

Algoritmos Numéricos

Exercício 01

1. Soluções dos Sistemas

a. $[-2 \ 3 \ 1; \ 2 \ 1 \ -4; \ 7 \ 10 \ -6] * [x_1; \ x_2; \ x_3] = [-5; \ -9; \ 2]$

I. Sem pivotação

```
raphael@raphael-ubuntu:~/Downloads/AlgNum/Ex01$ octave principal.m
QSocketNotifier: Can only be used with threads started with QThread
A =
   -2    3    1
    2    1   -4
    7   10   -6

b =
   -5
   -9
    2

n = 3
U =
   -2.0000    3.0000    1.0000
         0    4.0000   -3.0000
         0         0   12.8750

d =
   -5.0000
  -14.0000
   56.2500

Info = 0
x =
   4.3495  -0.2233   4.3689

r =
   8.8818e-16
         0
   1.7764e-15
```

II. Com pivotação

```
raphael@raphael-ubuntu:~/Downloads/AlgNum/Ex01$ octave principal.m
QSocketNotifier: Can only be used with threads started with QThread
A =
   -2    3    1
    2    1   -4
    7   10   -6

b =
   -5
   -9
    2

n = 3
U =
    7.0000   10.0000   -6.0000
         0    5.8571   -0.7143
         0         0   -2.5122

d =
    2.0000
   -4.4286
  -10.9756

Info = 0
x =
   4.3495  -0.2233   4.3689

r =
   8.8818e-16
         0
  -1.7764e-15
```

b. $\begin{bmatrix} 1 & -3 & 5 & 6 \\ -9 & 4 & -1 & 0 \\ 3 & 2 & -2 & 7 \\ 1 & 2 & 5 & -4 \end{bmatrix} \cdot \begin{bmatrix} x_1 \\ x_2 \\ x_3 \\ x_4 \end{bmatrix} = \begin{bmatrix} 17 \\ 29 \\ -11 \\ 7 \end{bmatrix}$

III. Sem pivotação

```
raphael@raphael-ubuntu:~/Downloads/AlgNum/Ex01$ octave principal.m
QSocketNotifier: Can only be used with threads started with QThread
A =
    1   -3    5    6
   -9    4   -1    0
    3    2   -2    7
    1    2    5   -4

b =
    17
    29
   -11
     7

n = 4
U =
    1.0000   -3.0000    5.0000    6.0000
     0  -23.0000   44.0000   54.0000
     0     0    4.0435   14.8261
     0     0     0   -33.3333

d =
    17.000
   182.000
    25.043
   -29.677

Info = 0
x =
   -3.6452  -0.2194   2.9290   0.8903

r =
     0
 7.1054e-15
     0
 1.7764e-15
```

IV. Com pivotação

```
raphael@raphael-ubuntu:~/Downloads/AlgNum/Ex01$ octave principal.m
QSocketNotifier: Can only be used with threads started with QThread
A =
    1   -3    5    6
   -9    4   -1    0
    3    2   -2    7
    1    2    5   -4

b =
    17
    29
   -11
     7

n = 4
U =
   -9.0000    4.0000   -1.0000     0
     0    3.3333   -2.3333    7.0000
     0     0    6.6000   -9.1333
     0     0     0   15.6566

d =
    29.0000
   -1.3333
   11.2000
   13.9394

Info = 0
x =
   -3.6452  -0.2194   2.9290   0.8903

r =
     0
 -3.5527e-15
  1.7764e-15
  6.2172e-15
```

$$c. \begin{bmatrix} 0 & 1 & 3 & 2 & 4 \\ 8 & -2 & 9 & -1 & 2 \\ 5 & 1 & 1 & 7 & 2 \\ -2 & 4 & 5 & 1 & 0 \\ 7 & -3 & 2 & -4 & 1 \end{bmatrix} * \begin{bmatrix} x_1 \\ x_2 \\ x_3 \\ x_4 \\ x_5 \end{bmatrix} = \begin{bmatrix} 3 \\ -5 \\ 6 \\ -1 \\ 8 \end{bmatrix}$$

V. Sem pivotação

```
raphael@raphael-ubuntu:~/Downloads/AlgNum/Ex01$ octave principal.m
QSocketNotifier: Can only be used with threads started with QThread
A =
    0    1    3    2    4
    8   -2    9   -1    2
    5    1    1    7    2
   -2    4    5    1    0
    7   -3    2   -4    1

b =
    3
   -5
    6
   -1
    8

n = 5
U =
    0    1.0000    3.0000    2.0000    4.0000
  8.0000   -2.0000    9.0000   -1.0000    2.0000
  5.0000    0    5.5000    6.5000    3.0000
  -2.0000    0    0   -28.1818   -8.5455
  7.0000    0    0    0    0.9097

d =
    3.0000
   -5.0000
    3.5000
  -25.6364
   12.7290

Info = 1
```

VI. Com pivotação

```
raphael@raphael-ubuntu:~/Downloads/AlgNum/Ex01$ octave principal.m
QSocketNotifier: Can only be used with threads started with QThread
A =
    0    1    3    2    4
    8   -2    9   -1    2
    5    1    1    7    2
   -2    4    5    1    0
    7   -3    2   -4    1

b =
    3
   -5
    6
   -1
    8

n = 5
U =
  8.0000   -2.0000    9.0000   -1.0000    2.0000
    0    3.5000    7.2500    0.7500    0.5000
    0    0   -9.2857    7.1429    0.4286
    0    0    0   -5.3846   -0.7231
    0    0    0    0    3.5643

d =
   -5.0000
   -2.2500
   10.5714
    7.8308
    8.3357

Info = 0
x =
    2.3475    4.3543   -2.3908   -1.7683    2.3387

r =
    0
  -1.7764e-15
  8.8818e-16
  3.3307e-15
  8.8818e-16
```

2. Comparação dos Vetores Resíduos

Sistema	Norma de Máxima Coluna do Vetor Resíduo, $\ r\ _\infty$	
	Sem Pivotação	Com Pivotação
a	3.3307e-15	1.7764e-15
b	7.1054e-15	6.2172e-15
c	-	3.3307e-15