

Questão 01 – Defina Sistemas Digitais? Quais suas vantagens e desvantagens com relação aos sistemas analógicos?

É uma combinação de dispositivos projetados para manipular informação lógica ou quantidades físicas que são representadas no formato digital;

Sistemas Digitais	
Vantagens	Desvantagens
São mais fáceis de serem projetados;	Necessidade de converter sinais analógicos em digitais;
Fácil armazenamento de informação;	O processamento dos sinais digitalizados requer tempo;
* Maior exatidão e precisão;	
A operação pode ser programada;	
São menos afetados por ruído;	
CI's podem ser fabricados com mais circuitos internos;	

Decimal (base 10)	Binário (base 2)	Octal (base 8)	Hexadecimal (base 16)	Base b (4)
830385	11001010101110110001	3125661	CABB1	3022232301
20	10100	24	14	110
3,25	11,01	3,2	3,4	3,1
72	001001000	110	48	1020

$$20_{(10)} = b^2 + b^1 + 0 \cdot b^0 = 20$$

$$b_1 = 4, \quad b_2 = -5$$

$$\underline{11,01} \\ 3,1$$

$$\underline{11001010101110110001} \\ 3022232301$$

$$20 = \frac{1}{16} \frac{0}{8} \frac{1}{4} \frac{0}{2} \frac{0}{1} = 10100_{(2)} \text{ hello}$$

$$\underline{110}_{(8)}, \underline{001}, \underline{001}, \underline{000} = 001001001_{(2)}$$

$$\begin{array}{ccccccc} \text{CABB1} & = & \underline{1100} & \underline{1010} & \underline{1011} & \underline{1011} & \underline{0001} \\ \downarrow \downarrow \downarrow & & & & & & \\ 12 & 10 & 8 & 4 & 2 & 1 & 0 \end{array} = 11001010101110110001$$

$$\underline{11,01}_{(2)} = 2^0 + 2^1 + 2^{-2} = 1 + 2 + 0,25 = 3,25_{(10)}$$

$$\begin{array}{ccccccc} \text{1100} & \text{1010} & \text{1011} & \text{1011} & \text{0001} \\ \downarrow & \downarrow & \downarrow & \downarrow & \downarrow \\ 12 & 10 & 8 & 4 & 2 & 1 & 0 \end{array} \quad \begin{array}{l} 1 \cdot 2^{15} + 1 \cdot 2^{14} + 0 \cdot 2^{13} + 0 \cdot 2^{12} + 1 \cdot 2^{11} + 0 \cdot 2^{10} + 1 \cdot 2^9 + 0 \cdot 2^8 + 1 \cdot 2^7 + 0 \cdot 2^6 + 1 \cdot 2^5 + \\ 1 \cdot 2^4 + 0 \cdot 2^3 + 0 \cdot 2^2 + 0 \cdot 2^1 + 1 \cdot 2^0 = 524.288 + 262.144 + 32.768 + 8.192 + 2048 + \\ 512 + 256 + 128 + 32 + 16 + 1 = 830.385_{(10)} \end{array}$$

$$\underline{001001001}_{(2)} = 2^0 + 2^3 + 2^6 = 1 + 8 + 64 = 73_{(10)}$$

$$\begin{array}{ccccccc} 3 & 1 & 2 & 5 & 6 & 6 & 1 \\ \downarrow & \downarrow & \downarrow & \downarrow & \downarrow & \downarrow & \downarrow \\ 0 & 1 & 1 & 0 & 0 & 1 & 0 & 1 & 0 & 1 & 1 & 1 & 0 & 1 & 1 & 0 & 0 & 0 & 1 \end{array} = 3125661_{(8)}$$

$$\begin{array}{cc} \begin{array}{ccc} 2 & 4 & \\ \downarrow & \downarrow & \\ 0 & 0 & 1 & 0 & 1 & 0 & 0 \end{array} = 24_{(4)} \\ \begin{array}{ccc} 1 & 4 & \\ \downarrow & \downarrow & \\ 0 & 0 & 1 & 0 & 1 & 0 & 0 \end{array} = 14_{(16)} \end{array} \quad \begin{array}{ccc} 0 & 1 & 0 & 0 & 1 & 0 & 0 & 1 \\ \downarrow & \downarrow & \downarrow & \downarrow & \downarrow & \downarrow & \downarrow & \downarrow \\ 4 & 9 & & & & & & \end{array} = 49_{(16)}$$

$$\begin{array}{ccc} 3 & 2 & \\ \downarrow & \downarrow & \\ 0 & 0 & 1 & 1 & , & 0 & 1 & 0 & 0 \end{array} = 3,2$$

$$\begin{array}{ccc} 3 & 4 & \\ \downarrow & \downarrow & \\ 0 & 0 & 1 & 1 & , & 0 & 1 & 0 & 0 \end{array} = 3,4$$

3) Porque o número 8 não existe na sequência octal (0,1,2,3,4,5,6,7)

4) a)
$$\begin{array}{r} 10101 \\ \times 11 \\ \hline 10101 \\ 10101+ \\ \hline 111111 \end{array}$$

b)
$$\begin{array}{r} 111 \\ 100110 \\ \times 1010 \\ \hline 110000 \end{array}$$

c)
$$\begin{array}{r} 110 \quad | 10 \\ 10 \quad 11 \\ \hline 010 \\ 10 \\ \hline 00 \end{array}$$

$$\begin{array}{r} 10,1101 \\ \times 0,1011 \\ \hline 11101 \\ 11101+ \\ 100000++ \\ 1101++++ \\ 00000++++ \\ \hline 0,10001111 \end{array}$$

d)
$$111,01 \quad | 10,1$$

$$\begin{array}{r} 11101 \quad | 1010 \\ -1010 \quad 10,11100... \\ \hline 010010 \\ -1010 \\ \hline 010000 \leftarrow \\ -1010 \\ \hline 001100 \\ 1010 \\ \hline 001000 \end{array}$$

e)
$$10110,1101 \quad | 1,1000$$

$$\begin{array}{r} 101101101 \quad | 11000 \\ -11000 \downarrow \\ 0101011 \\ -11000 \downarrow \\ 0100110 \\ -11000 \downarrow \\ 0011101 \\ 11000 \\ \hline 00101000 \\ -11000 \\ \hline 0100000 \\ -11000 \\ \hline 001000 \end{array}$$

