

```
> with(geometry);with(plots);Digits:=30;_EnvHorizontalName := x;
  _EnvVerticalName := y;
```

```
[Apollonius, AreCollinear, AreConcurrent, AreConcyclic, AreConjugate, AreHarmonic,
  AreOrthogonal, AreParallel, ArePerpendicular, AreSimilar, AreTangent, CircleOfSimilitude,
  CrossProduct, CrossRatio, DefinedAs, Equation, EulerCircle, EulerLine, ExteriorAngle,
  ExternalBisector, FindAngle, GergonnePoint, GlideReflection, HorizontalCoord, HorizontalName,
  InteriorAngle, IsEquilateral, IsOnCircle, IsOnLine, IsRightTriangle, MajorAxis, MakeSquare,
  MinorAxis, NagelPoint, OnSegment, ParallelLine, PedalTriangle, PerpenBisector,
  PerpendicularLine, Polar, Pole, RadicalAxis, RadicalCenter, RegularPolygon,
  RegularStarPolygon, SensedMagnitude, SimsonLine, SpiralRotation, StretchReflection,
  StretchRotation, TangentLine, VerticalCoord, VerticalName, altitude, apothem, area, asymptotes,
  bisector, center, centroid, circle, circumcircle, conic, convexhull, coordinates, detail, diagonal,
  diameter, dilatation, directrix, distance, draw, dsegment, ellipse, excircle, expansion, foci, focus,
  form, homology, homothety, hyperbola, incircle, inradius, intersection, inversion, line, medial,
  median, method, midpoint, orthocenter, parabola, perimeter, point, powerpc, projection, radius,
  randpoint, reciprocation, reflection, rotation, segment, sides, similitude, slope, square, stretch,
  tangentspc, translation, triangle, vertex, vertices]
```

```
[animate, animate3d, animatecurve, arrow, changecoords, complexplot, complexplot3d, conformal,
  conformal3d, contourplot, contourplot3d, coordplot, coordplot3d, cylinderplot, densityplot,
  display, display3d, fieldplot, fieldplot3d, gradplot, gradplot3d, graphplot3d, implicitplot,
  implicitplot3d, inequal, interactive, listcontplot, listcontplot3d, listdensityplot, listplot, listplot3d,
  loglogplot, logplot, matrixplot, odeplot, pareto, plotcompare, pointplot, pointplot3d, polarplot,
  polygonplot, polygonplot3d, polyhedra_supported, polyhedraplot, replot, rootlocus, semilogplot,
  setoptions, setoptions3d, spacecurve, sparsematrixplot, sphereplot, surfdata, textplot, textplot3d,
  tubeplot]
```

*Digits := 30*

*\_EnvHorizontalName := x*

*\_EnvVerticalName := y*

```
> distancia := proc( i )
>   local r, s, t; global p4;
>
>   r := (c_a*clave)/(clave-i*c_a);
>   s := -(r - raiz);
>   t := ((s*clave)-(c_a*clave))/(c_a*s);
>   s := (c_a*clave)/(clave-t*c_a);
>   p4 := round(t);
>
>   point(P1, [i, r]):
>   point(P2, [t, s]):
>
```

```

>   return distance(P1,P2);
>
[ > end proc:
[ >
[ > lower := proc( left, right )
[ >   local l, m_1, m, m1, r, new_left, middle, new_right, diff,
[   divisor;
[ >
[ >   new_left := left;
[ >   new_right:= right;
[ >   diff := new_right - new_left;
[ >   divisor := div;
[ >
[ >   if( diff < 4 ) then
[ >     new_right := right + (4-diff);
[ >     diff := new_right - new_left;
[ >   end if;
[ >
[ >   middle := ceil( new_left+((new_right-new_left)/2) );
[ >
[ >   l := distancia( new_left );
[ >   m_1:= distancia( middle-1 );
[ >   m := distancia( middle );
[ >   m1 := distancia( middle+1 );
[ >   r := distancia( new_right );
[ >
[ >   if( diff = 4 ) then
[ >     if( l < m_1 ) then
[ >       return [new_left,l];
[ >     elif( m_1 < m ) then
[ >       return [middle-1,m_1];
[ >     elif( m < m1 ) then
[ >       return [middle,m];
[ >     elif( m1 < r ) then
[ >       return [middle+1,m1]
[ >     else
[ >       return [new_right,r];
[ >     end if;
[ >   elif( (l < m_1) or (m_1 < m) ) then
[ >     new_right:= middle-1;
[ >     return lower( new_left, new_right );
[ >   elif( (m_1 > m) and (m < m1) ) then
[ >     return [middle,m];
[ >   elif( (m > m1) and ( (m1 < r) or ( r < m1) ) ) then
[ >     new_left := middle+1;
[ >     return lower( new_left, new_right );
[ >   end if;
[ >
[ > end proc:
[

