality will have substantial effects on the estimates. Given considerable uncertainty regarding the true case fatality, which may depend on local sociodemographic and environmental conditions, and the fact that COVID-19 related deaths may be undercounted during the course of the pandemic, these estimates may fail to capture the overall extent of population infection.⁵

Most closely related to our paper is Manski and Molinari (2020), who use data on the total number of total tests and the positive test rate to estimate ranges for population COVID-19 infection rates for Illinois, New York, and Italy in early April. Their approach only requires the imposition of weak monotonicity assumptions for

⁵See Riou et al. (2020*b*); Han et al. (2020); Wu et al. (2020); Clay, Lewis and Severnini (2018, 2019); Clay et al. (2020); Katz and Sanger-Katz (2020); Prakash and Hall (2020).

identification. Their estimated bounds for infection rates are 0.1%-51.7% for Illinois, 0.8%-64.5% for New York, and 0.3%-51.0% for Italy. These are wide, model-free bounds. Below we estimate much narrower intervals, which are conditional on the accuracy of our model. While we have developed our method for use during this crisis to use the available information as fully as possible, policy makers should be aware that bounds that include model uncertainty would be wider than ours by some unknown amount, as is not uncommon in econometric analyses. The model-free bounds of Manski and Molinari (2020) serve as a remind of that issue.

2 Data

Our analysis draws on daily data on total test results (positive plus negative) and positive tests across Canadian provinces and U.S. states for the period March 31 to May 5. Provincial data were obtained from the Epidemiological Data from the COVID-19 Outbreak in Canada project (Berry et al., 2020). This project is conducted by a team of researchers from the University of Toronto and the University of Guelph and provides information on cases and testing across provinces based on publicly available information from government reports and news media. We exclude days in which there were identified changes in provincial reporting standards and days in provincial health authorities did not release information on completed tests. In addition, we use information on the number of positive tests by age group, which is available on provincial health departments, and provincial population estimates from Statistics Canada (2020). We supplement these data with information on the total tests results and positive cases across U.S. states for the same time period from the COVID Tracking Project, a site launched by journalists from The Atlantic that publishes high-quality

⁶There are a large number of missing observations from B.C. because daily testing results were not always released.

data on the outbreak across U.S. states (Meyer, Kissane and Madrigal, 2020).

Figure 1 reports the daily tests and positive cases across the four provinces. Daily testing was fairly stable in Quebec throughout April. In contrast, there were substantial increases in daily testing in both Ontario and Alberta, and to a lesser extent in B.C.

[insert Figure 1 here]

3 Methodology

In this section, we present the theoretical framework developed in Benatia, Godefroy and Lewis (2020) to estimate COVID-19 prevalence. This framework motivates estimating equation (6).

3.1 Theory

To evaluate population disease prevalence, we develop a simple selection model for COVID-19 testing and used the framework to link observed rates of positive tests to population disease prevalence. We consider a stable population, normalized to size one, and denote A and B as the number of sick and healthy individuals, respectively. Let p_n denote the probability that a sick person is tested and q_n the probability that a healthy person is tested, given a total number of tests, n. Thus, we have:

$$n = p_n A + q_n B,$$

and assuming the test is accurate, the number of positive tests is:

$$s = p_n A$$
.

This simple framework highlights how non-random testing will bias estimates of the population disease prevalence. Using Bayes' rule, we can write the relative probability of testing as the following:

$$\frac{p_n}{q_n} = \frac{Pr(sick|tested, n)/Pr(healthy|tested, n)}{Pr(sick|n)/Pr(healthy|n)},$$

which is equal to one if tests are randomly allocated, Pr(sick|tested, n) = Pr(sick|n). When testing is targeted to individuals who are more likely to be sick, we have Pr(sick|tested, n) > Pr(sick|n) and Pr(healthy|tested, n) < Pr(healthy|n), so the ratio will be greater than one. In this scenario, the ratio of sick to healthy people in the sample, $p_n A/q_n B$, will exceed the ratio in the overall population, A/B.