5) a) $20/4 = 5$ dígitos hexa b) $2^{20} = 1048576$

c) $\underline{0} \underline{0} \underline{0} \underline{0} \underline{0}$ a $\underline{F} \underline{F} \underline{F} \underline{F} \underline{F}$

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a) $(+30) = 00011110 \xrightarrow{C1} 11100001 \xrightarrow{C2} (-30) 11100010$
 $(+15) = 00001111 \xrightarrow{C2} 11110000 \xrightarrow{C2} (-15) 11110000$
 $+ \rightarrow 000101101 = 45$
 32168471
 $(1)11010010 \rightarrow \text{negative}$

overflow

b) $(+84) = 01010100$
 $(+56) = 00111000$
 $(1)0001100 \rightarrow \text{overflow}$

c) $-97 + 78$

$(+97) = 01100001 \xrightarrow{C1} 10011110 \xrightarrow{C2} 10011111$
 $(+78) = 01001110$
 $+ 01001110$
 $11101101 \rightarrow \text{negative}$
 00010010
 10011
 19
 $\therefore -19$

$75(8) - 30(8)$

e) $(+75)_8 = 00111101 = 61_{(10)}$

$(+30)_8 = 00011000 = 24_{(10)} \xrightarrow{C1} 11100111 \rightarrow 11101000$
 $100100101 \rightarrow 37_{(10)} \text{ e } 45(8)$
 $\rightarrow \text{positivo}$

f) $-22(16) - 10(16)$

$00100010 = 34 \xrightarrow{C1} 11011101 \xrightarrow{C2} 11011110$
 $00011101 = 29$
 11100010
 11100011
 $(1)11000001 \rightarrow \text{negative}$
 00111110
 1
 00111111
 $-3 F(16)$
 $= 63(10)$

Decimal

7) a)
$$\begin{array}{r} 0111 \ 0100 \\ 0010 \ 0011 \\ \hline 1001 \ 0111 \end{array}$$

 b)
$$\begin{array}{r} 0110 \ 0010 \ 0011 \\ 0101 \ 1001 \ 1001 \\ \hline 1011 \ 1011 \ 1100 \\ + 0110 \ 0110 \ 0110 \\ \hline 10010 \ 00100010 \end{array}$$
 (BCD) = 1222 (10)

→ 97 (10)

c)
$$\begin{array}{r} 0101 \ 1000 \ 1000 \ 1000 \\ 0011 \ 1001 \ 1001 \\ \hline 0101 \ 1100 \ 0010 \ 0001 \\ + 0110 \ 0110 \ 0110 \\ \hline 0110 \ 00101000 \ 0111 \end{array}$$
 (BCD) = 6287

8) a)
$$\begin{array}{r} 3E91 \\ + 2F93 \\ \hline 6E24 \end{array}$$

 b)
$$\begin{array}{r} 91B \\ 6F2 \\ \hline 100D \end{array}$$

 c)
$$\begin{array}{r} D191 \\ AAAB \\ \hline 17C3C \end{array}$$

 d)
$$\begin{array}{r} FFFF \\ - 2F93 \\ \hline D06C \\ + 1 \\ \hline D06D \end{array}$$
 + 3E91 + D06D = OEFE
 ① OEFE
 ↳ descartar

2F00 < 4000

$$\begin{array}{r} FFFF \\ - EF00 \\ \hline 10FF \\ + 1 \\ \hline 1000 \end{array}$$

$$\begin{array}{r} FFFF \\ + C000 \\ \hline EF00 \\ + 1 \\ \hline C000 \end{array}$$

9)
$$\begin{array}{l} y=C \\ x=4 \\ z=8 \end{array}$$

$$\begin{array}{r} FFF FFF \\ - 1E9 27Q \\ \hline E16 D8(F-Q) \\ + 1 \\ \hline E16 D8(F-Q+1) \end{array}$$

$$\begin{aligned} 8 + (F - Q + 1) &= 7 \\ 8 + 15 - Q + 1 &= 14 \\ Q = 10 &\rightarrow Q = A \end{aligned}$$

$$\begin{array}{l} 4C7PE8 \\ + E16D8A \\ \hline \end{array}$$

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a)
$$5A_{(16)} = 90_{(10)} \quad B^2 + 3 \cdot B^1 + 2 = 90$$