```

```

[ >
[ > higher := proc( i )
[ >   local p1, p2, p3;
[ >   p1 := distancia( i-1 );
[ >   p2 := distancia( i );
[ >   p3 := distancia( i+1 );
[ >   if( (p1 > p2) and (p1 > p3) ) then
[ >     return [i-1,p1];
[ >   elif( (p2 > p1) and (p2 > p3) ) then
[ >     return [i,p2];
[ >   else return [i+1,p3];
[ >   end if;
[ > end proc:
[ >
[ > ask_one := proc( low, up, div )
[ >   local res, l, u;
[ >
[ >   l := distancia( low );
[ >   u := distancia( up );
[ >
[ >   if( l < u ) then
[ >     res := evalf(u/l);
[ >   else
[ >     res := evalf(l/u);
[ >   end if;
[ >
[ >   return res;
[ >
[ > end proc:
[ >
[ > tanto13 := proc( p1, p2, p3 )
[ >   local d1, d2, t, i, low_below, low_over, div, low_div, over_div,
[ >   top, temp;
[ >   global clave, raiz, a, c_a;
[ >   clave := p1 * p2;
[ >   raiz := evalf(sqrt(clave));
[ >
[ >   print(p1,p2,clave,raiz);
[ >
[ >   a := evalf( clave / ( clave - raiz ) );
[ >   c_a:= a * raiz;
[ >
[ >   # Original Triangle T1
[ >
[ >   low_below := [p1-1,distancia( p1-1 )];
[ >   top       := higher( trunc( raiz ) );
[ >   low_over  := [p2-1,distancia( p2-1 )];
[ >
[ >   point( PT1, low_below );

```

```

> point( PT2, top );
> point( PT3, low_over );
>
> triangle( T1, [PT1,PT2,PT3] );
>
> centroid( C1, T1 );
> orthocenter( O1, T1 );
>
> incircle( incl, T1 );
> print( "incircle center", coordinates( center( incl ) ) );
> print( "incircle radius", radius( incl ) );
>
> circumcircle( circl, T1, 'centername'=0 );
> print( "circumcircle center", coordinates( center( circl ) ) );
> print( " circumcircle radius", radius( circl ) );
>
> print( low_below );
> print( top );
> print( low_over );
> print( abs( low_below[2]-low_over[2] ) );
>
> print( area( T1 ) );
> print( coordinates( C1 ) );
> print( coordinates( O1 ) );
>
> printf("\n");
>
> # Guess Triangle T2
>
>
> low_below := [p3-1,distancia( p3-1 )];
> div        := p4;
> top        := higher( trunc(raiz) );
> low_over   := [div,distancia( div )];
>
> if( low_below[2] > low_over[2] ) then
>   temp := low_below[2];
>   low_below[2] := low_over[2];
>   low_over[2] := temp;
> end if;
>
> point( P4, low_below );
> point( P5, top );
> point( P6, low_over );
> triangle( T2, [P4,P5,P6] );
>
> centroid( C2, T2 );
> orthocenter( O2, T2 );
>

```

```

> incircle( inc2, T2, 'centername'=0 );
> print( "incircle center", coordinates( center( inc2 ) ) );
> print( "incircle radius", radius( inc2 ) );
>
> circumcircle( circ2, T2, 'centername'=0 );
> print( "circumcircle center", coordinates( center( circ2 ) ) );
> print( "circumcircle radius", radius( circ2 ) );
>
> line( ref, y=VerticalCoord(C2),[x,y] );
> reflection( T3, T2, ref );
>
> print( p3-1, div );
> print( low_below );
> print( top );
> print( low_over );
> print( abs( low_below[2]-low_over[2] ) );
>
> print( area( T2 ) );
> print( coordinates( C2 ) );
> print( coordinates( O2 ) );
>
> # printf("\n");
> #
> # div := 2;
> # low_below := lower( 1, trunc(raiz), div );
> # low_over := lower( trunc(raiz), clave, div );
> # low_div := distancia( low_below[1], 1 );
> # over_div:= distancia( low_over[1], 1 );
> # print( div );
> # print( low_below, low_div );
> # print( low_over, over_div );
> # print( abs( low_below[2]-low_over[2] ), abs( low_div-over_div)
);
> #
> # printf("\n");
> #
> # div := 0.5;
> # low_below := lower( 1, trunc(raiz), div );
> # low_over := lower( trunc(raiz), clave, div );
> # low_div := distancia( low_below[1], 1 );
> # over_div:= distancia( low_over[1], 1 );
> # print( div );
> # print( low_below, low_div );
> # print( low_over, over_div );
> # print( abs( low_below[2]-low_over[2] ), abs( low_div-over_div)
);
> #
> printf("\n");
>

```

```

> #   div := p3;
> #   low_below := lower( 1, trunc(raiz), div );
> #   low_over  := lower( trunc(raiz), clave, div );
> #   low_div := distancia( low_below[1], 1 );
> #   over_div:= distancia( low_over[1], 1 );
> #   print( div );
> #   print( low_below, low_div );
> #   print( low_over, over_div );
> #   print( low_below[2]-low_over[2] , low_div-over_div );
>
> draw( [T1(colour=green), T2(colour=red), C1(colour=green),
C2(colour=red), O1(colour=magenta), O2(colour=black)],
axes=normal, scaling=unconstrained );
>
> end proc:
>
> p1:=3;p2:=11;p3:=1;tanto13(p1,p2,p3);
                                p1 := 3
                                p2 := 11
                                p3 := 1
                                3, 11, 33, 5.74456264653802865985061146822
"incircle center", [5.98361899487045425030055085433, 23.9099364641591591674911937075]
"incircle radius", 3.93497097185390768923514236837
"circumcircle center",
[6.000000000000000000000000000220, 142.019471047614327540833507142]
" circumcircle radius", 122.110037819336817730980534807
[2, 19.9749654923052514782560513392]
[5, 264.125414130823295189417437639]
[10, 19.9749654923052514782560513392]
0.
976.601794554072174844645545200

$$\left[ \frac{17}{3}, 101.358448371811266048643180106 \right]$$

[4.999999999999999999999999999999, 20.0364030202051430642625260317]
"incircle center", [15.2410943277894198690524277492, 47.9404326403377207178237944542]
"incircle radius", 14.9149098818062525647123412940
"circumcircle center",
[15.999999999999999999999999999984, 148.283386957320641855976182769]
"circumcircle radius", 116.363118124543771328988895931
0, 32
[0, 33.0255227585314681531114531599]