We assume that the severity of selection bias can be expressed a function of the number of tests:

$$\frac{p_n}{q_n} = f(n; \theta) \tag{1}$$

where n is number of conducted tests and θ is a vector of parameters to be estimated. According to this setup, we can write the fraction of positive tests, s/n, as follows:

$$\frac{s}{n} = \frac{1}{1 + \frac{q_n}{p_n} \frac{B}{A}} \tag{2}$$

Taking logs and using the fact that the latter term in the denominator is much larger than one, we can make the following approximation:⁷

$$\log \frac{s}{n} \approx \log \left(\frac{p_n}{q_n} \frac{A}{B} \right) = \log \left(\frac{p_n}{q_n} \right) + \log \left(\frac{A}{B} \right) \tag{3}$$

Equation (3) shows that the log share of positive tests in the sample can be approx-

⁷The median ratio of negative to positive tests, $\frac{q_n B}{p_n A}$, across Canadian provinces was 21 during the sample period.

imated by the sum of the log ratio of the relative probability of testing, p_n/q_n , and the unobserved log ratio of sick to healthy people in the population, A/B.

3.2 From Theory to Estimation

To conduct the estimation, we adopt a first difference estimator, using as the dependent variable the difference $\log \frac{s_{i,t}}{n_{i,t}} - \log \frac{s_{i,t-1}}{n_{i,t-1}}$ on two consecutive days t-1 and t in a given province/state i. Given the last equation, this first difference is equal to:

$$\log \frac{s_{i,t}}{n_{i,t}} - \log \frac{s_{i,t-1}}{n_{i,t-1}} = \log f(n_{i,t};\theta) - \log f(n_{i,t-1};\theta) + u_{i,t}$$
(4)

where $u_{i,t} = \log\left(\frac{A_{i,t}}{B_{i,t}}\right) - \log\left(\frac{A_{i,t-1}}{B_{i,t-1}}\right) + \epsilon_{i,t}$ is a mean zero error term that depends on the change in ratio of sick to healthy individuals in the population from t-1 to t and an idiosyncratic component, $\epsilon_{i,t}$.

Equation (4) forms the basis of our empirical analysis. Our identifying assumption is strict exogeneity in the error term: $E(u_{i,t}|n_{i,t},n_{i,t-1})$. This assumption ensures that the errors are uncorrelated with any function of changes in the number of tests, $\Delta n_{i,t}$, and will be violated if changes in the population infection rate were systematically related to testing capacity. This assumption is supported by the short time interval in the daily first difference specification, which limits the scope for disease evolution. Also, in robustness tests, we control for province/state fixed effects, which allow for jurisdiction-specific exponential growth in underlying disease prevalence from one day to the next. These controls do not affect the main coefficient estimates.

Notice that by focusing on a daily first difference estimator, we are able to partial out the unobserved log ratio of sick to healthy people in the population, $A_{i,t}/B_{i,t}$. As a result, changes in the share of positive tests depends on the number of tests *only* through a selection channel.

How does this assumption enable us to estimate population infection rates? Using day-to-day changes in the share of positive tests and day-to-day changes in the number of tests, we can recover $\log f(n; \hat{\theta})$ by estimating equation (4). This term captures how changes in the share of positive tests are predicted to change with n. We can then use this prediction to recover population infection rates. Denote $\frac{\widehat{S_{pop}}}{n_{pop}}$ as the predicted fraction of positive tests if the entire population in province i were tested on date t, i.e. $n_{i,t} = pop_i$. We can rewrite the first difference equation (4) as:

$$\log \frac{\widehat{s_{pop}}}{n_{pop i,t}} = \log \frac{s_{i,t}}{n_{i,t}} + \log f(pop_i; \hat{\theta}) - \log f(n_{i,t}; \hat{\theta})$$
(5)

That is, the predicted log fraction of positive tests in the population is equal to the log fraction of positive tests in the sample plus an adjustment factor that corrects for non-random testing. One could also view our exercise as a reduced form estimation of the relationship between the fraction of individuals who test positive and the size of the tested population (holding constant the population share of sick). Once this relationship has been consistently estimated, we can predict the share of positive tests for any value of n, including when $n = pop_i$.

3.3 Empirical Implementation

To implement the procedure described in section 3.2, we specify the following functional form for the selection process into testing, $f(n; \theta)$:

$$\frac{p_n}{q_n} = f(n; \theta) = 1 + e^{\gamma + \beta n}.$$

The term $e^{\gamma+\beta n} \geq 0$ reflects the fact that testing has been targeted towards higher risk populations, with the intercept, γ , capturing the severity of selection bias when testing is limited. Meanwhile, the coefficient $\beta < 0$ identifies how selection bias decreases

with n as the ratio p_n/q_n approaches one. Intuitively, as testing expands, the sample will become more representative of the overall population, and the selection bias will diminish.