$$x = 8$$

b)
$$20_{(10)} = c^2 + c^1 + 0 \cdot c^0 = 20$$

$$x = 4, \quad x = -5$$

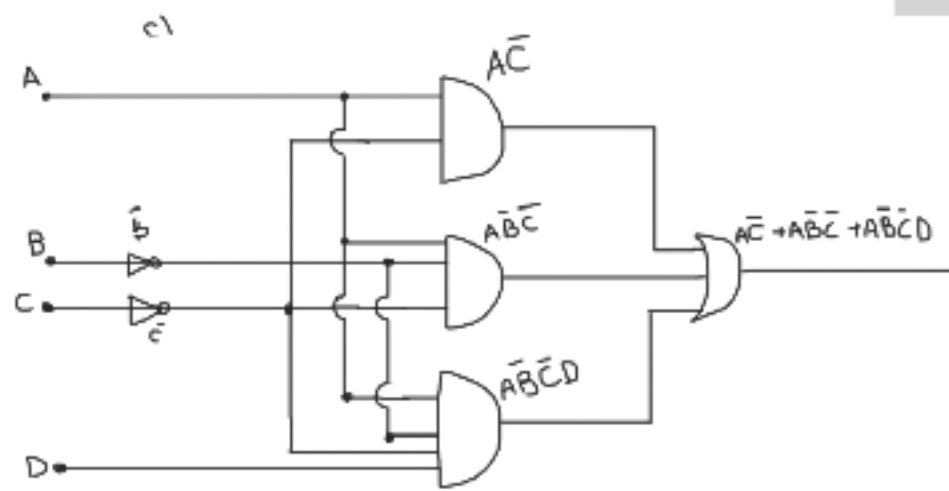
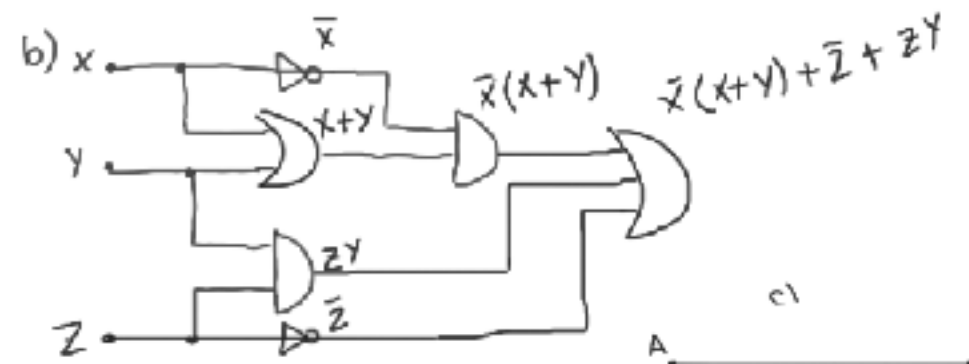
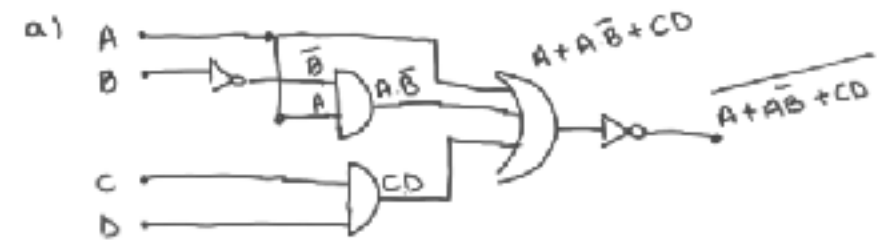
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- | | | |
|----|----|--|
| a) | 6D | → 0110 1101 X |
| b) | A3 | → 1010 0011 → Alterado - 2 - Escrita ✓ - Ñ protegido |
| c) | FB | → 1111 1011 → Alterado - 7 - Escrita X - Ñ protegido |
| d) | 57 | → 0101 0111 → Inalterado - 5 - Escrita ✓ - Protegido |

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	a	b	c
	6 3 2 -1	7 3 1 -2	8 7 -4 -2
0	0 0 0 0	0 0 0 0	0 0 0 0
1	0 0 1 1	0 1 0 1	0 1 1 1
2	0 0 1 0	0 1 1 1	1 0 1 1
3	0 1 0 0	0 1 0 0	0 1 1 0
4	0 1 1 1	0 1 1 0	1 0 1 0
5	1 0 1 0	1 0 0 1	0 1 0 1
6	1 0 0 0	1 0 1 1	1 0 0 1
7	1 0 1 1	1 0 0 0	0 1 0 0
8	1 0 1 0	1 0 1 0	1 0 0 0
9	1 1 0 0	1 1 1 1	1 1 1 1

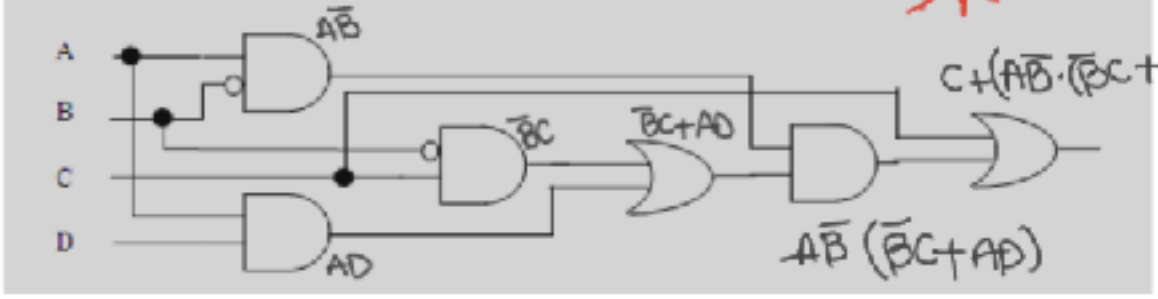
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	A	B	C	D	B+C	B	C	B+C	A(B+C)	a) A(B+C) + (B+C)	B+C	B+D	b) A(B+C)(B+D)	AC	AC	B C	c) AC + B C
0	0	0	0	0	0	1	1	1	0	0	1	1	0	0	1	1	1
1	0	0	0	1	0	1	1	1	0	0	1	1	0	0	1	1	1
2	0	0	1	0	1	1	0	1	0	0	0	1	0	0	1	0	1
3	0	0	1	1	1	1	0	1	0	0	0	1	0	0	1	0	1
4	0	1	0	0	1	0	1	1	0	0	1	0	0	0	1	0	1
5	0	1	0	1	1	0	1	1	0	0	1	1	0	0	1	0	1
6	0	1	1	0	1	0	0	0	0	0	1	0	0	0	1	0	1
7	0	1	1	1	1	0	0	0	0	0	1	1	0	0	1	0	1
8	1	0	0	0	0	1	1	1	1	0	1	1	1	0	1	1	1
9	1	0	0	1	0	1	1	1	1	0	1	1	1	0	1	1	1
10	1	0	1	0	1	1	0	1	1	1	0	1	0	1	0	0	0
11	1	0	1	1	1	1	0	1	1	1	0	1	0	1	0	0	0
12	1	1	0	0	1	0	1	1	1	1	1	0	0	0	1	0	1
13	1	1	0	1	1	0	1	1	1	1	1	1	1	0	1	0	1
14	1	1	1	0	1	0	0	0	0	0	1	0	0	1	0	0	0
15	1	1	1	1	1	0	0	0	0	0	1	1	1	1	0	0	0

Questão 15 - Dado o circuito lógico:



