Probabilistic Abductive Logic Programming using Dirichlet Priors

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Why probabilistic programming?

Goal: Generalized inference for a class of probabilistic models.

Probabilistic program = "generative story", execution = inference.

The traditional way:

 ${\sf realization} = {\sf model} \ {\sf development} + {\sf derivation} \ {\sf of} \ {\sf inference} \ {\sf algo}. \ +$

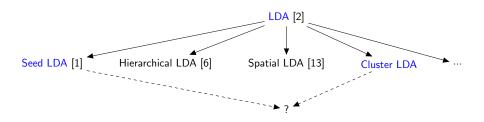
implementation + execution

Using probabilistic programming:

 $realization = model \ development + execution$

⇒ Less effort, less time, more models!

E.g. Latent Dirichlet Allocation (LDA) and variations



Why another probabilistic programming language?

Probabilistic Programming

- tendency towards Universal Probabilistic Programming
- typically based on functional programming (Scheme for Church [5], Clojure for Anglican [11], etc.)
- inference in some discrete models, e.g. LDA, can be slow and doesn't always converge

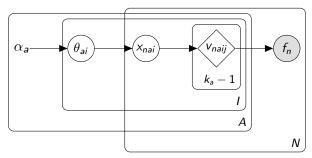
Probabilistic Logic

- [7] describes generalized inference for discrete models with Dirichlet priors, but no probabilistic programming
- typical probabilistic logic programming languages don't support Dirichlet priors
- Markov logic has an inherent limitation: no recursive definitions.

 $[\]Rightarrow$ peircebayes

peircebayes (PB)

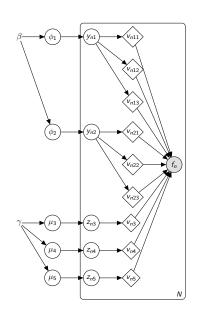
 a probabilistic abductive logic programming language designed for inference in probabilistic models with categorical variables and Dirichlet priors.



- \bullet α are parameters of Dirichlet distributions
- $\theta \sim \mathsf{Dirichlet}(\alpha)$ and $x \sim \mathsf{Cat}(\theta)$
- \bullet v are boolean encodings of x (i.e. annotated disjunction compilation)
- *f* are outputs of boolean functions of *v*. The functions are computed using abduction.

Latent Dirichlet Allocation (LDA)

- LDA is well studied model for topic modelling [2].
- Corpus = set of *D* documents.
- A document is a bag of words.
- V is the size of the vocabulary, # of unique words in the corpus.
- Each word is sampled from one of T topics.
- A topic is a categorical distribution over V categories.
- A document is a mixture of topics.
- Task: infer topics and their mixtures per document.



LDA in peircebayes

```
observe(d(1), [ (w(1), 4), (w(4), 2) ]).
observe(d(2), [ (w(3), 1), (w(4), 5) ]).
observe(d(3), [ (w(1), 4), (w(2), 2) ]).
pb_dirichlet(1.0, mu, 2, 3).
pb_dirichlet(1.0, phi, 4, 2).
generate(Doc, Token) :-
    Topic in 1...2,
    mu(Topic, Doc),
    phi(Token, Topic).
pb_plate(
  [observe(d(Doc), TokenL),
    member((w(Token), Count), TokenL)],
    Count.
    [generate(Doc, Token)]).
```

LDA Experiment

Usenet comp.* dataset (only test documents):

- 1911 documents
- 35850 unique words
- average document length: ~ 108 words
- 10 topics, priors: $\beta = 50/T$, $\gamma = 0.1$

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LDA with seed constraints

```
observe(d(1), [ (w(1), 4), (w(4), 2) ]). % ...
pb_dirichlet(1.0, mu, 2, 3).
pb_dirichlet(1.0, phi, 4, 2).
seed_naf(Token) :- seed(Token, _).
seed(1, [1]). seed(4, [2]).
pb_plate(
  [observe(d(Doc), TokenL), member((w(Token), Count), TokenL),
     \+ seed_naf(Token) ],
  Count.
  [Topic in 1..2, mu(Topic, Doc), phi(Token, Topic)]).
pb_plate(
  [observe(d(Doc), TokenL), member((w(Token), Count), TokenL),
     seed_naf(Token) ],
  Count.
  [ seed(Token, TopicL), member(Topic, TopicL),
     mu(Topic,Doc), phi(Token,Topic) ]).
```

Seed LDA Experiment

- experiment inspired by [1]
- 4777 documents
- 27206 unique words (tokenize + WordNet lemmatizer)
- average document length:
 ~ 72 words
- 20 topics, priors: $\beta = 50/T$, $\gamma = 0.01$
- 2 topics are seeded: (hardware, machine, memory, cpu), and (software, program, version, shareware)





Cluster LDA Experiment

Data - all arXiv abstracts in 2007 in five categories.

Partition 25 topics in 5 clusters of 5 topics. The generative story of a word is: choose cluster, choose topic from cluster, choose word from topic.

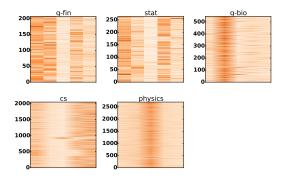
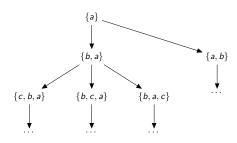


Figure: Cluster mixture for each category (x - topic clusters, y - documents, darker colour - higher probability).