We substitute this function into the first difference regression model, taking a third order power series approximation of the log function, which yields the following estimating equation:⁸

$$\log \frac{s_{i,t}}{n_{i,t}} - \log \frac{s_{i,t-1}}{n_{i,t-1}} = \alpha_1 \left[e^{\beta \frac{n_{i,t}}{pop_i}} - e^{\beta \frac{n_{i,t-1}}{pop_i}} \right] + \alpha_2 \left[e^{2\beta \frac{n_{i,t}}{pop_i}} - e^{2\beta \frac{n_{i,t-1}}{pop_i}} \right] + \alpha_3 \left[e^{3\beta \frac{n_{i,t}}{pop_i}} - e^{3\beta \frac{n_{i,t-1}}{pop_i}} \right] + \nu_{i,t}$$
(6)

We estimate equation (6) by non-linear least squares, allowing for heteroskedastic errors.⁹ After estimation, we derive predicted values for population infection rates based on equation (5), using the Delta method to construct confidence intervals.

Before turning to the main results, several caveats should be highlighted. First, the estimates of population infection rates depend on a correctly specified functional relationship between the positive test rate and the size of the tested sample. While the model fits the data well (see below), an important assumption underlying our analysis is that this observed relationship in the tested sample – who typically comprises less than one percent of the population – would continue to hold if testing were expanded out to the broader population. The accuracy of this extrapolation depends on a smoothness condition on the functional form, and may be violated if, for example, some segments of the population can easily be tested while other groups cannot.

The first difference derivation is based on the following equation: $\log \frac{s}{n} \approx \log \left(1 + e^{\gamma + \beta n}\right) + \log \frac{A}{B} \approx \sum_{k=1}^{M} \frac{(-1)^{k-1} e^{k\gamma}}{k} e^{k\beta n} + \log \frac{A}{B}$. The results are not sensitive to the inclusion of higher order terms. Our baseline estimating equation does not include a constant, although we explore the robustness of the results to jurisdiction specific intercepts.

⁹Similar standard errors are found in models that allow for within-state/province serial correlation. ¹⁰There is little guidance from theory about the functional form of relationship, and there is no individual-level survey data to shed light on who is tested.

We also constrain the population coefficients (α_i , β) to be the same across jurisdictions. This assumption requires that decisions regarding how to prioritize tests were made similarly across provinces and U.S. states. Although states had latitude to implement their own diagnostic testing procedures, the guidance laid out for testing prioritization by the CDC was broadly similar to the policies implemented across Canadian provincial health departments (CDC, 2020). We also estimate the model for three distinct one-week intervals, March 31 - April 7, April 14 - 21, and April 28 - May 5, to allow for the possibility that decisions over how to allocate tests across the population may have changed from late March to early May. Because policy decisions regarding testing of elderly populations may have differed across jurisdictions, we also report estimates based solely on cases among individuals under age 70.

Finally, our analysis depends on the quality of diagnostic testing, and systematic false negative test results may affect the population disease prevalence estimates (Liu et al., 2020; Ai et al., 2020; Yang et al., 2020). Because our analysis focuses on day-to-day variation, however, changes in the rates of misdiagnosis should not be systematically related to changes in the number of implemented tests. As a result, these errors should not bias the coefficient estimates, but may reduce precision through classical measurement error (Wooldridge, 2002).

4 Results

Table 1, Panel A reports the estimates for equation (1) across three time periods: March 31 - April 7, April 14 - 21, and April 28 - May 5. We estimate the model

¹¹To see why this is the case, let $\pi < 1$ denote the fixed probability that a test is positive if an individual is sick, so that some fraction of sick individuals may not be detected by testing. In this case, the researcher observes s/n but the actual share of positive cases among the tested sample is $\frac{s}{\pi n}$. Provided that the rate of false negatives is constant over time, the term π drops out of the first difference equation (4), so it will not affect the main estimates.

separately for all ages (cols. 1, 3, 5) and excluding cases among individuals over age 70 (cols. 2, 4, 6). Consistent with the theoretical framework, we find large estimates of β ranging from -1,092 to -1,391, which implies that the sample selection in testing approaches zero as the number of tests approaches the total population size. We also find alternating signs on the coefficient $\hat{\alpha}_1$, $\hat{\alpha}_2$, $\hat{\alpha}_3$, consistent with the estimates of the power series approximation developed in Benatia, Godefroy and Lewis (2020).

