

<https://github.com/UB-Quantic/Qubit-Calibration>

Qubit Calibration

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IFAE Summer Fellowship @ Quantum Computing Technology Group
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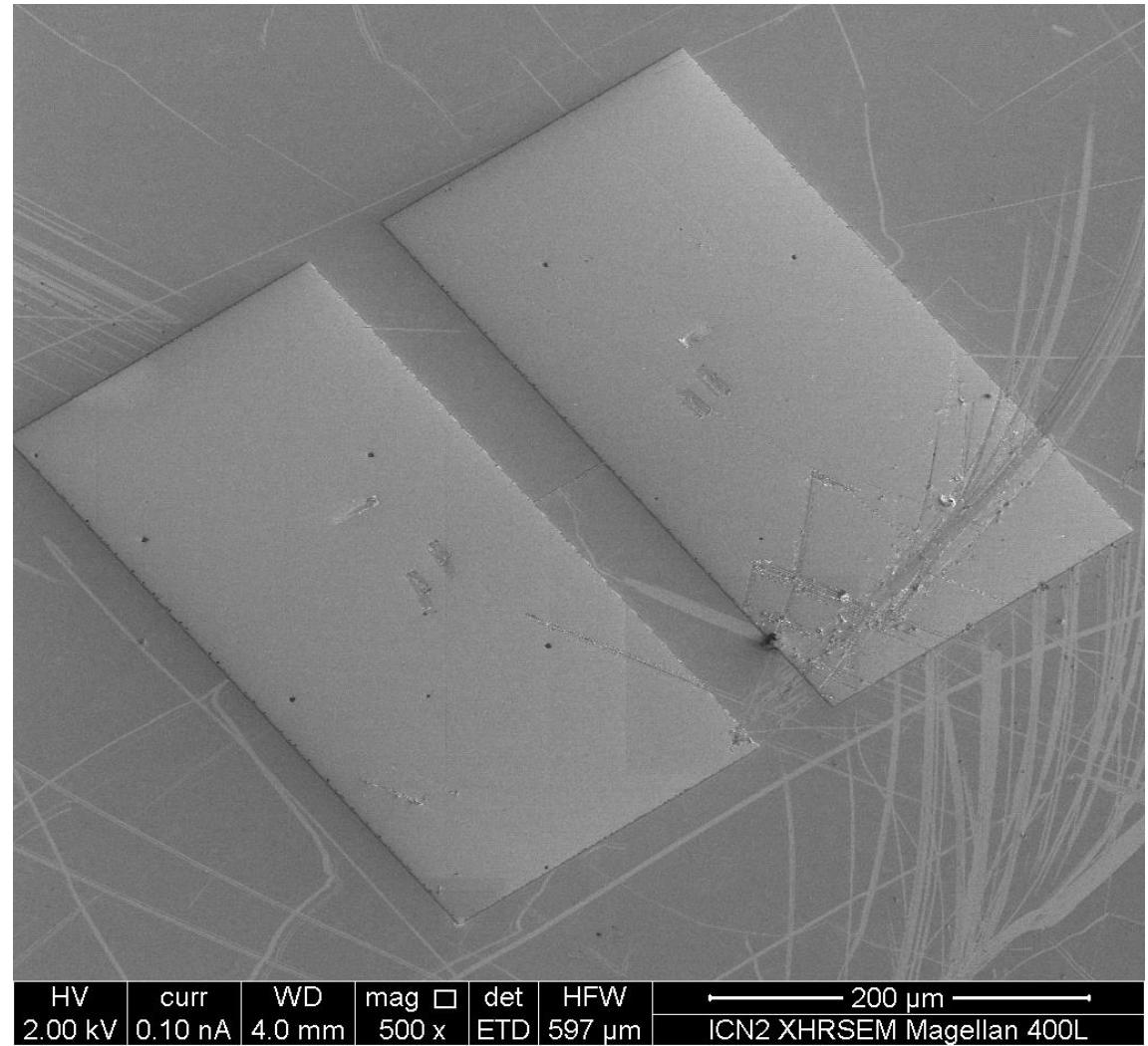
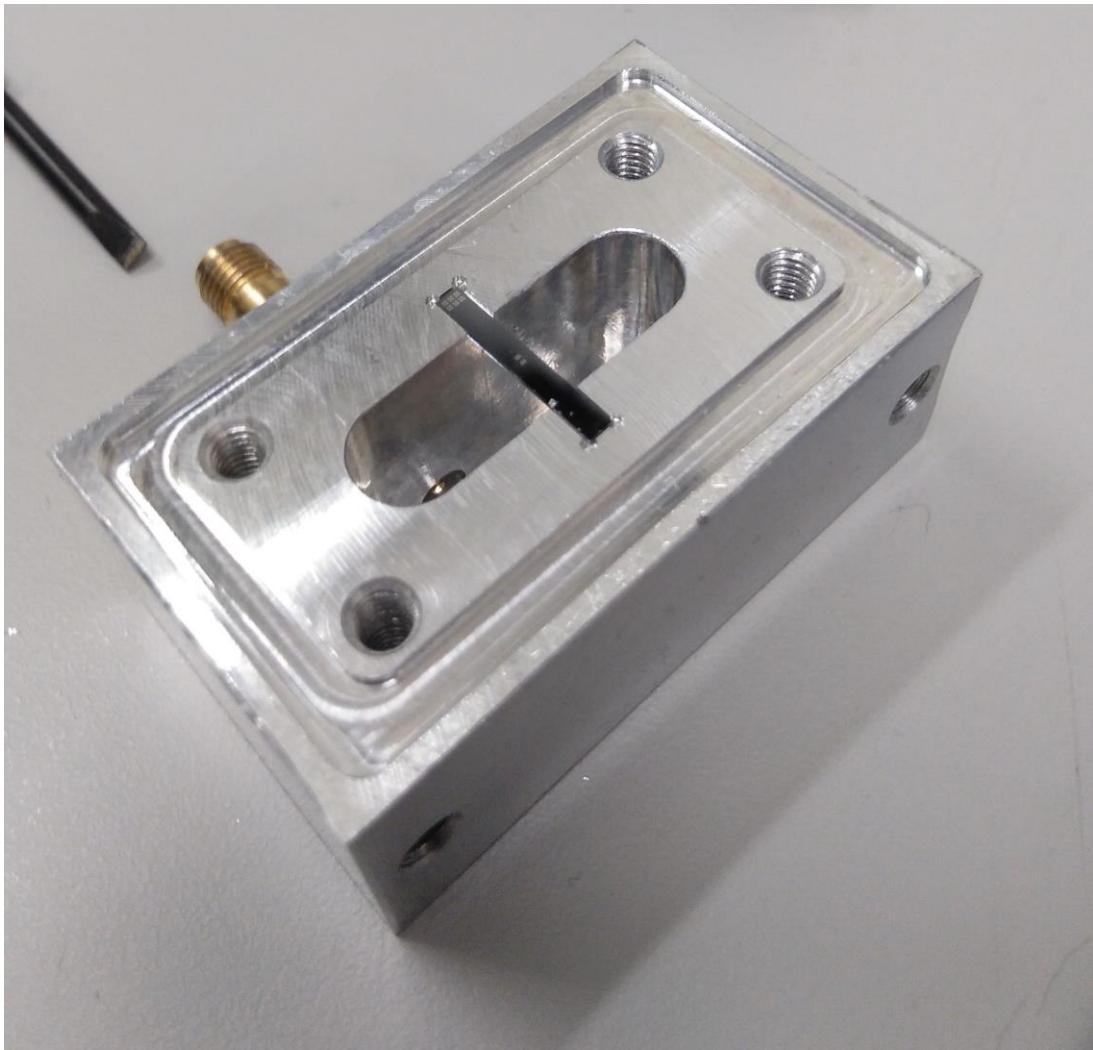
Outline

- Theoretical Background
- Technical Aspects
- Calibration Results
- DRAG scaling constant
- Reset Pulse

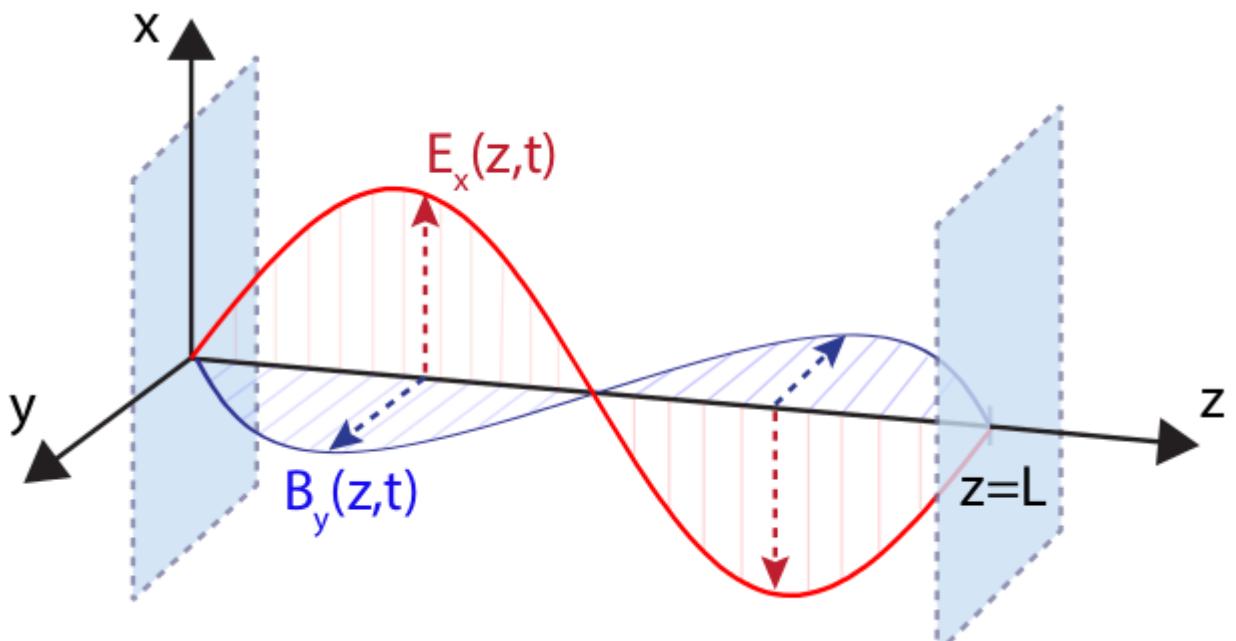
Theoretical Background

- [1] - P. Krantz, M. Kjaergaard, F. Yan, T. P. Orlando, S. Gustavsson, and W. D. Oliver, A quantum engineer's guide to superconducting qubits, *Appl. Phys. Rev.* 6, 021318 (2019).
- [2] - Naghiloo, M. (2019). Introduction to experimental quantum measurement with superconducting qubits. arXiv preprint arXiv:1904.09291.
- [6] - Sangil Kwon and Akiyoshi Tomonaga and Gopika Lakshmi Bhai and Simon J. Devitt and Jaw-Shen Tsai, Tutorial: Gate-based superconducting quantum computing. arXiv preprint arXiv:2009.08021, (2020)

Cavity Quantum Electrodynamics (cQED)



The cavity



$$\hat{H} = \omega_c \left(\hat{a}^\dagger \hat{a} + \frac{1}{2} \right)$$

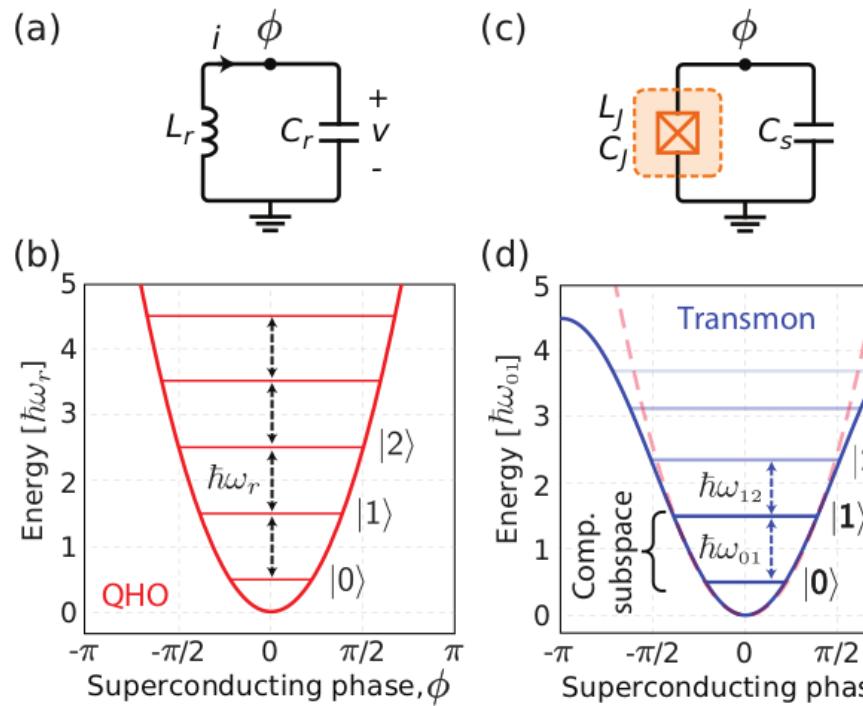
Photon number or Fock states

$$|n\rangle \quad n = 0, 1, 2, \dots$$

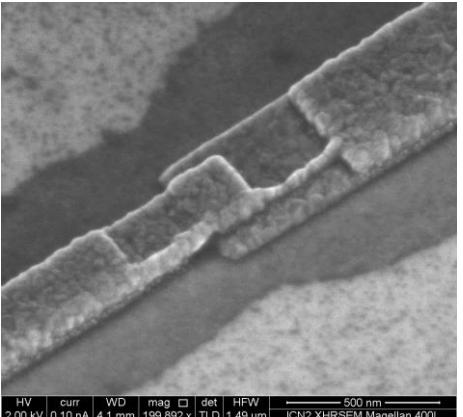
Coherent state

$$|\alpha\rangle = \sum_n c_n |n\rangle$$

The qubit



Ref. [1]



QCT @ IFAE

Nonlinear oscillator

$$\hat{H} = \omega_{01} \hat{b}^\dagger \hat{b} + \frac{\alpha}{2} \hat{b}^\dagger \hat{b}^\dagger \hat{b} \hat{b}$$

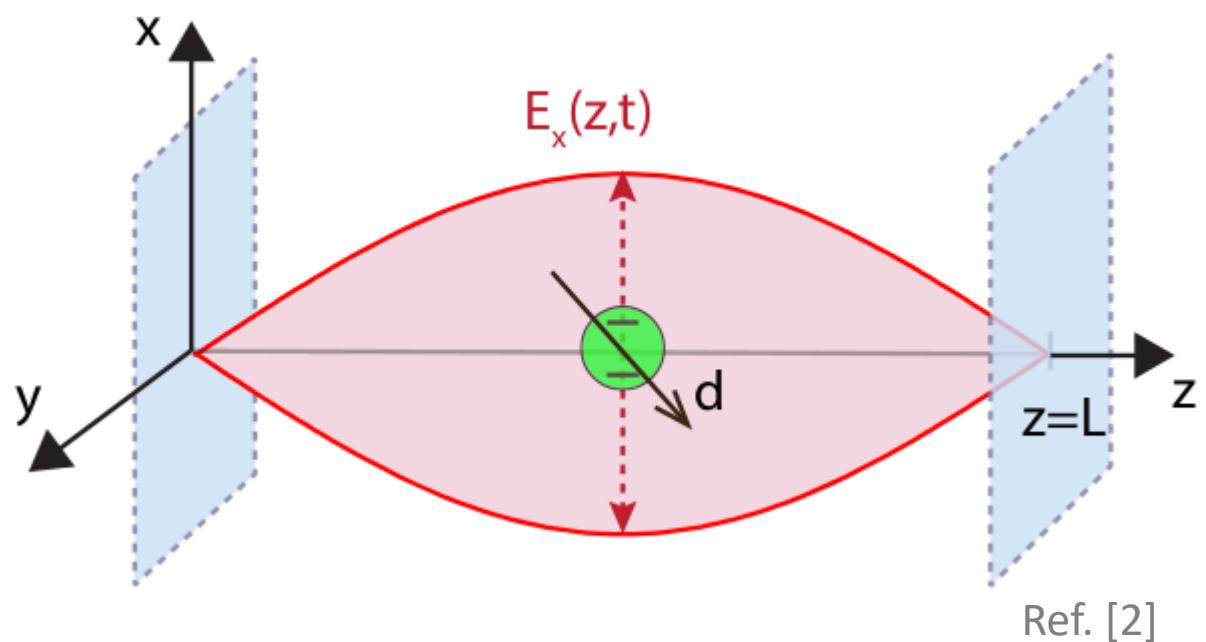
Reasonable anharmonicity:

$$\frac{\alpha}{2\pi} = E_{12} - E_{01} \sim -300 \text{ MHz}$$

Two-level system:

$$\hat{H} = -\frac{\omega_q}{2} \sigma_z$$

Jaynes-Cummings model



$$\theta_n = \frac{1}{2} \tan^{-1}(2g\sqrt{n+1}/\Delta)$$

$$\Delta = \omega_q - \omega_c$$

Dipole interaction

$$\hat{H}_{int} = -\hat{d} \cdot \hat{E}_x \left(\frac{L}{2}, t \right)$$

$$= -g(\hat{a}^\dagger + \hat{a})(\sigma_+ + \sigma_-)$$

Total Hamiltonian:

$$\hat{H} = \omega_c \left(\hat{a}^\dagger \hat{a} + \frac{1}{2} \right) - \frac{\omega_q}{2} \sigma_z - g(\hat{a}^\dagger + \hat{a})(\sigma_+ + \sigma_-)$$

No interaction ($g=0$):

Bare states $\{|g\rangle|n\rangle, |e\rangle|n\rangle\}$

After RWA:

$$\hat{H}_{JC} = \omega_c \left(\hat{a}^\dagger \hat{a} + \frac{1}{2} \right) - \frac{\omega_q}{2} \sigma_z - g(\hat{a}^\dagger \sigma_- + \hat{a} \sigma_+)$$

Dressed states

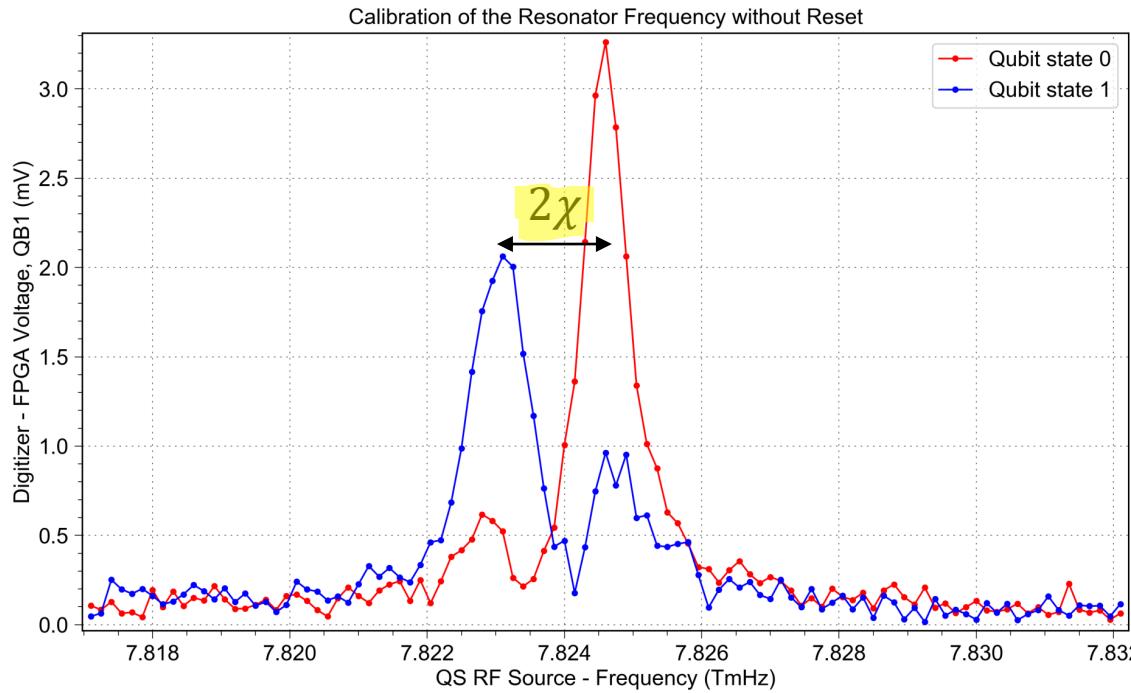
$$|0, -\rangle = |g\rangle|0\rangle$$

$$|n, -\rangle = \cos \theta_n |g\rangle|n+1\rangle - \sin \theta_n |e\rangle|n\rangle$$

$$|n, +\rangle = \sin \theta_n |g\rangle|n+1\rangle + \cos \theta_n |e\rangle|n\rangle$$

Dispersive regime $\Delta \gg g$

$$\hat{H}_{JC} = \omega_c \left(\hat{a}^\dagger \hat{a} + \frac{1}{2} \right) - \frac{\omega_q}{2} \sigma_z - g(\hat{a}^\dagger \sigma_- + \hat{a} \sigma_+)$$



$$\chi = \frac{g^2}{\Delta} \quad \text{Dispersive shift}$$

Unitary transformation

$$\hat{T} = e^{\frac{g}{\Delta}(\sigma_- a^\dagger - \sigma_+ a)}$$

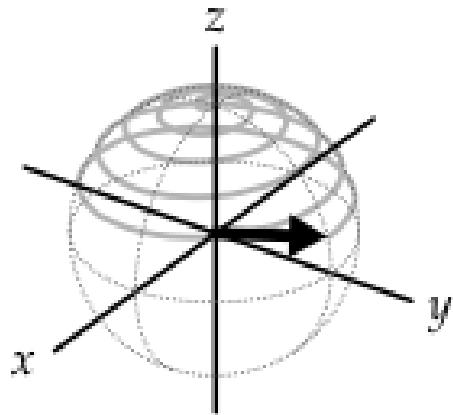
$$\hat{H}_{dis} = \omega_c \hat{a}^\dagger \hat{a} - \frac{1}{2} \omega_q \sigma_z - \frac{g^2}{\Delta} \hat{a}^\dagger \hat{a} \sigma_z$$

$$\hat{H}_{dis} = (\omega_c - \chi \sigma_z) \hat{a}^\dagger \hat{a} - \frac{1}{2} \omega_q \sigma_z$$

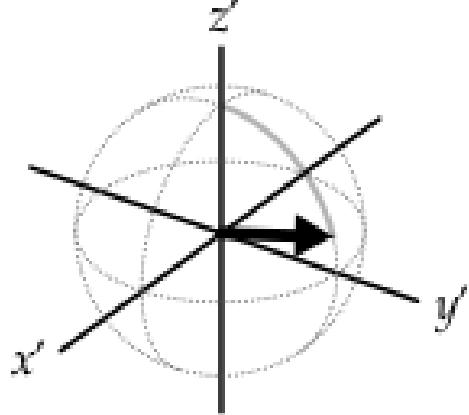
$$\hat{H}_{dis} = \omega_c \hat{a}^\dagger \hat{a} - \frac{1}{2} (\omega_q + 2\chi \bar{n}) \sigma_z$$

Driven qubit

Inertial frame



Rotating frame



Ref. [6]

$$v(t) = s(t) \sin(\omega_d t + \phi)$$

$$= s(t) (\cos \phi \sin(\omega_d t) + \sin \phi \cos(\omega_d t))$$

$$= s(t) (I \sin(\omega_d t) + Q \cos(\omega_d t))$$

$$I = \cos \phi$$

$$Q = \sin \phi$$

Rabi drive:

$$U_{rf,}^{\phi=0}(t) = \exp\left(\frac{i}{2}\Omega V_0 \int_0^t s(t') dt'\right) \sigma_x$$

$$H = -\underbrace{\frac{\omega_q}{2} \sigma_z}_{H_0} + \underbrace{\Omega V_0 v(t) \sigma_y}_{H_d}$$

Rotating frame

$$H = \underbrace{0}_{\tilde{H}_0} + \underbrace{\Omega V_0 v(t) (\cos(\omega_q t) \sigma_y - \sin(\omega_q t) \sigma_x)}_{\tilde{H}_d}$$

RWA

$$\tilde{H}_d = -\frac{\Omega}{2} V_0 s(t) \begin{pmatrix} 0 & e^{i(\delta\omega t + \phi)} \\ e^{-i(\delta\omega t + \phi)} & 0 \end{pmatrix}$$

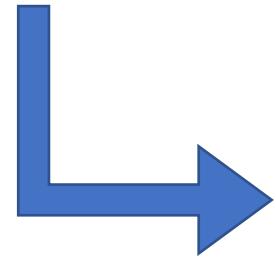
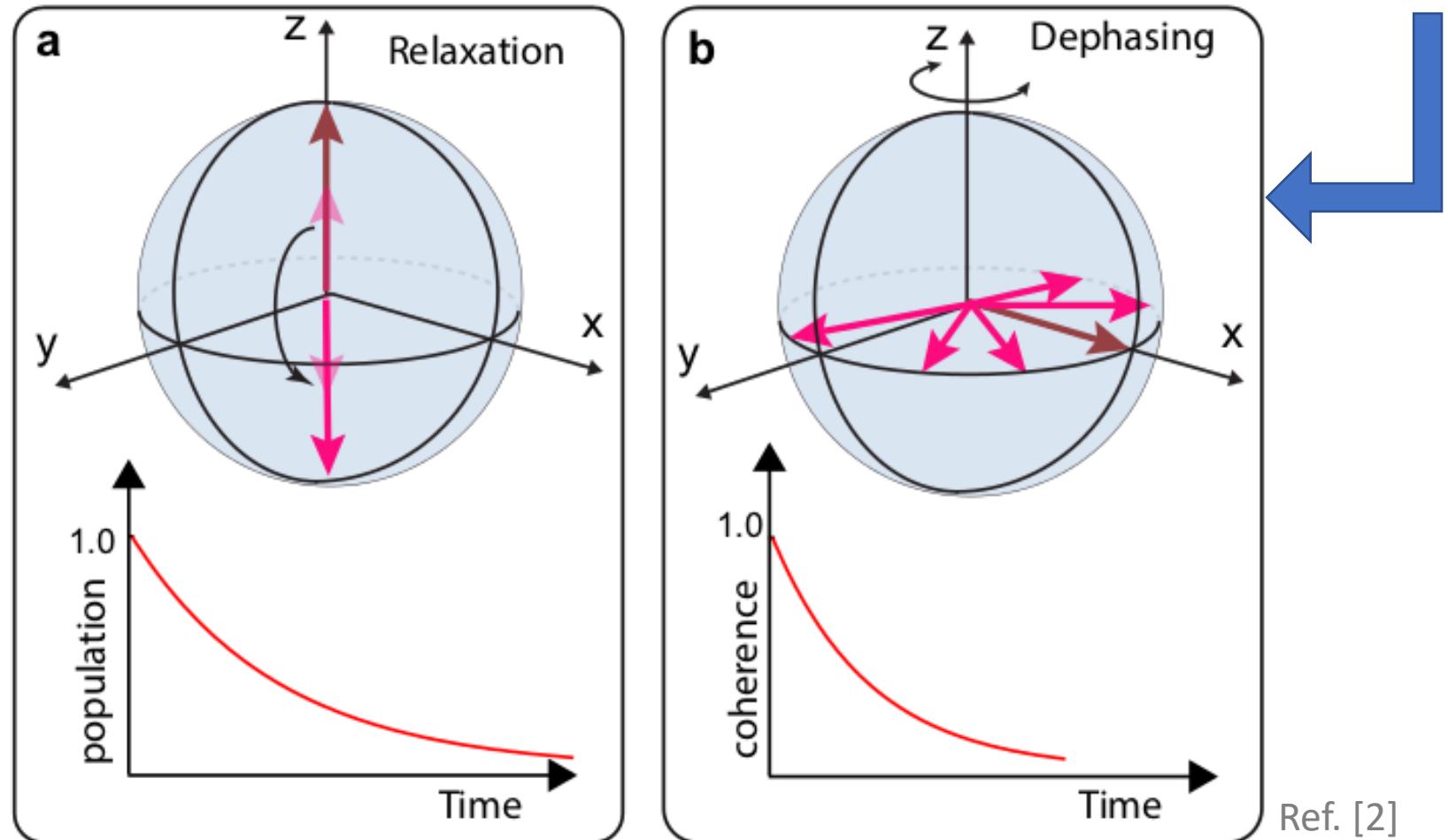
Without detuning:

$$\boxed{\tilde{H}_d = -\frac{\Omega}{2} V_0 s(t) (I \sigma_x + Q \sigma_y)}$$

Dissipation

$$P_e(t) = P_e(0)e^{-t/T_1}$$

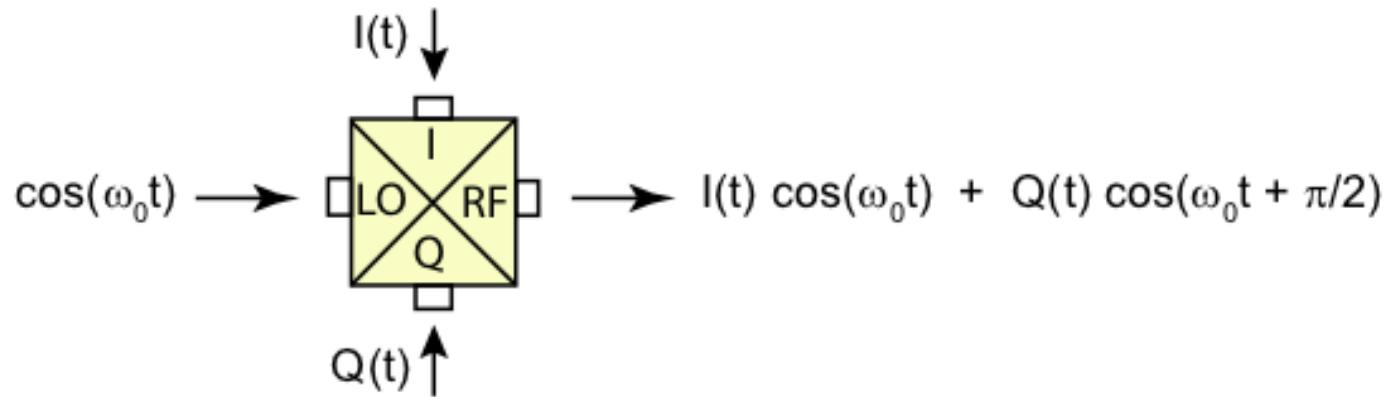
$$\frac{1}{T_2} = \frac{1}{2T_1} + \frac{1}{T_\varphi}$$