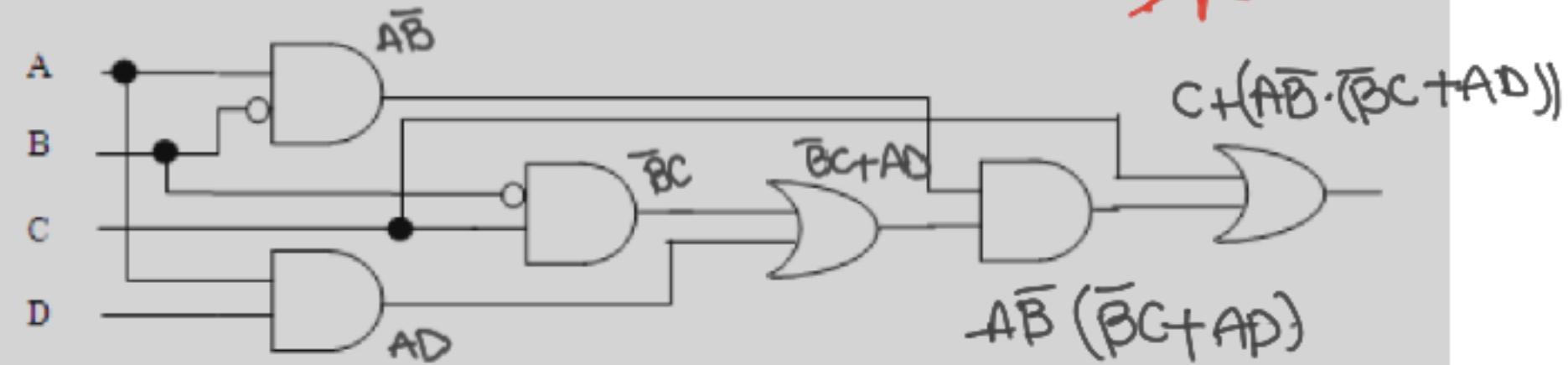
a) $C + AB(BC+AD)$

b)

	A	B	C	D	B	W	X	Y	Z	K	C+K
0	0	0	0	0	1	0	0	0	0	0	0
1	0	0	0	1	1	0	0	0	0	0	0
2	0	0	1	0	1	0	1	0	1	0	1
3	0	0	1	1	1	0	1	0	1	0	1
4	0	1	0	0	0	0	0	0	0	0	0
5	0	1	0	1	0	0	0	0	0	0	0
6	0	1	1	0	0	0	0	0	0	0	1
7	0	1	1	1	0	0	0	0	0	0	1
8	1	0	0	0	1	1	0	0	0	0	0
9	1	0	0	1	1	1	0	1	1	1	1
10	1	0	1	0	1	1	1	0	1	1	1
11	1	0	1	1	1	1	1	1	1	1	1
12	1	1	0	0	0	0	0	0	0	0	0
13	1	1	0	1	0	0	0	1	1	0	0
14	1	1	1	0	0	0	0	0	0	0	1
15	1	1	1	1	0	0	0	1	1	0	1

c) 1

Questão 15 - Dado o circuito lógico:



a) Defina a expressão lógica de saída;

b) Apresente a tabela de verdade;

c) Qual o valor lógico da saída para a seguinte condição de entrada

$A=D=0$ e $B=C=1$;

a) $C + A\bar{B}(\bar{B}C + AD)$

b)

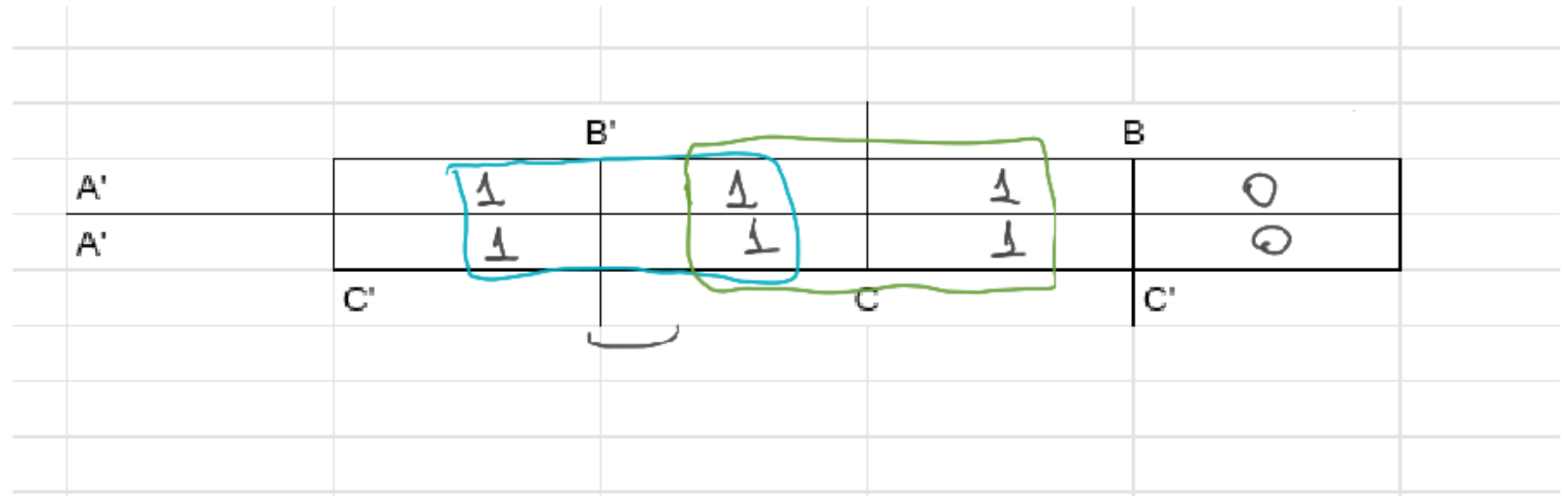
	A	B	C	D	\bar{B}	$A\bar{B}$	$\bar{B}C$	AD	$X+Y$	WZ	$C+K$
0	0	0	0	0	1	0	0	0	0	0	0
1	0	0	0	1	1	0	0	0	0	0	0
2	0	0	1	0	1	0	1	0	1	0	1
3	0	0	1	1	1	0	1	0	1	0	1
4	0	1	0	0	0	0	0	0	0	0	0
5	0	1	0	1	0	0	0	0	0	0	0
6	0	1	1	0	0	0	0	0	0	0	1
7	0	1	1	1	0	0	0	0	0	0	1
8	1	0	0	0	1	1	0	0	0	0	0
9	1	0	0	1	1	1	0	1	1	1	1
10	1	0	1	0	1	1	1	0	1	1	1
11	1	0	1	1	1	1	1	1	1	1	1
12	1	1	0	0	0	0	0	0	0	0	0
13	1	1	0	1	0	0	0	1	1	0	0
14	1	1	1	0	0	0	0	0	0	0	1
15	1	1	1	1	0	0	0	1	1	0	1