[insert Table 1 here]

Figure 2 presents scatterplots of the relationship between daily changes in per capita testing the share of positive tests across states and provinces for the three time periods. The downward sloping relationships imply that larger day-to-day increases in the number of conducted tests are associated with decreases in the share of positive tests. A symptom of selection bias is that variables that have no structural relationship with the dependent variable may appear to be significant (Heckman, 1979). So, these patterns strongly suggest non-random testing, since daily changes in testing should be unrelated to population disease prevalence except through a selection channel.

[insert Figure 2 here]

Table 2 reports the results for Quebec, Ontario, Alberta, and B.C. that adjust observed COVID-19 case rates for non-random testing based on the procedure described in Section 3. Column 2 report the estimates for all age population infection rates on April 4, April 18, and May 2, along with heteroskedasticity robust 95 percent confidence intervals. Column 4 reports the average estimates for the three time periods March 31 - April 4, April 14 - 18, and April 28 - May 2. These latter averages mitigate sampling error in the daily prevalence estimates, which depend on the observed share of positive tests on any particular day.

[insert Table 2 here]

The results reveal widespread disparities in COVID-19 prevalence across provinces. Population infection rates range from more than 2 percent in Quebec to less than 0.4 percent in B.C. Trends in infection rates differed significantly across provinces. Infection rates in B.C. declined modestly over the sample period. In Ontario, infection rates rose from early to mid-April and subsequently declined. Meanwhile, Quebec and Alberta experienced steady increases in population infection rates over the sample period.

Columns 3 and 5 report the estimated population infection rates among individuals below age 70.¹² These estimates will not be influenced by specific policies regarding the testing of elderly population and residents of senior residential facilities that may have differed across provinces.¹³ For Alberta and B.C., the results are similar to overall population prevalence. Meanwhile, the estimates are systematically lower in Ontario and Quebec, particularly in the latter periods. These results are consistent with the timing of the shift in testing of elderly facilities in these two provinces (CBC, April 8, 2020; Jones, April 22, 2020).

[insert Figure 3 here]

Table 3 explores the robustness of the main estimates to controls for province and state fixed effects. These controls allow for growth rates in underlying disease prevalence that are specific to each locality, to account for the fact that the true infection rate may evolve even with a 24-hour period. Because the intercepts are allowed to differ across each jurisdiction, they also account for variation in the daily evolution of the

¹²Figure 3 presents both all-age and below age 70 population infection rates.

¹³To derive these estimates, we subtract the number of cases among the elderly from the total daily cases and total daily tests across provinces. Because we lack data on *total* tests by age group, negative tests among the elderly are included in the denominator, so these estimates should be interpreted as a lower bound estimate for disease prevalence.

disease across states and provinces due to differing enforcement of social distancing or other location-based determinants of disease spread. The results (reported in cols. 2, 4, 6, and 8) are virtually identical to the baseline estimates. Moreover, the augmented model tends to produce more precise confidence intervals, although as noted earlier we emphasize that these confidence intervals are conditional on our model.

[insert Table 3 here]

To interpret the findings, we calculate the total population infections in mid-April and compare them to the number of diagnosed cases in each province. We multiply the average estimated prevalence from April 14-18 (Table 2, Panel B, col. 4) by the total province population and compare them to the cumulative diagnosed cases by April 23. The gap in the two periods captures the typical five-day incubation period, to account for the fact that individuals may not seek testing until symptom onset (Li et al., 2020a; Lauer et al., 2020). In principal, these numbers capture two distinct measures of COVID-19 spread: current infections versus cumulative infections. Nevertheless, given limited COVID-19 infection prior to mid-March and the fact that viral presence is detectable by PCR testing three weeks after initial symptom onset (Cai et al., 2020; Zhou et al., 2020), population infection rates in mid-April are likely to be similar to cumulative infections since onset.