 T_2 

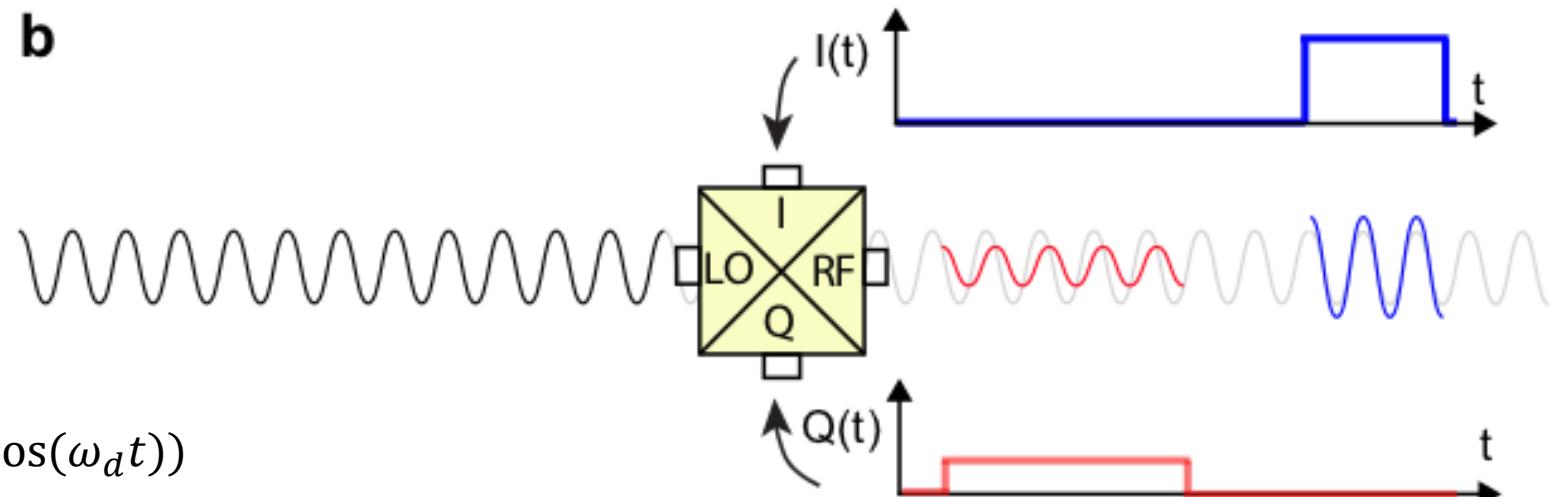
Technical Aspects

IQ mixing

a



b



$$v(t) = s(t) (\tilde{I} \sin(\omega_d t) + \tilde{Q} \cos(\omega_d t))$$

$$\tilde{H}_d = -\frac{\Omega}{2} V_0 s(t) (\tilde{I} \sigma_x + \tilde{Q} \sigma_y)$$

Single Sideband Modulation (SSB)

Signal leakage from LO to RF

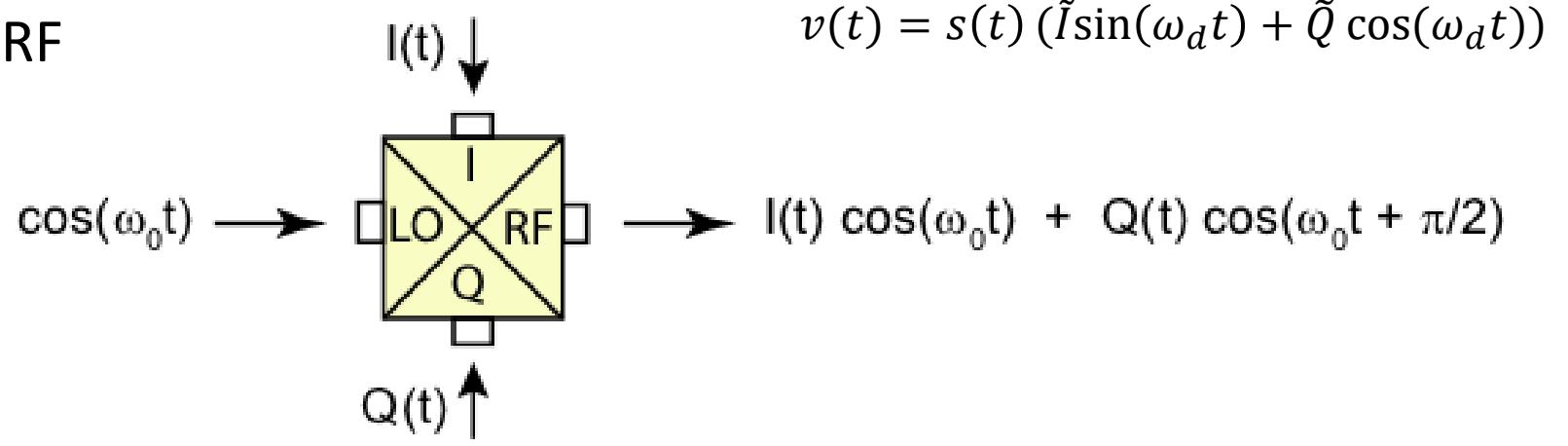
$$\omega_{LO} = \omega_d + \omega_{SSB}$$

$$\omega_{SSB} \sim 70\text{MHz}$$

Labber generates:

$$I(t) = s(t)(\tilde{I}\cos(\omega_{SSB}t - \phi) - \tilde{Q}\cos(\omega_{SSB}t - \phi + \pi/2))$$

$$Q(t) = s(t)(-\tilde{I}\sin(\omega_{SSB}t - \phi) + \tilde{Q}\sin(\omega_{SSB}t - \phi + \pi/2))$$



Single Sideband Modulation (SSB)

Signal leakage from LO to RF

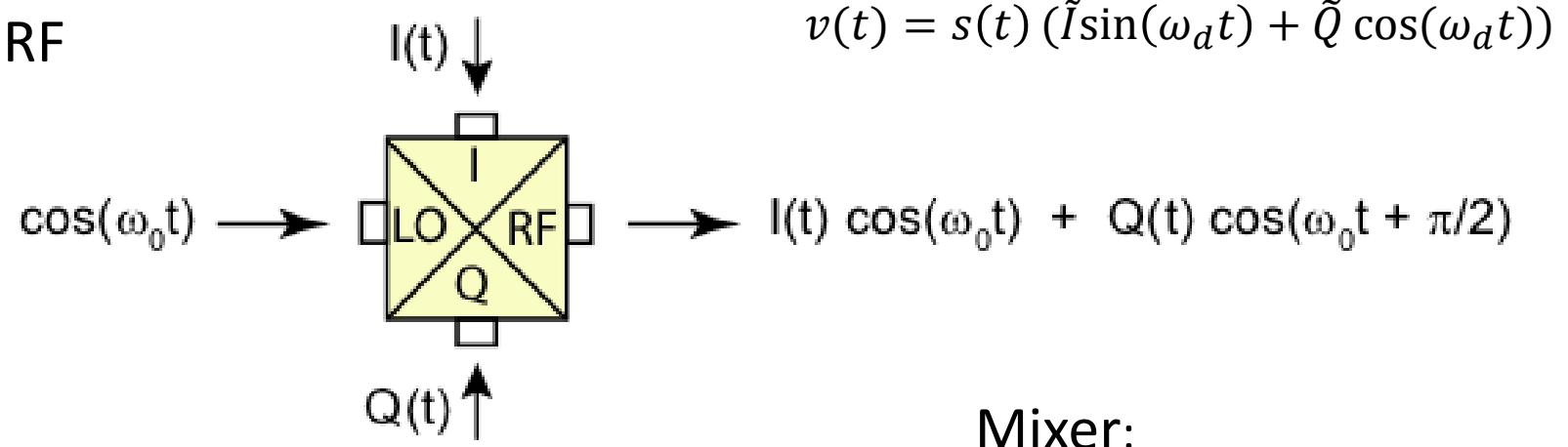
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Labber generates:

$$I(t) = s(t)(\tilde{I}\cos(\omega_{SSB}t - \phi) - \tilde{Q}\cos(\omega_{SSB}t - \phi + \pi/2)) \quad \times \cos(\omega_{LO}t)$$

$$Q(t) = s(t)(-\tilde{I}\sin(\omega_{SSB}t - \phi) + \tilde{Q}\sin(\omega_{SSB}t - \phi + \pi/2)) \quad \times \cos(\omega_{LO}t + \pi/2)$$



Single Sideband Modulation (SSB)

Signal leakage from LO to RF

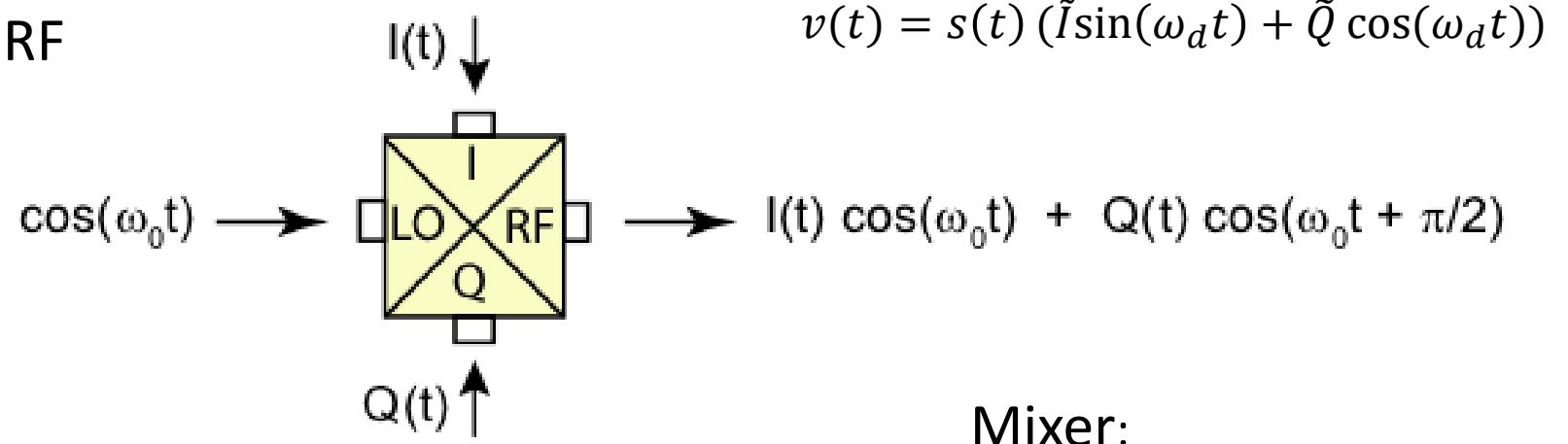
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$$I(t) = s(t)(\tilde{I}\cos(\omega_{SSB}t - \phi) - \tilde{Q}\cos(\omega_{SSB}t - \phi + \pi/2)) \quad \times \cos(\omega_{LO}t)$$

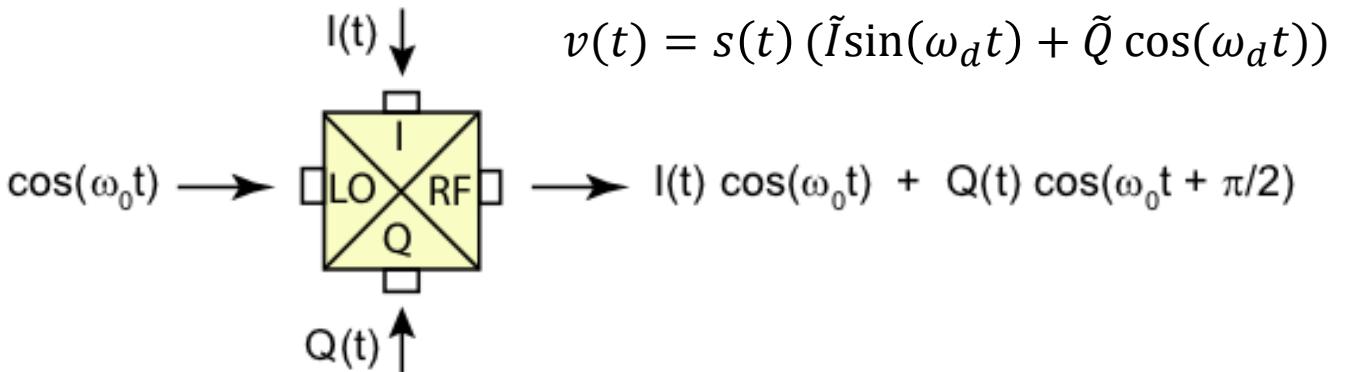
$$Q(t) = s(t)(-\tilde{I}\sin(\omega_{SSB}t - \phi) + \tilde{Q}\sin(\omega_{SSB}t - \phi + \pi/2)) \quad \times \cos(\omega_{LO}t + \pi/2)$$



$$s(t)(\tilde{I}\cos((\omega_{LO} - \omega_{SSB})t + \phi) - \tilde{Q}\sin((\omega_{LO} - \omega_{SSB})t + \phi))$$

Derivative Reduction by Adiabatic Gate (DRAG)

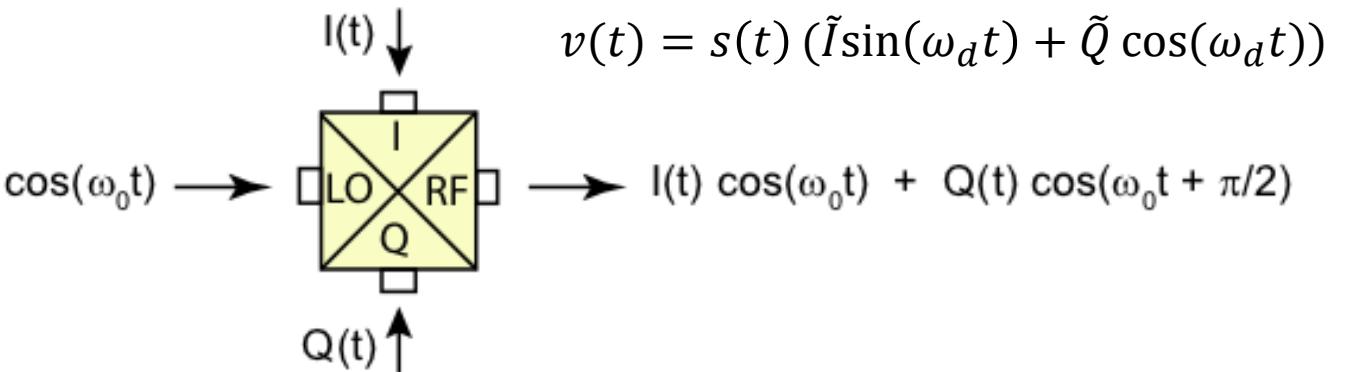
- **Leakage errors:** Excitations outside of the computational subspace
- **Phase errors:** Accumulation of a phase



$$s(t) \rightarrow \tilde{s}(t) = \begin{cases} s(t) & \text{on } \tilde{I} \\ \beta s'(t) & \text{on } \tilde{Q} \end{cases}$$

Derivative Reduction by Adiabatic Gate (DRAG)

- **Leakage errors:** Excitations outside of the computational subspace



- **Phase errors:** Accumulation of a phase

Labber generates:

$$s(t) \rightarrow \tilde{s}(t) = \begin{cases} s(t) & \text{on } \tilde{I} \\ \beta s'(t) & \text{on } \tilde{Q} \end{cases}$$

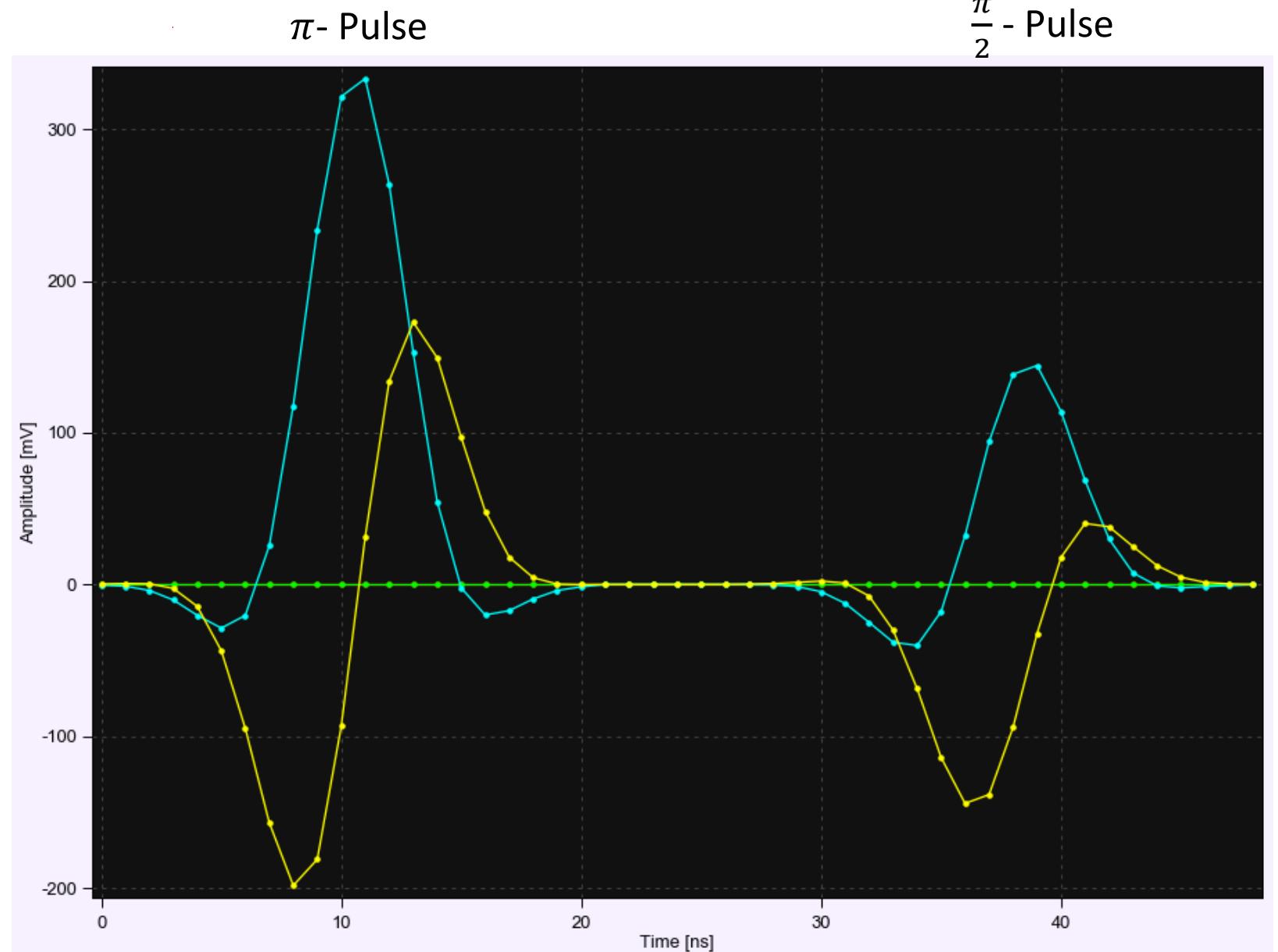
Mixer:

$$I(t) = s(t)\tilde{I}\cos(\omega_{SSB}t - \phi) - \beta s'(t)\tilde{Q}\cos(\omega_{SSB}t - \phi + \pi/2) \quad \times \cos(\omega_{LO}t) \quad +$$
$$Q(t) = -s(t)\tilde{I}\sin(\omega_{SSB}t - \phi) + \beta s'(t)\tilde{Q}\sin(\omega_{SSB}t - \phi + \pi/2) \quad \times \cos(\omega_{LO}t + \pi/2)$$

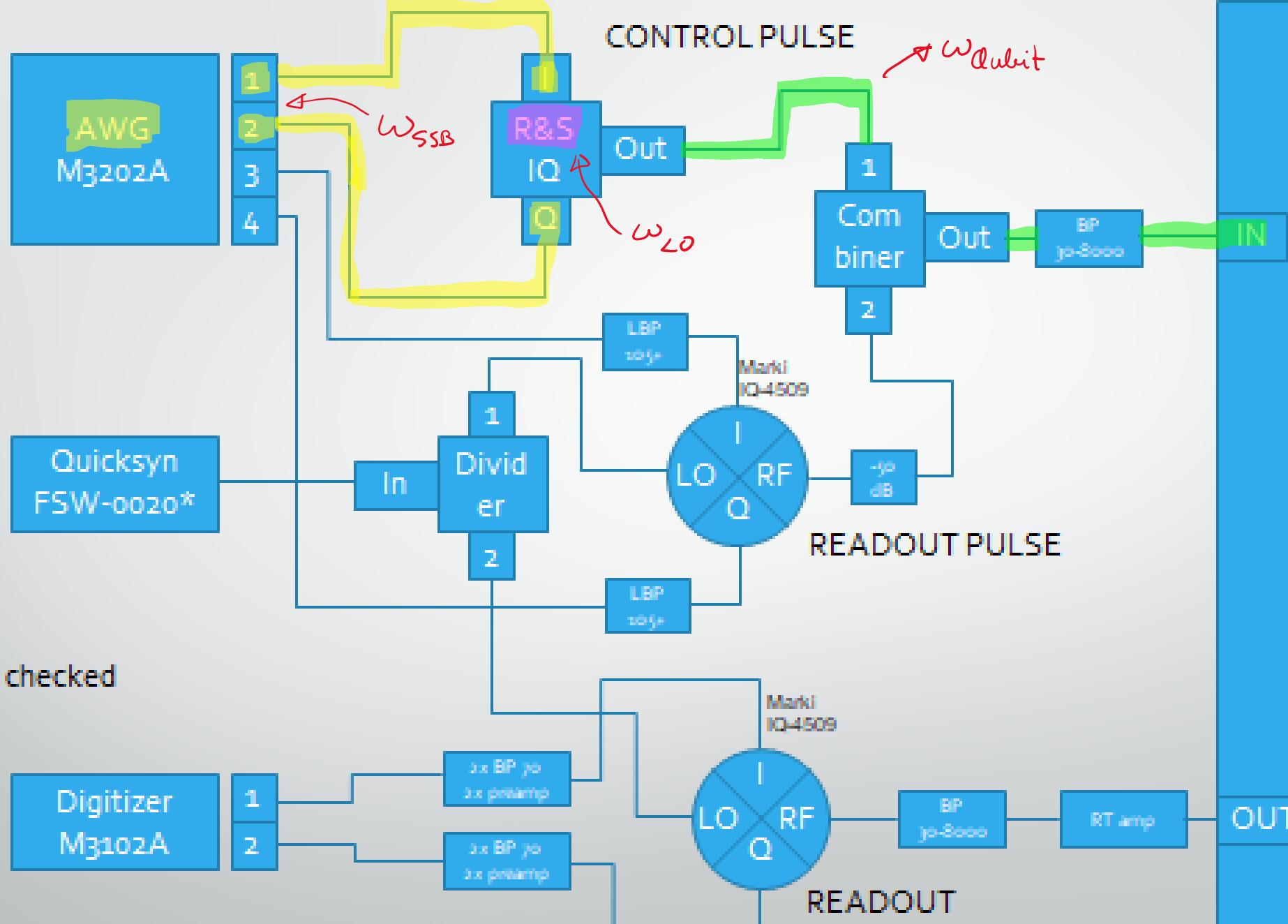
$$s(t)\tilde{I}\cos((\omega_{LO} - \omega_{SSB})t + \phi) - \beta s'(t)\tilde{Q}\sin((\omega_{LO} - \omega_{SSB})t + \phi)$$

Pulses

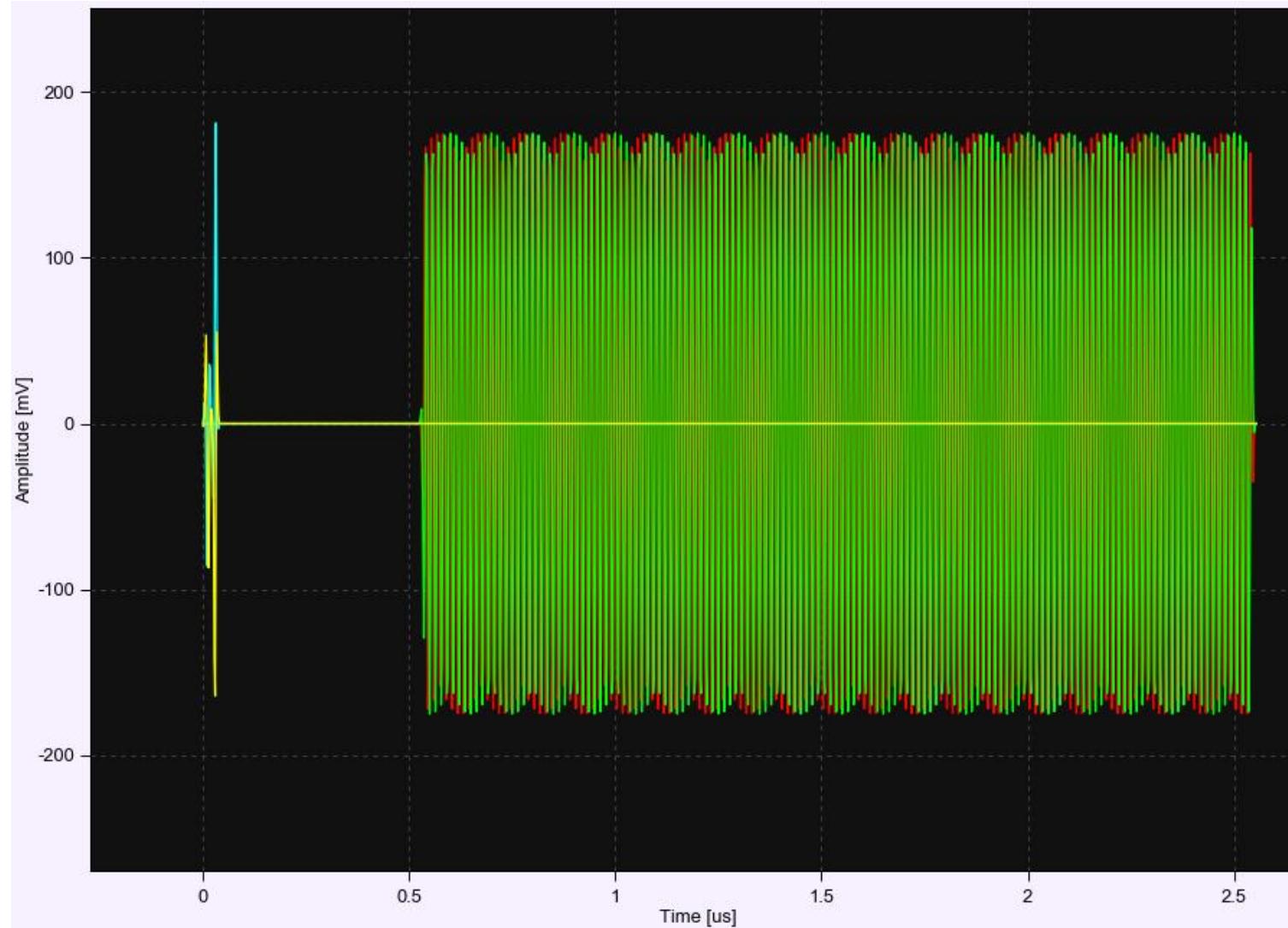
- Gaussian envelope
- SSB and DRAG
- Fixed width
- Variable:
 - Amplitude (Volts)
 - Phase