c) = 1

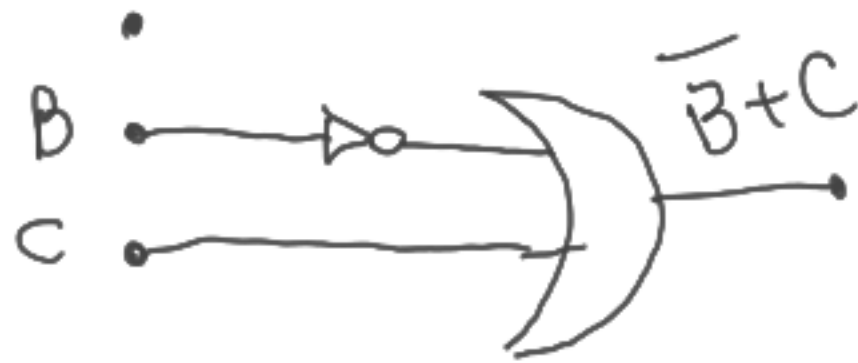
Questão 16 - Considere a seguinte tabela de verdade:

A	B	C	f(A, B, C)	\overline{B}
0	0	0	1	1
0	0	1	1	1
0	1	0	0	0
0	1	1	1	0
1	0	0	1	1
1	0	1	1	1
1	1	0	0	0
1	1	1	1	0

- Escreva a expressão da função f(A, B, C);
- Implemente o circuito lógico.
- Simule esse circuito utilizando o software Circuit Maker;



$$\overline{B} + C$$



Questão 17 Através de manipulações algébricas, e utilizando os axiomas e os teoremas da álgebra de Boole binária que conhece, verifique as seguintes igualdades:

- a) $(A + \bar{B} + AB)(A + \bar{B})\bar{A}B = 0$; ✓
 b) $\overline{AB(D + D\bar{C})} + (A + D\bar{A}C)B = B$; ✓
 c) $[(\bar{B} + C)A] + (\bar{C}\bar{D}) = CD$.

$$\begin{aligned} \text{a)} & (A + \bar{B} + AB)(A + \bar{B})\bar{A}B \\ & (A + \bar{B} + AB)(\cancel{A\bar{A}}^0 + \cancel{\bar{A}B}^0) \\ & (A + \bar{B} + AB)(0) = 0 \end{aligned}$$

$$\begin{aligned} \text{b)} & \overline{AB(D + D\bar{C})} + (A + D\bar{A}C)B = \\ & \bar{A}\bar{B}\bar{D} + \bar{A}\bar{B}\bar{C}D + AB + \bar{A}B\bar{C}D \\ & (\cancel{C+C})^1 \bar{A}\bar{B}D + AB + \bar{A}B\bar{D} \\ & \bar{A}\bar{B}D + AB + \bar{A}B\bar{D} \\ & \bar{A}B(\cancel{D+\bar{D}})^1 + AB \rightarrow B(\bar{A} + A) = B \end{aligned}$$

$$\begin{aligned} \text{c)} & \overline{[(\bar{B} + C)A]} + (\bar{C}\bar{D}) \\ & \overline{[(\bar{B} + C)A]} \cdot \overline{\bar{C}\bar{D}} \\ & [(\bar{B} + C) + \bar{A}] \cdot CD \\ & (\bar{B} + C + \bar{A})CD \\ & CD\bar{B} + CD + \bar{A}CD \end{aligned}$$

$\rightarrow CD(\bar{B} + 1 + \bar{A}) = CD$

Questão 18 – Simplifique algebricamente:

- a) $ABCD + ABC\bar{D} + \bar{A}BC\bar{D} + \bar{A}B\bar{C}\bar{D} + \bar{A}\bar{B}C\bar{D} + \bar{A}\bar{B}\bar{C}\bar{D}$;
 b) $\bar{X} + XY\bar{Z} + \bar{Y}$;
 c) $XY + WXY\bar{Z} + \bar{X}Y$;
 d) $\bar{X}\bar{Y}Z + YZ + XZ$.

$$\begin{aligned} \text{a)} & \overline{ABCD} + \overline{ABC\bar{D}} + \overline{\bar{A}BC\bar{D}} + \overline{\bar{A}B\bar{C}\bar{D}} + \overline{\bar{A}\bar{B}C\bar{D}} + \overline{\bar{A}\bar{B}\bar{C}\bar{D}} \\ & ABC(\cancel{D+\bar{D}})^1 + \bar{A}B\bar{D}(\cancel{C+C})^1 + \bar{A}\bar{B}\bar{D}(\cancel{C+C})^1 \\ & ABC + \bar{A}B\bar{D} + \bar{A}\bar{B}\bar{D} \rightarrow ABC + \bar{A}\bar{D}(\cancel{B+\bar{B}})^1 \rightarrow \underline{ABC + \bar{A}\bar{D}} \end{aligned}$$

$$\begin{aligned} \text{b)} & \bar{X} + \underline{XY\bar{Z}} + \bar{Y} \\ & \bar{X} + \underline{Y\bar{Z}} + \bar{Y} \\ & \underline{\bar{X} + \bar{Z} + \bar{Y}} \end{aligned}$$

3ª identidade

$$\begin{aligned} A + \bar{A}B &= A + B \\ \hookrightarrow A + \bar{A}B &= \overline{\bar{A} + \bar{A}B} = \overline{\bar{A} \cdot \bar{A}\bar{B}} = \overline{\bar{A} \cdot (\bar{A} + \bar{B})} \\ &= \overline{\bar{A} \cdot (A + B)} = \overline{\bar{A} \cdot A + \bar{A} \cdot B} = \overline{\bar{A} \cdot B} = A + B \\ \bar{A} + AB &= \bar{A} + B \\ \hookrightarrow \bar{A} + AB &= \overline{\bar{\bar{A}} + \bar{A}B} = \overline{A \cdot (\bar{A} + B)} = \overline{A\bar{A} + A \cdot B} \\ &= \overline{A \cdot B} = \bar{A} + B \end{aligned}$$

$$\begin{aligned} \text{c)} & XY + WXY\bar{Z} + \bar{X}Y \\ & Y(\underline{X} + WX\bar{Z} + \underline{\bar{X}}) \\ & Y(1 + WX\bar{Z}) = Y \end{aligned}$$

$$\begin{aligned} \text{d)} & \bar{X}\bar{Y}Z + YZ + XZ \\ & Z(\bar{X}\bar{Y} + Y + X) \\ & Z(\underbrace{Y + \bar{X} + X}_1) = Z \end{aligned}$$

$$\begin{aligned} A + \bar{A}\bar{B} & \\ \hookrightarrow \overline{\bar{A} + \bar{A}\bar{B}} &= \overline{\bar{A} \cdot (\bar{A} + \bar{B})} = \overline{\bar{A} \cdot A + \bar{A} \cdot \bar{B}} = \overline{\bar{A} \cdot \bar{B}} = A + B \end{aligned}$$

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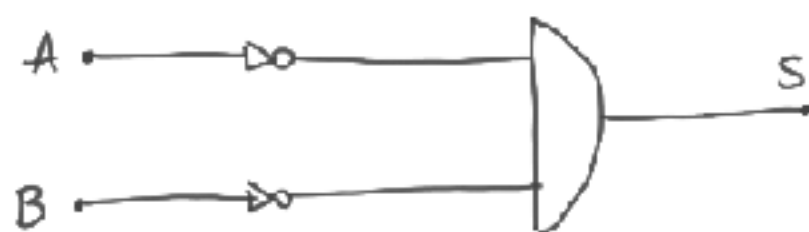
A	B	C	Z
0	0	0	0
0	0	1	1
0	1	1	0
0	1	0	1
1	1	0	0
1	1	1	1
1	0	1	0
1	0	0	1

$$\begin{aligned}
 Z &= \bar{A}\bar{B}C + \bar{A}B\bar{C} + ABC + A\bar{B}\bar{C} \\
 &= \bar{C}(\underbrace{\bar{A}B + A\bar{B}}_{A+B}) + C(\underbrace{\bar{A}\bar{B} + AB}_{A+B}) \\
 &= C \cdot (A+B) + C(\overline{A+B}) \\
 &= C + (A+B) = A+B+C
 \end{aligned}$$

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Sensor 4 bits = $2^4 = 16$ posibilidades

45/15 = 3 steps



l	A	B	C	D	S
0	0	0	0	0	1
3	0	0	0	1	1
6	0	0	1	0	1
9	0	0	1	1	1
⋮					0

$$Z = \bar{A}\bar{B}\bar{C}\bar{D} + \bar{A}\bar{B}\bar{C}D + \bar{A}\bar{B}C\bar{D} + \bar{A}\bar{B}CD$$

$$Z = \bar{A}\bar{B}\bar{C}(\bar{D}+D) + \bar{A}\bar{B}C(\bar{D}+D)$$

$$Z = \bar{A}\bar{B}\bar{C} + \bar{A}\bar{B}C$$

$$Z = \bar{A}\bar{B}(\bar{C}+C) = \boxed{\bar{A}\bar{B}}$$

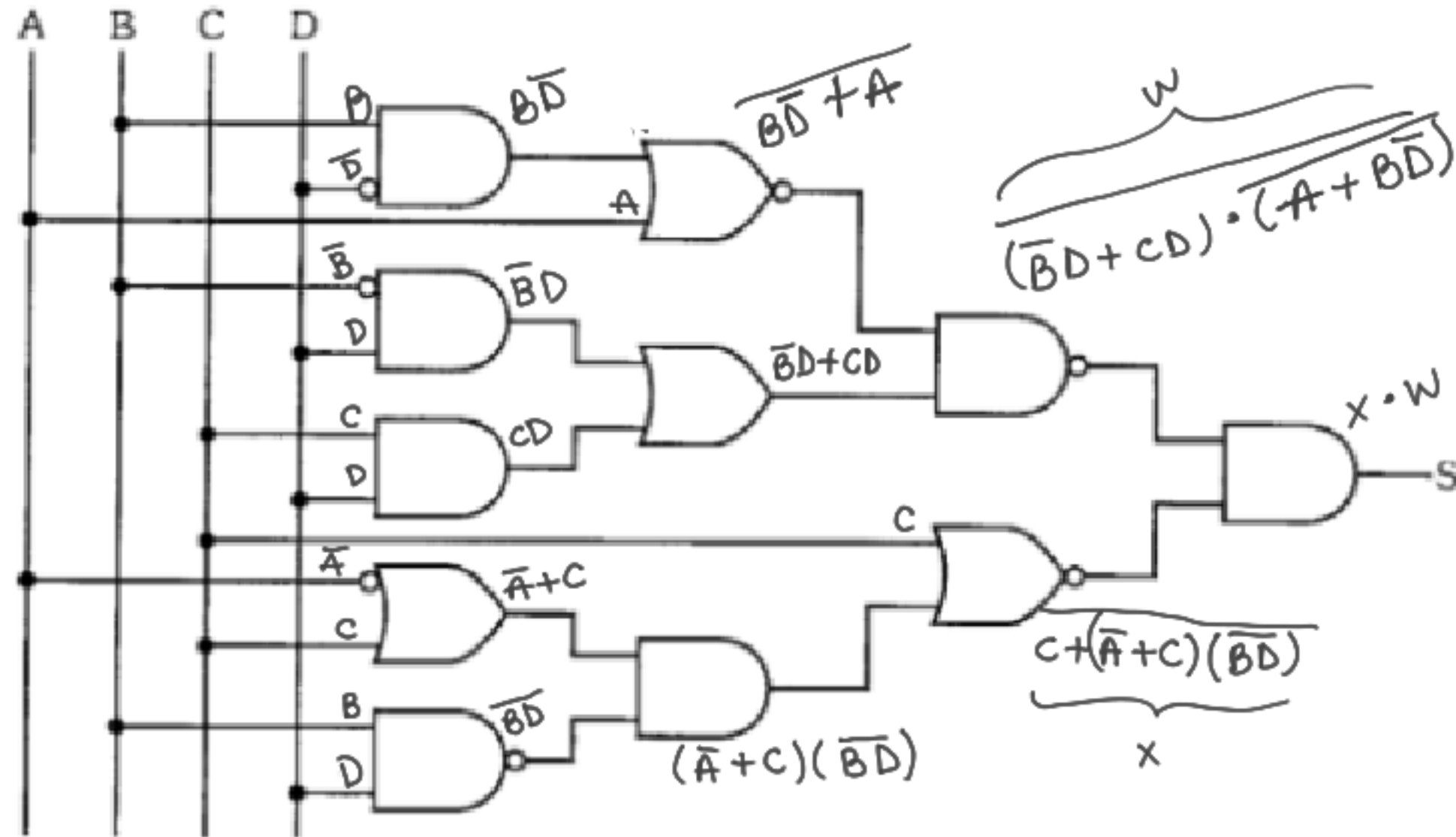
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$$\begin{aligned}
 a) A + \bar{A} \cdot B &= \overline{\overline{A + \bar{A} \cdot B}} = \overline{\bar{A} \cdot \overline{\bar{A} \cdot B}} = \overline{\bar{A} \cdot \bar{A} + \bar{A} \cdot B} \\
 &= \overline{\bar{A} \cdot (A+B)} = \overline{\bar{A} \cdot \bar{A} + \bar{A} \cdot B} = \overline{\bar{A} \cdot B} = \bar{A} + B \\
 &= A + B
 \end{aligned}$$

$$b) AB + \bar{A}C + BC$$

A	B	C	A_	AB	A_C	BC	AB+A_C	AB+A_C+BC
0	0	0	1	0	0	0	0	0
0	0	1	1	0	1	0	1	1
0	1	1	1	0	1	1	1	1
0	1	0	1	0	0	0	0	0
1	1	0	0	1	0	0	1	1
1	1	1	0	1	0	1	1	1
1	0	1	0	0	0	0	0	0
1	0	0	0	0	0	0	0	0

Questão 22 - Considerando o circuito digital abaixo, determine: (a) a expressão lógica, (b) a tabela da verdade, (c) a expressão simplificada e o (d) conseqüente circuito digital somente com portas NÃO e OU de duas entradas.



$$S = \overline{[(\bar{A} + C)(\bar{B}D)] + C} \cdot \overline{(\bar{B}D + CD) \cdot (A + B\bar{D})}$$

$$S = \left[\overline{(A + B\bar{D}) \cdot (\bar{B}D + CD)} \right] \left[\overline{C + (\bar{A} + C)(\bar{B}D)} \right]$$

$$[(A + \overline{BD}) + (\overline{BD} + CD)] [\overline{C} \cdot (\overline{A + C})(\overline{BD})]$$

$$[A + B\overline{D} + (\overline{B}\overline{D} \cdot \overline{C}\overline{D})][\overline{C} \cdot (\overline{A} + \overline{C}) + (\overline{B}\overline{D})]$$

$$[(A + B\bar{D}) + (B + \bar{D}) \cdot (\bar{C} + \bar{D})][\bar{C} \cdot (A\bar{C}) + (BD)]$$

$$[A + \underline{B\bar{D}} + B\bar{C} + \underline{B\bar{D}} + \underline{\bar{D}\bar{C}} + \underline{\bar{D}\bar{D}}][A\bar{C}\bar{C} + B\bar{C}D]$$

$$[A + B\bar{C} + \bar{D}(B + \bar{B} + \bar{C} + 1)][A\bar{C} + B\bar{C}D]$$

$$[A + B\bar{C} + \bar{D}][A\bar{C} + B\bar{C}D]$$

$$A\bar{A}\bar{C} + A\bar{B}\bar{C}D + A\bar{C}\bar{D} + \cancel{B\bar{C}\bar{D}D} + A\bar{B}\bar{C} + B\bar{B}\bar{C}\bar{C}D$$

$$A\bar{C} + AB\bar{C}D + A\bar{C}\bar{D} + AB\bar{C} + B\bar{C}D$$

$$\overline{C} (A + ABD + \overline{A}\overline{D} + AB + BD)$$

$$\overline{C} (A(\underbrace{1 + BD + \overline{D} + B}_1) + BD) \rightarrow \overline{C} (A + BD)$$

Questão 23: Demonstre a identidade de cada uma das seguintes equações lógicas:

a) $A + \overline{A}B = A + B$

b) $AB + \overline{A}C + B.C = AB + \overline{A}C$

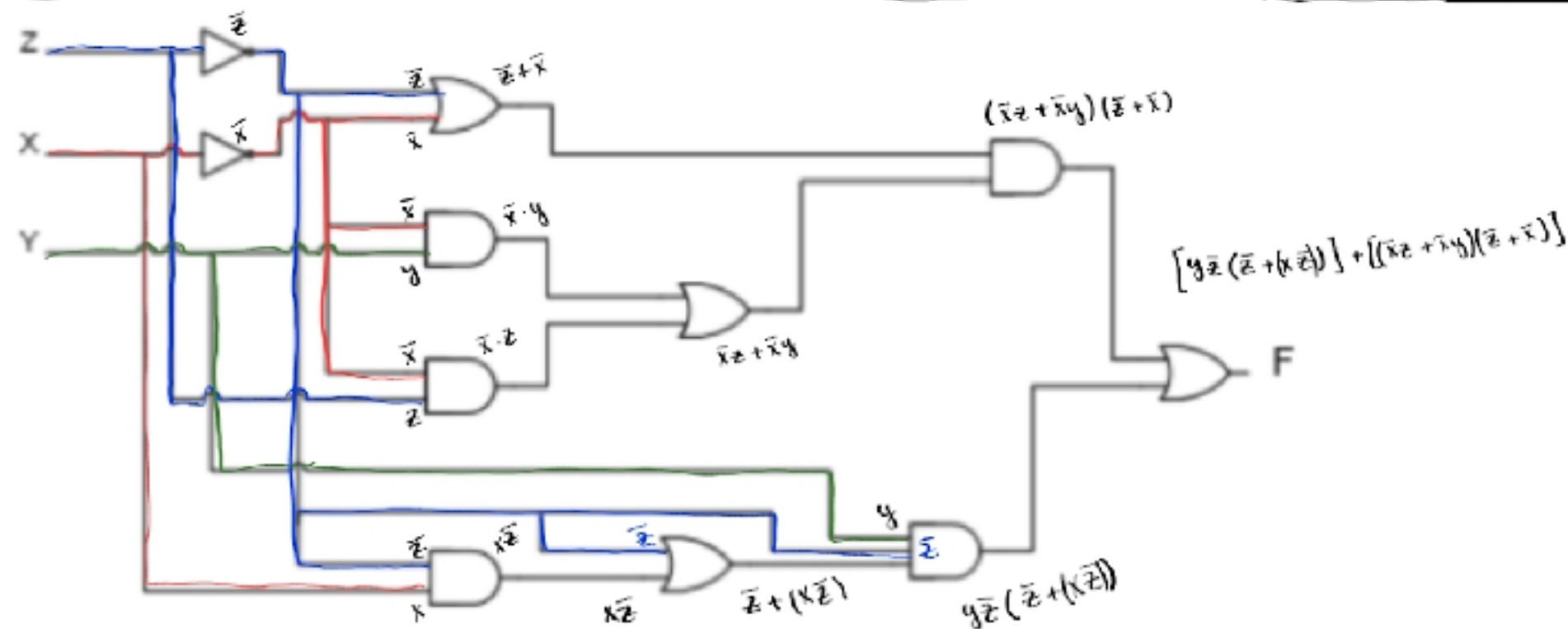
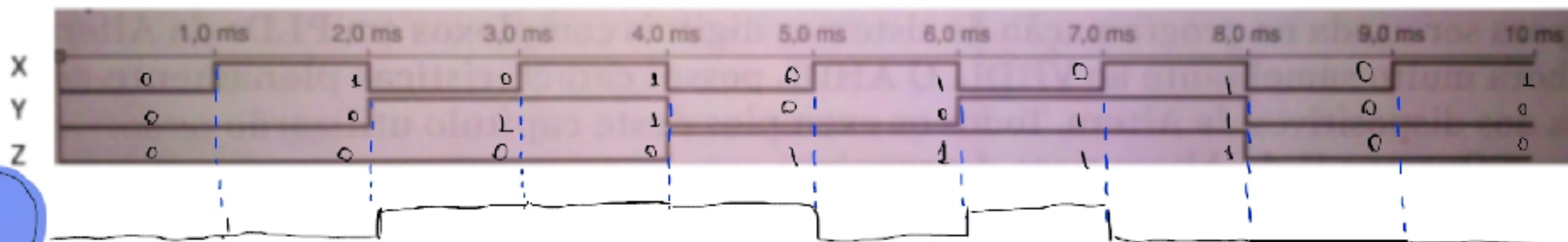
a) $A + \overline{A} \cdot B = \overline{\overline{A + \overline{A}B}} = \overline{\overline{A} \cdot \overline{\overline{A}B}} = \overline{\overline{A} \cdot \overline{\overline{A} + B}} = \overline{\overline{A} \cdot (A + \overline{B})} = \overline{\overline{A}A + \overline{A}\overline{B}} = \overline{\overline{A}\overline{B}} = \overline{\overline{A}} + \overline{\overline{B}} = A + B$

b) $AB + \overline{A}C + BC$

A	B	C	A_	AB	A_C	BC	AB+A_C	AB+A_C+BC
0	0	0	1	0	0	0	0	0
0	0	1	1	0	1	0	1	1
0	1	1	1	0	1	1	1	1
0	1	0	1	0	0	0	0	0
1	1	0	0	1	0	0	1	1
1	1	1	0	1	0	1	1	1
1	0	1	0	0	0	0	0	0
1	0	0	0	0	0	0	0	0

Questão 24 – Considerando o circuito digital abaixo, determine:

- a expressão lógica,
- a tabela da verdade,
- a expressão simplificada
- conseqüente circuito digital somente com portas NE (NAND) de duas entradas.
- A forma de onda do sinal saída para as seguintes condições de entrada:



$$\begin{aligned}
 & [y\bar{z}(\bar{x}+x\bar{z})] + [(\bar{x}z+\bar{x}y)(\bar{z}+\bar{x})] \\
 & [y\bar{z}(y\bar{z} \cdot \bar{z}(1+x))] + [\bar{x}z\bar{z} + \bar{x}\bar{x}z + \bar{x}yz + \bar{x}\bar{x}y] \\
 & [y\bar{z}(y\bar{z} \cdot \bar{z})] + [\bar{x}z + \bar{x}yz + \bar{x}y] \\
 & [y\bar{z}(\bar{z}(y+1))] + [\bar{x}(z+yz+y)] \\
 & [y\bar{z}] + [\bar{x}(z(1+y)+y)] \\
 & y\bar{z} + [\bar{x}(z+y)] \\
 & y\bar{z} + \bar{x}z + \bar{x}y \cdot 1 = (z+\bar{z})
 \end{aligned}$$

$$\begin{aligned}
 & \bar{x}y(z+\bar{z}) + y\bar{z} + \bar{x}z \\
 & \bar{x}yz + \bar{x}y\bar{z} + y\bar{z} + \bar{x}z \\
 & \bar{x}z(y+1) + y\bar{z}(\bar{x}+1) = \bar{x}z + y\bar{z}
 \end{aligned}$$

b

X	Y	Z	\bar{X}	\bar{Z}	$\bar{x}z$	$y\bar{z}$	S
0	0	0	1	1	0	0	0
0	0	1	1	0	1	0	1
0	1	0	1	1	0	1	1
0	1	1	1	0	1	0	1
1	0	0	0	1	0	0	0
1	0	1	0	0	0	0	0
1	1	0	0	1	0	1	1
1	1	1	0	0	0	0	0