Table 4 presents the results. We find widespread undetected population infection. By April 23, 41,371 cases had been identified across the four provinces, however our estimates suggest that there were more than a half million infected individuals. In Quebec and Alberta, there were 11 to 12 population infections for each diagnosed case. In Ontario, we find that there were 15 population infections per diagnosed case. These gaps align with differences in testing across provinces – Alberta (27 per 1,000) and Quebec (22 per 1,000) versus Ontario (13 per 1,000). Meanwhile, B.C. had the smallest

fraction of undetected cases, despite conducting just 14 tests per 1,000 population. This discrepancy can likely be attributed to the fact that the scope of the outbreak was substantially more limited in B.C., allowing officials to better identify clusters of cases.

[insert Table 4 here]

5 Discussion

This paper provides new evidence on the population prevalence of COVID-19 in Quebec, Ontario, Alberta, and B.C. from late March to early May. Our analysis adapts a sample selection model approach developed in Benatia, Godefroy and Lewis (2020). We find widespread population infection that exceed official reported cases by factors of 9 to 15 across provinces.

Our findings are comparable to recent prevalence estimates from the U.S. and countries in Western Europe. The estimated infection rates in Quebec are similar to those from the United Kingdom (2.7%), and several U.S. states (Pennsylvania – 2.4%, Rhode Island – 2.4%, and Massachusetts – 3.4%). Meanwhile, the rates in Ontario are similar to Austria (1.1%), Denmark (1.1%), Vermont (1.4%), Virginia (1.4%), and Idaho (1.5%) in early April. Our results are also consistent with recent evidence from serological testing across several U.S. jurisdictions that show widespread undetected infection by mid-April (Bendavid et al., 2020; Goodman and Rothfeld, April 23, 2020; Conarck and Chang, April 24, 2020).

Our analysis provides a complement to existing methods used to estimate population infection rates. These approaches either require strong assumptions on unknown

¹⁴See Ferguson et al. (2020); Johndrow, Lum and Ball (2020); Javan, Fox and Meyers (2020); Benatia, Godefroy and Lewis (2020).

disease parameters, or accurate measurement of COVID-related deaths, which may be undercounted over the course of the pandemic. Our estimation approach builds on standard econometric techniques. As high frequency test data become more widely available at finer geographic units, this approach could be applied to estimate population infection rates at the city or district level. The current estimates depend on the accuracy of an extrapolation of the functional form relating the number of tests and the positive case rate to the large untested population. In ongoing work, we hope to refine the estimation procedure and explore the sensitivity of the results to various functional form assumptions.

As physical distancing policies continue to be relaxed, it will be essential that policymakers have access to timely data on infection rates. Given the potential for widespread undiagnosed infection, the expansion of randomized population-based PCR testing may play a key role in identifying localized outbreaks. Meanwhile, widespread implementation of serological testing will help identify the large numbers of individuals with some level of immunity to the virus.

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Figures and Tables

(a) Quebec

(b) Ontario

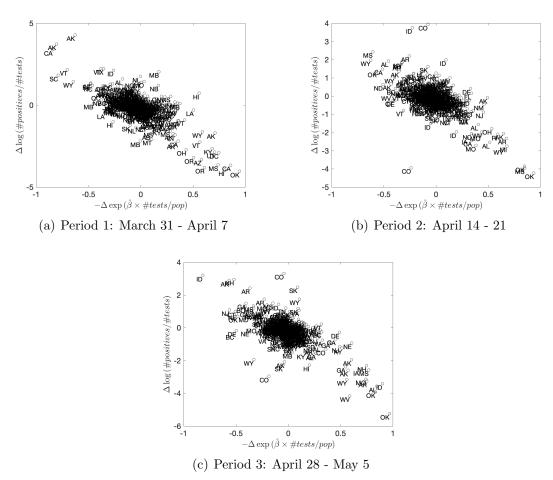
(c) Alberta

(d) B.C.

Figure 1: Daily Testing and New Cases Across Provinces

Notes: This figure reports the total daily coronavirus tests and the number of new cases per 100,000 population by province. The trends are based on data from (Berry et al., 2020). We exclude days in which there were identified changes in provincial reporting standards and days in provincial health authorities did not release information on completed tests. Source: Berry et al. (2020); Statistics Canada (2020).