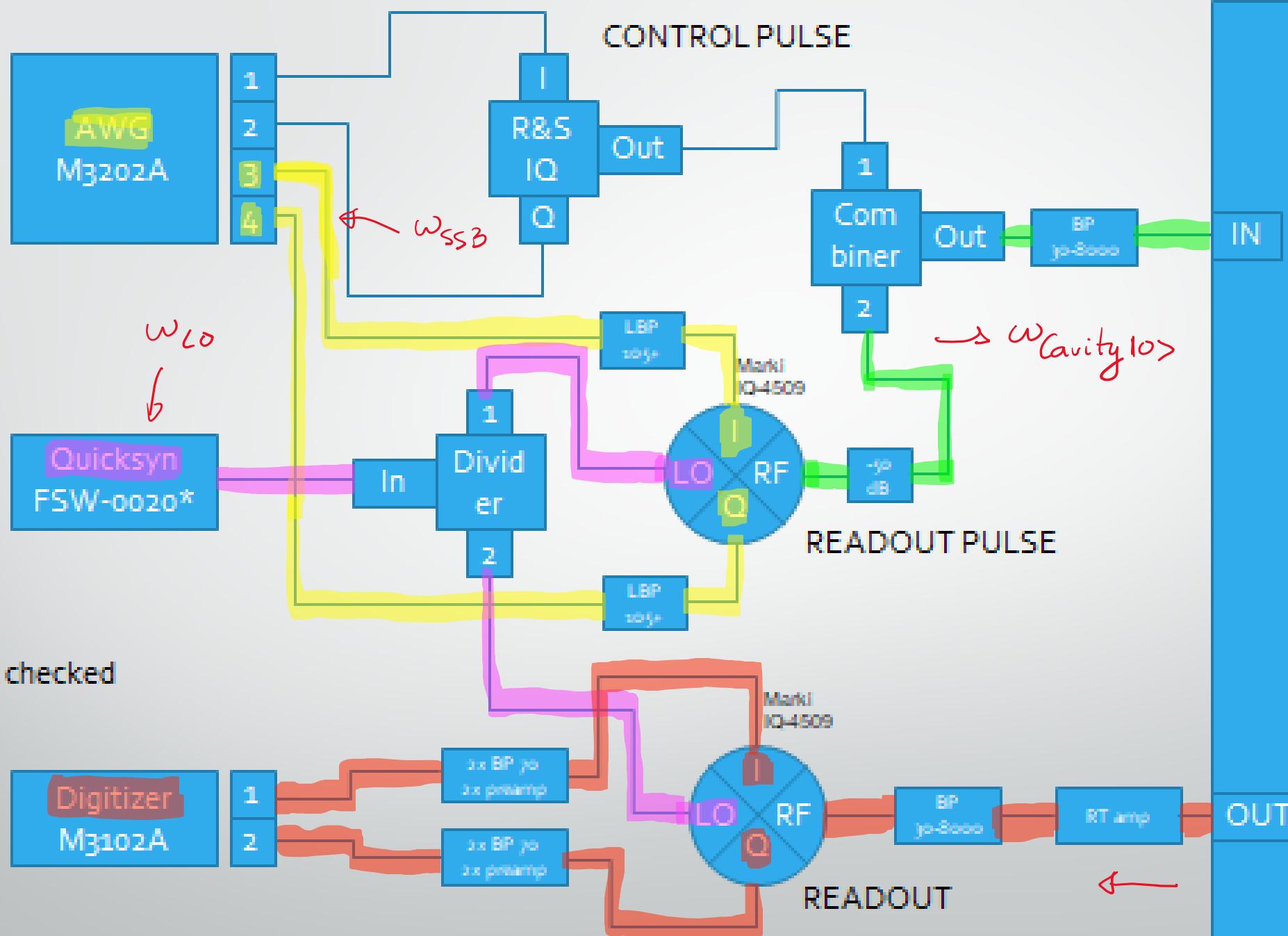
FRIDGE



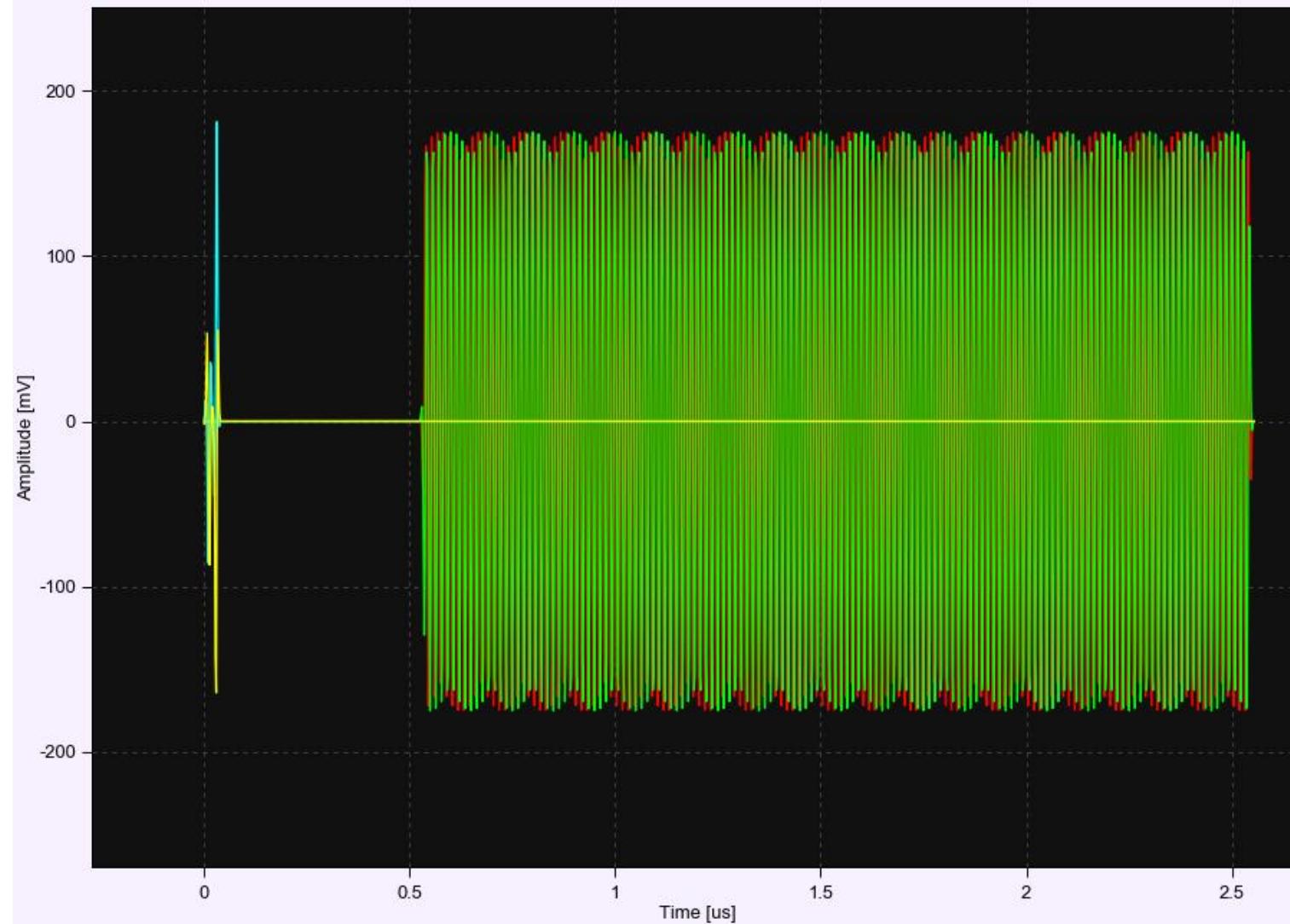
Readout pulse



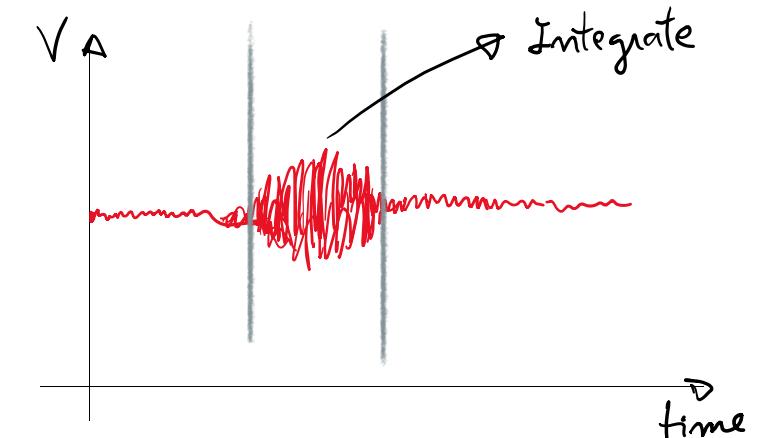
FRIDGE



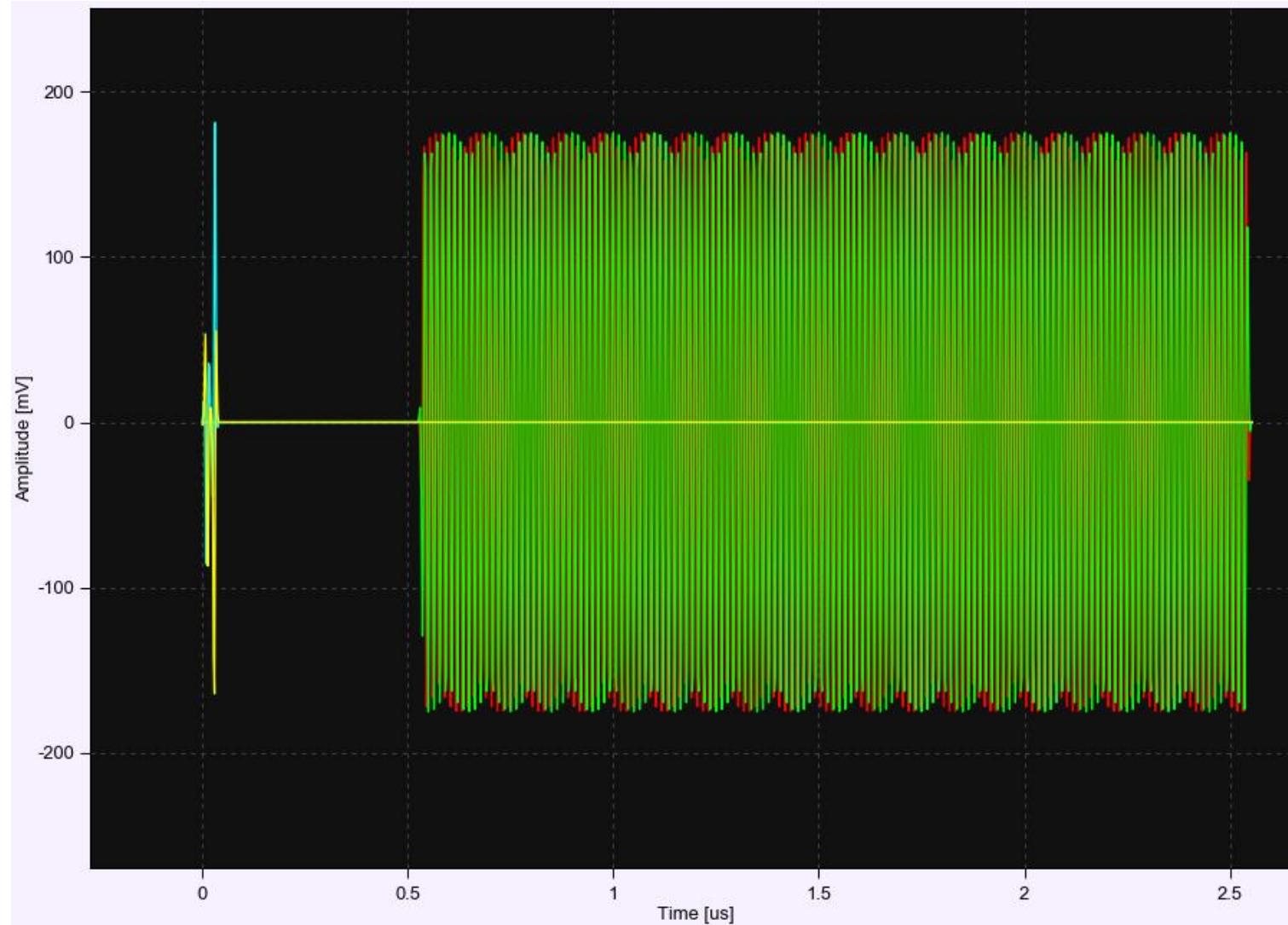
Readout pulse



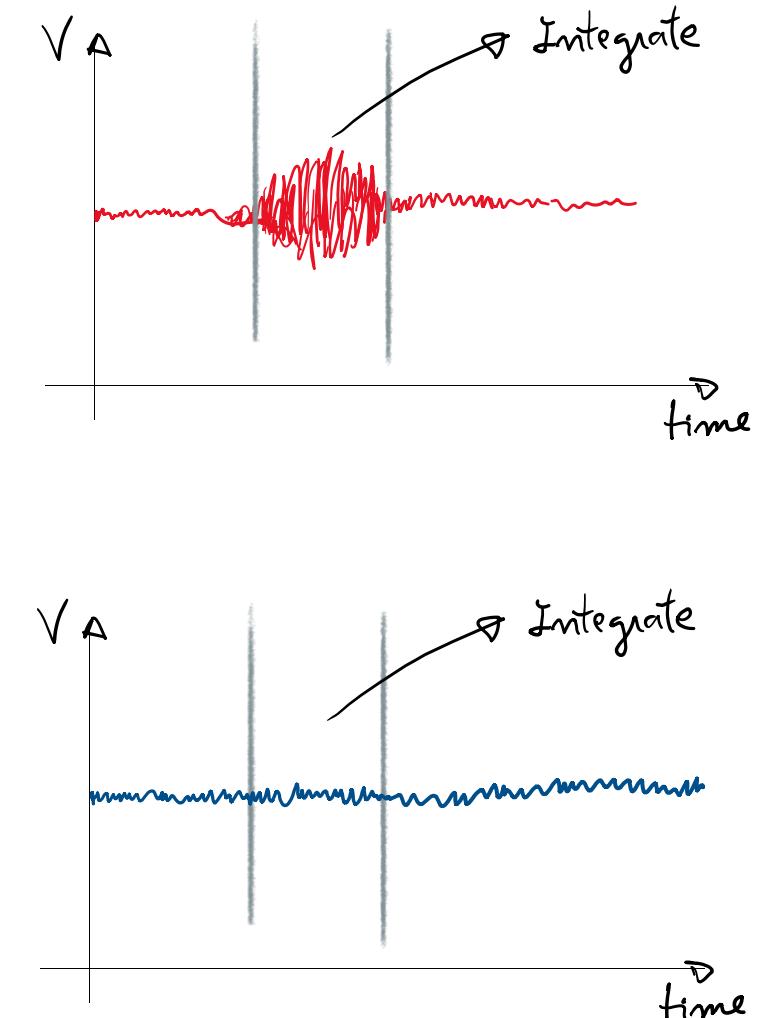
Digitizer signal



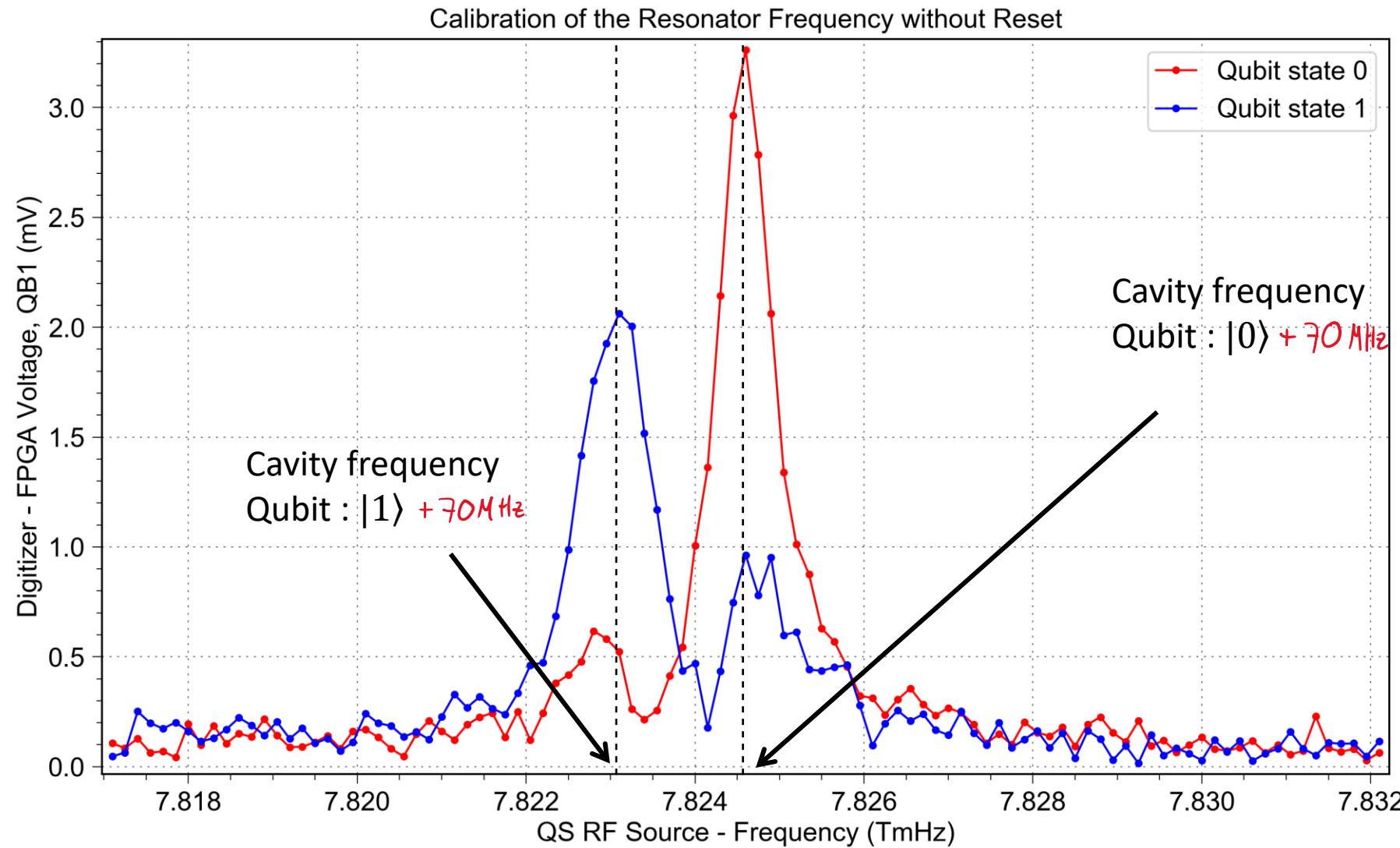
Readout pulse



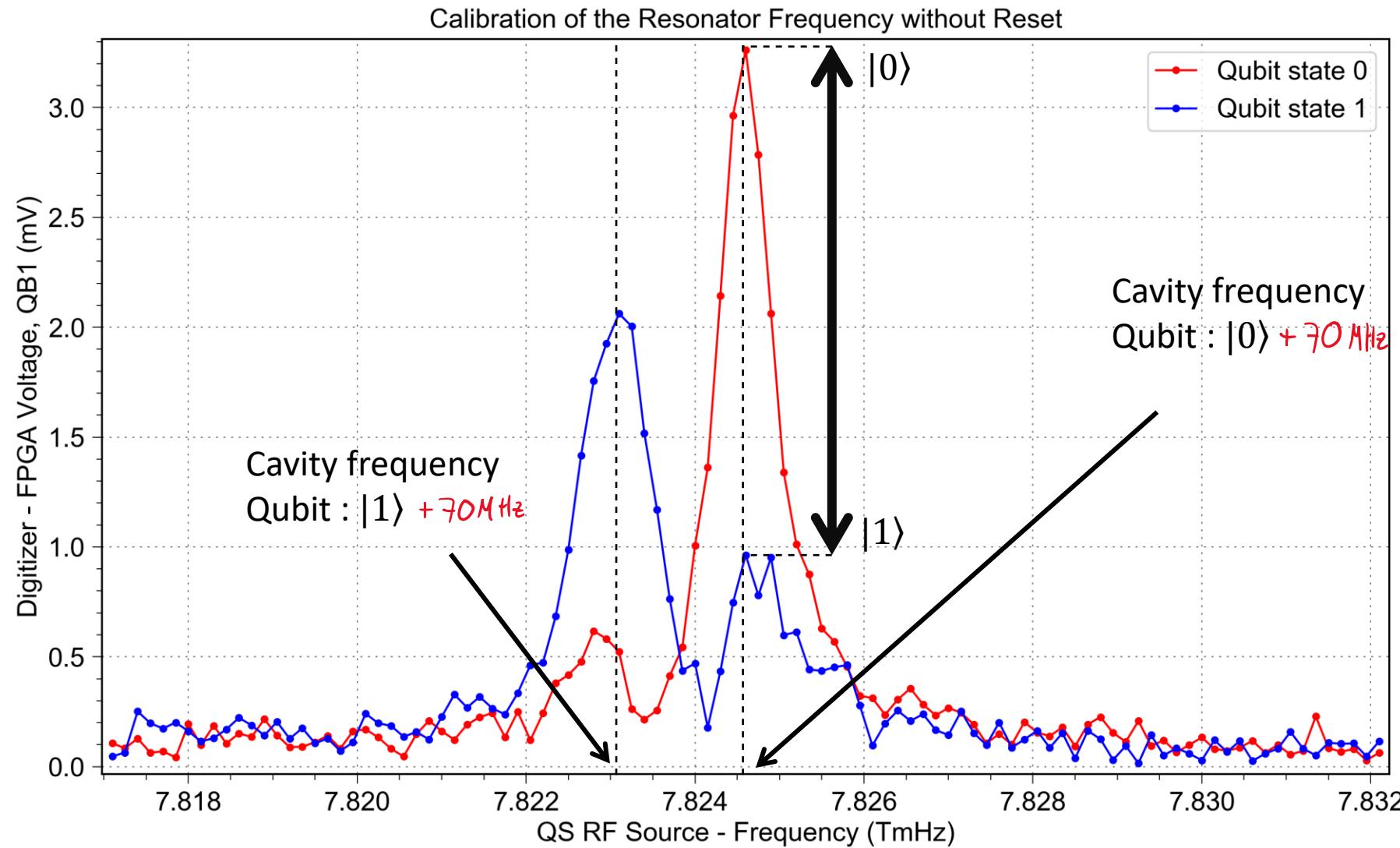
Digitizer signal



Readout pulse



Readout pulse



The program

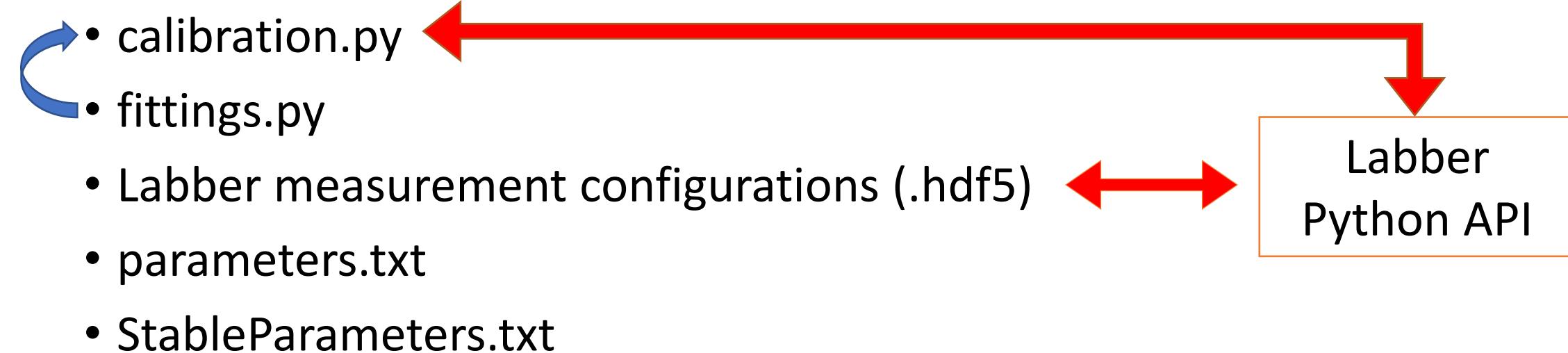
- calibration.py
- fittings.py
- Labber measurement configurations (.hdf5)
- parameters.txt
- StableParameters.txt

The program

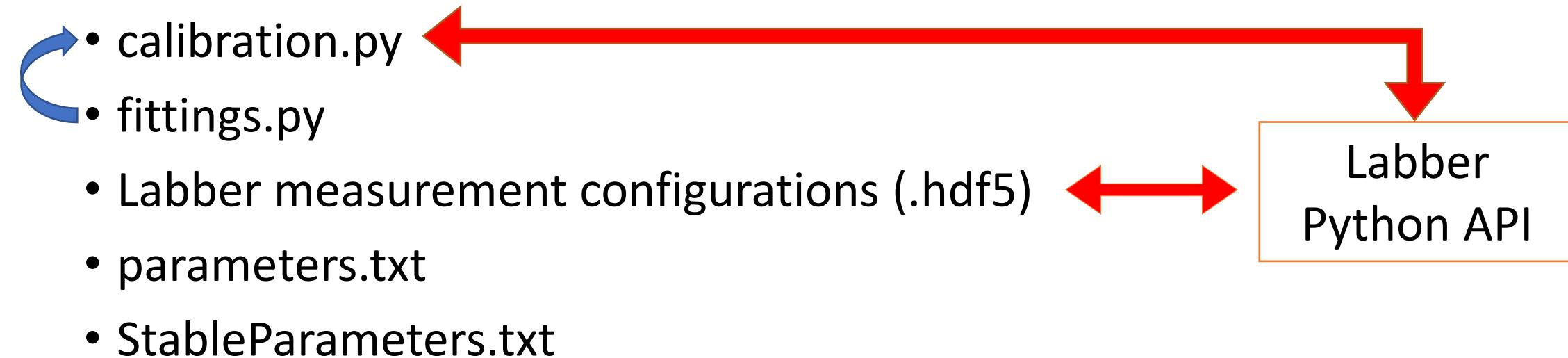
- calibration.py
 - fittings.py
 - Labber measurement configurations (.hdf5)
 - parameters.txt
 - StableParameters.txt
-
- The diagram illustrates the dependencies between the listed files and the Labber Python API. A horizontal red double-headed arrow connects 'calibration.py', 'fittings.py', and 'parameters.txt'. Another horizontal red double-headed arrow connects 'Labber measurement configurations (.hdf5)' and 'StableParameters.txt'. A vertical red arrow points from 'Labber Python API' down to 'Labber measurement configurations (.hdf5)'. The 'Labber Python API' is enclosed in a light orange rectangular box.

Labber
Python API

The program



The program



```
from calibration import *
%matplotlib inline
cal = Calibration('parameters.txt')
```

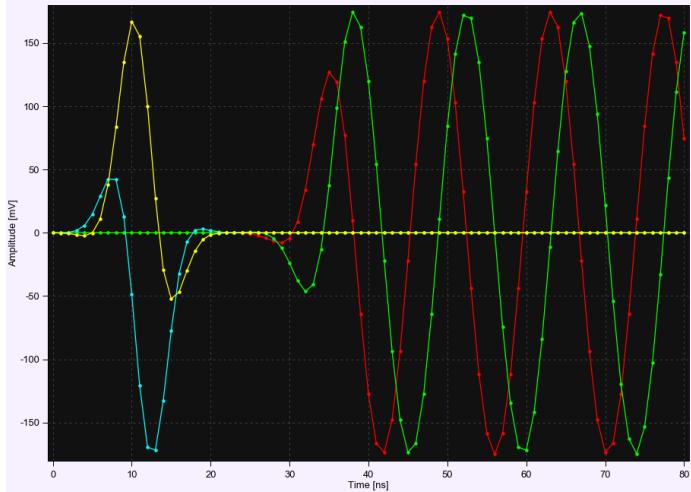
Calibration Results

- Voltage amplitude of a Pi Pulse
- Coherence times: T_1 , T_2 and T_φ, G
- Qubit Frequency
- Cavity frequencies