```



"circumcircle radius", 2973.14340158260026844890305371

[22, 161.184372725336399464929337969]

[36, 6107.40626080718289310952758531]

[60, 161.184372725336399464929337966]

 $0.3 \cdot 10^{-26}$ 

112978.215873555083379247366700

$$\left[ \frac{118}{3}, 2143.25833541928523067979542042 \right]$$
[illegible]

"incircle center", [603.924020538242779703998506570, 2001.87731754191300923534952034]

"incircle radius", 599.320666730931072726697129621

"circumcircle center",

[700.9999999999999999999999630, 3749.75535890095619434761130460]

"circumcircle radius", 2449.64135645592907831891423049

0, 1402

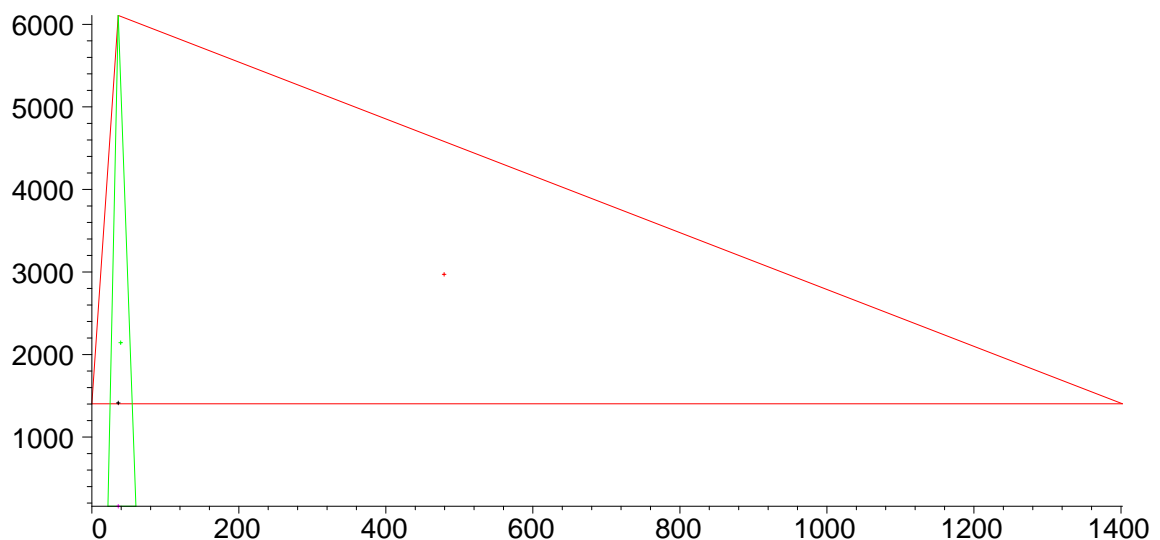
[0, 1402.55665081098193650865239061]

[36, 6107.40626080718289310952758531]

[1402, 1402.55665081098193650865239084]

 $0.23 \cdot 10^{-24}$ 
$$0.329809957660733687057721351148 \cdot 10^7$$
$$\left[ \frac{1438}{3}, 2970.83985414304892204227745559 \right]$$

[36.0000000000000000000000007480, 1413.00884462723437743160975757]