Figure 2: Daily Changes in Testing and the Share of Positive Cases



Notes: This figure reports the relationship between daily changes in the exponential of per capita testing and daily changes in the log share of positive tests for the three time periods: March 31 - April 7, April 14 - 21, and April 28 - May 5. The relationship in each period is obtained using the estimated coefficient of β from the main estimates of equation (6) (see Table 1, cols. 1, 3, 5). Source: Authors' calculations.

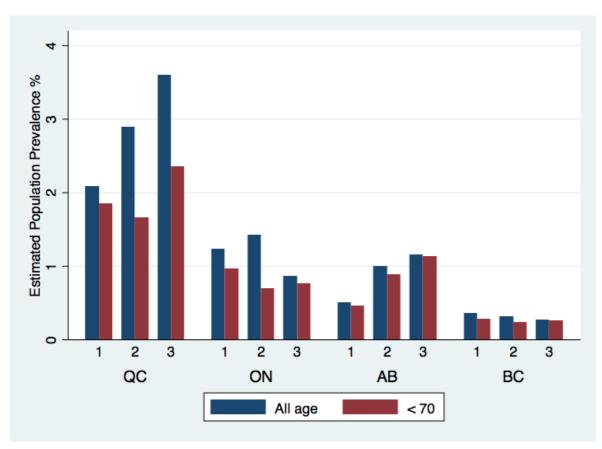


Figure 3: Population COVID-19 Infection Rates by Province and Period

Notes: This figure reports average population infection rates across provinces for three different time periods: 1 - (March 31 - April 4); 2 (April 14 - April 18); 3 (April 28 - May 2). These average infection rates are obtained using the estimation procedure described in Section 3. All age population prevalence estimates are based on all cases and tests. To derive population prevalence for less than 70 year olds, we subtract the number of cases among the elderly from the total daily cases and total daily tests across provinces.

Table 1: Coefficient Estimates from Equation (6)

	Period 1: Mar 31 - Apr 7		Period 2:		Period 3:	
	$\frac{\text{Mar 31}}{\text{All age}}$ (1)	$\frac{-\operatorname{Apr} 7}{<70}$ (2)	$\frac{\text{Apr I}}{\text{All age}}$ (3)	$\frac{4 - 21}{< 70}$ (4)	$\frac{\text{Apr } 28 - \text{All age}}{\text{All age}}$ (5)	$\frac{\text{May 5}}{<70}$ (6)
Panel A: Base	(/		()			()
$lpha_1$	$11.570 \\ (2.090)$	$ 11.704 \\ (2.157) $	10.004 (1.564)	10.347 (1.625)	8.199 (1.640)	8.159 (1.679)
$lpha_2$	-23.975 (3.946)	-24.327 (4.064)	-20.765 (3.155)	-21.675 (3.260)	-16.026 (3.393)	-15.960 (3.472)
$lpha_3$	$17.545 \\ (2.230)$	$17.781 \\ (2.292)$	$15.628 \\ (1.929)$	$16.230 \\ (1.984)$	12.255 (2.096)	$12.225 \\ (2.139)$
β	-1390.815 (156.032)	-1381.209 (156.412)	-1608.010 (204.343)	-1578.140 (193.004)	-1107.816 (182.211)	-1092.915 (182.714)
$\sigma_{ u}$	0.516 (0.017)	0.527 (0.018)	0.579 (0.020)	0.593 (0.021)	0.608 (0.022)	0.609 (0.022)
$\frac{\text{Observations}}{Panel\ B:\ Augm}$	443 nented Model	443 with Province	410 ce / State Fis	408 red Effects	399	399
α_1	$11.313 \\ (1.512)$	11.422 (1.561)	10.045 (1.115)	10.333 (1.153)	8.026 (1.155)	7.994 (1.181)
$lpha_2$	-23.469 (2.856)	-23.757 (2.943)	-20.818 (2.248)	-21.589 (2.315)	-15.540 (2.399)	-15.487 (2.450)
$lpha_3$	$17.261 \\ (1.614)$	17.454 (1.660)	$15.649 \\ (1.378)$	$16.162 \\ (1.414)$	11.866 (1.491)	$ \begin{array}{c} 11.844 \\ (1.518) \end{array} $
β	-1405.202 (117.348)	-1394.489 (117.919)	-1596.620 (143.886)	$ \begin{array}{c} -1573.924 \\ (137.678) \end{array} $	-1111.405 (131.964)	-1096.945 (132.088)
$\sigma_{ u}$	0.512 (0.012)	0.522 (0.012)	0.575 (0.014)	0.589 (0.015)	0.602 (0.015)	0.604 (0.015)
Observations	443	443	410	408	399	399