Pi Pulse calibration

$$A \cos^2(2\pi x/T + \phi) + c$$

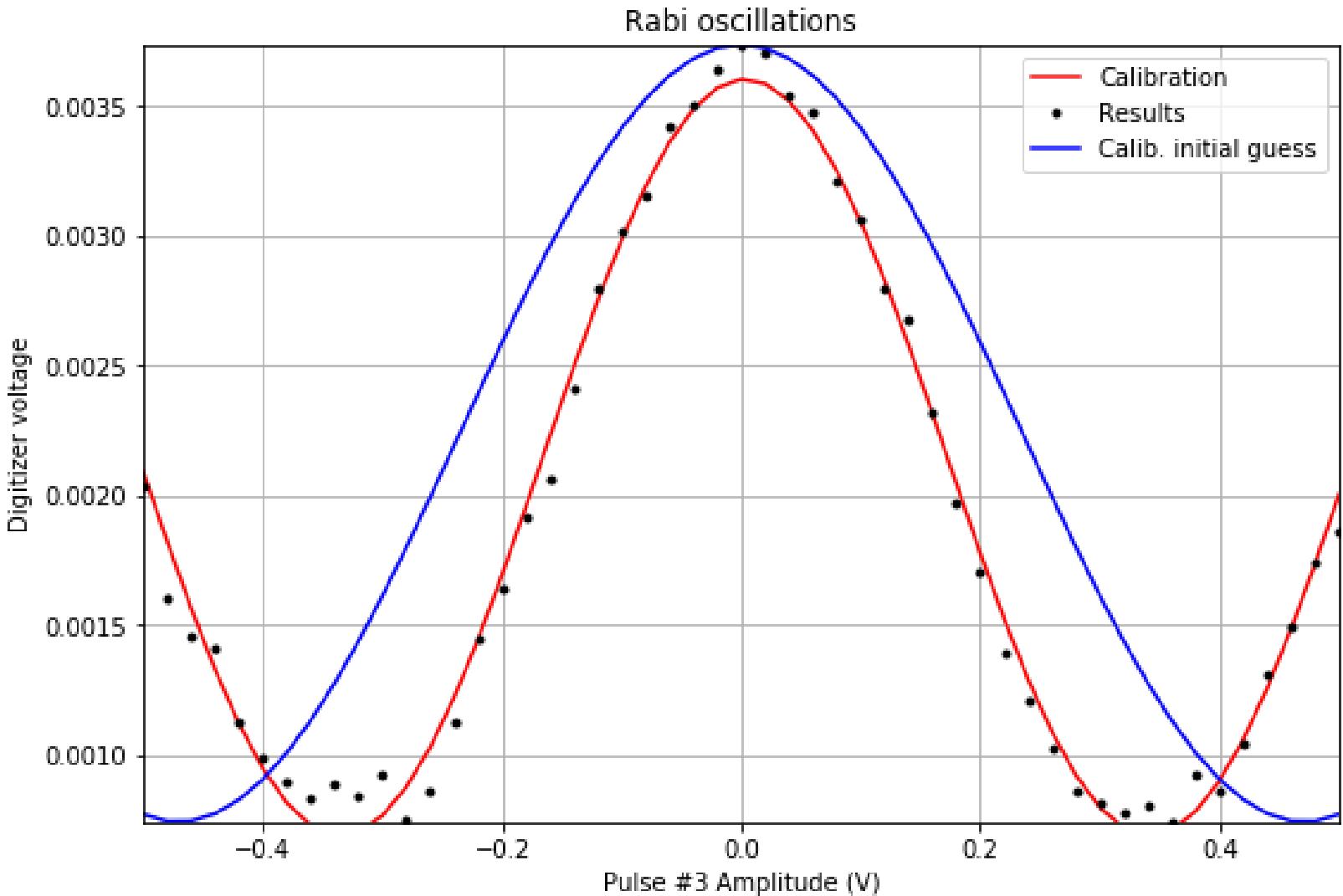
cal.getPiPulse()



cal._PiPulse = 0.338 V

cal._Amax = 0.0036 V

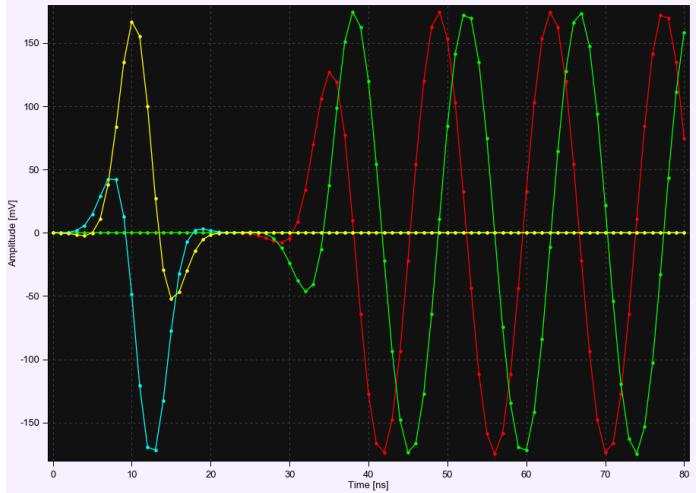
cal._Amin = 0.0007 V



Pi Pulse calibration

$$A \cos^2(2\pi x/T + \phi) + c$$

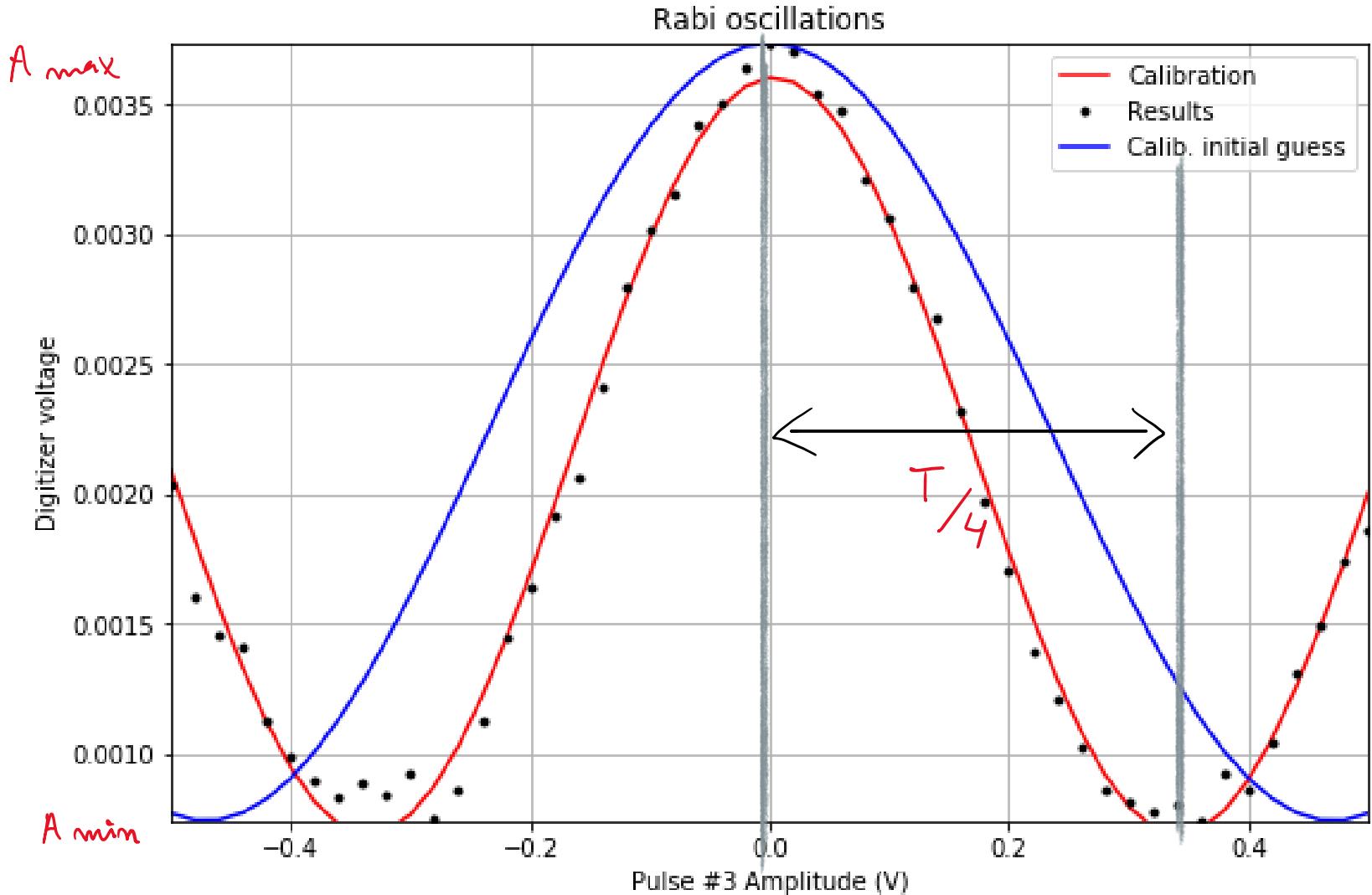
cal.getPiPulse()



cal._PiPulse = 0.338 V

cal._Amax = 0.0036 V

cal._Amin = 0.0007 V

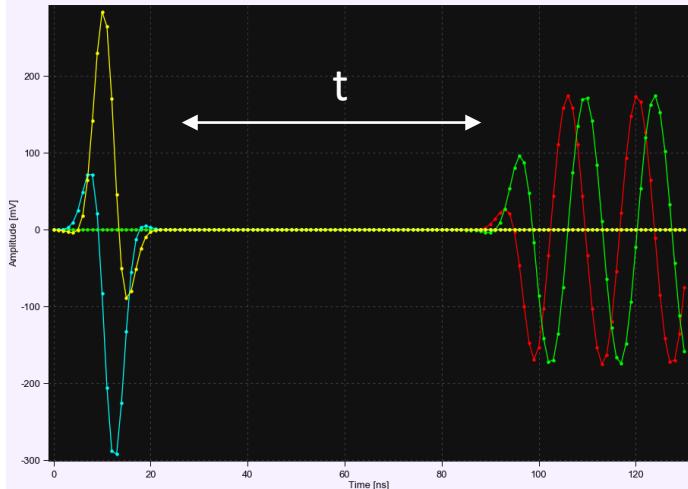


T1 calibration

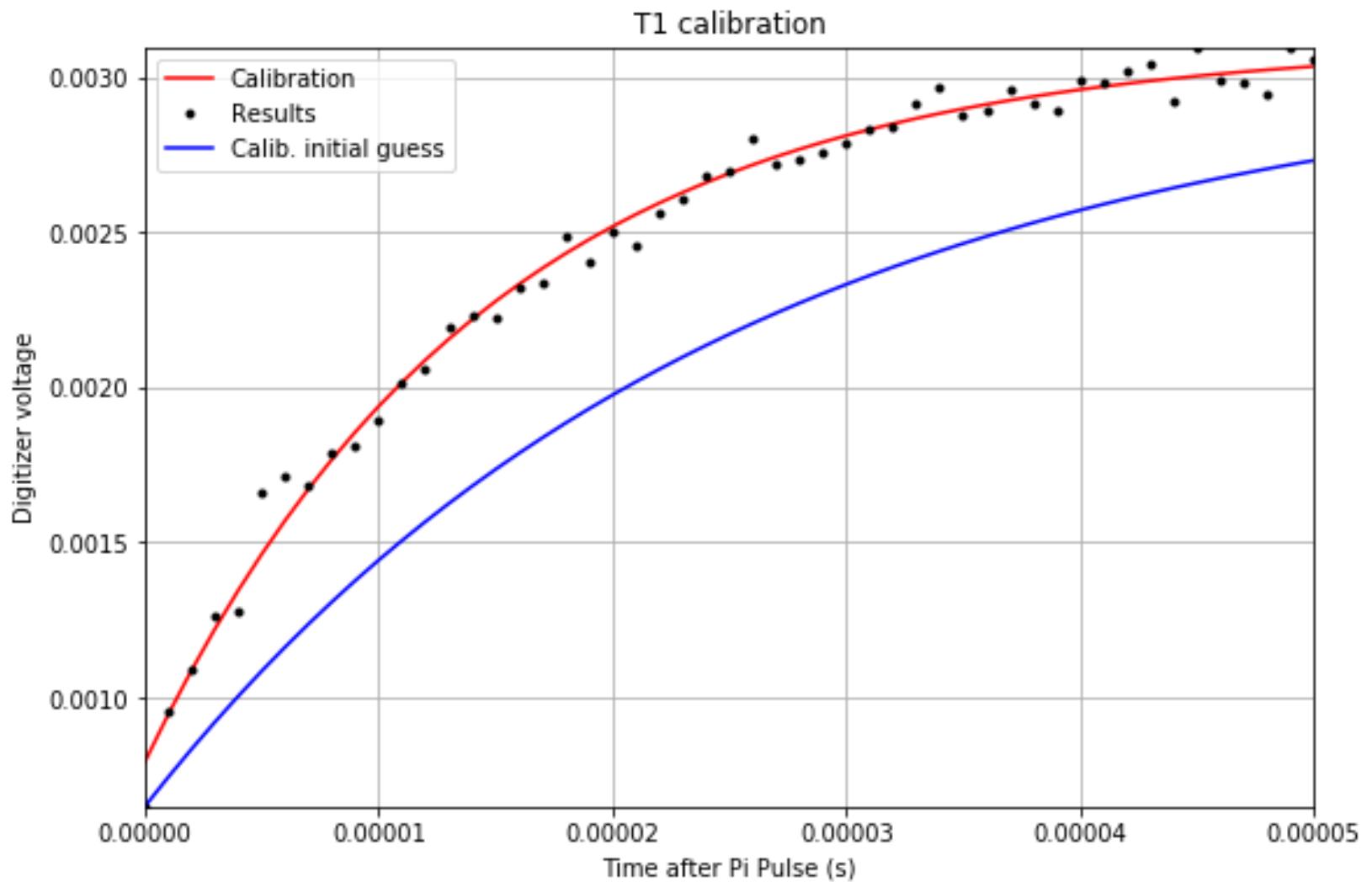
$$A + Be^{-t/T_1}$$

cal.getT1()

$X\pi$ - pulse

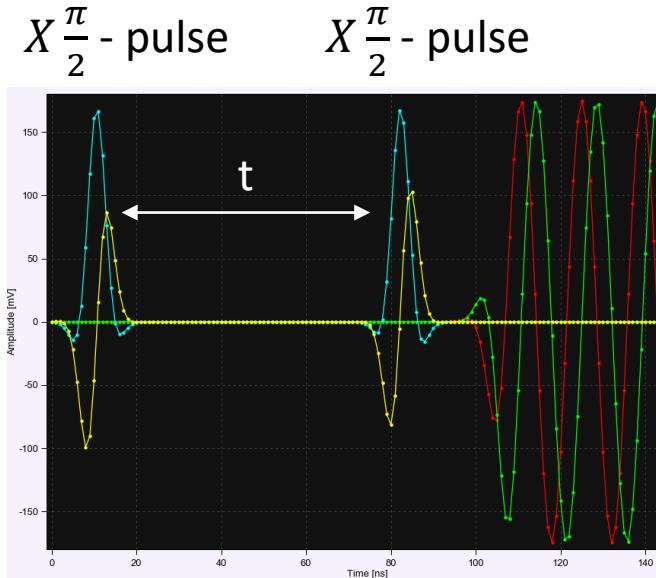


cal._T1 = 14.67 us



T₂ calibration (Ramsey)

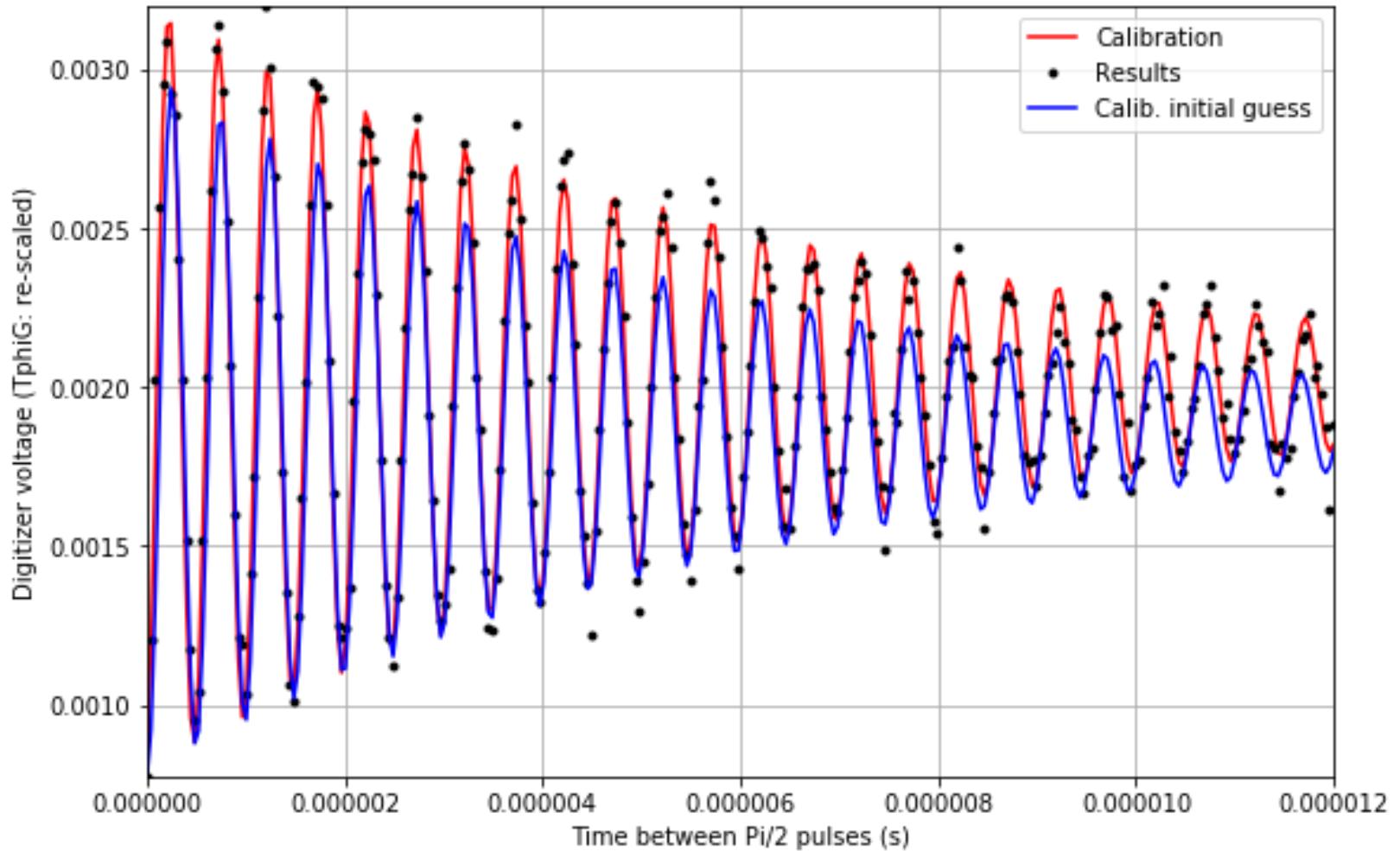
cal.getT2Ramsey()



cal._T2Ramsey = 6.77 us

$$A + Be^{-t/T_2} \cos\left(\frac{2\pi t}{T} + \phi\right)$$

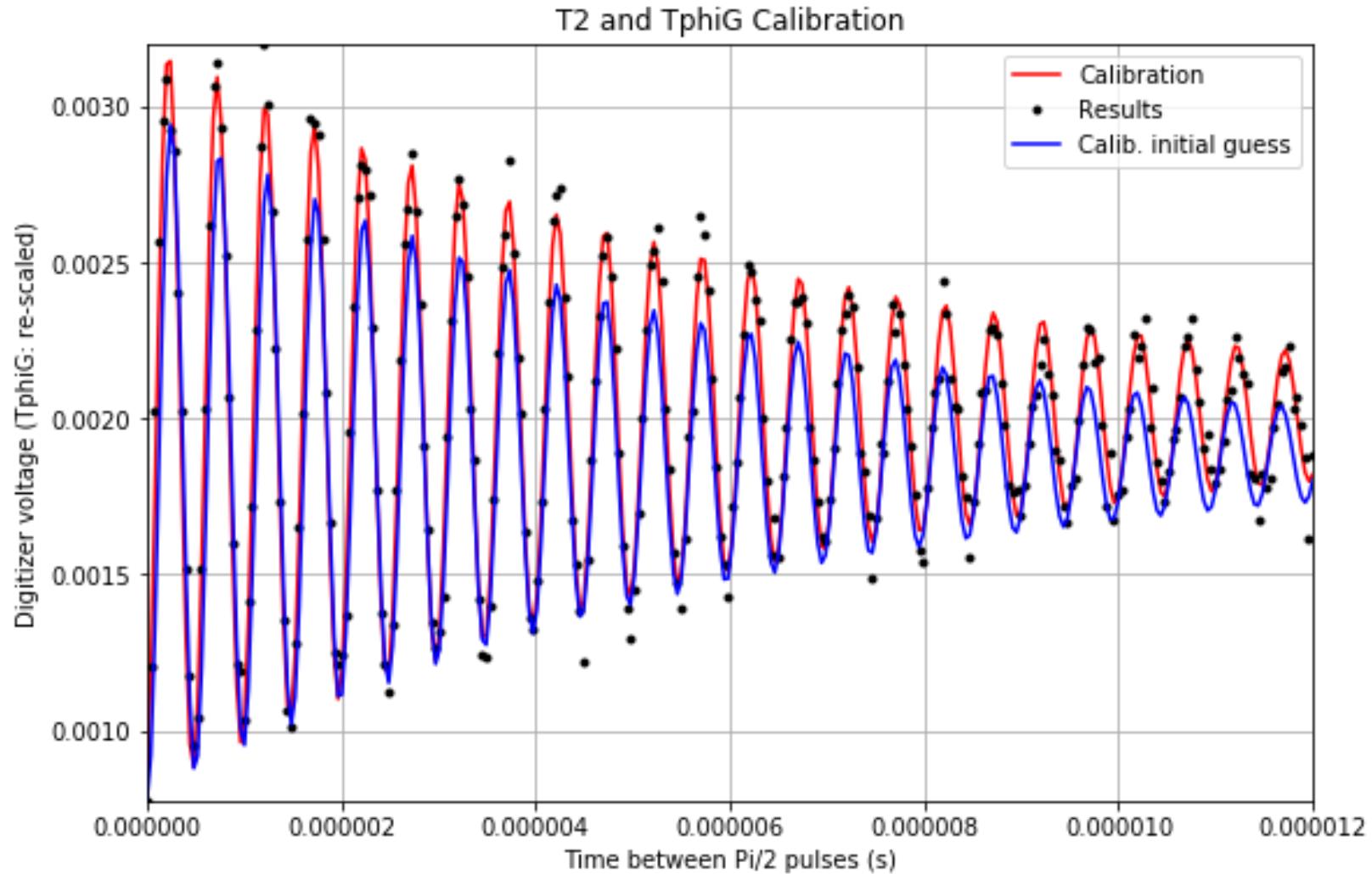
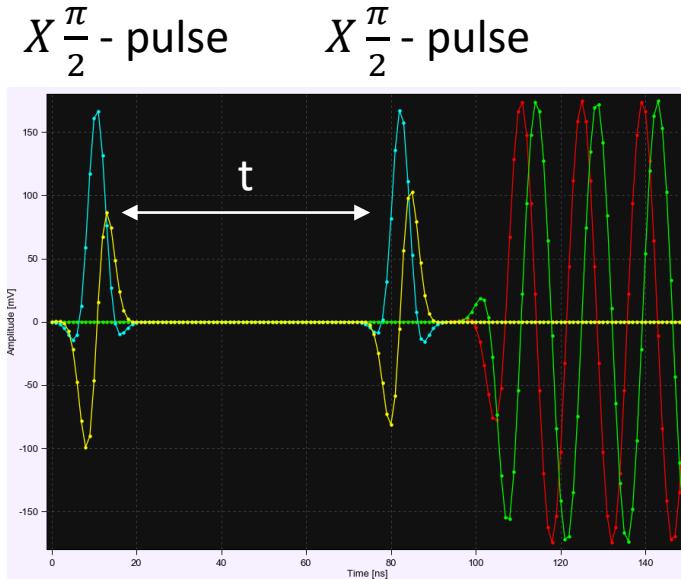
T₂ and TphiG Calibration



$T_{\varphi, G}$ calibration (Ramsey)

$$A + Be^{-t^2/T_{\varphi,G}^2} e^{-t/2T_1} \cos\left(\frac{2\pi t}{T} + \phi\right)$$

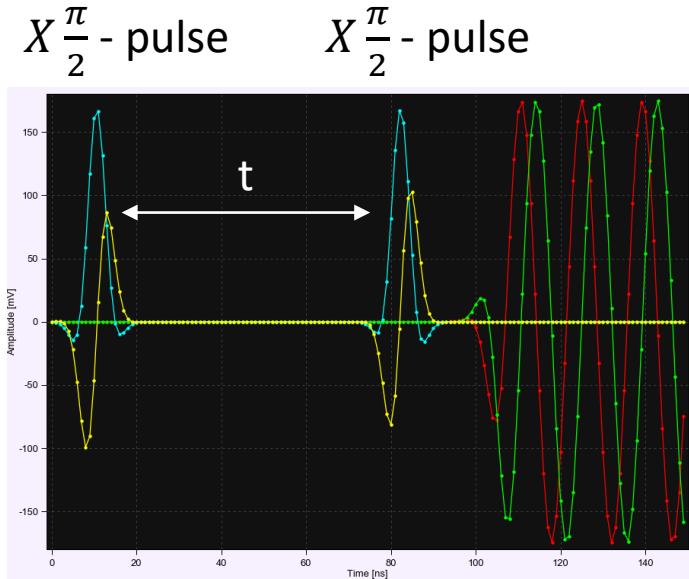
cal.getT2Ramsey(
TphiG = True)



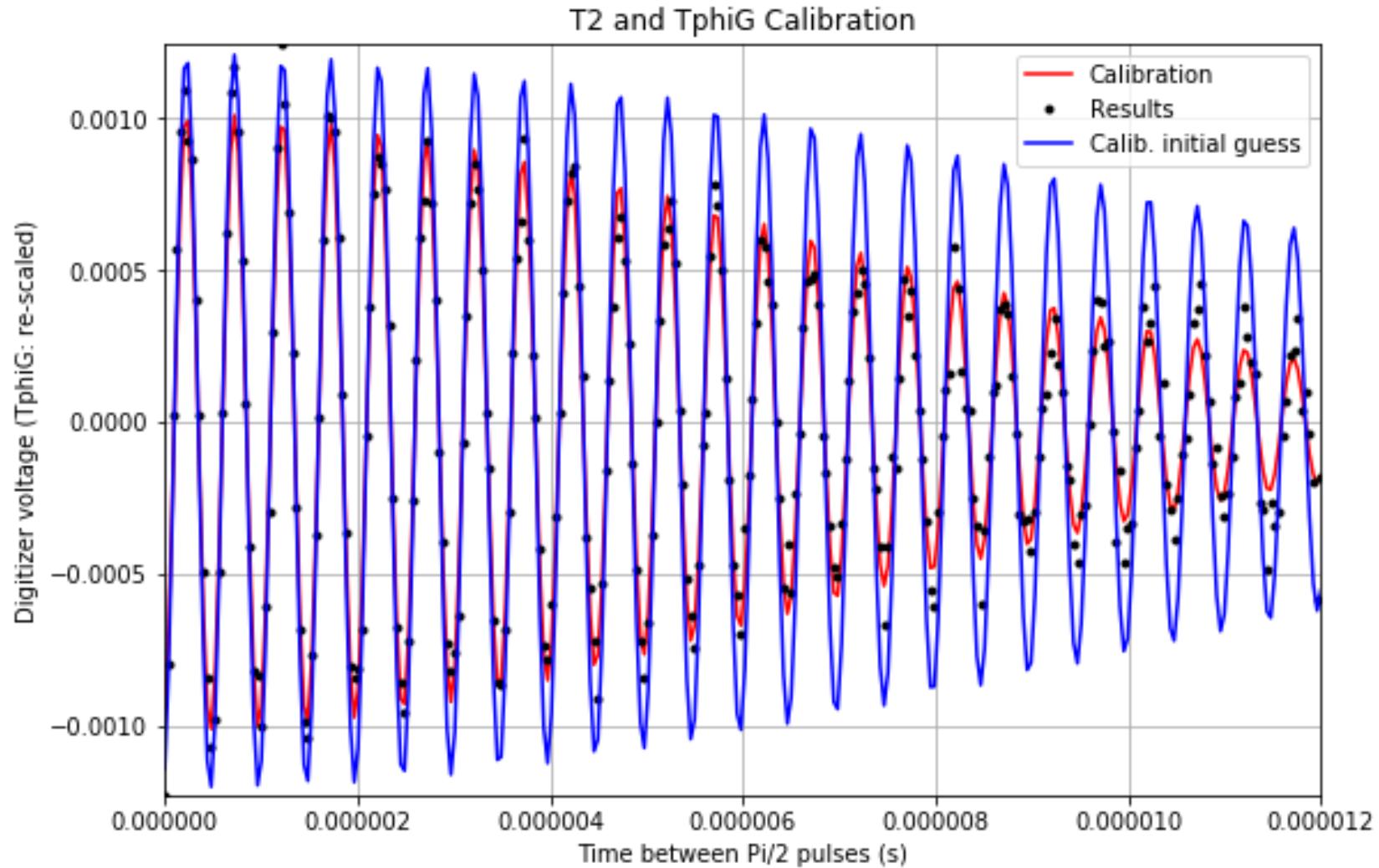
$T_{\varphi,G}$ calibration (Ramsey)

$$A + Be^{-t^2/T_{\varphi,G}^2} \cos\left(\frac{2\pi t}{T} + \phi\right)$$

```
cal.getT2Ramsey(  
    TphiG = True)
```

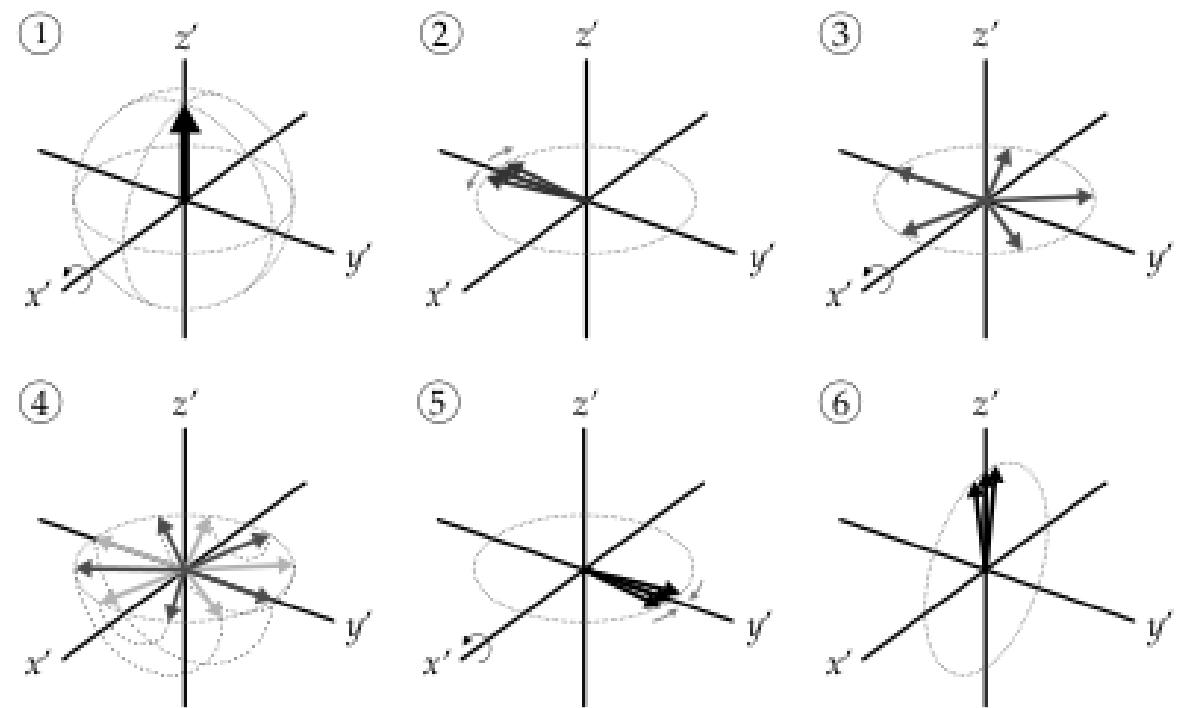
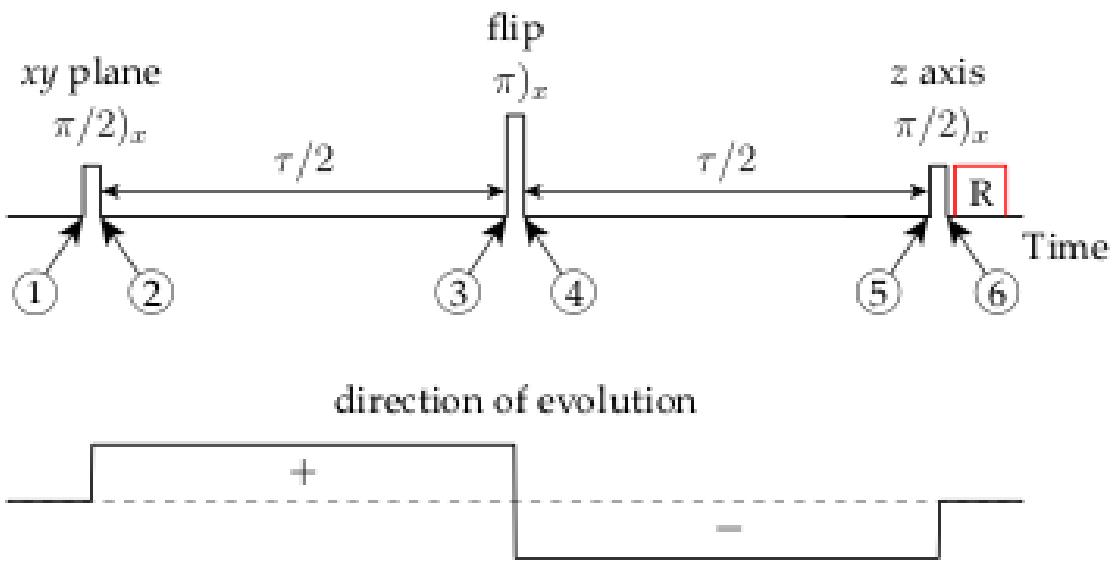


cal._TphiG = 9.35 us



T₂ calibration (Hahn Echo)