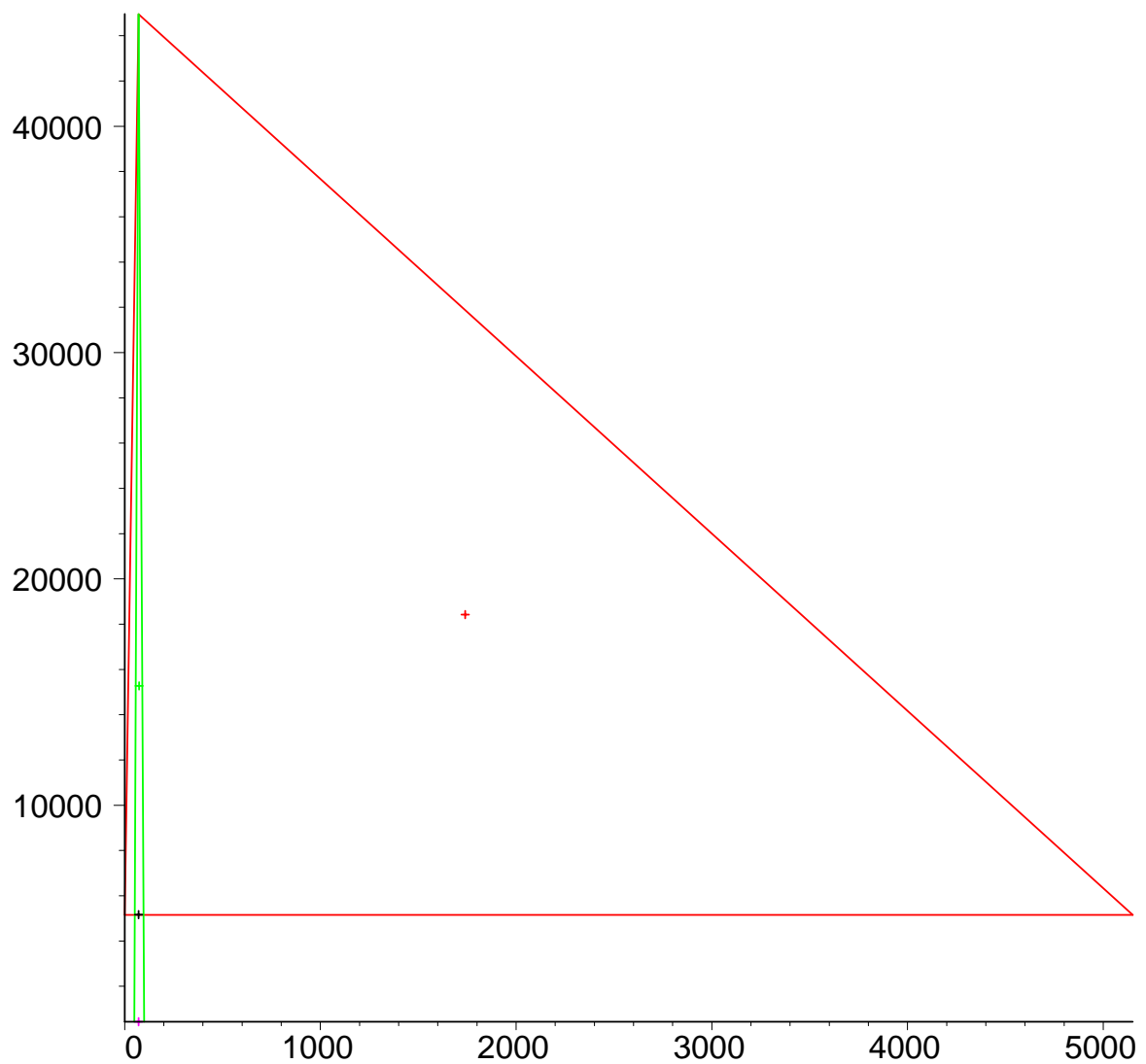




```

> p1:=51;p2:=101;p3:=1;tanto13(p1,p2,p3);detail(T3);
      p1 := 51
      p2 := 101
      p3 := 1
      51, 101, 5151, 71.7704674639924579612321524611
"incircle center", [74.9977541789383059784562420893, 452.144594744227191144826248296]
      "incircle radius", 24.9859674557355488704062699825
"circumcircle center",
      [75.0000000000000000000000042135, 22690.7206768977927404444797786]
      "circumcircle radius", 22263.5760859930924083764719403
      [50, 427.158627288491642274419978317]
      [71, 44954.2964035595704642668662660]
      [100, 427.158627288491642274419978307]
      0.10 10-25
      0.111317844440677697054981115719 107
       $\left[\frac{221}{3}, 15269.5378860455179162719020742\right]$ 
      [70.9999999999999999999999911961, 427.172304340968267926746666220]
"incircle center", [2413.66450295269434621514706612, 7559.89170217773321215553576692]
      "incircle radius", 2409.36296696706951363288412949
"circumcircle center",
      [2574.9999999999999999999999730, 25047.8827343830056046466011232]
      "circumcircle radius", 20063.2829110387512332091217914
      0, 5150
      [0, 5150.52873521066369852265163714]
      [71, 44954.2964035595704642668662660]
      [5150, 5150.52873521066369852265163781]
      0.67 10-24
      0.102494701745998434921791352670 109
       $\left[\frac{5221}{3}, 18418.4512913269659537707231803\right]$ 
      [71.0000000000000000000000054048, 5159.58840521488665201896729447]

```



*name of the object: T3*

*form of the object: triangle2d*

*method to define the triangle: points*

*the three vertices: [[0., 31686.3738474432682090187947235], [71., -8117.3938209056385567254199054], [5150., 31686.3738474432682090187947228]]*

> p1:=101;p2:=103;p3:=1;tantol3(p1,p2,p3);

p1 := 101

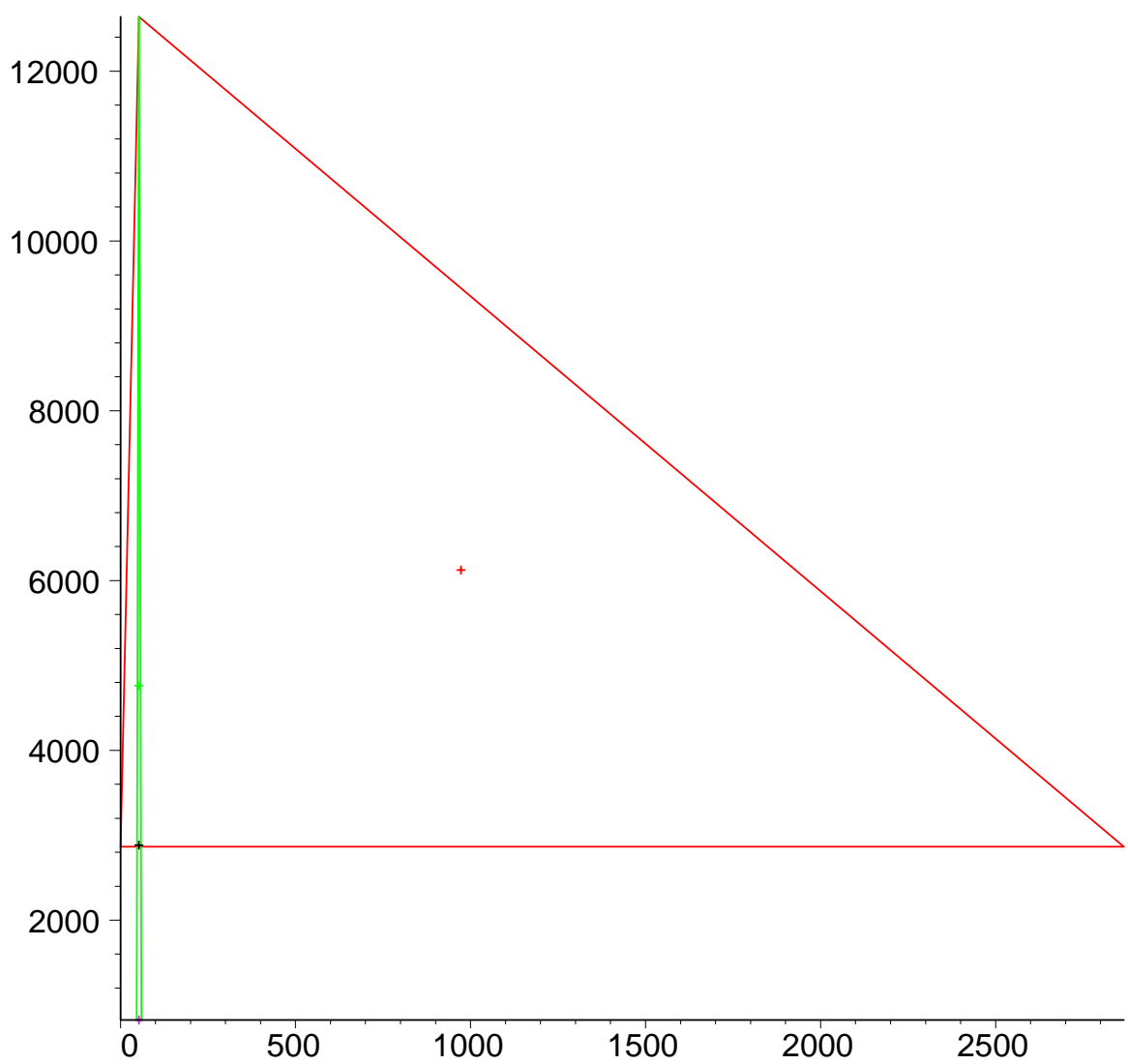
p2 := 103

p3 := 1





[illegible]



```
> p1:=1237;p2:=9743;p3:=1;tanto13(p1,p2,p3);
```

$p1 := 1237$

$$p2 := 9743$$
$$p3 := 1$$

1237, 9743, 12052091, 3471.61216151804607080526185951

"incircle center", [5488.86188870934450863580915203, 15471.5832913835093440097006345]

"incircle radius", 4252.70893372383953355886735047

"circumcircle center",

[5488.999999999999999999996200, 0.310823713612061962008237226186 10<sup>8</sup>]

"circumcircle radius",  $0.310711527779225306954078484467 \cdot 10^8$

[1236, 11218.8743576596698104508332840]

[3471, 0.621535240735964945809238949526 10<sup>8</sup>]

[9742, 11218.8743576596698104508332840]

0.

$$0.264291224012362764876965477840 \cdot 10^{12}$$
$$\left[ \frac{14449}{3}, 0.207253206074372713068482655397 \cdot 10^8 \right]$$

[3471.0000000000000000000000002, 11219.0998994215188973513817607]

"incircle center",

$[0.531184934008602761101854489402 \cdot 10^7, 0.173635718513840005489347934805 \cdot 10^8]$

"incircle radius",  $0.531148135080753615449321346024 \cdot 10^7$

"circumcircle center",

$[0.60260449999999999999999997055 \cdot 10^7, 0.371023899262090901352177152452 \cdot 10^8]$

"circumcircle radius", 0.257649125683724232405489674001  $10^8$

0, 12052090

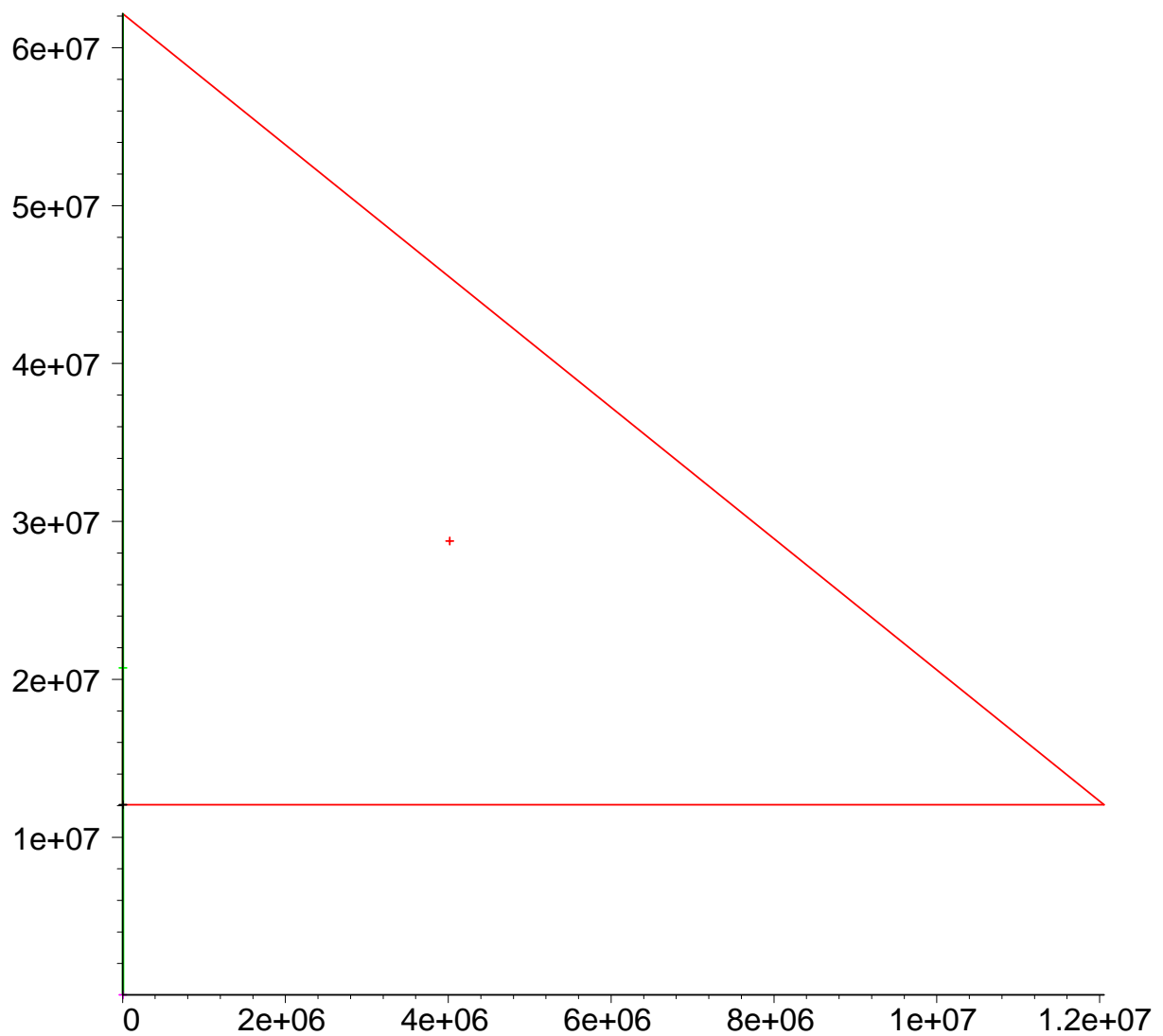
$[0, 0.120520905005764643944415800140 \cdot 10^8]$

[3471, 0.621535240735964945809238949526 10<sup>8</sup>]

[12052090, 0.120520905005764643944415800282  $10^8$ ]

 $0.142 \cdot 10^{-19}$ 
$$0.301913493275529487805100821524 \cdot 10^{15}$$
$$\left[ \frac{12055561}{3}, 0.287525683582498077899356849983 \cdot 10^8 \right]$$

[3471.000000000000000000005895228, 0.120529252223312430993716245044  $10^8$ ]



```
> Digits:=100;p1:=nextprime(34535453557357476867834464267);p2:=nextp
rime(6574853557357476867834464267);p3:=345354535573574768678344642
73;tantol3(p1,p2,p3);
```

*Digits := 100*

*p1 := 34535453557357476867834464273*

*p2 := 6574853557357476867834464297*

*p3 := 34535453557357476867834464273*

*34535453557357476867834464273, 6574853557357476867834464297,*  
*227065549676545736071953404916578362536146720832940561081, 0.15068694358720\*  
*8555496349318213817235512271380385829878862240300216313561122375253986222\*



$$2099727851708 \cdot 10^{29}$$

"incircle center", [0.205551535573574768678344642839355272260220352311432183175\  
2726087735313858516842980970320082304654452 10<sup>29</sup>, 0.614791723239362961808263\  
2223988855451372190520565198305058806746189249869457679835634773665943870\  
299 10<sup>29</sup>]

[illegible]

```
"circumcircle center", [0.2055515355735747686783446428400000000000000000000\
    00000000000000000008435171372114471102862840544 1029, 0.59484291432003964368\
    5257666795355305848179172189562784770325142686490442664642518801727814580\
    3861820 1057]
```

"circumcircle radius",  $0.59484291432003964368525766674785643352424287600873646215184365881727685374589905357511405637378919688 \cdot 10^{57}$

[34535453557357476867834464272, 0.474988723239362961808263222520528405658752\0016850733921587650633613201534015475998495349736237258661 10<sup>29</sup>]

[15068694358720855549634931820, 0.118968582864007928737051533354321173937242\2048198299247288736429024258799541115364213437607514813868 10<sup>58</sup>]

[6574853557357476867834464296, 0.4749887232393629618082632225205284056587520\ 016850733921587650633613201534015475998495349736237258661  $10^{29}$ ]

0.

$$0.166321647901369004612260155025938846515169939104836927319417931671429112\backslash$$

[18726333824478603095101286796, 0.396561942880026429123505111212736494673431\5468533172972642807033853363999593766808817302067290259660  $10^{57}$ ]

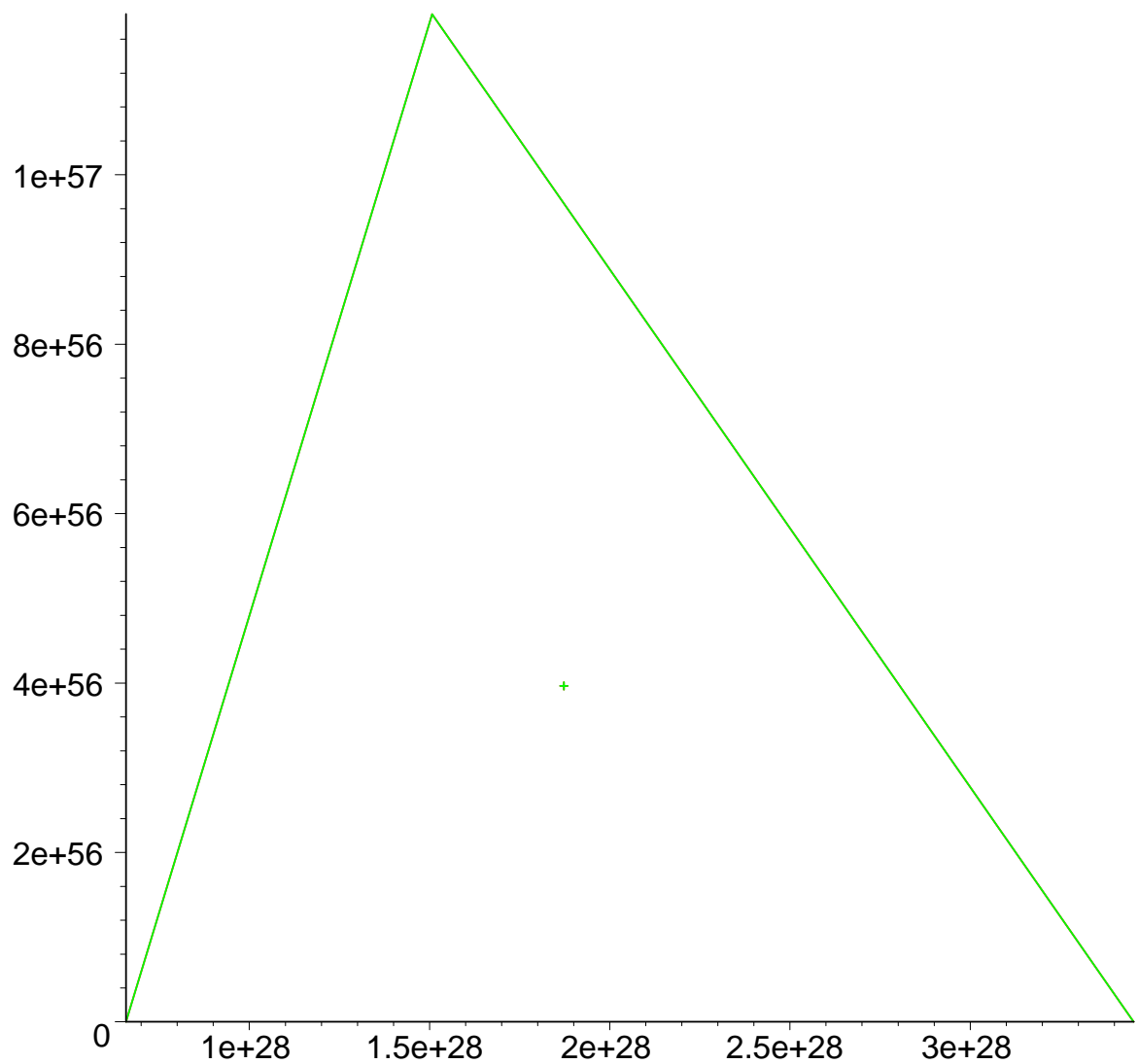
[illegible]

"incircle center", [0.205551535573574768678344642839355272260220352311432183175\ 2726087735313858516842980970320082304654452 10<sup>29</sup>, 0.614791723239362961808263\ 2223988855451372190520565198305058806746189249869457679835634773665943870\ 299 10<sup>29</sup>]

[illegible]

```
"circumcircle center", [0.2055515355735747686783446428400000000000000000000\
    000000000000000000000008435171372114471102862840544 1029, 0.59484291432003964368\
```