Repeated Insertion Model (RIM) [4]



- Assume a totally ordered set S of N items.
- A preference is a permutation of S.
- A preference profile is a distribution over all the permutations of S.
- Assume *K* preference profiles.
- Observed data: A list of permutations of S.
- Task: Infer the parameters of the *K* distribution profiles and their mixture.

RIM Experiment

- 5000 persons surveyed for preference over 10 Sushi ingredients [8]
- experiment inspired by [9], K=6 preference profiles, priors: 50/K for preference profile mixtures and 0.1 for all categorical distributions

$\pi_1 = 0.155$	$\pi_2 = 0.194$	$\pi_3 = 0.134$	$\pi_4 = 0.194$	$\pi_5 = 0.197$	$\pi_6 = 0.126$
fatty tuna					
shrimp	tuna	sea eel	sea urchin	tuna	shrimp
salmon roe	shrimp	tuna	salmon roe	shrimp	tuna
sea eel	squid	shrimp	shrimp	squid	sea eel
squid	egg	squid	sea eel	sea eel	squid
tuna	tuna roll	tuna roll	tuna	tuna roll	salmon roe
tuna roll	sea eel	salmon roe	tuna roll	salmon roe	tuna roll
sea urchin	cucumb. roll	sea urchin	squid	sea urchin	sea urchin
egg	salmon roe	egg	egg	cucumb. roll	egg
cucumb. roll	sea urchin	cucumb. roll	cucumb. roll	egg	cucumb. roll

Table: Mixture parameters and modes of preference profiles on the Sushi dataset.

Summary and Conclusions

We introduce peircebayes – a probabilistic abductive logic programming language tailored for inference in discrete models with Dirichlet priors. We show 4 probabilistic models and experiments in peircebayes:

- √ vanilla LDA.
 - ✓ LDA with seed constraints.
 - ✓ cluster LDA.
 - \square the repeated insertion model (RIM).

Future work:

- □ explore other models that fit the paradigm, e.g. Bayesian prevalence model [10], citation influence model [3].
- ☐ explore inductive learning in peircebayes.
- develop a non-parametric peircebayes based on work in Dirichlet Processes [12].
- ☐ improve scalability from medium to large datasets.

Thank You!

Online resources on peircebayes: http://raresct.github.io.

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Cluster LDA

```
pb_dirichlet(10.0, psi, 5, 5769).
pb_dirichlet(10.0, theta1, 5, 5769). % ...
pb_dirichlet(10.0, theta5, 5, 5769).
pb_dirichlet(0.1, phi1, 26834, 5). % ...
pb_dirichlet(0.1, phi5, 26834, 5).
pb_plate(
  [observe(d(Doc), TokenL), member((w(Token), Count), TokenL)],
  Count, [generate(Doc, Token)]).
create_term(Functor, Idx, Cat, Distrib, Term) :-
  number_chars(Idx, LIdx), atom_chars(Functor, LFunctor),
  append(LFunctor, LIdx, LF), atom_chars(F, LF),
  Term = .. [F, Cat, Distrib].
generate(Doc, Token) :-
  Cluster in 1..5, Topic in 1..5, psi(Cluster, Doc),
  create_term(theta, Cluster, Topic, Doc, Term1), pb_call(Term1),
  create_term(phi, Cluster, Token, Topic, Term2), pb_call(Term2).
```

RIM in peircebayes (I)

```
observe([0,9,6,3,7,2,8,1.5.4]).
observe([5.0.3.4.6.9.8.1.7.2]).
% ... 4998 'observe' facts ommited
pb_dirichlet(8.33333333333, pi, 6, 1).
pb_dirichlet(0.1, p2, 2, 6).
                                   pb_dirichlet(0.1, p7, 7, 6).
pb_dirichlet(0.1, p3, 3, 6).
                                   pb_dirichlet(0.1, p8, 8, 6).
pb_dirichlet(0.1, p4, 3, 6).
                                   pb_dirichlet(0.1, p9, 9, 6).
pb_dirichlet(0.1, p5, 5, 6).
                                   pb_dirichlet(0.1, p10, 10, 6).
pb_dirichlet(0.1, p6, 6, 6).
pb_plate( [observe(Sample)], 1,
    [generate([0,1,2,3,4,5,6,7,8,9], Sample)]).
generate([H|T], Sample):-
    K in 1..6, pi(K, 1), generate(T, Sample, [H], 2, K).
```

RIM in peircebayes (II)

```
generate([], Sample, Sample, _Idx, _K).
generate([ToIns|T], Sample, Ins, Idx, K) :-
    % insert next element at Pos yielding a new list Ins1
    append(_, [ToIns|Rest], Sample),
    insert_rim(Rest, ToIns, Ins, Pos, Ins1),
    % build prob predicate in Pred
   number_chars(Idx, LIdx), append(['p'], LIdx, LF),
    atom_chars(F, LF), Pred = .. [F, Pos, K],
    % call prob predicate and recurse
    pb_call(Pred), Idx1 is Idx+1,
    generate(T, Sample, Ins1, Idx1, K).
insert_rim([], ToIns, Ins, Pos, Ins1) :-
    append(Ins, [ToIns], Ins1), length(Ins1, Pos).
insert_rim([H|_T], ToIns, Ins, Pos, Ins1) :-
    nth1(Pos, Ins, H), nth1(Pos, Ins1, ToIns, Ins).
insert_rim([H|T] , ToIns, Ins, Pos, Ins1) :-
    \+member(H, Ins), insert_rim(T, ToIns, Ins, Pos, Ins1).
```