Notes: This table reports the estimation of the coefficients from equation (6). We estimate the model separately for each time period and for all age versus cases among individuals less than 70 years old. Panel A reports the coefficient estimates from the baseline model. Panel B reports the estimates from augmented models that include province and state fixed effects. Heteroskedasticity robust standard errors are reported in parentheses.

Table 2: Estimated Population Infection Rates for COVID-19

	Positive Tests (%)	Estimated Population Prevalence (%)		Ave. Estimated Pop. Prevalence (%)	
		All age	< 70	All age	< 70
	(1)	(2)	(3)	(4)	(5)
Panel A: C	COVID-19 Prevalence	in Early April			
	April 4	April 4		March 31 - April 4	
Quebec	14.22	2.22 [1.03, 4.82]	$ \begin{array}{c} 1.95 \\ [0.87, 4.35] \end{array} $	2.08	1.85
Ontario	7.31	$0.86 \\ [0.41, 1.79]$	$0.61 \\ [0.29, 1.32]$	1.23	0.96
Alberta	4.93	$0.69 \\ [0.33, 1.43]$	$0.63 \\ [0.30, 1.34]$	0.51	0.46
B.C.	2.51	$0.23 \\ [0.11, 0.49]$	$0.12 \\ [0.05, 0.26]$	0.36	0.28
Panel B: C	COVID-19 Prevalence	in Mid-April			
	April 18	April 18		April 14 - 18	
Quebec	13.95	$ 2.70 \\ [1.52, 4.81] $	$2.56 \\ [1.45, 4.53]$	2.89	1.66
Ontario	5.93	$ \begin{array}{c} 1.21 \\ [0.67, 2.18] \end{array} $	$0.80 \\ [0.44, 1.48]$	1.42	0.7
Alberta	4.03	$ \begin{array}{c} 1.11 \\ [0.59, 2.09] \end{array} $	$ \begin{array}{c} 1.05 \\ [0.55, 2.00] \end{array} $	1.00	0.89
B.C.	2.79	$0.43 \\ [0.24, 0.75]$	$0.36 \\ [0.20, 0.63]$	0.31	0.24
Panel C: C	COVID-19 Prevalence	in Early May			
	May 2	May 2		April 28 - May 2	
Quebec	10.87	$2.91 \\ [1.51, 5.63]$	1.98 [1.01, 3.90]	3.60	2.35
Ontario	2.69	$0.76 \\ [0.39, 1.47]$	$0.75 \\ [0.38, 1.48]$	0.86	0.76
Alberta	2.56	$0.60 \\ [0.32, 1.13]$	$0.57 \\ [0.30, 1.10]$	1.16	1.13
B.C.	1.25	$0.23 \\ [0.13, 0.43]$	$0.24 \\ [0.13, 0.45]$	0.27	0.26

Notes: Column (1) reports the fraction of positive tests on the relevant day. Columns 2-3 report the coefficient estimates for population prevalence of COVID-19 based on the methodology described in Section 3. Heteroskedasticity robust 95% confidence intervals are reported in brackets. We report the results for all age prevalence and prevalence among individuals less than 70 years old. Column 4-5 report the average estimates for population prevalence of COVID-19 for the three time periods.