[illegible]



```
> p1:=16347336458092538484431338838650908598417836700330923121811108
52389333100104508151212118167511579;p2:=19008712816648221131268515
739354139754718967899685154936666385390880271038021044989571912614
65571;p3:=1;tanto13(p1,p2,p3);
```

```
p1 := 163473364580925384844313388386509085984178367003309231218111085238933\
3100104508151212118167511579
```

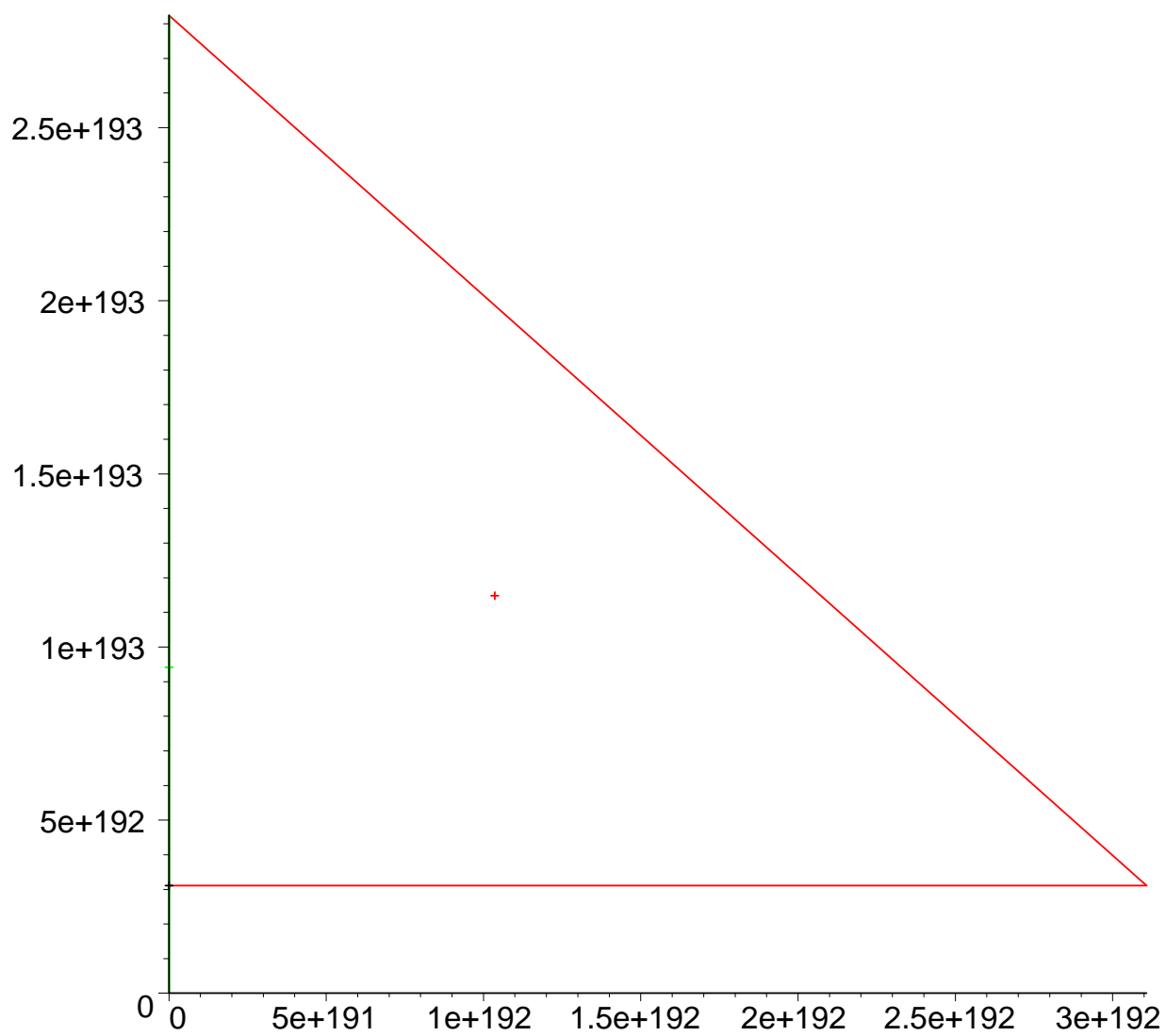
```
p2 := 190087128166482211312685157393541397547189678996851549366663853908802\
7103802104498957191261465571
```

```
p3 := 1
```

```
1634733645809253848443133883865090859841783670033092312181110852389333100\
```

104508151212118167511579, 1900871281664822113126851573935413975471896789968\  
 515493666638539088027103802104498957191261465571, 3107418240490043721350750\  
 0358885679300373460228427275457201619488232064405180815045563468296717232\  
 8678243791627283803341547107310850191954852900733772482278352574238645401\  
 4691736602477652346609, 0.1762787066122860943811705736776226385093299156422\  
 107330123170327876780025762012912130622946534606220  $10^{97}$   
 "incircle center", [0.176780246373703798078499272890025241765684023000080390292\  
 3874695738680101953306325084654714488574  $10^{97}$ , 0.469041938276641617075092101\  
 6632673388172665967371895527381514678023286141688648962493629248163994117  $10^{98}$ ]  
 "incircle radius", 0.1330688179277841323418588450351615578150565599677115907427\  
 638433493470018487981738725365469769959995  $10^{96}$   
 "circumcircle center", [0.19024324778511706943070287395081947116785253684715445\  
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