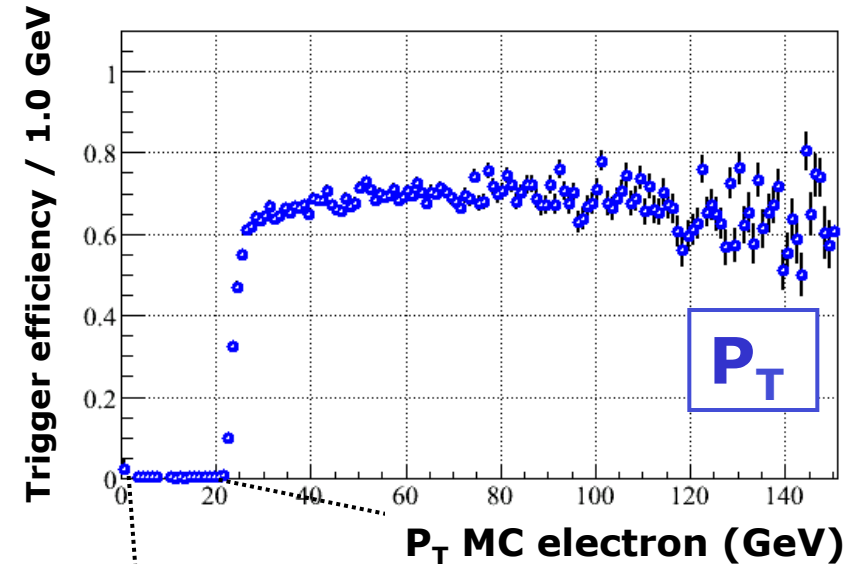
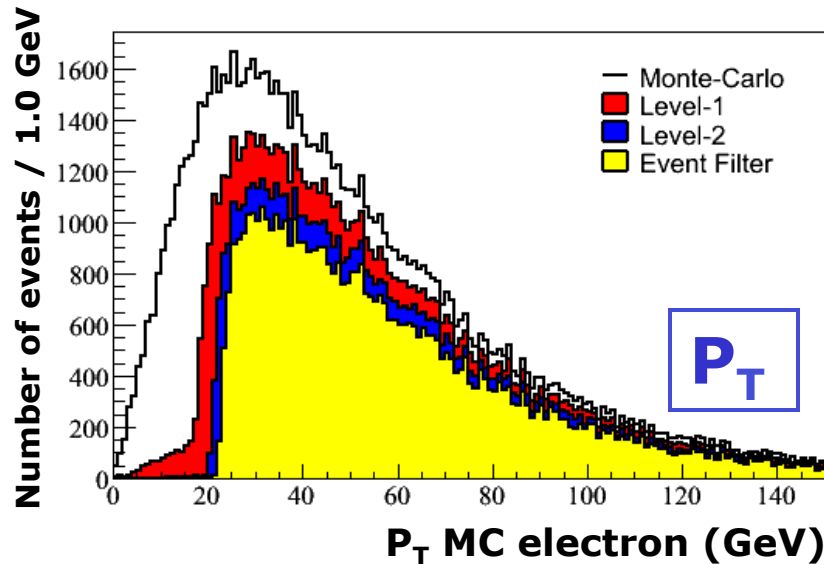


# **Binomial Error intervals & Extra leptons in $t\bar{t}$ events**

*Ivo van Vulpen  
(Nikhef)*

# Binomial Error intervals

# Trigger efficiencies: Example: EM25i in tt(electron) events



Issues when making the plot:

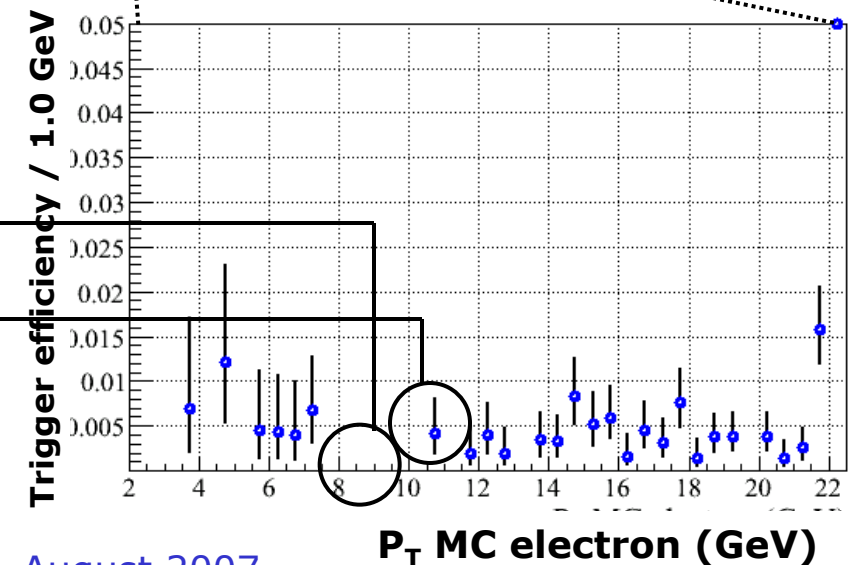
**A** How to treat weighted events ?

-  $N_{\text{tot}} < 0$ ,  $N_{\text{sel}} < 0$  or  $N_{\text{sel}} > N_{\text{tot}}$

**B** Correct Binomial errors

i.e. not simply  $\sqrt{\epsilon(1-\epsilon)/N}$

→ Discuss in (T5) Trigger meeting



# Binomial distribution

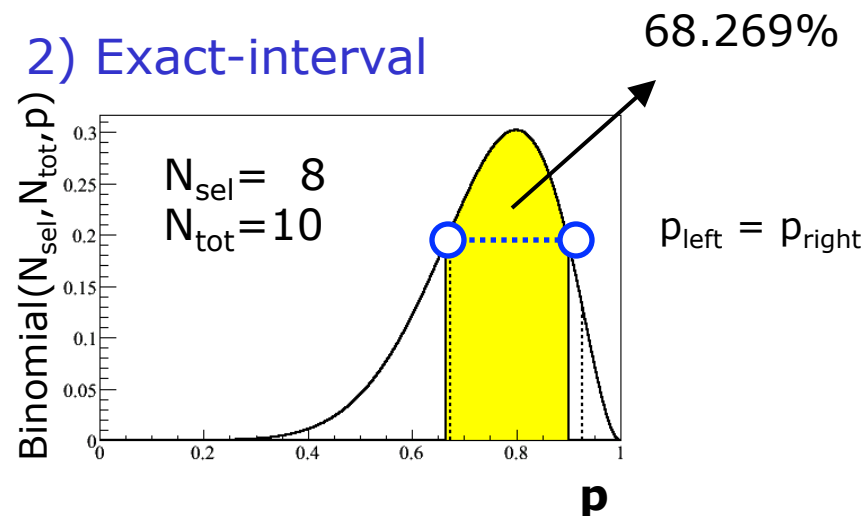
$$f(N_{\text{sel}} | N_{\text{tot}}, p) = \frac{N_{\text{tot}}!}{N_{\text{sel}}!(N_{\text{tot}} - N_{\text{sel}})!} p^{N_{\text{sel}}} (1-p)^{N_{\text{tot}} - N_{\text{sel}}}$$

- Select  $N_{\text{sel}}$  events out of a sample of  $N_{\text{tot}}$  events  
Throw a dice 10x  $\rightarrow$  probability to find 4x1 =  $\binom{10}{4}(0.16)^4(0.84)^6 = 4.8\%$
- Given  $N_{\text{tot}}$  and  $N_{\text{sel}} \rightarrow$  information on  $p$  (efficiency) and it's uncertainty

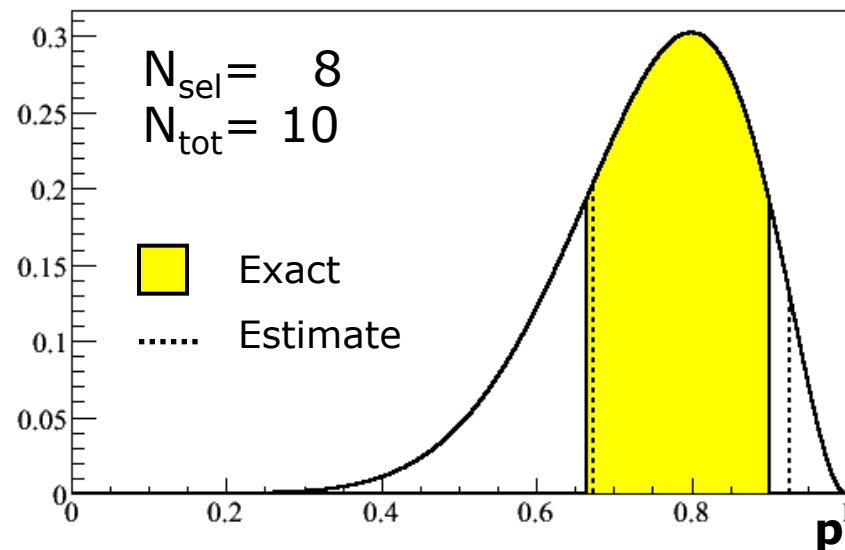
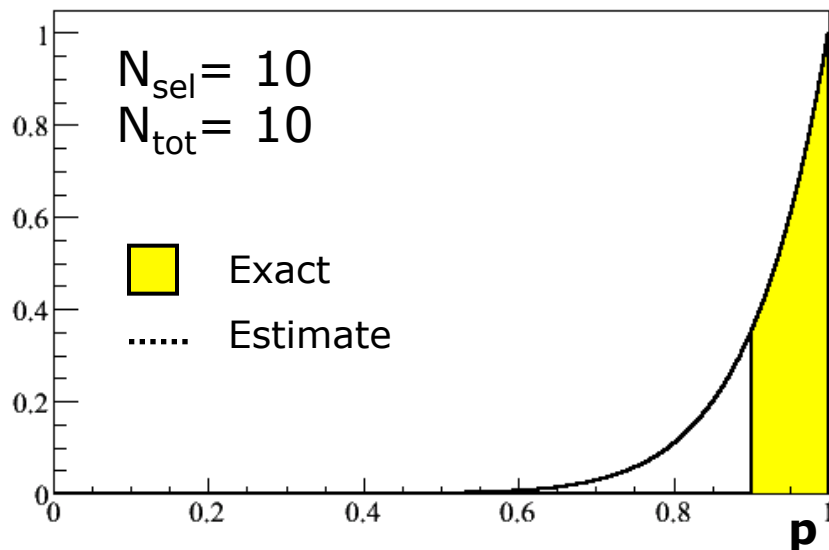
## 1) Estimated-interval

$$\Delta p = \sqrt{\frac{p(1-p)}{N_{\text{tot}}}}$$

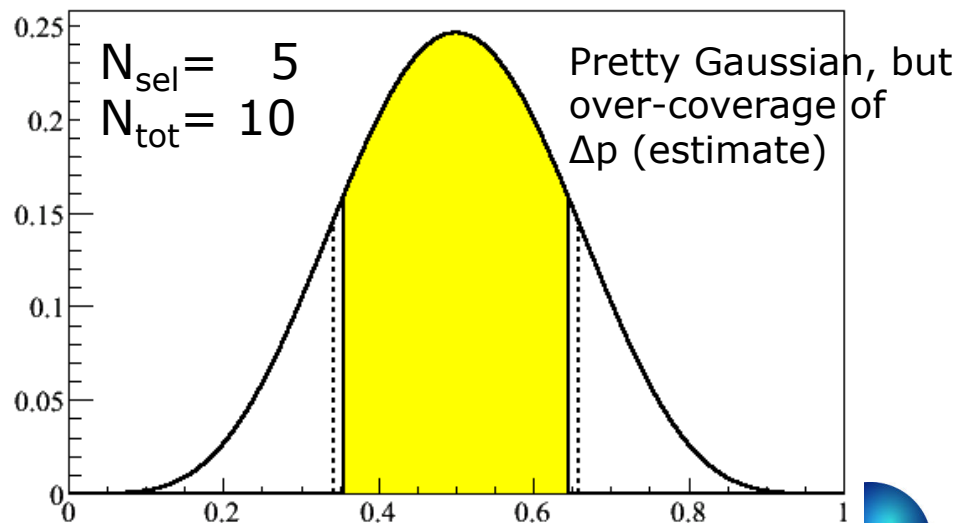
## 2) Exact-interval



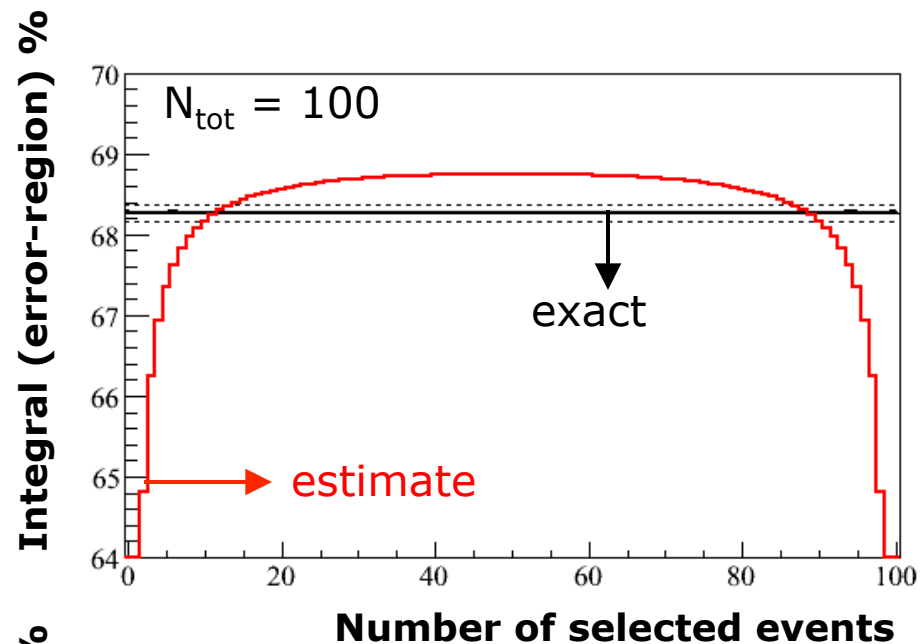
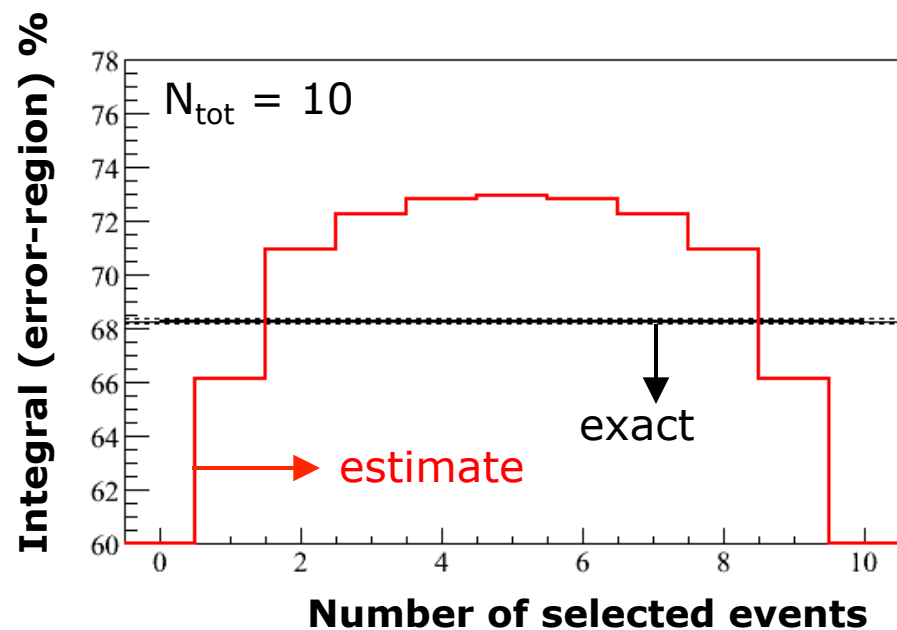
# Difference in uncertainty region [estimate/exact]



$N_{\text{sel}}, N_{\text{tot}}$	$\Delta p(\text{estimate})$	$\Delta p(\text{exact})$
10,10	$\pm 0.000$	+0.000 -0.100
8,10	$\pm 0.126$	+0.101 -0.136
5,10	$\pm 0.158$	+0.145 -0.144

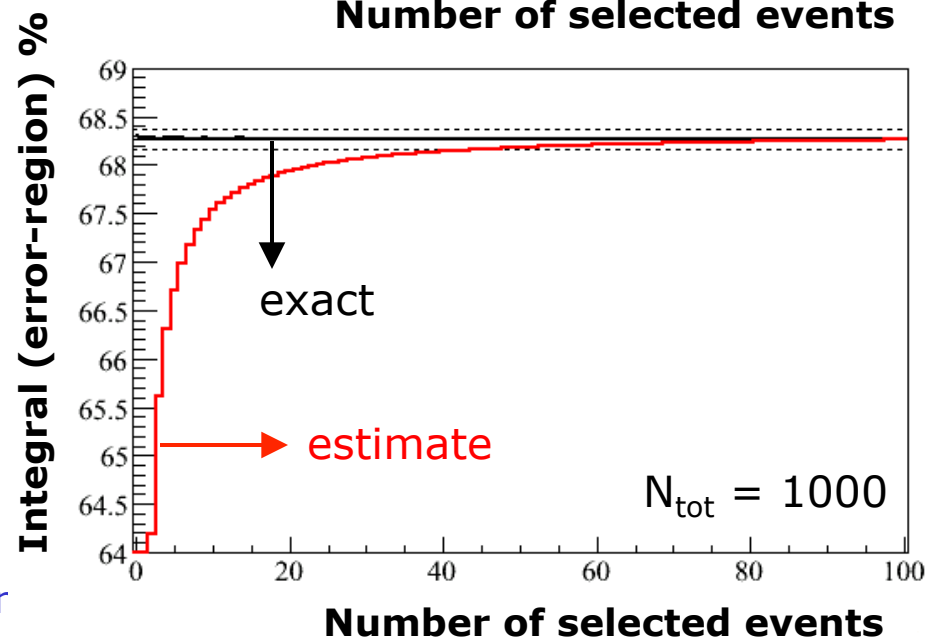


# Difference in coverage [estimate/exact]



Coverage: integral  $\Delta p$  region

- Under/over-coverage when using estimated-interval

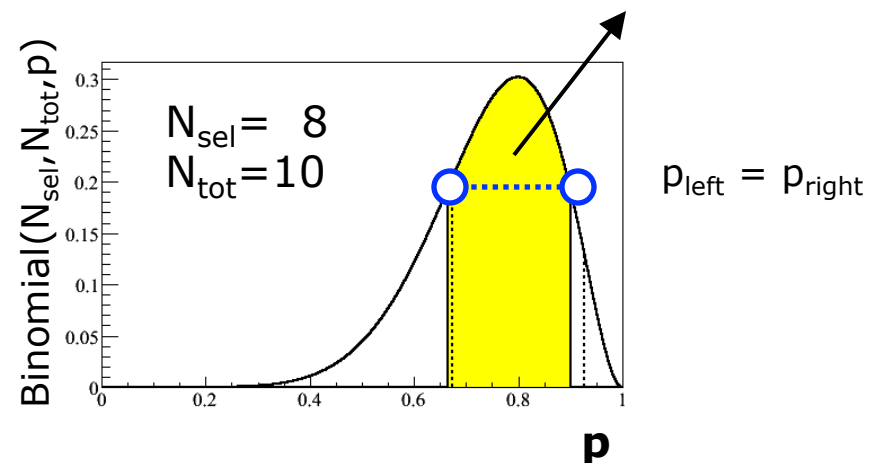


# Computing exact interval

Step left/right from  $p_{\max}$  until:

**a)** integral is gaussian one sigma equiv.

**b)**  $p_{\text{left}} = p_{\text{right}}$



At each step need:

Probability: 
$$f(N_{\text{sel}} | N_{\text{tot}}, p) = \frac{N_{\text{tot}}!}{N_{\text{sel}}!(N_{\text{tot}} - N_{\text{sel}})!} p^{N_{\text{sel}}} (1-p)^{N_{\text{tot}} - N_{\text{sel}}}$$

↳ In root `TMath::Binomial`

Integral: 
$$\int_0^x x^k (1-x)^{N-k} dx = B(p, k+1, N-k+1)$$

↳ Incomplete Beta function  
In root `TMath::BetaIncomplete`

# Numerical problems when computing exact interval:

$$f(N_{\text{sel}} | N_{\text{tot}}, p) = \frac{N_{\text{tot}}!}{N_{\text{sel}}!(N_{\text{tot}} - N_{\text{sel}})!} p^{N_{\text{sel}}} (1-p)^{N_{\text{tot}} - N_{\text{sel}}}$$

$N_{\text{sel}}=200, N_{\text{tot}}=1000$  at  $p=0.5$ :  $6.6 \cdot 10^{+215} \times 6.2 \cdot 10^{-61} \times 1.5 \cdot 10^{-241}$

Solution: just remove Binomial coefficient and use logarithms.

$$\int_0^x x^k (1-x)^{N-k} dx = B(p, k+1, N-k+1)$$

`= TMath::BetaIncomplete(p,k+1,N-k+1)`

`= something / TMath::Beta(k+1,N-k+1)`

`= something / TMath::Exp(TMath::LnGamma(p)+TMath::LnGamma(q)-TMath::LnGamma(p+q))`

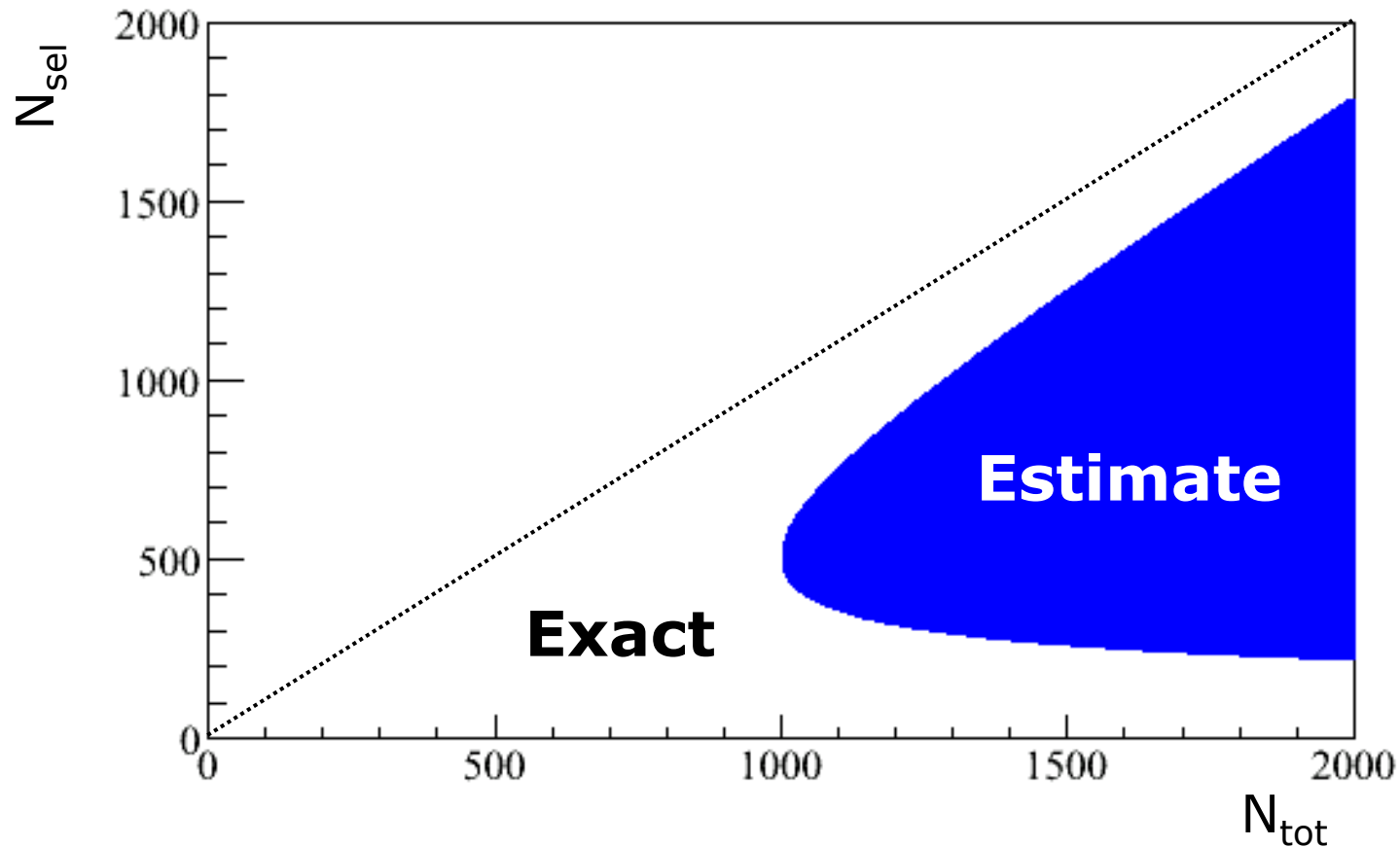
Problem if argument < -700 since  $10^{-300} = 0 \rightarrow \text{Integral} = \text{inf or NaN}$

$$\begin{aligned} \text{Beta}(x, y) &= \frac{\Gamma(x)\Gamma(y)}{\Gamma(x+y)} \\ &= e^{\ln(\Gamma(x)) + \ln(\Gamma(y)) - \ln(\Gamma(x+y))} \end{aligned}$$

Solution: switch to estimate if this happens



## Where do you use estimate:



In principle could do exact in larger region by using Stirling's approximation for  $\text{Beta}(x,y)$  and work with logarithms.

# Existing code in Root

→ Exact Binomial interval can already be computed in Root:

**TGraphAsymmErrors::BayesDivide(const TH1\* pass, const TH1\* total)**

(code by Andy Haas and Marc Paterno)

**TMath::BinomialI(n.p.k)** → should be updated  
(coded by Anna Kreshuk)

Contains already the  
computation of the  
correct interval

→ Short routine presented in previous slides:

<http://www.nikhef.nl/~ivov/BinomialErrorInterval/> **BinomialErrorInterval.C**

Please check/verify:

**BinomialErrorInterval( Int\_t N<sub>sel</sub>, Int\_t N<sub>tot</sub>, Double\_t \*ErrorRegion)**

To get printout: Example(N<sub>tot</sub>, N<sub>sel</sub>)

# Weighted events

- MC@NLO weighted events +1 and -1 ( $\sim 13.4\%$  has  $w=-1$ )
- What to do with bins where:  $N_{\text{tot}} < 0$ ,  $N_{\text{sel}} < 0$  or  $N_{\text{sel}} > N_{\text{tot}}$  ?

Several private discussions, but no consensus, no clear strategy.

- 1) Use weight = 1 in all plots
  - + 'An electron is an electron'
  - Trigger could depend on weight (event topology, phase space, ...)
- 2) Combine the two trigger curves for weight=+1 and weight=-1  
Not sure how-to, analysis dependent ?



**What do you do  
with weighted  
events ?**

Should have discussion in ATLAS (T5-group) and arrive at common approach to create turn-on curves.

# Extra leptons in $t\bar{t}$ events

• **Number of selected events for 100 pb<sup>-1</sup>  
(no trigger)**

	Before selection	After selection	Selection efficiency
<b>TTbar(5200)</b>	<b>46277.8</b>	<b>6172.0</b>	<b>13.3%</b>
electron	12329.2	2168.6	17.6%
muon	12350.2	2871.4	23.2%
tau	12415.0	427.1	3.4%
fully-leptonic	9181.7	704.8	7.7%
<b>W+jets</b>	<b>79266.7</b>	<b>1601.0</b>	<b>2.0%</b>

Mass window 141<M <sub>t</sub> <189 +M <sub>W</sub> -cut
<b>1420.9</b>
527.3
719.9
105.2
68.7
<b>129.8</b>

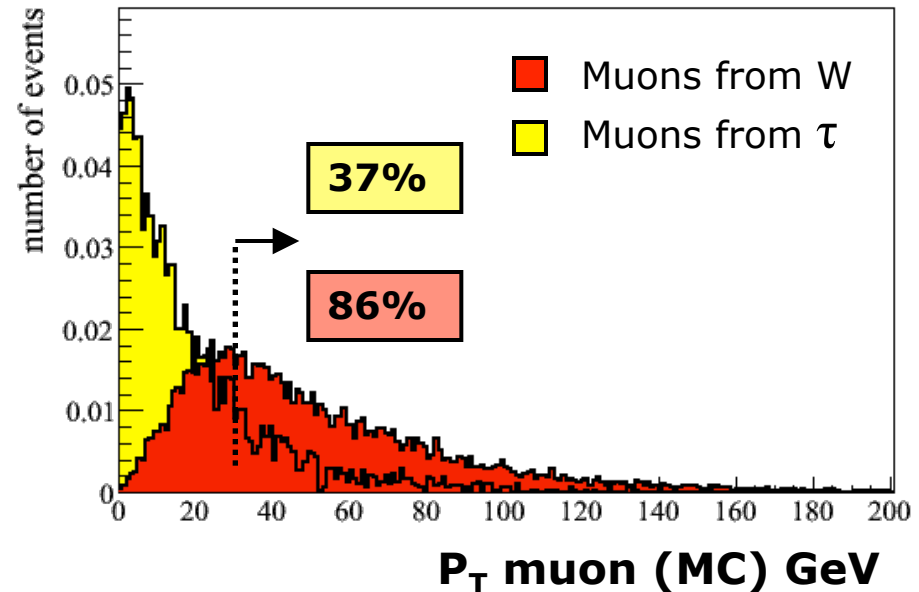
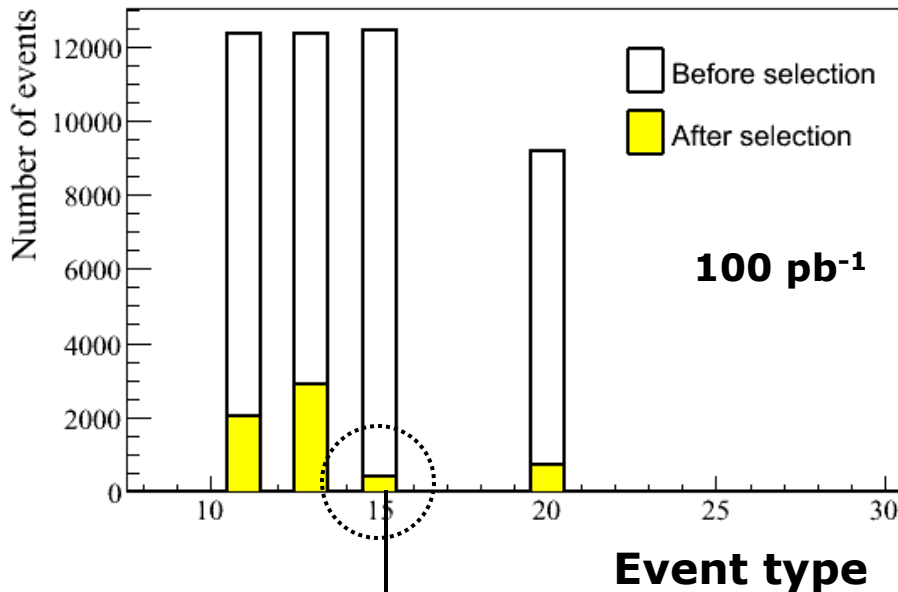
→ Similar numbers to Udine-group/Akira

Issues: Electron definition (isolation/medium/cracks)

# Leptons from top events: example: muons from tau's

11/13/15 = semi-leptonic  $t\bar{t}$  (elec/muon/tau)  
 20 = fully-leptonic  $t\bar{t}$

Alexander Doxiadis



Efficiency for tau's (in a muon analysis):  
 $\sim \epsilon(\text{muon}) * 0.17 * (0.37/0.86) * ..$

# QCD background in commissioning analysis

## → QCD events passing event selection:

- Jet requirements No problem
- $E_T$ -miss > 20 GeV  $\sim 9\%$  (rel. 11, FastSim estim.)
- Single isolated lepton ? (electron or muon)

## → Origin extra leptons:

Semi-leptonic B(D)-decays

Photon conversions

*Non-prompt*

$\pi$  faking electron

*Fake*

## → Determine rate:

QCD **FastSim** (Release 11)

TTbar **FullSim** (next slide)

QCD fullsim ??

$10^{-5}$  (egama)  $\rightarrow 10^{-4}$  SUSY/TOP ?

## QCD FastSim estimate:

- + Correct jet topologies
- How well do you model the relevant parameters ?

## TTbar FullSim:

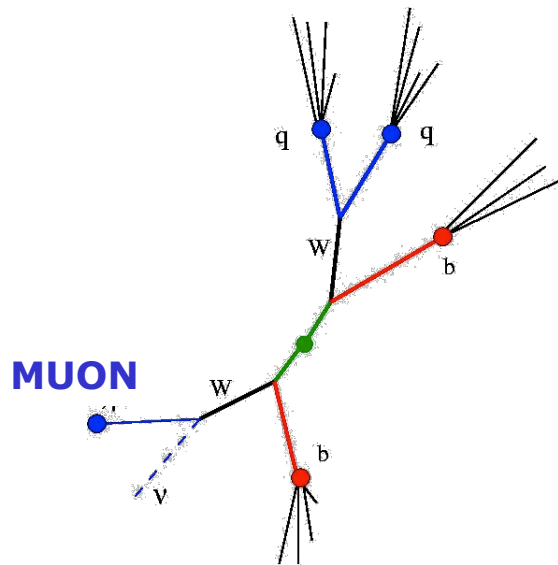
- + Best modeling of detector, photon conversions etc.
- Different jets:
  - \* B/Q-jets in ttbar, Q and gluon-jets in QCD
  - \* higher-Pt jets in ttbar
  - \* Different topologies

→ Can we translate it to QCD events ?

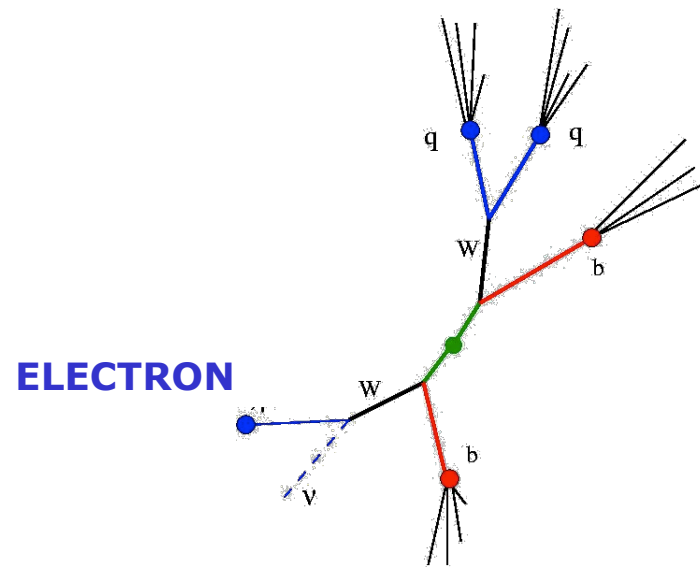
## QCD Fullsim:

Not available, only SUSY sample with hard filter cuts  
Issue: should we produce it ?





Do we see electrons ?



Do we see muons ?

- Then what ...
- # 'wrong' leptons per jet
  - Find origin of these extra leptons
  - Get # QCD jets and compute QCD efficiency

TTbar sample (5200): no weights  $\rightarrow$  ~520k events with ~2.1M jets ( $P_T > 20$  GeV)

● Monte-Carlo statistics (no weights, *before* event selection)

# tt(muon) events = 139,105  
 # jets ( $P_T > 20$  GeV) = 565,646  
 # *tight* electrons = 343



'Extra' electrons/jet =  $60.6 \cdot 10^{-5}$

# tt(electron) events = 138,652  
 # jets ( $P_T > 20$  GeV) = 606,897  
 # good muons = 207



'Extra' muons/jet =  $34.1 \cdot 10^{-5}$

● Expected # events (*after* event selection,  $100 \text{ pb}^{-1}$ , no trigger) for the electron and muon analysis separately

Analysis		tt(electron)	tt(muon)	tt(tau)	tt(leptonic)	TOTAL
	1 electron	2163.1	2.5	177.4	299.7	2642.7
	1 muon	5.4	2868.9	249.7	405.1	3529.2

● Monte-Carlo statistics (no weights, *before* event selection)

# tt(muon) events = 139,105  
# jets ( $P_T > 20$  GeV) = 565,646

# **tight** electrons = 343  
# **medium** electrons = 814



'Extra' electrons/jet =  $60.6 \cdot 10^{-5}$   
 $144 \cdot 10^{-5}$

# tt(electron) events = 138,652  
# jets ( $P_T > 20$  GeV) = 606,897

# good muons = 207



'Extra' muons/jet =  $34.1 \cdot 10^{-5}$

- Expected # events (**after** event selection, **100 pb<sup>-1</sup>**, no trigger) for the electron and muon analysis separately

Analysis

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- Expected # events (**after** event selection, **100 pb<sup>-1</sup>**, no trigger) for the electron and muon analysis separately

Analysis

	tt(electron)	tt(muon)	tt(tau)	tt(leptonic)	TOTAL
1 electron	2646.7	12.6	240.3	338.6	3238.2
1 muon	4.4	2860.2	249.1	361.6	3475.3

More electrons ... but you loose some muons, probably because of Nleptons ==1 cut

## