

### Tarefa 3: Exponenciação Rápida

Calcule  $a^{e-1} \pmod{e}$  para  $e \in \{3, 5, 7\}$  e  $a \in \{1, 2, 3, 4, 5\}$

$$\begin{array}{lll} 1^{3-1} \pmod{3} & 1^{5-1} \pmod{5} & 1^{7-1} \pmod{7} \\ 1^2 = 1 \cdot 1 = \boxed{1} & 1^4 = 1^2 \cdot 1^2 = 1 \cdot 1 = \boxed{1} & 1^6 = 1^3 \cdot 1^3 = 1 \cdot 1 = \boxed{1} \\ & 1^2 = 1 \cdot 1 = 1 & 1^3 = 1 \cdot 1 \cdot 1 = 1 \end{array}$$

$$\begin{array}{lll} 2^{3-1} \pmod{3} & 2^{5-1} \pmod{5} & 2^{7-1} \pmod{7} \\ 2^2 = 2 \cdot 2 = 4 = \boxed{1} & 2^4 = 2^2 \cdot 2^2 = 4 \cdot 4 = 16 = \boxed{1} & 2^6 = 2^3 \cdot 2^3 = 1 \cdot 1 = \boxed{1} \\ & 2^2 = 2 \cdot 2 = 4 & 2^3 = 2 \cdot 2 \cdot 2 = 8 = 1 \end{array}$$

$$\begin{array}{lll} 3^{3-1} \pmod{3} & 3^{5-1} \pmod{5} & 3^{7-1} \pmod{7} \\ 3^2 = 3 \cdot 3 = 9 = \boxed{0} & 3^4 = 3^2 \cdot 3^2 = 4 \cdot 4 = 16 = \boxed{1} & 3^6 = 3^3 \cdot 3^3 = 6 \cdot 6 = 36 = \boxed{1} \\ & 3^2 = 3 \cdot 3 = 9 = 4 & 3^3 = 3 \cdot 3 \cdot 3 = 27 = 6 \end{array}$$

$$\begin{array}{lll} 4^{3-1} \pmod{3} & 4^{5-1} \pmod{5} & 4^{7-1} \pmod{7} \\ 4^2 = 4 \cdot 1 = 16 = \boxed{1} & 4^4 = 4^2 \cdot 4^2 = 1 \cdot 1 = \boxed{1} & 4^6 = 4^3 \cdot 4^3 = 1 \cdot 1 = \boxed{1} \\ & 4^2 = 4 \cdot 1 = 16 = 1 & 4^3 = 4 \cdot 4 \cdot 4 = 64 = 1 \end{array}$$

$$\begin{array}{lll} 5^{3-1} \pmod{3} & 5^{5-1} \pmod{5} & 5^{7-1} \pmod{7} \\ 5^2 = 5 \cdot 5 = 25 = \boxed{1} & 5^4 = 5^2 \cdot 5^2 = 0 \cdot 0 = \boxed{0} & 5^6 = 5^3 \cdot 5^3 = 6 \cdot 6 = 36 = \boxed{1} \\ & 5^2 = 5 \cdot 5 = 25 = 0 & 5^3 = 5 \cdot 5 \cdot 5 = 125 = 6 \end{array}$$