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2 # TITLE: ex5 machine learning BIU
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 4 # DATE: 03/01/2023
 7 import scipy.io
 8 from sklearn.model_selection import train_test_split
 9 import numpy as np
10 from matplotlib import pyplot as plt
11 from sklearn.metrics import accuracy_score
12 from tqdm import tqdm
13
14
15 def helper_retrieve(data):
16
       a1 = np.split(data, 15)
17
       a2 = np.array(a1)
       a31 = a2[:, 0:8, :]
18
19
       a32 = a2[:, 8:11, :]
20
21
       train = np.concatenate(a31)
22
      test = np.concatenate(a32)
23
24
      return train, test
25
26
27 def retrieve_data():
       mat = scipy.io.loadmat('facesData.mat')
28
29
       faces = mat.get('faces')
       labels = mat.get('labeles')
30
31
32
      X_train, X_test = helper_retrieve(faces)
33
      y_train, y_test = helper_retrieve(labels)
34
35
       return X_train, X_test, y_train, y_test
36
37
38 def extract_eigenvectors(X: np.ndarray, mu: np.ndarray):
      A = np.matmul((X - mu).T, X - mu)
39
40
       w, v = np.linalg.eig(A)
41
      return w.real.astype('float64'), v.real.astype('float64')
42
43
44 def sort_eigenvectors(w, v):
45
      indexes = np.argsort(np.abs(w))
46
47
       v = v[:, indexes]
48
      w = w[indexes]
49
50
      v = np.flip(v, axis=1)
51
      w = np.flip(w, axis=0)
52
53
      return w, v
54
55
56 def show_PCA(mu, v):
57
      fig = plt.figure(figsize=(10, 2))
58
       num = 8
59
      # Display the mean
60
       fig.add_subplot(1, num, 1)
      plt.imshow(mu.reshape((32, 32)).T, cmap='gray')
61
62
       plt.title(f"mu")
      plt.axis('off')
63
64
       # Displaying the first 5 eigenvectors
65
66
       for i in range(num-1):
67
          fig.add_subplot(1, num, i+2)
68
          plt.imshow(v[:, i].reshape((32, 32)).T, cmap='gray')
          plt.title(f"v{i}")
69
          plt.axis('off')
70
71
       fig.canvas.manager.set_window_title('show_PCA')
72
73
       plt.show()
74
75
76 def compute_projection(v, x_T, mu, K):
77
78
       v_k = v[:, :K]
```

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79
        projection = np.matmul(x_T - mu, v_k)
 80
        reconstruction = mu + np.matmul(projection, v_k.T)
 81
 82
        return projection, reconstruction
 83
 84
 85 def reconstruct_image(v, mu, x_T):
86
 87
        # Build the displaying window
 88
        fig = plt.figure(figsize=(7, 7))
 89
       rows = 5
 90
       cols = 5
 91
 92
        for i in range(24):
 93
            # We choose the i first eigenvectors
 94
 95
            projection, reconstruction = compute_projection(v, x_T, mu, i)
 96
 97
            fig.add_subplot(rows, cols, i+1)
 98
 99
            # Display the projected eigenvector
100
            plt.imshow(reconstruction.reshape((32, 32)).T, cmap='gray')
101
            plt.axis('off')
            plt.title(f"K={i}")
102
103
104
        projection, reconstruction = compute_projection(v, x_T, mu, v.shape[1])
105
106
        fig.add_subplot(rows, cols, 25)
107
108
        # Display the projected eigenvector
109
        plt.imshow(reconstruction.reshape((32, 32)).T, cmap='gray')
110
        plt.axis('off')
        plt.title(f"K=1024")
111
112
113
        fig.canvas.manager.set_window_title('reconstruct_image')
114
        plt.show()
115
116
117 def mesure_projections(projections_train, projections_test, y_train):
118
119
        label_list = []
120
121
        for i in range(len(projections_test)):
122
123
            # Measure the euclidian distance between one train projection and
            # all the test projections
124
125
            dist = np.linalg.norm(projections_train - projections_test[i], axis=1)
126
127
            # Extract the index from the train set for which the distance is minimal
128
            index_train = np.argmin(dist)
129
130
            # Find the corresponding label of this train sample
131
            label = y_train[index_train]
132
133
            label_list.append(label)
134
135
        return np.array(label_list)
136
137
138 def show_accuracy_graph(X_train, mu, X_test, y_train, y_test):
139
        accuracy_list = []
140
       x = list(range(1, 50, 1))
141
        for i in tqdm(x):
142
143
            K = i
144
145
            # Get the projections of all the train set
            projections_train, _ = compute_projection(v, X_train, mu, K)
146
147
            # Get the projections of all the test set
148
149
            projections_test, _ = compute_projection(v, X_test, mu, K)
150
151
            # Mesure the distance from each projection of the train set
152
            # to all the projections of the train set
153
            y_pred = mesure_projections(
154
                projections_train, projections_test, y_train)
155
156
            # Compute the accuracy classification score.
157
            accuracy = accuracy_score(y_test, y_pred)
```

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158
159
            accuracy_list.append(accuracy)
160
161
        plt.plot(x, accuracy_list)
162
        plt.xlabel("K")
        plt.ylabel("Accuracy")
163
164
        plt.title("Accuracy of the PCA projections")
165
        plt.show()
166
167
168 if __name__ == "__main__":
169
170
       # Creating training and testing sets
       X_train, X_test, y_train, y_test = retrieve_data()
171
172
173
       # Find the mean image
174
       mu = X_train.mean(0)
175
176
       # Find the eigenvectors
177
       w, v = extract_eigenvectors(X_train, mu)
178
179
       # Sort the eigenvectors
180
       w, v = sort_eigenvectors(w, v)
181
        # Transpose the first image of the dataset
182
183
       x_T = np.reshape(X_train[0], (1, 1024))
184
        # Show the principal components
185
186
       show_PCA(mu, v)
187
188
       # Show the reconstruction of the images
189
        reconstruct_image(v, mu, x_T)
190
191
        # Show the accuracy graph
192
        show_accuracy_graph(X_train, mu, X_test, y_train, y_test)
193
        K = 16
194
195
196
        # Get the projections of all the train set
197
       projections_train, _ = compute_projection(v, X_train, mu, K)
198
199
        # Get the projections of all the test set
200
        projections_test, _ = compute_projection(v, X_test, mu, K)
201
202
        # Mesure the distance from each projection of the train set
        # to all the projections of the train set
203
       y_pred = mesure_projections(
204
            projections_train, projections_test, y_train)
205
206
        # Compute the accuracy classification score.
207
208
        accuracy = accuracy_score(y_test, y_pred)
209
210
        print(f"Accuracy: {accuracy*100}%")
211
```