Table 3: Robustness Exercises: Fixed Effects Models

	Est	imated Populat	ion Prevalence	(%)	Ave. Es	timated Po	p. Prevalence	e (%)	
	All age		< 70		All age		< 70		
	Baseline	Add fixed effects	Baseline	Add fixed effects	Baseline	Add fixed effects	Baseline	Add fixed effects	
	(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	
Panel A:	COVID-19 Prev	valence in Early	April						
	April 4				March 31 - April 4				
Quebec	2.22 [1.03, 4.82]	2.32 [1.33, 4.08]	1.95 [0.87, 4.35]	2.04 [1.14, 3.67]	2.08	2.17	1.85	1.93	
Ontario	0.86 [0.41, 1.79]	$0.89 \\ [0.52, 1.52]$	$0.61 \\ [0.29, 1.32]$	$0.64 \\ [0.37, 1.11]$	1.23	1.28	0.96	1.00	
Alberta	$0.69 \\ [0.33, 1.43]$	$0.72 \\ [0.42, 1.22]$	$0.63 \\ [0.30, 1.34]$	$0.65 \\ [0.38, 1.14]$	0.51	0.54	0.46	0.48	
B.C.	$0.23 \\ [0.11, 0.49]$	$0.24 \\ [0.14, 0.41]$	$0.12 \\ [0.05, 0.26]$	$0.12 \\ [0.07, 0.22]$	0.36	0.38	0.28	0.29	
Panel B:	COVID-19 Prev	valence in Mid-A	April						
	April 18					April 14 - 18			
Quebec	2.70 [1.52, 4.81]	2.67 [1.77, 4.03]	2.56 [1.45, 4.53]	2.55 [1.70, 3.82]	2.89	2.85	1.66	1.66	
Ontario	$ \begin{array}{c} 1.21 \\ [0.67, 2.18] \end{array} $	$ \begin{array}{c} 1.19 \\ [0.78, 1.82] \end{array} $	$0.80 \\ [0.44, 1.48]$	$0.80 \\ [0.52, 1.24]$	1.42	1.40	0.7	0.76	
Alberta	$1.11 \\ [0.59, 2.09]$	$ \begin{array}{c} 1.09 \\ [0.70, 1.72] \end{array} $	1.05 [0.55, 2.00]	1.05 [0.66, 1.66]	1.00	0.98	0.89	0.89	
B.C.	$0.43 \\ [0.24, 0.75]$	$0.42 \\ [0.28, 0.63]$	$0.36 \\ [0.20, 0.63]$	$0.35 \\ [0.23, 0.53]$	0.31	0.31	0.24	0.23	
Panel C:	COVID-19 Prev	valence in Early	May						
	May 2			April 28 - May 2					
Quebec	2.91 [1.51, 5.63]	2.97 [1.87, 4.73]	1.98 [1.01, 3.90]	$2.02 \\ [1.25, 3.26]$	3.60	3.66	2.35	2.39	
Ontario	0.76 [0.39, 1.47]	0.77 [0.48, 1.24]	0.75 [0.38, 1.48]	0.78 [0.47, 1.24]	0.86	0.88	0.76	0.78	
Alberta	0.60 [0.32, 1.13]	0.61 [0.39, 0.96]	0.57 [0.30, 1.10]	0.59 [0.37, 0.93]	1.16	1.18	1.13	1.16	
B.C.	0.23 [0.13, 0.43]	$0.24 \\ [0.15, 0.37]$	0.24 [0.13, 0.45]	0.24 [0.16, 0.37]	0.27	0.27	0.26	0.26	

Notes: This table explores the sensitivity of the findings to controls for province/state fixed effects. Columns 1 - 4 report the estimated population infection rates on the relevant date. Heteroskedasticity robust 95% confidence intervals are reported in brackets. Columns 5 - 8 report the average estimates for population prevalence of COVID-19 for the three time periods. Columns 1, 3, 5, and 7 report the baseline estimates, while columns 2, 4, 6, and 8 report the estimates based on augmented models that include province and state fixed effects.

Table 4: Diagnosed Cases and Estimated Total Cases of COVID-19

	Positive COVID-19 Tests, by April 23	Estimated Total COVID-19 Cases	Ratio of Total Cases to Positive Tests (2)/(1)	COVID-19 Tests per 1,000 Population
	(1)	(2)	(3)	(4)
Quebec	21,832	245,215	11.2	21.9
Ontario	13,995	206,845	14.8	13.4
Alberta	3,720	43,713	11.8	27.0
B.C.	1,824	15,721	8.6	13.5

Notes: Columns (1) reports the cumulative number of positive COVID-19 tests by April 23. Column (2) reports the total number of COVID-19 cases implied by the average estimated population prevalence from April 14 to April 18 (Table 2, Panel B, col. 4). Column (4) reports the cumulative number of COVID-19 tests by April 23 per 1,000 population.

Source: Berry et al. (2020); Statistics Canada (2020); authors' calculations.