Hahn echo pulse sequence

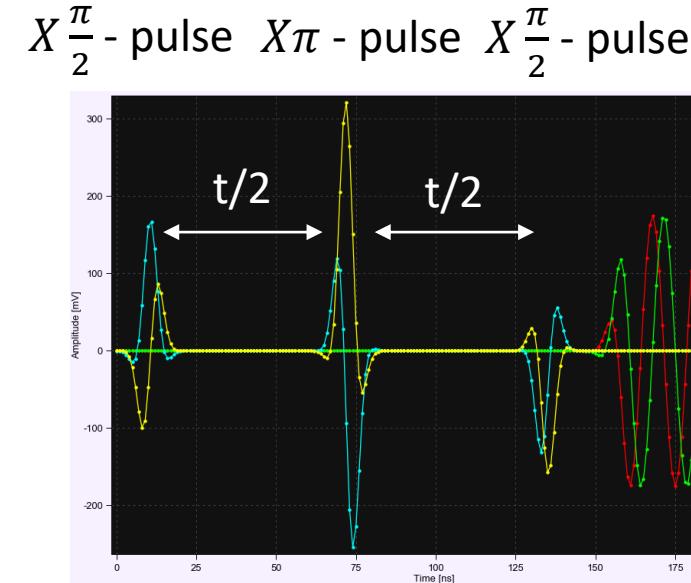


Ref. [6]

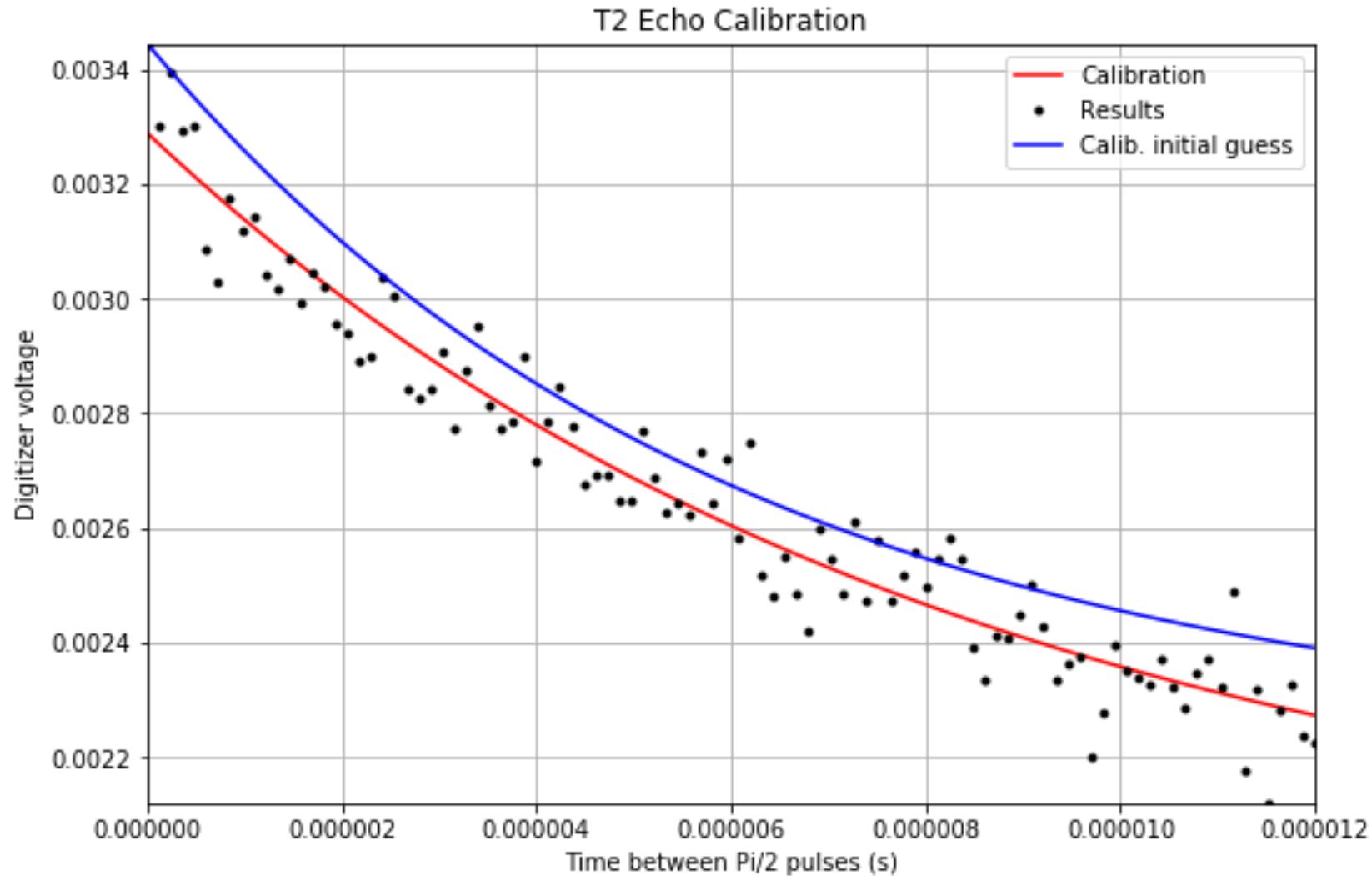
T₂ calibration (Hahn Echo)

$$A + Be^{-t/T_2}$$

cal.getT2Echo()



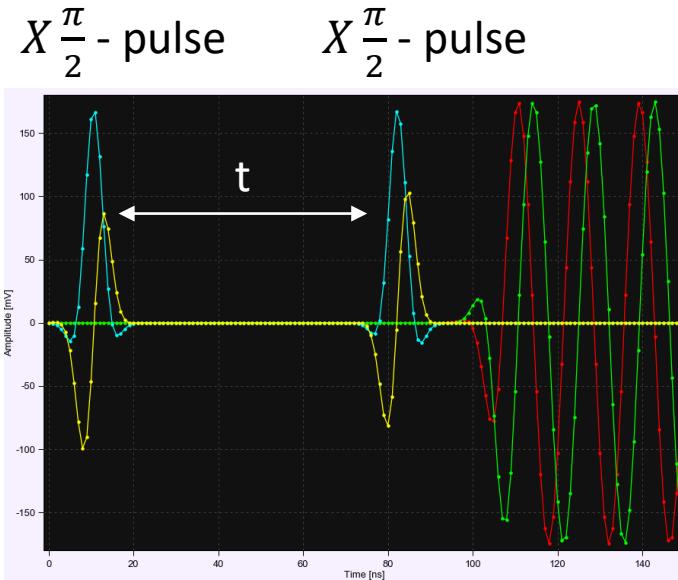
cal._T2Echo = 8.24 us



Qubit Frequency calibration

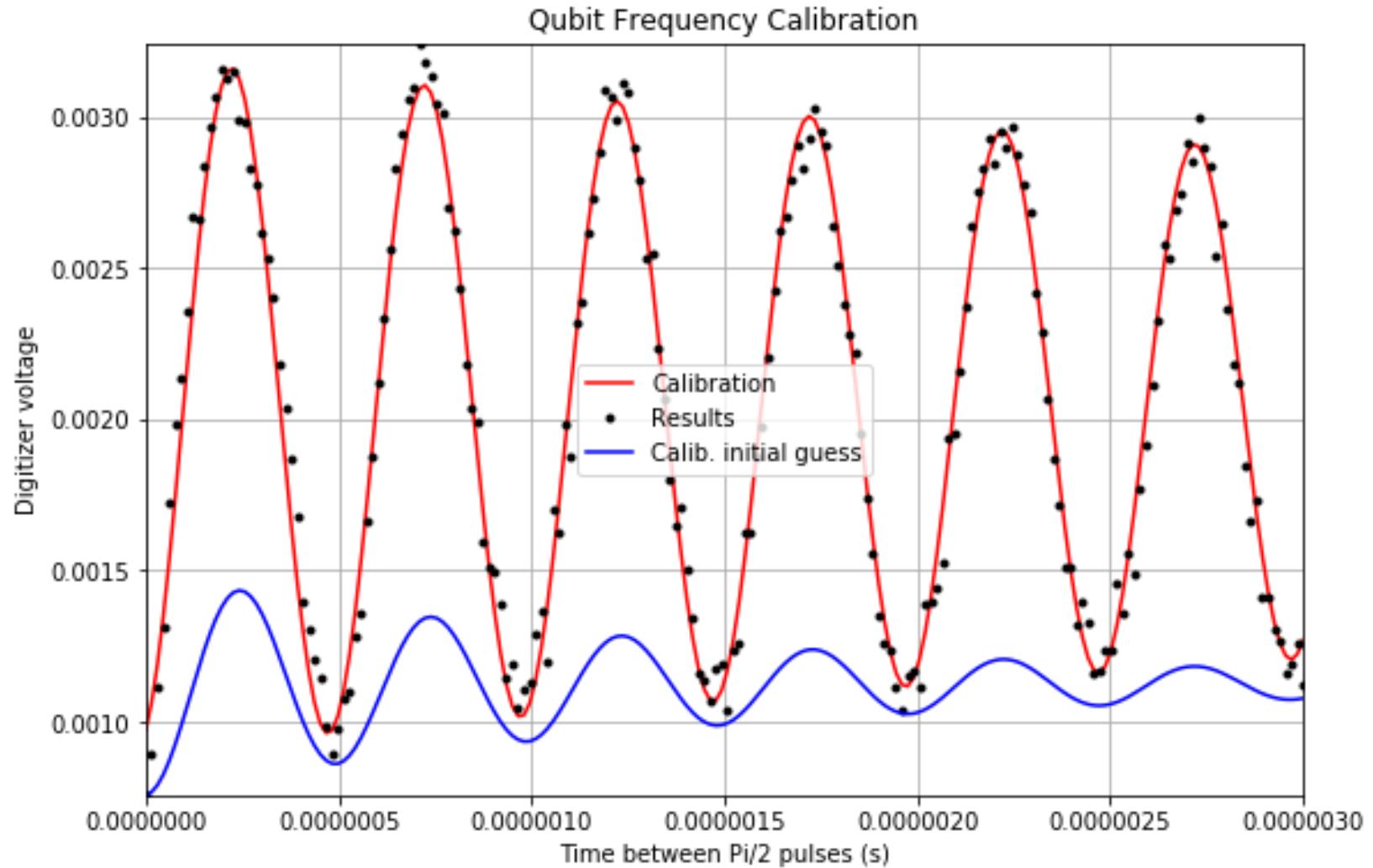
$$A + Be^{-t/T_2} \cos\left(\frac{2\pi t}{T} + \phi\right)$$

cal.getQubitFreq()



$$\frac{1}{T} = f_d - f_q$$

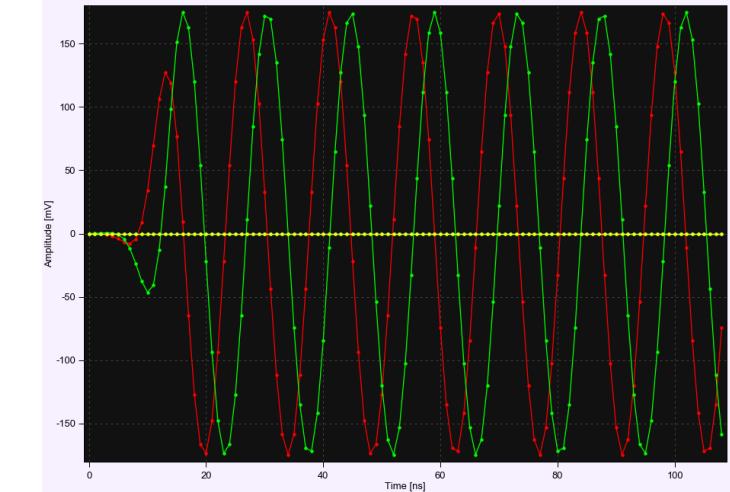
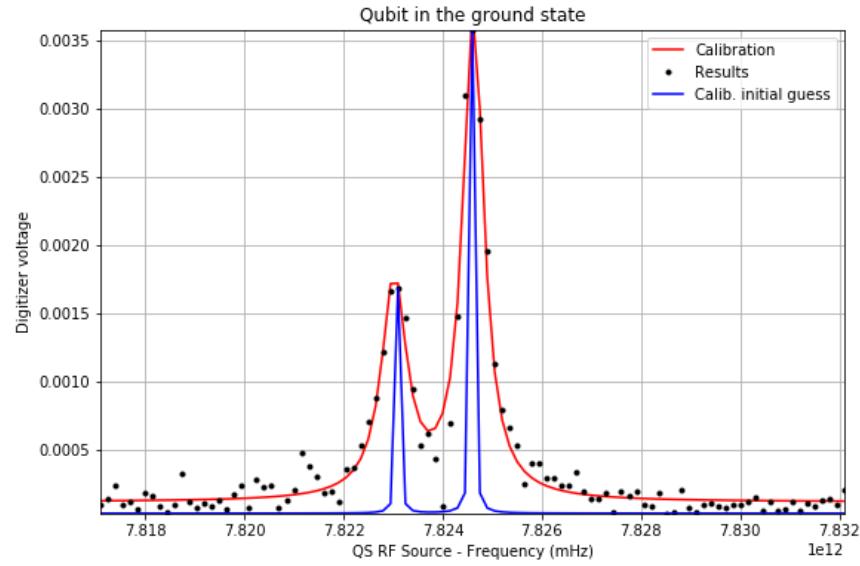
cal._QubitFreq = 4.8250361 GHz



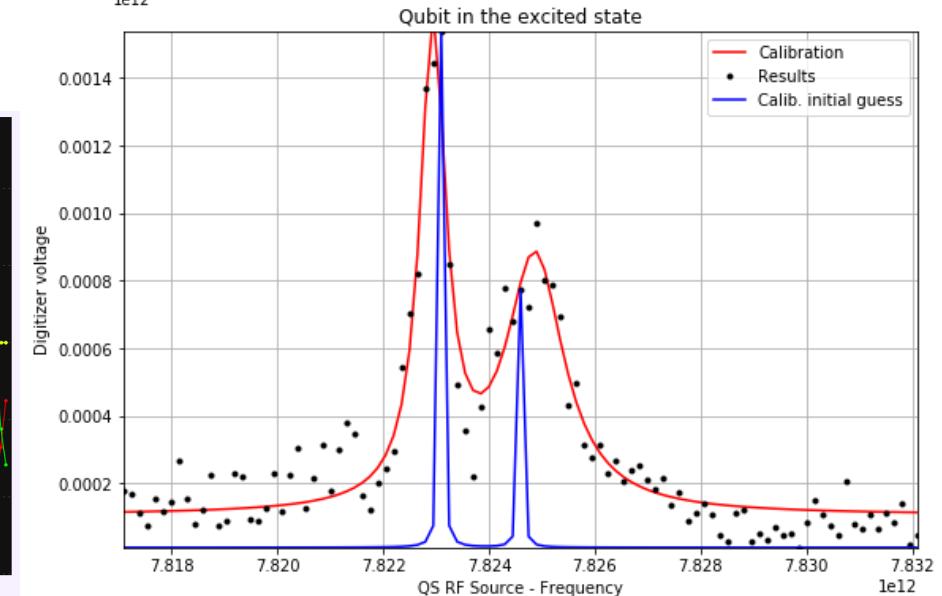
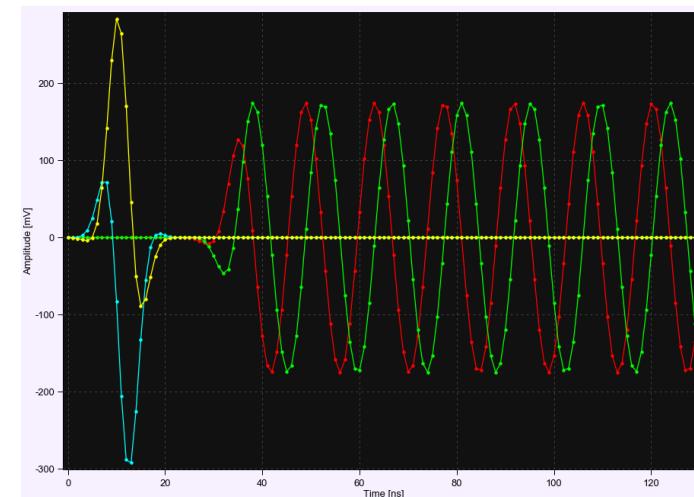
Cavity Frequencies calibration

cal.getResonatorFreq()

$$\frac{A_0}{(x-f_0)^2 - (\kappa_0/2)^2} + \frac{A_1}{(x-f_1)^2 - (\kappa_1/2)^2} + C$$



X π - pulse



cal._ResonatorFreq0 = 7.75462 GHz

cal._ResonatorFreq1 = 7.75294 GHz

<https://github.com/UB-Quantic/Qubit-Calibration>

Qubit Calibration

Raquel García Bellés

IFAE Summer Fellowship @ Quantum Computing Technology Group
July – August 2020

Outline

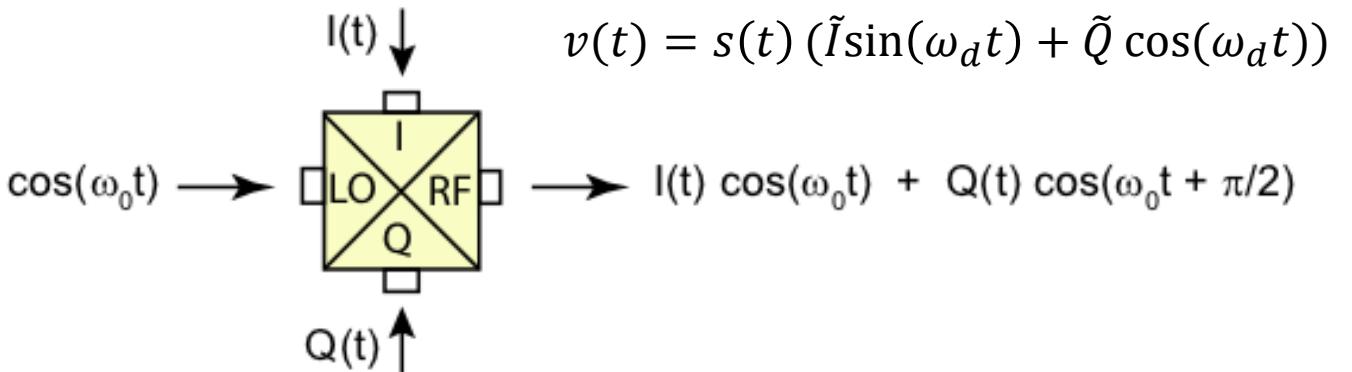
- Theoretical Background
- Technical Aspects
- Calibration Results
- DRAG scaling constant
- Reset Pulse

DRAG scaling constant

- [1] - P. Krantz, M. Kjaergaard, F. Yan, T. P. Orlando, S. Gustavsson, and W. D. Oliver, A quantum engineer's guide to superconducting qubits, *Appl. Phys. Rev.* 6, 021318 (2019).
- [5] - Matthias Baur. "Realizing quantum gates and algorithms with three superconducting qubits". PhD thesis. ETH Zurich, Mar. 2012.

Derivative Reduction by Adiabatic Gate (DRAG)

- **Leakage errors:** Excitations outside of the computational subspace



- **Phase errors:** Accumulation of a phase
Labber generates:

$$s(t) \rightarrow s'(t) = \begin{cases} s(t) & \text{on } \tilde{I} \\ \beta s'(t) & \text{on } \tilde{Q} \end{cases}$$

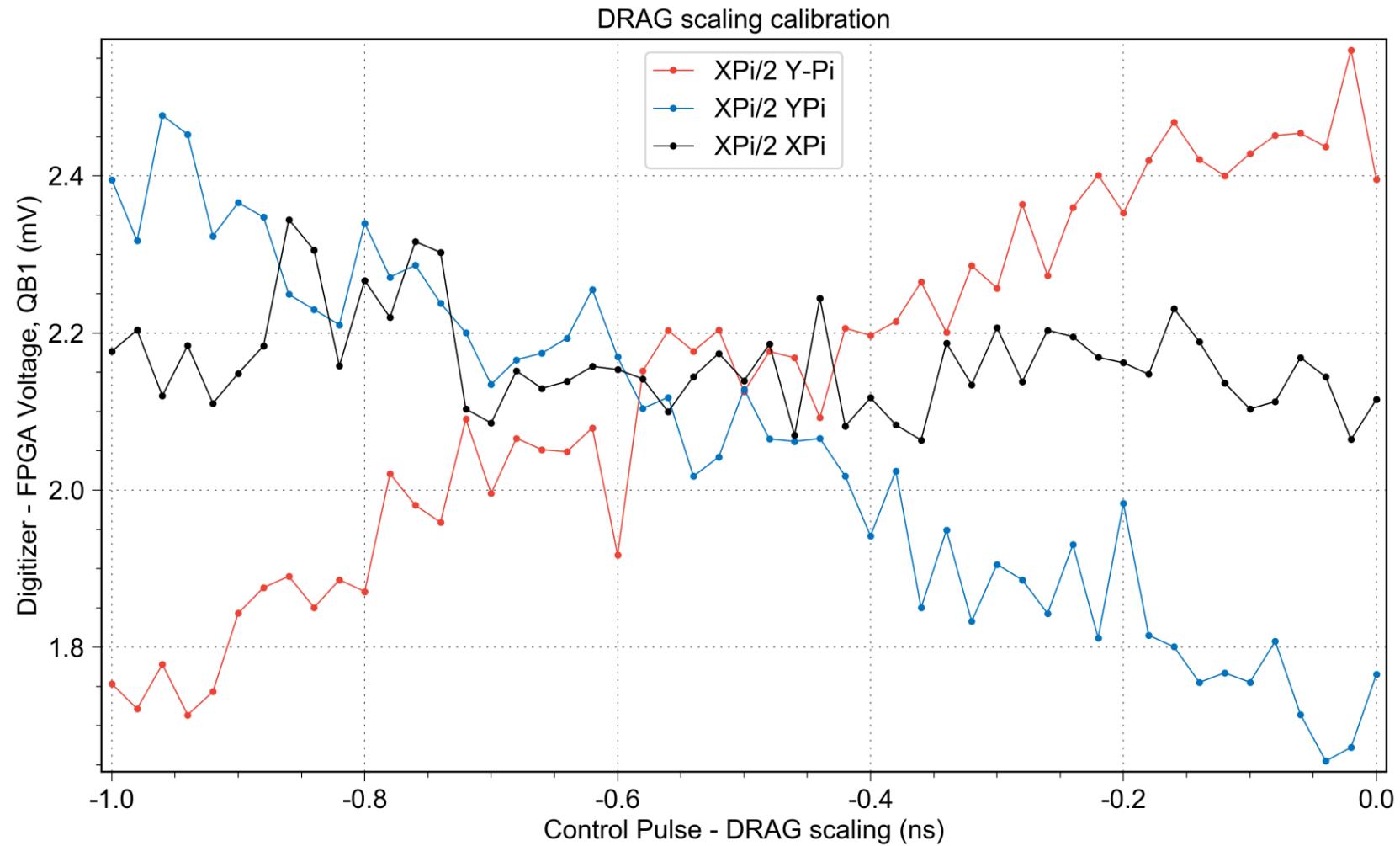
Mixer:

$$I(t) = s(t)\tilde{I}\cos(\omega_{SSB}t - \phi) - \beta s'(t)\tilde{Q}\cos(\omega_{SSB}t - \phi + \pi/2) \quad \times \cos(\omega_{LO}t) \quad +$$
$$Q(t) = -s(t)\tilde{I}\sin(\omega_{SSB}t - \phi) + \beta s'(t)\tilde{Q}\sin(\omega_{SSB}t - \phi + \pi/2) \quad \times \cos(\omega_{LO}t + \pi/2)$$

$$s(t)\tilde{I}\cos((\omega_{LO} - \omega_{SSB})t + \phi) - \beta s'(t)\tilde{Q}\sin((\omega_{LO} - \omega_{SSB})t + \phi)$$

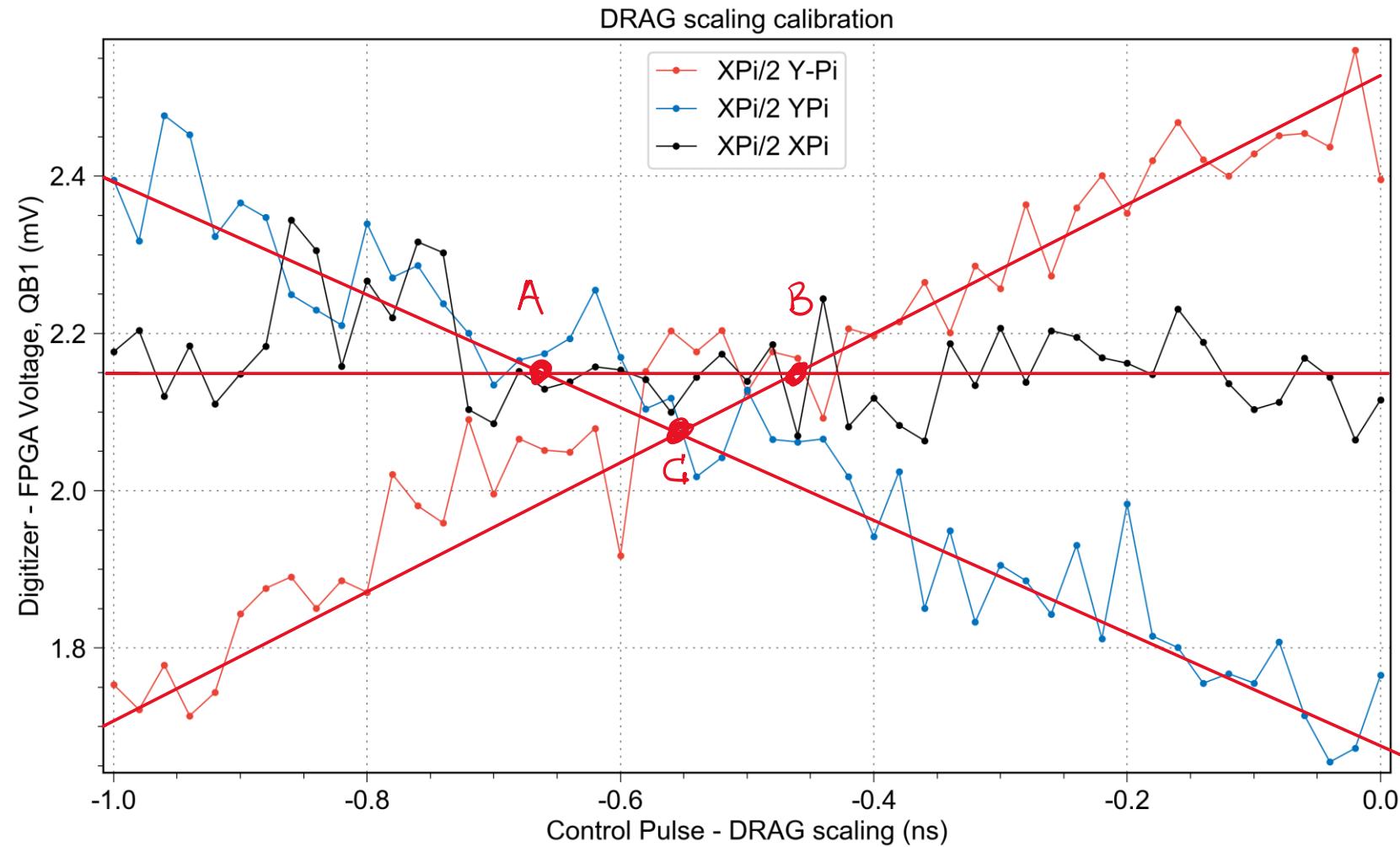
DRAG scaling constant

cal.getDRAG()



DRAG scaling constant

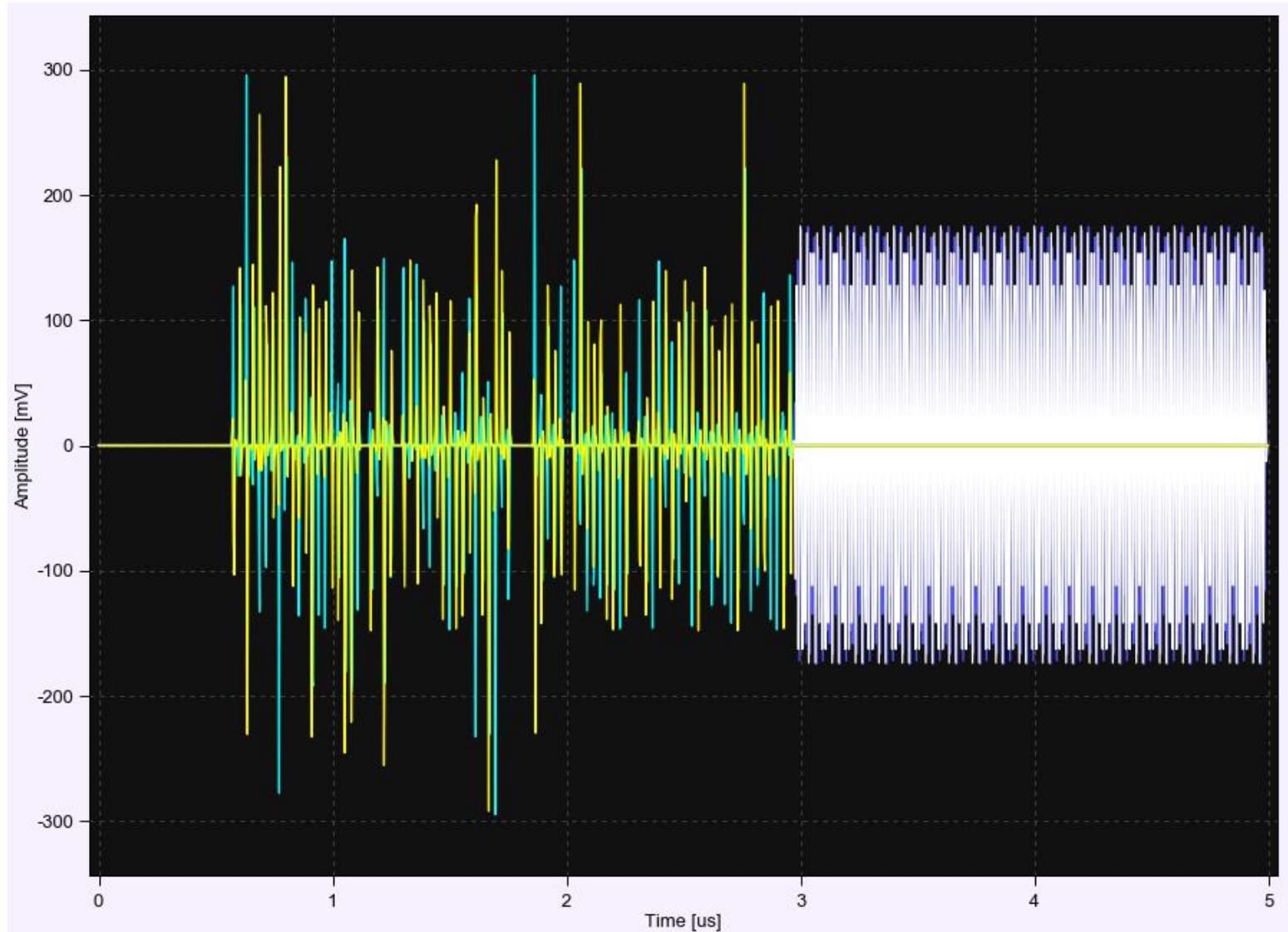
cal.getDRAG()



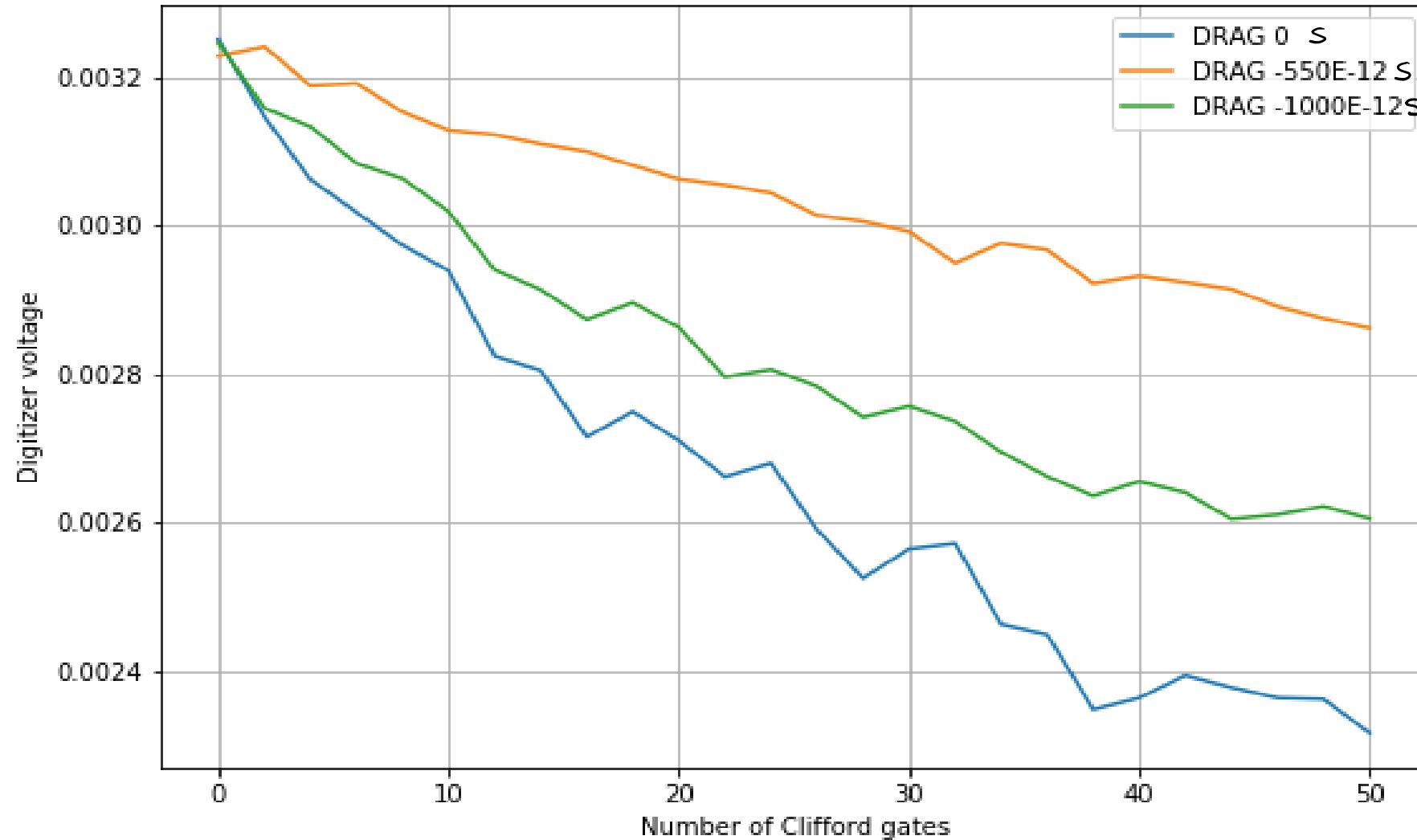
cal._DRAG = -598E-12 s

Randomized Benchmarking

- Apply N Clifford gates
- Last gate: Reverses all the other

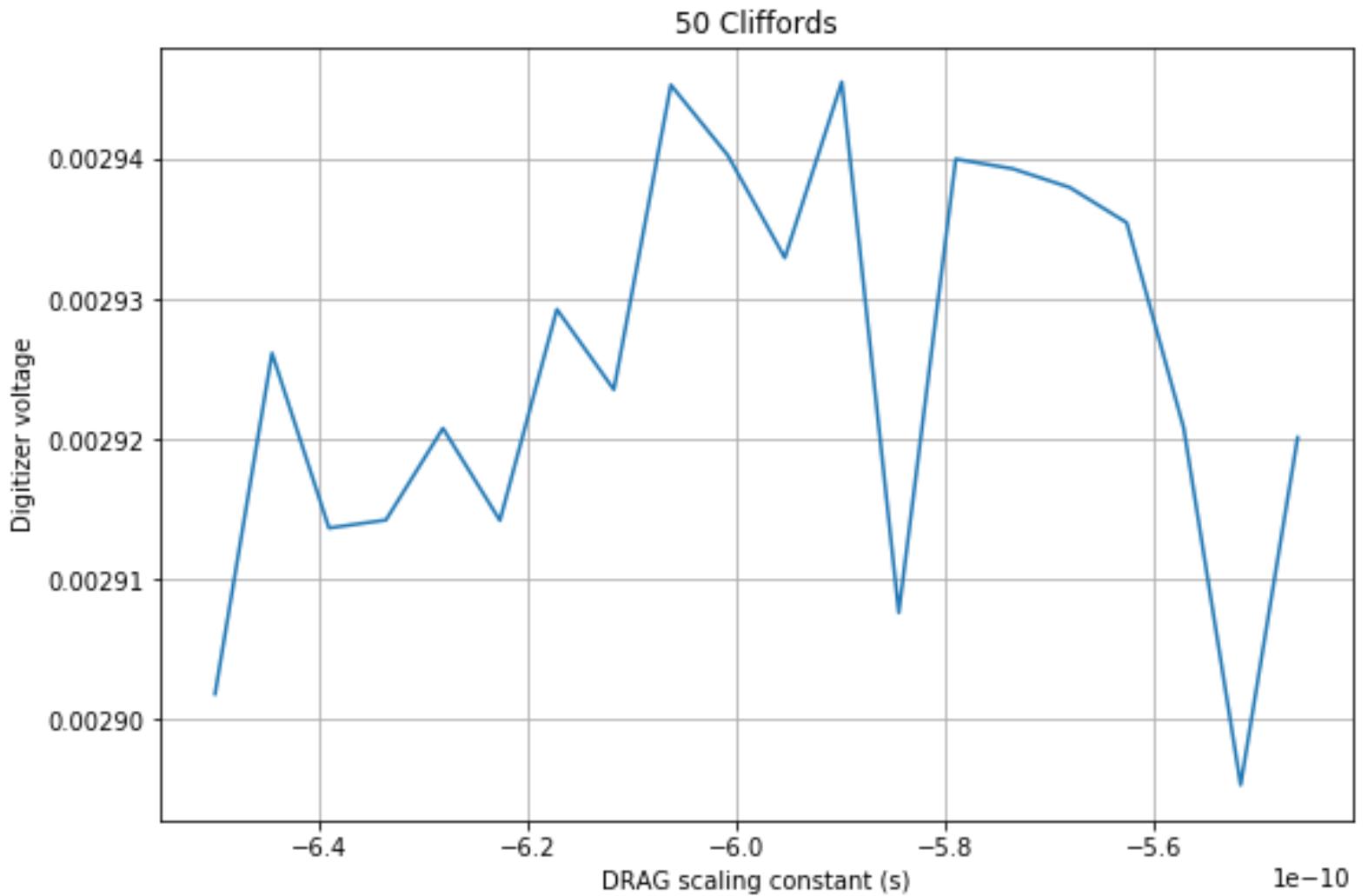


Randomized Benchmarking



Randomized Benchmarking

cal.getDRAG()

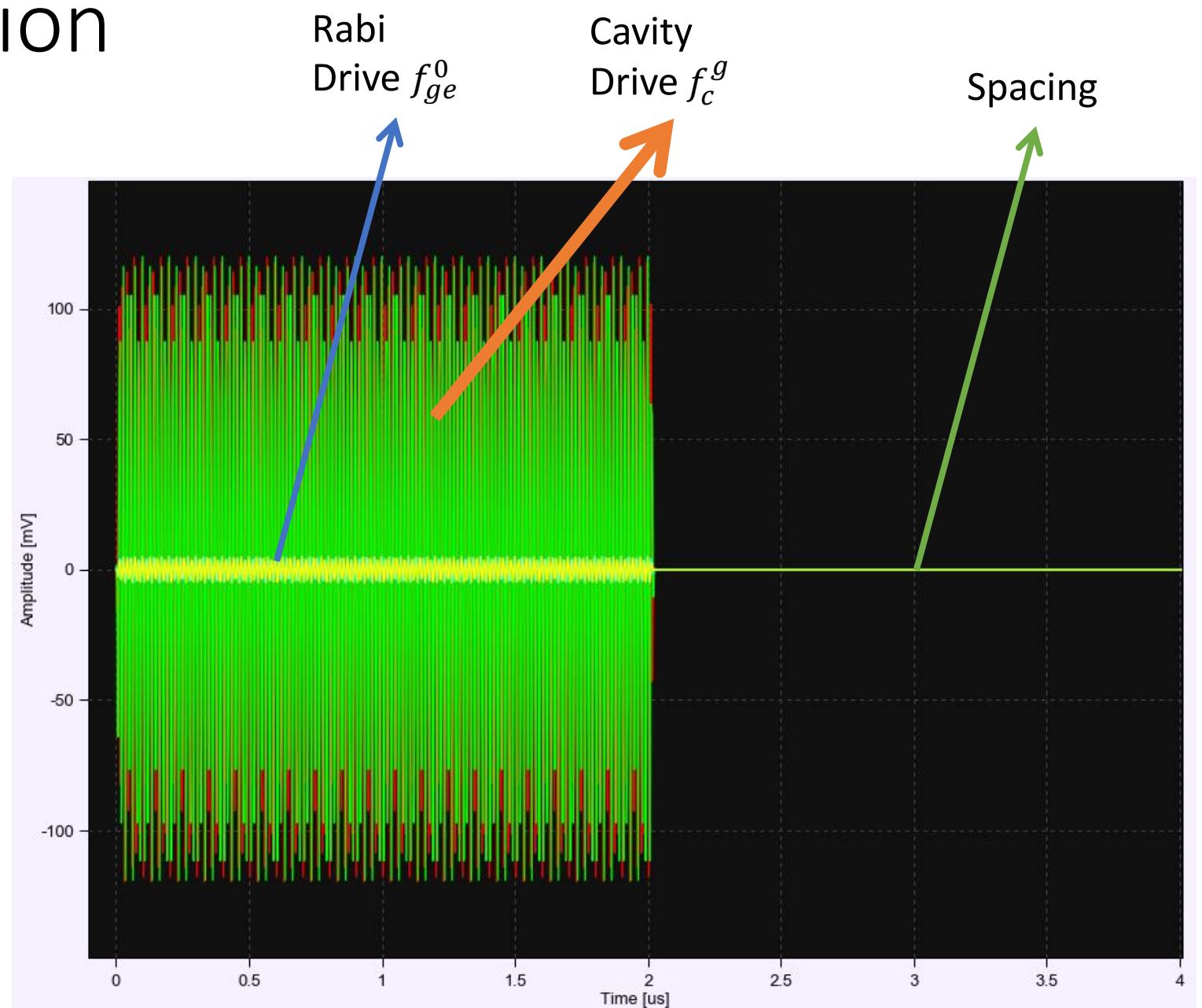
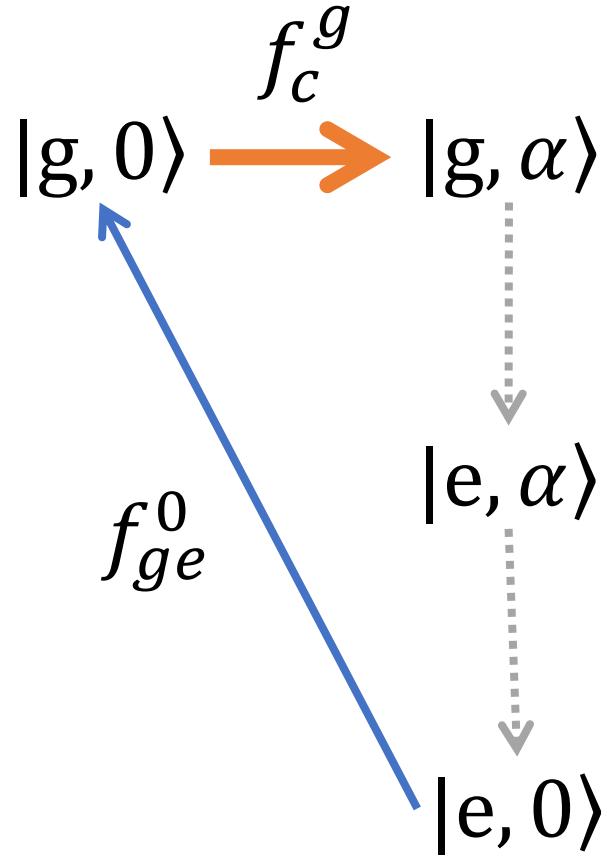


cal._DRAG = -590E-12 s

RESET calibration

- [3] - Geerlings, K., Leghtas, Z., Pop, I. M., Shankar, S., Frunzio, L., Schoelkopf, R. J., ... & Devoret, M. H. (2013). Demonstrating a driven reset protocol for a superconducting qubit. *Physical review letters*, 110(12), 120501.
- [4] - McClure, D. T., Paik, H., Bishop, L. S., Steffen, M., Chow, J. M., & Gambetta, J. M. (2016). Rapid driven reset of a qubit readout resonator. *Physical Review Applied*, 5(1), 011001.

RESET calibration

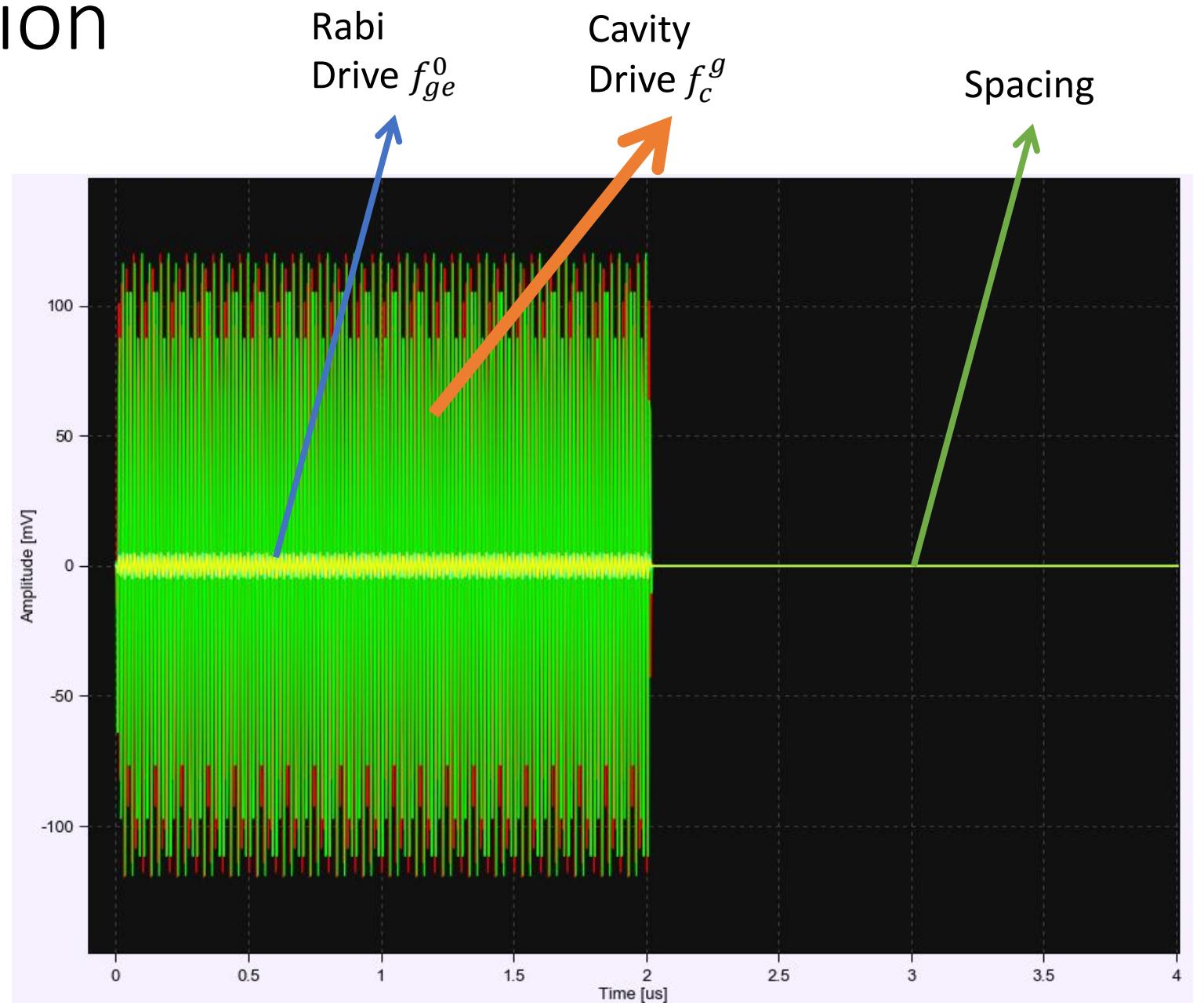


RESET calibration

$|g, 0\rangle \longleftrightarrow |g, \alpha\rangle$

$|e, \alpha\rangle$

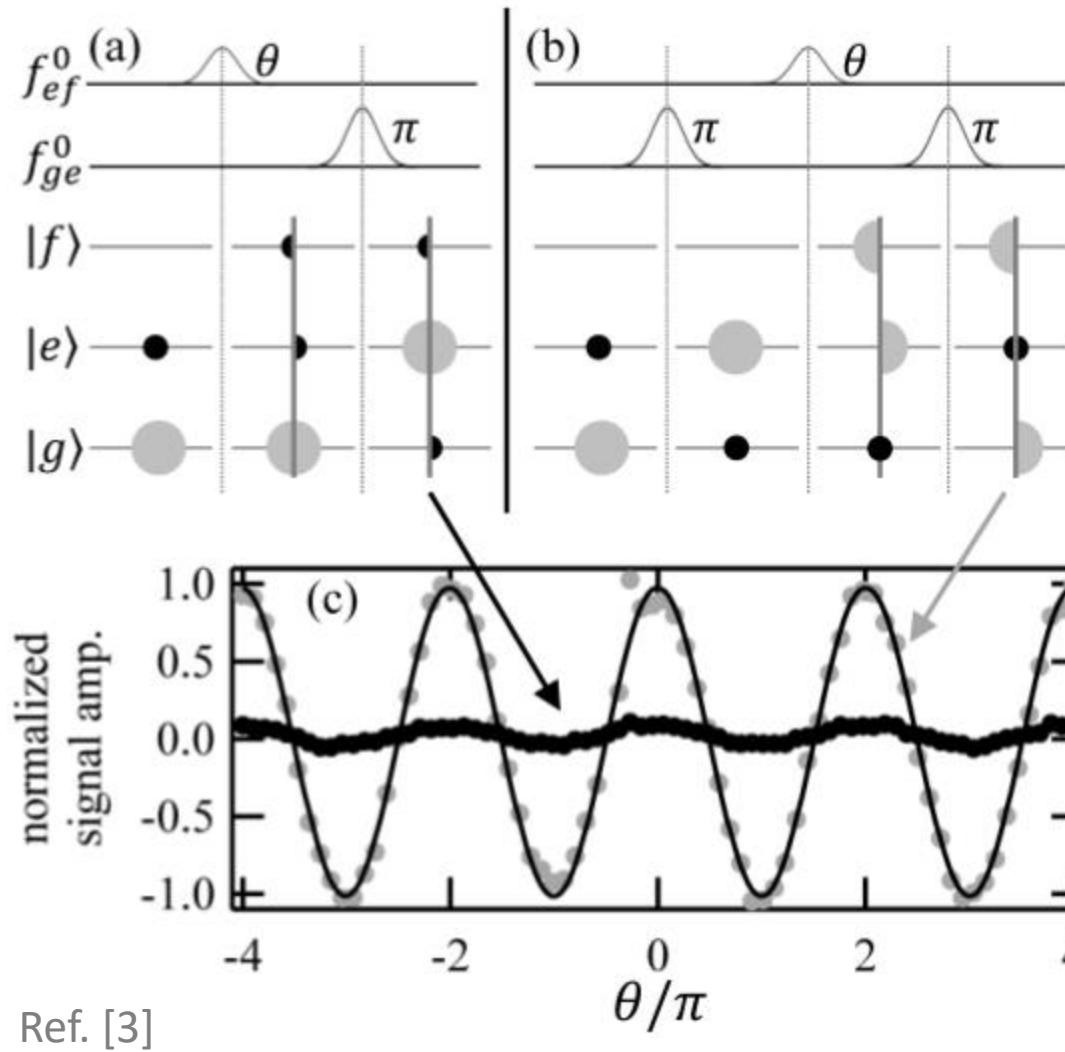
$|e, 0\rangle$



RPM measurement

$|1\rangle \rightarrow |2\rangle$ transition

(a) Proportional
to the **excited**
state population



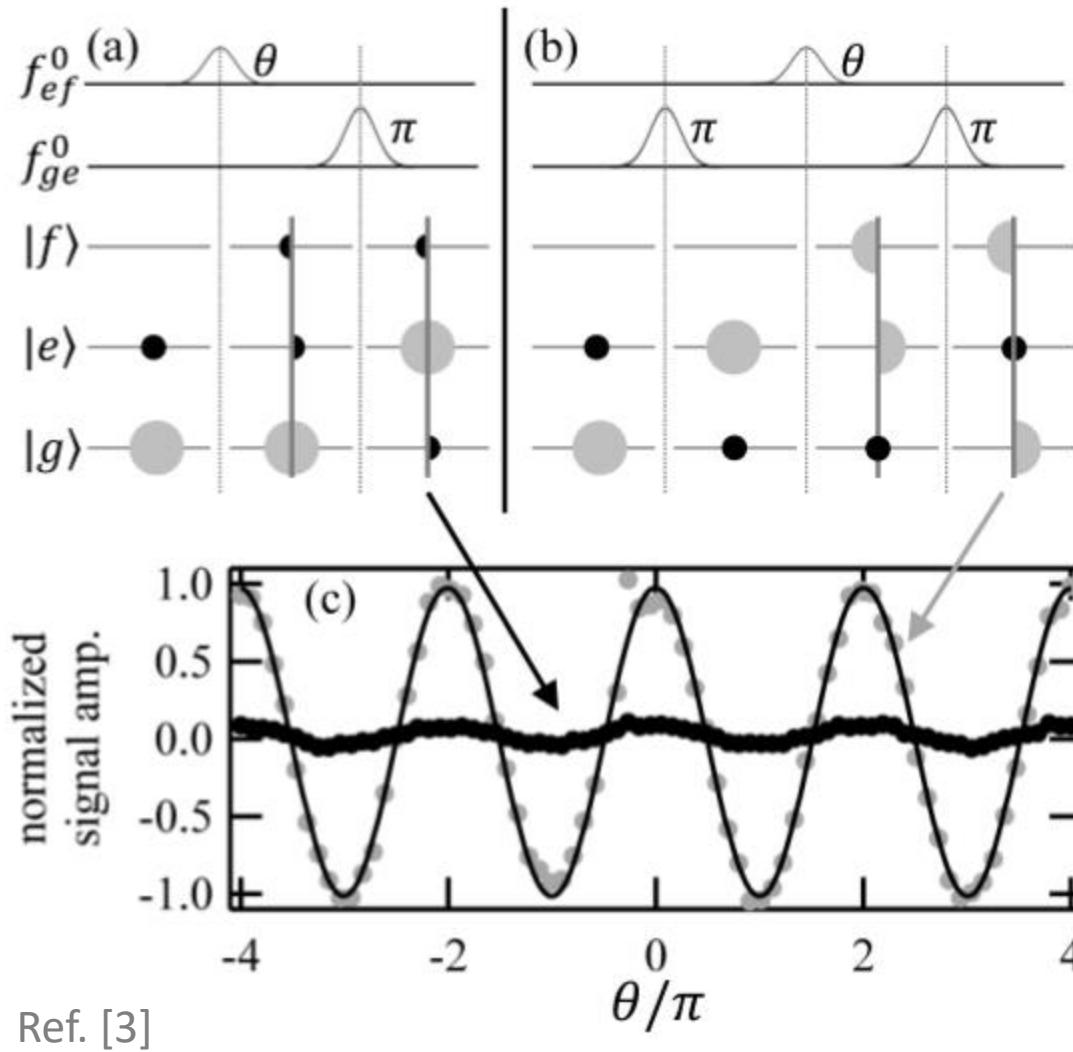
Ref. [3]

