

MATHEMATICAL FOUNDATION FOR COMPUTER SCIENCE

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FINITE STATE AUTOMATA

- *Sequential Circuits and Finite state Machine*
- *Finite State Automata*
- *Non-deterministic Finite State Automata*
- *Language and Grammars*
- *Language and Automata*
- *Regular Expression*

GENERATING GRAMMAR FOR THE LANGUAGE:

I. First write the Regular Expression for the language.

Some Basic Rules:

$$a^*$$
$$A \rightarrow aA / \epsilon$$
$$(a+b)^*$$
$$A \rightarrow aA / bA / \epsilon$$
$$(a+b)^+$$
$$A \rightarrow aA / bA / a / b$$

Q. Write the Grammar that generates string having Following Properties:

a) String of exactly length two

$$\text{R.E.} = (a+b)(a+b)$$

$$S \rightarrow AA$$

$$A \rightarrow a/b$$

b) String of at most length 2

$$\text{R.E.} = (a+b+\epsilon)(a+b+\epsilon)$$

$$S \rightarrow AA$$

$$A \rightarrow a/b/\epsilon$$

c) Starts with a

$$\text{R.E.} = a(a+b)^*$$

$$S \rightarrow aA$$

$$A \rightarrow aA/bA/\epsilon$$

c) Ends with ba

$$\text{R.E.} = (a+b)^*ba$$

$$S \rightarrow Aba$$

$$A \rightarrow aA/bA/\epsilon$$

d) Stats with a and ends with b

$$\text{R.E.} = a(a+b)^*b$$

$$S \rightarrow aAb$$

$$A \rightarrow aA/bA/\epsilon$$

e) Starts and ends with same symbol

$$\text{R.E.} = a(a+b)^*a + b(a+b)^*b$$

$$S \rightarrow aAa/bAb/a/b$$

$$A \rightarrow aA/bA/\epsilon$$

f) Starts and ends with different symbol

$$\text{R.E.} = a(a+b)^*b + b(a+b)^*a$$

$$S \rightarrow aAb/bAa$$

$$A \rightarrow aA/bA/\epsilon$$

c) Ends with ba

$$\text{R.E.} = (a+b)^*ba$$

$$S \rightarrow Aba$$

$$A \rightarrow aA/bA/\epsilon$$

Q. Write the Context Free Grammar that generates Palindrome string over $\Sigma(a, b)$

$S \rightarrow \epsilon / a / b$

$S \rightarrow aSa / bSb$

Properties of regular language;

1. If L and M are regular languages, then $L \cup M$ (**UNION**) is a regular language.
Let L and M be the languages of regular expressions R and S , respectively. Then $R+S$ is a regular expression whose language is $L \cup M$.
2. If L is regular languages, then L^* (**Kleen Closure**) is a regular language.
Let L the languages of regular expressions R . Then R^* is a regular expression whose language is L^*
3. If L and M are regular languages, then $L.M$ (**Concatenation**) is a regular language.
Let L and M be the languages of regular expressions R and S , respectively. Then $R.S$ is a regular expression whose language is $L.M$.
4. If L is a regular language over Σ , then \bar{L} (**Complement**) is also a regular language.
Construct a DFA for L . This can be transformed into a DFA for \bar{L} by making all accepting states non-accepting and vice versa.
5. If L and M are regular languages, then $L \cap M$ (**Intersection**) is a regular language.
 $RE_1 = a(a^*)$ and $RE_2 = (aa)^*$
So, $L_1 = \{ a, aa, aaa, aaaa, \dots \}$ (Strings of all possible lengths excluding Null)
 $L_2 = \{ \epsilon, aa, aaaa, aaaaaa, \dots \}$ (Strings of even length including Null)
 $L_1 \cap L_2 = \{ aa, aaaa, aaaaaa, \dots \}$ (Strings of even length excluding Null)
 $RE (L_1 \cap L_2) = aa(aa)^*$ which is a regular expression itself.

Properties of regular language;

6. If L and M are regular, then so is $L - M$ (**Difference**).

Proof: $M - N = M \cap \bar{N}$

7. If L is regular, then so is L^R (**Reversal**).

Let, $L = \{01, 10, 11, 10\}$

$RE(L) = 01 + 10 + 11 + 10$

$L^R = \{10, 01, 11, 01\}$

$RE(L^R) = 01 + 10 + 11 + 10$ which is regular