(b) Proportional
to the **ground**
state population

RPM measurement

$|1\rangle \rightarrow |2\rangle$ transition

(a) Proportional
to the **excited**
state population

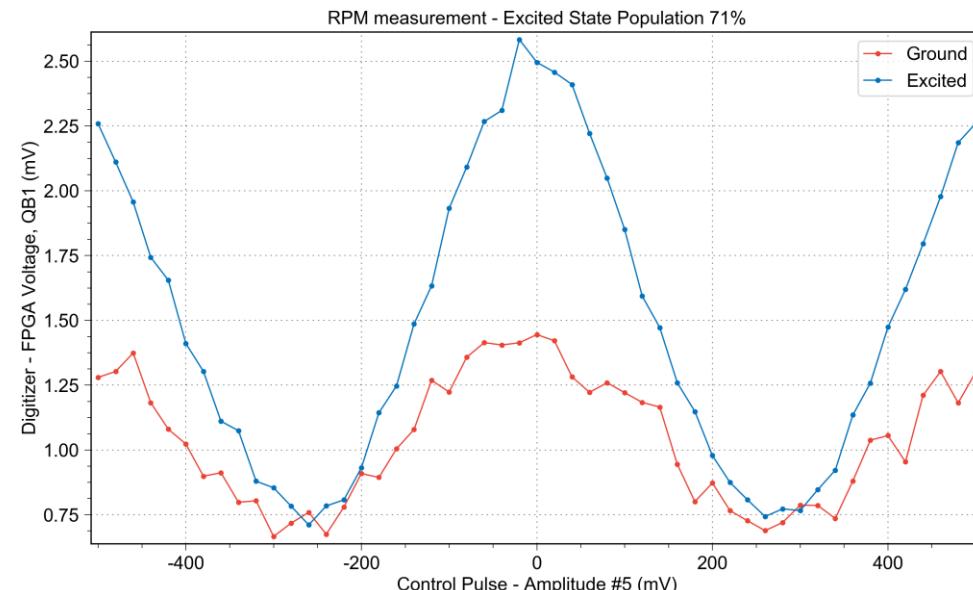
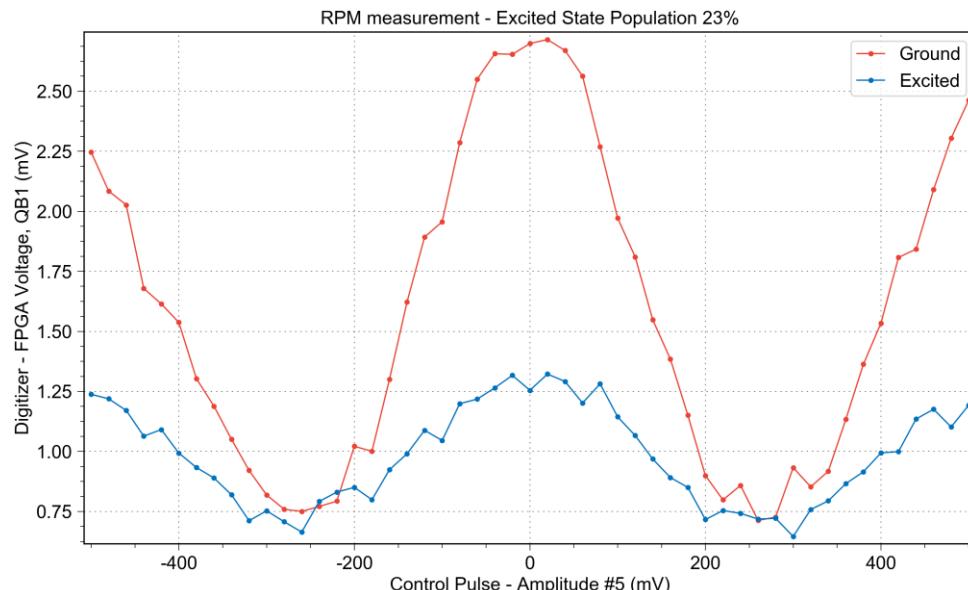
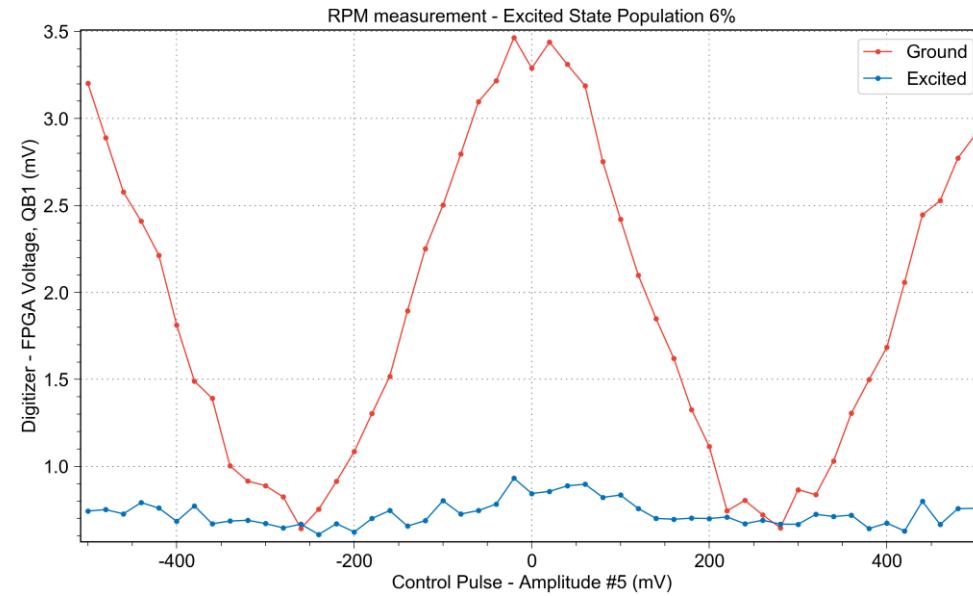
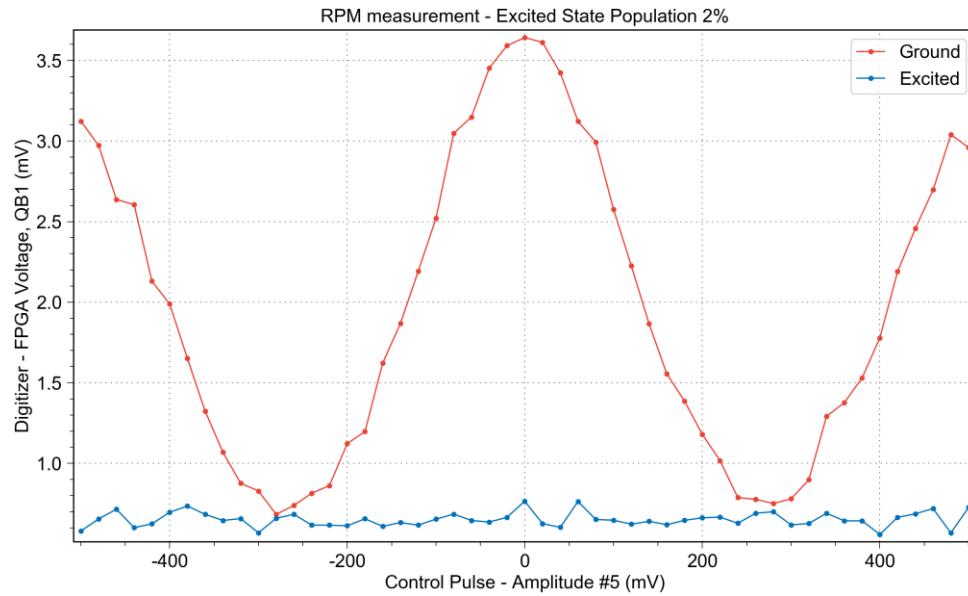


Ref. [3]

$$P_e = \frac{A_e}{A_e + A_g}$$

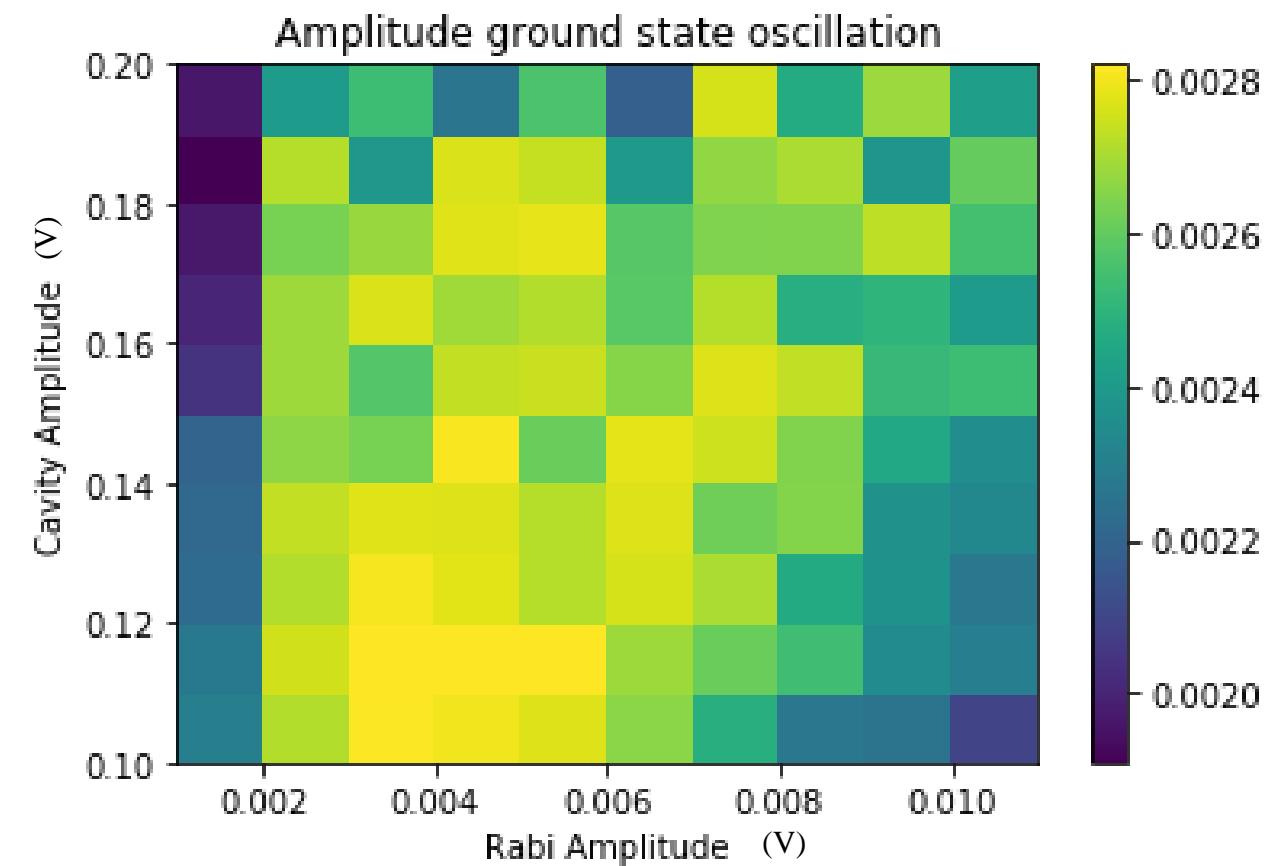
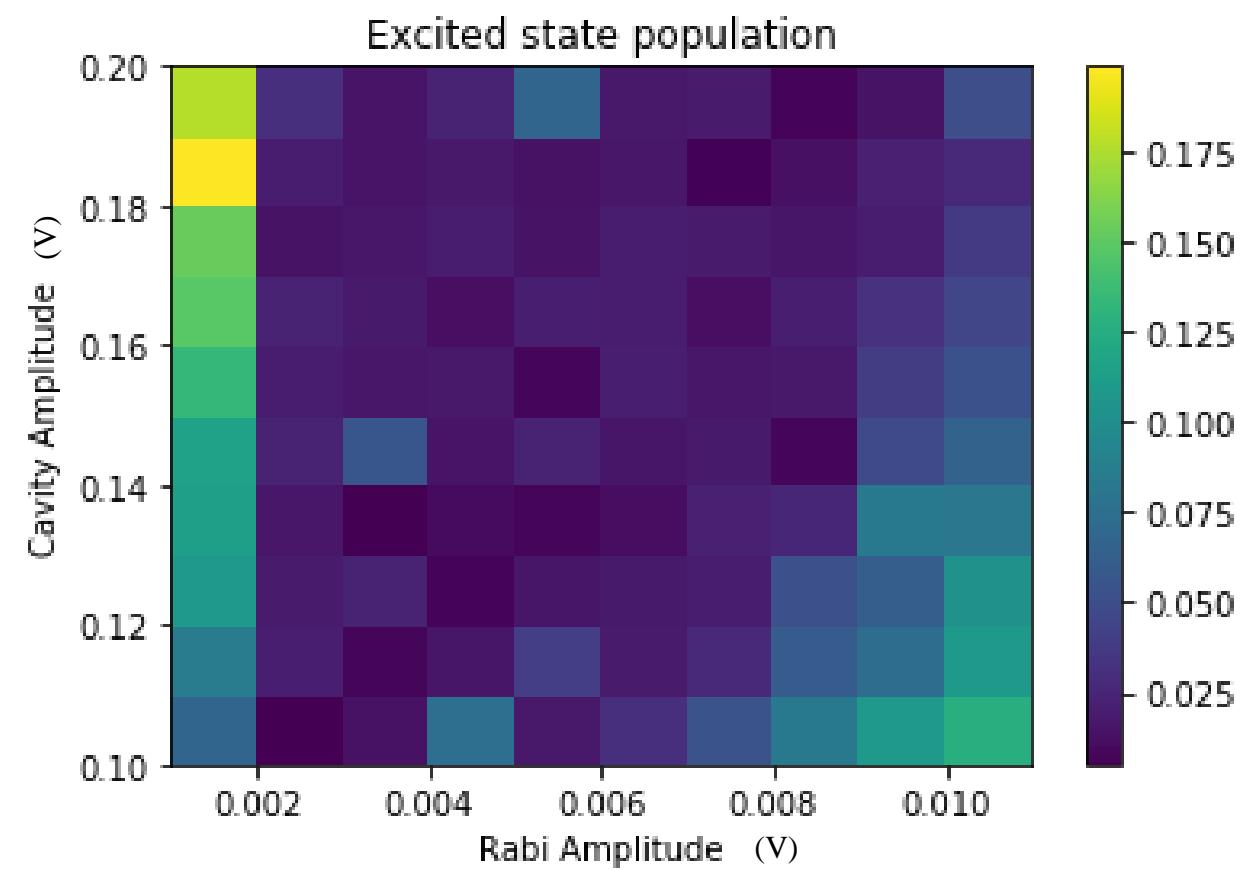
(b) Proportional
to the **ground**
state population

RPM measurement



Amplitudes calibration

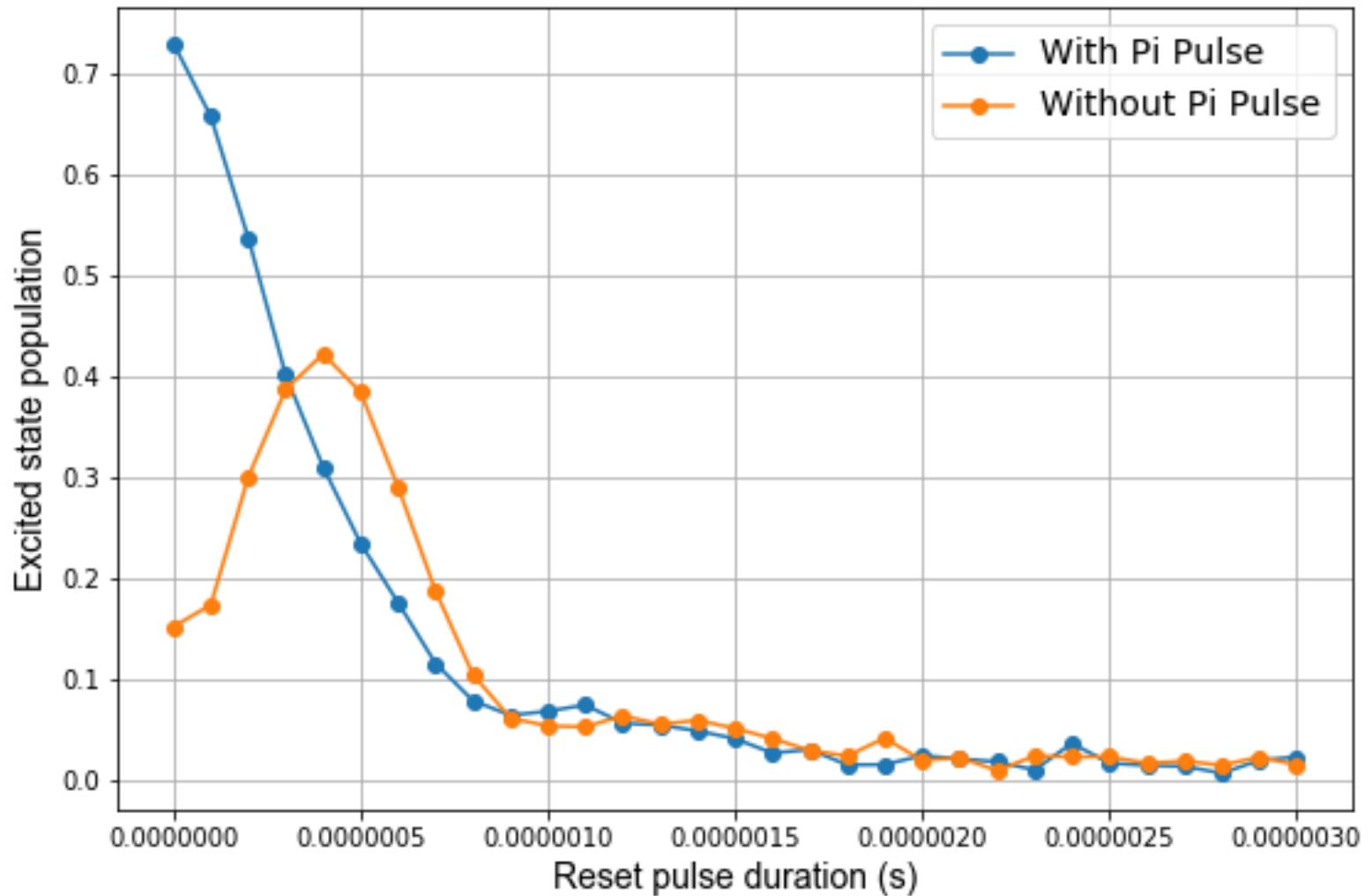
```
cal.getReset(  
    Amplitudes = True)
```



cal._ResetRabiAmplitude = 4 mV
cal._ResetCavityAmplitude = 110 mV

Duration calibration

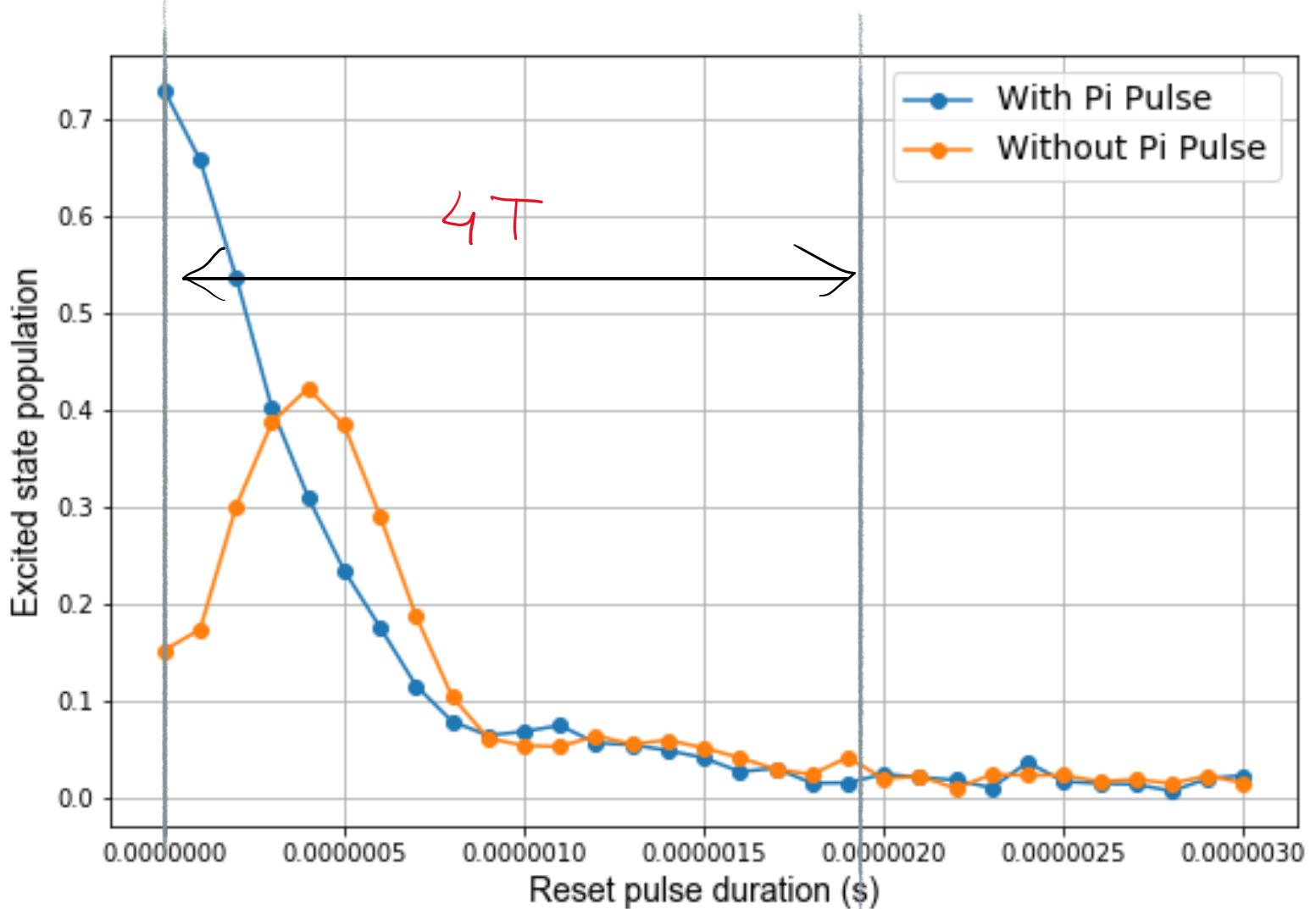
```
cal.getReset(  
Length = True)
```



Duration calibration

```
cal.getReset(  
Length = True)
```

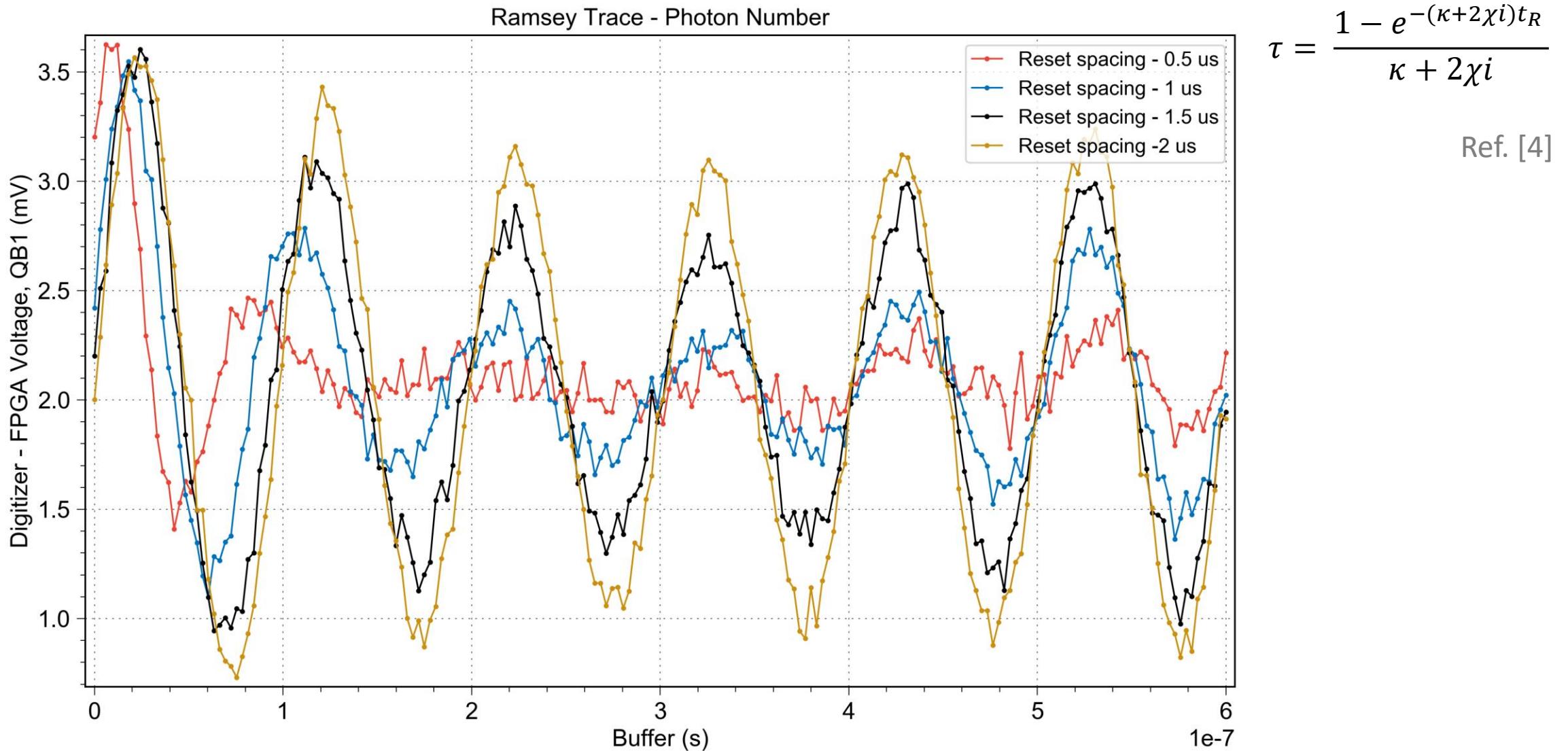
$$A + Be^{-t/T}$$



cal._ResetLength = 2 us

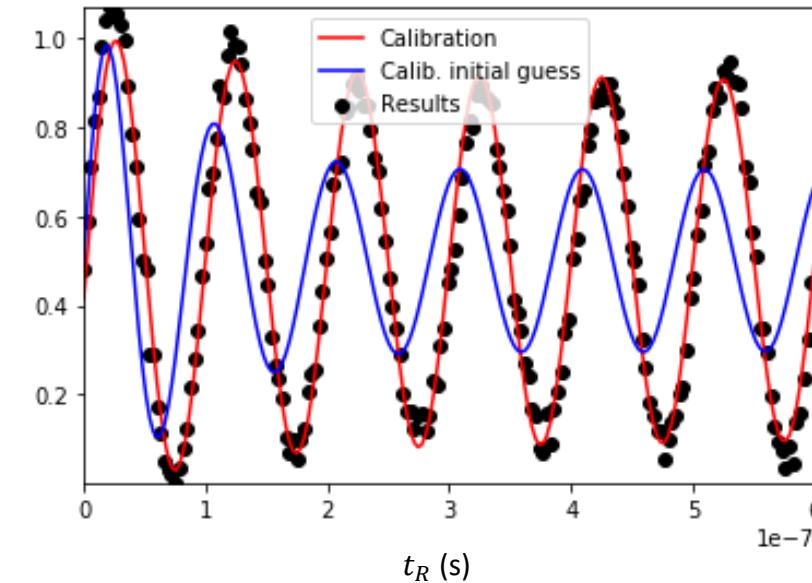
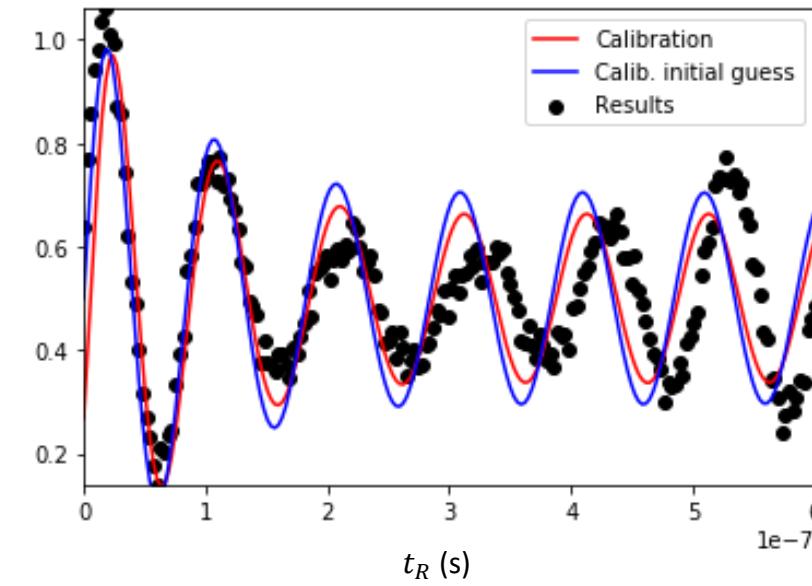
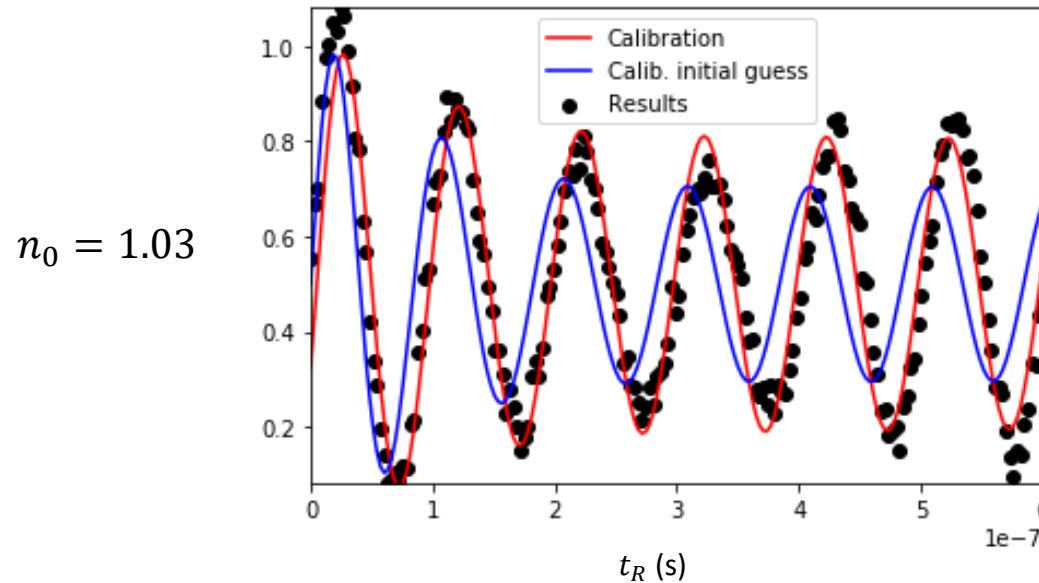
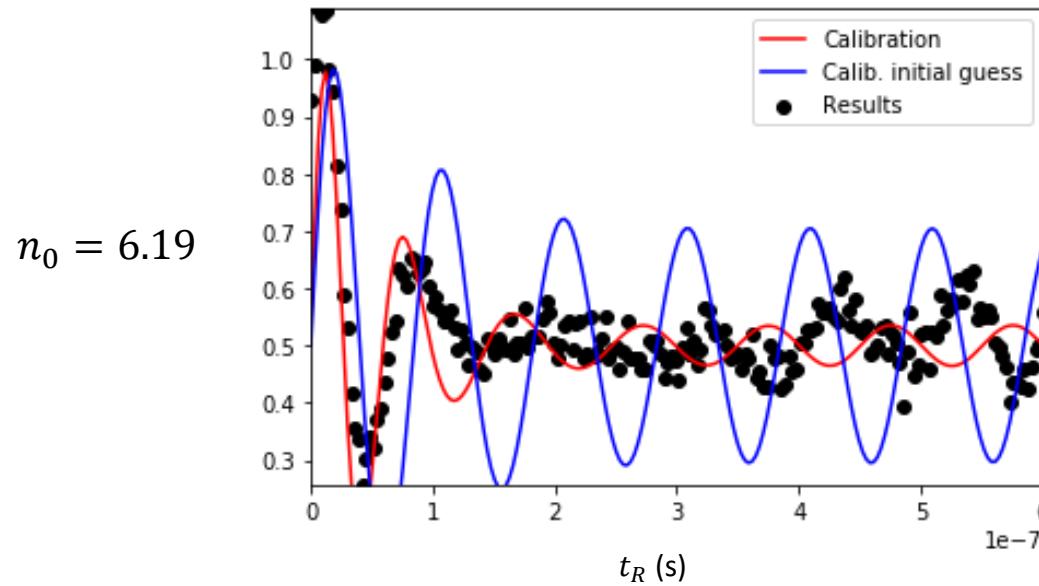
Spacing calibration

$$\frac{1}{2} \left[1 - \text{Im}(\exp(-\left(\frac{1}{T_{2Echo}} + \Delta i \right) t_R + (\phi_0 - 2n_0\chi\tau)i)) \right]$$



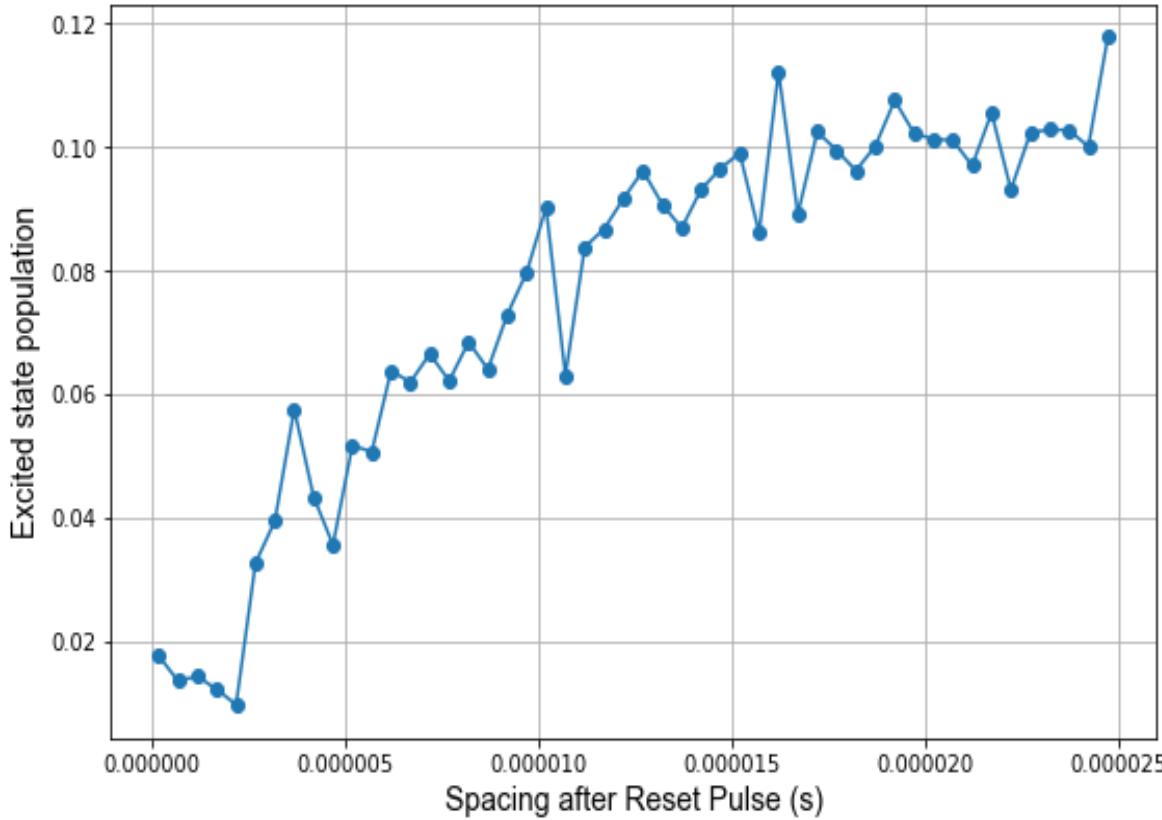
Number of photons

$$\frac{1}{2} \left[1 - \text{Im}(\exp(-\left(1/T_{2Echo} + \Delta i\right) t_R + (\phi_0 - 2n_0\chi\tau)i)) \right]$$

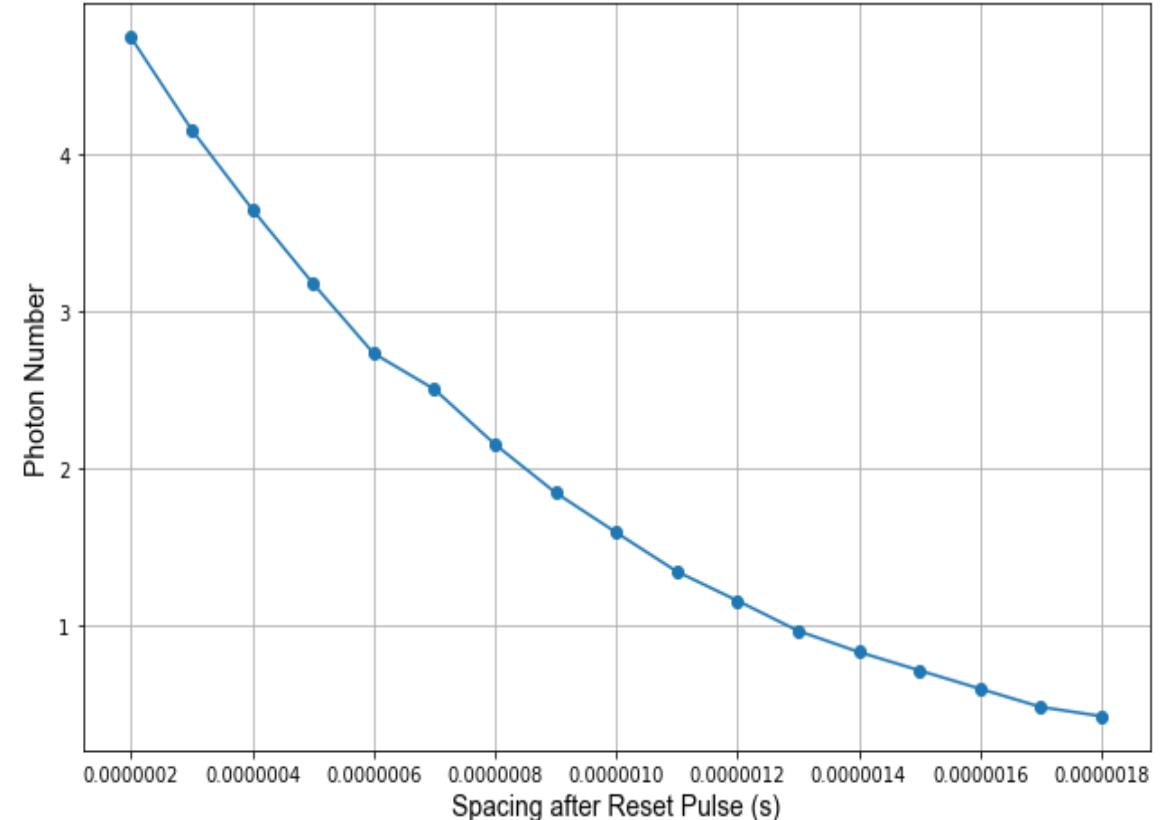


Spacing calibration

cal.getReset(
Spacing = True)

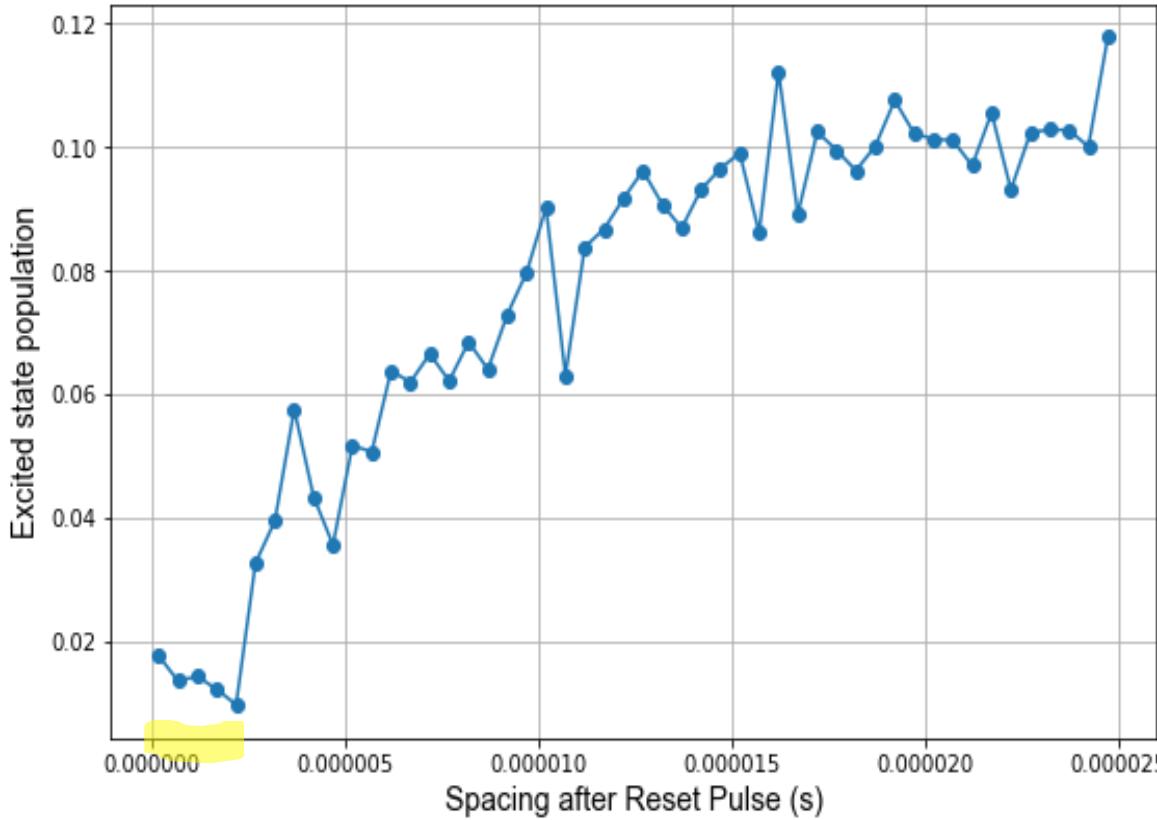


cal._ResetSpacing = 2 us

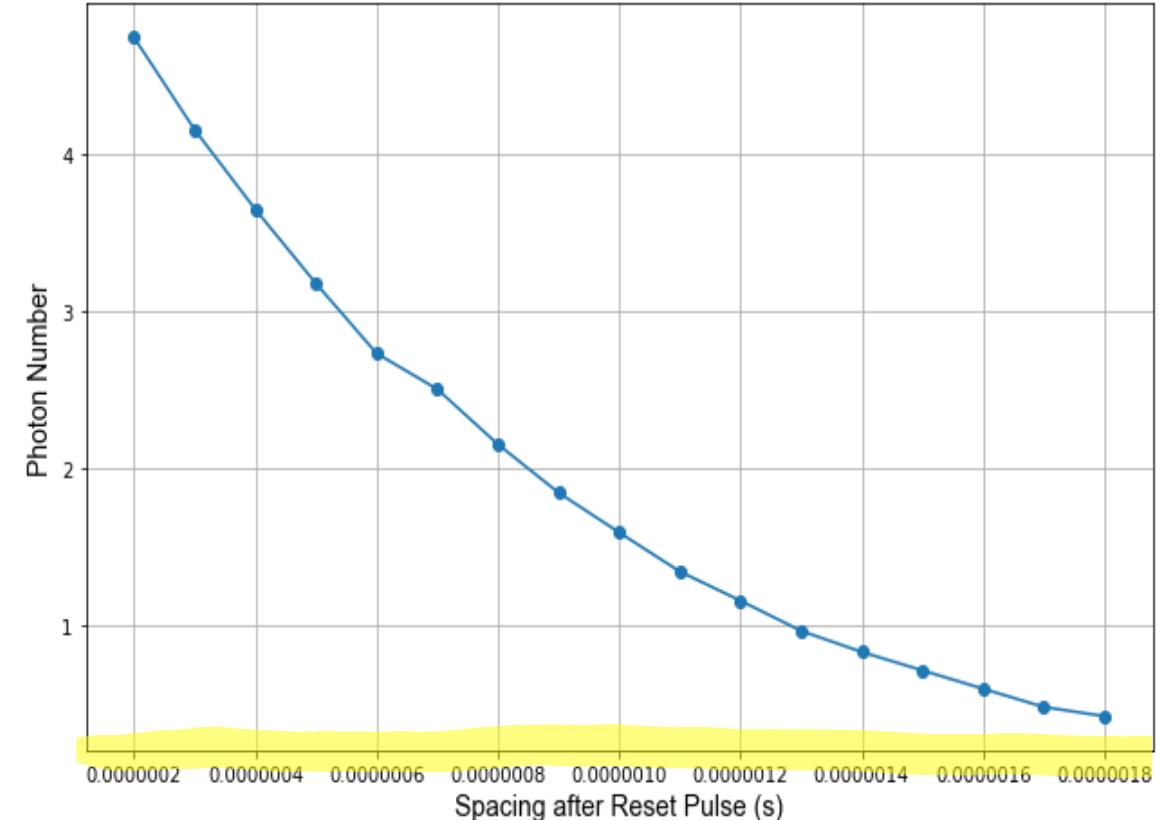


Spacing calibration

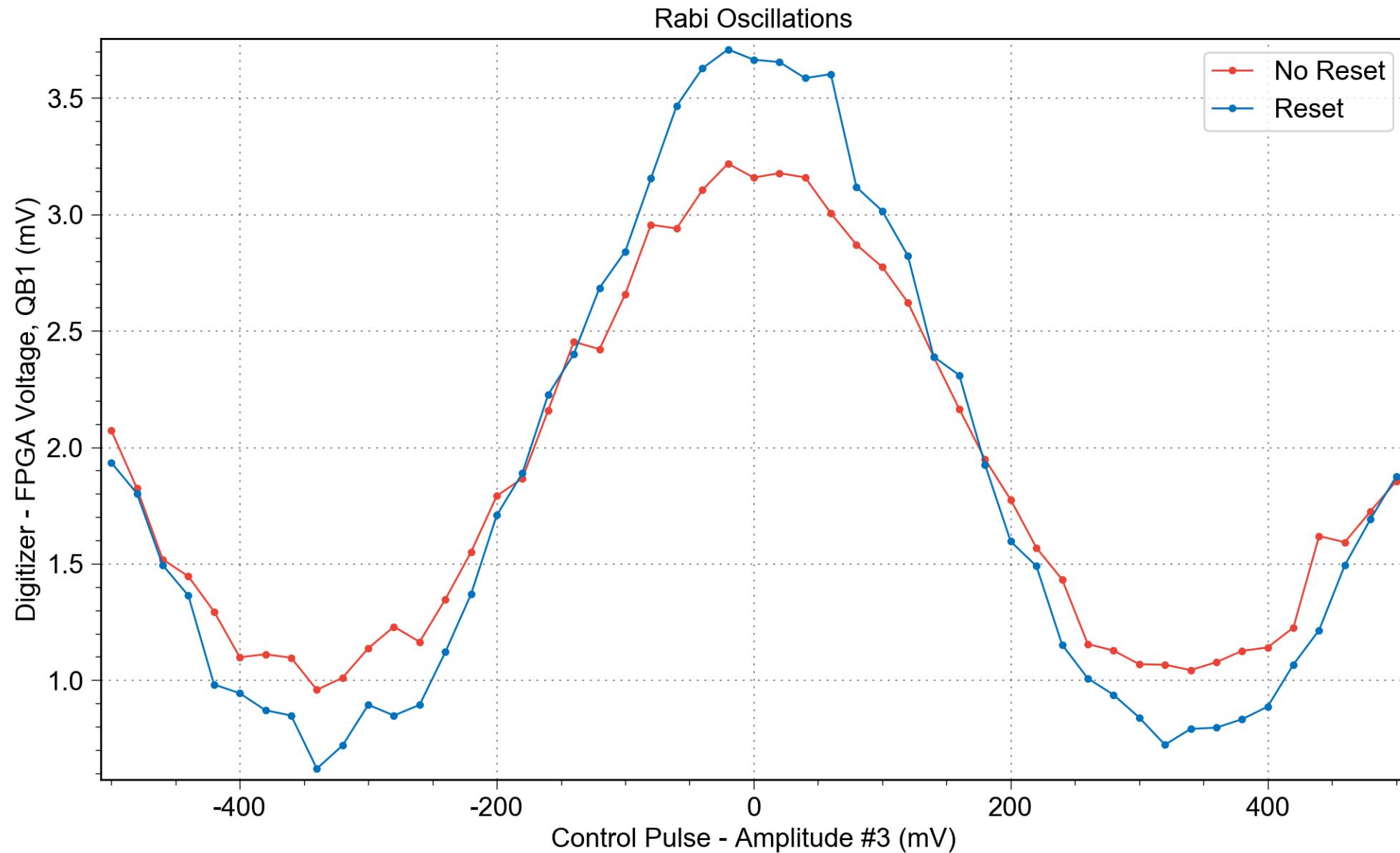
cal.getReset(
Spacing = True)



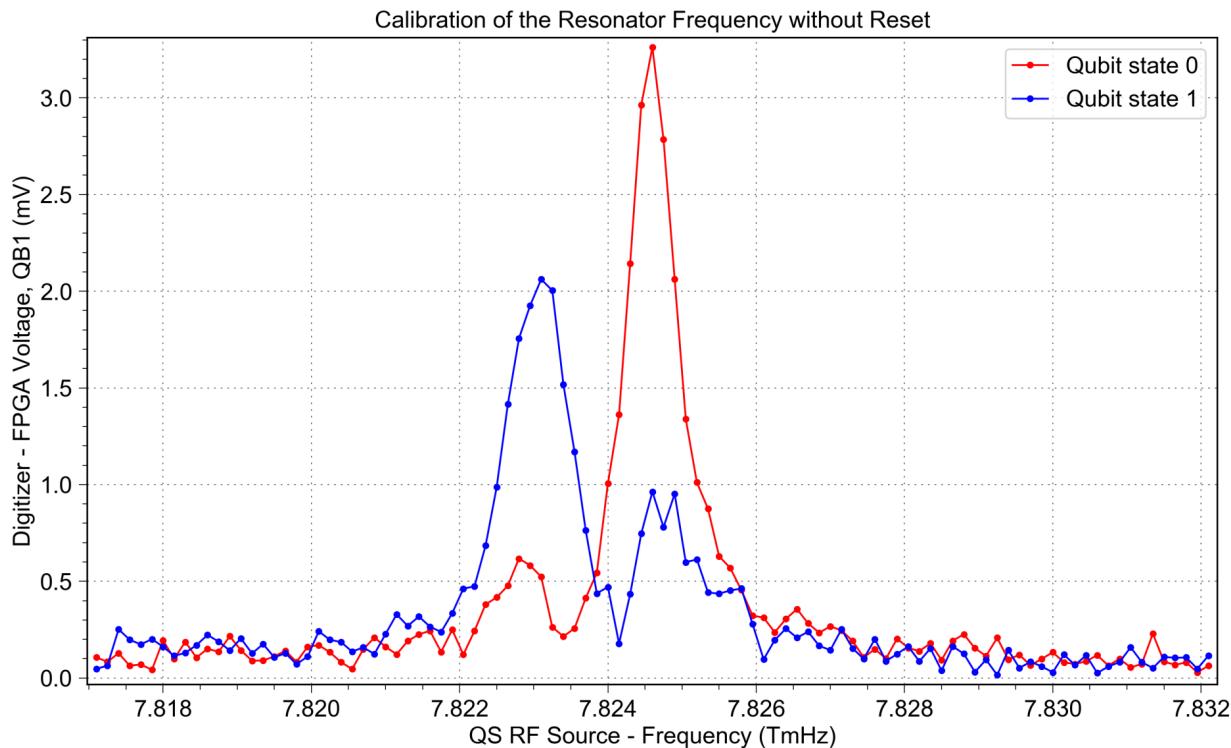
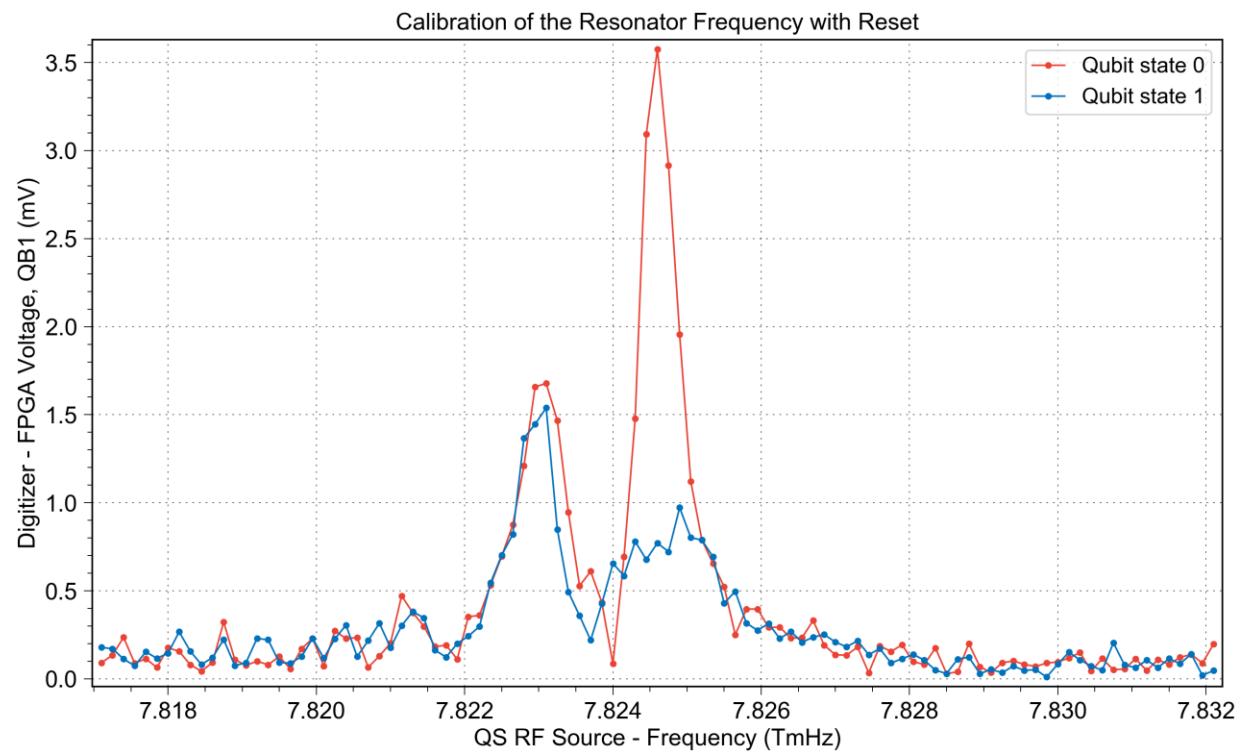
cal._ResetSpacing = 2 us



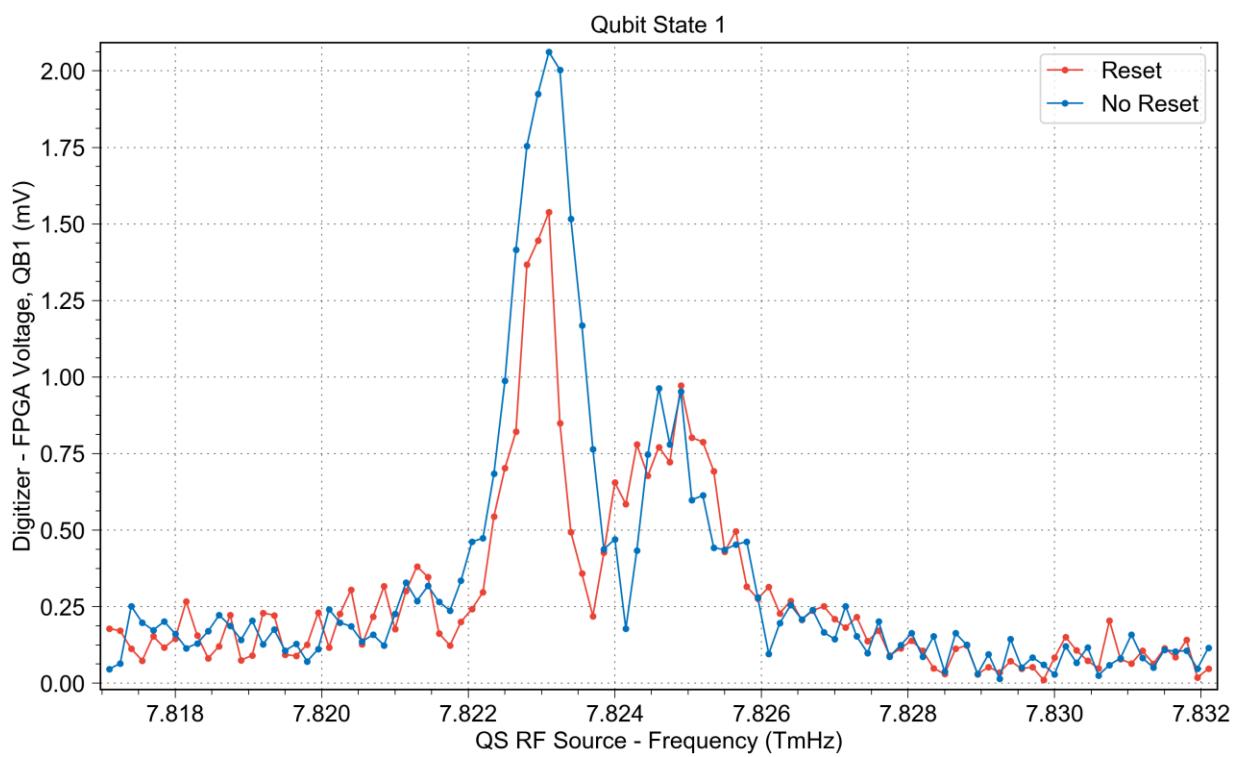
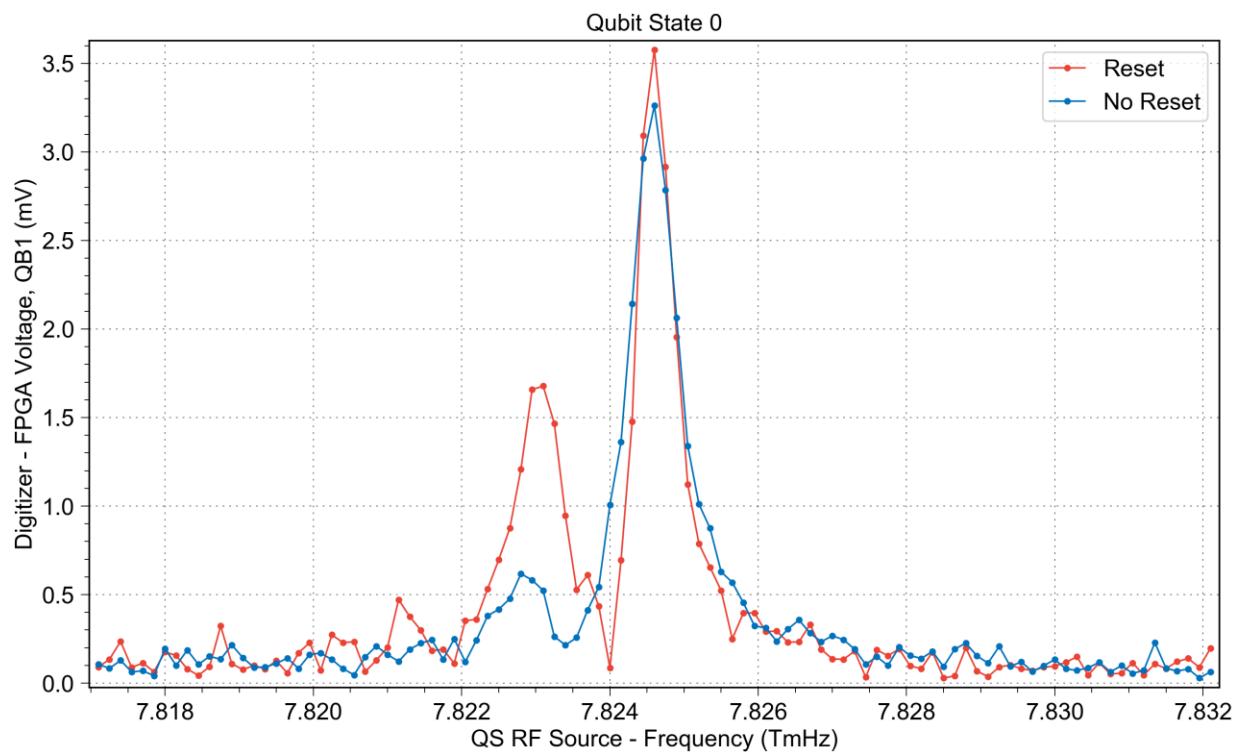
Reset vs. No Reset



Reset vs. No Reset



Reset vs. No Reset



Reset vs. No Reset

Reset

	Result	Runtime
π pulse	0.338 V	15 s
Amax	0.0036 V	
Amin	0.0007 V	
T_1	14.67 us	15 s
T_2	6.77 us	2 min
$T_{\varphi,G}$	9.35 us	
T_{2Echo}	8.24 us	30 s
Qubit Frequency	4.8250361 GHz	1 min
Cavity Frequency $ 0\rangle$	7.75462 GHz	1 min
Cavity Frequency $ 1\rangle$	7.75294 GHz	

No Reset

	Result	Runtime
	0.337 V	30 s
	0.0032 V	
	0.0010 V	
	14.56 us	30 s
	8.65 us	3 min
	11.75 us	
	9.92 us	1 min
	4.8250351 GHz	2 min
	7.75460 GHz	2 min
	7.75305 GHz	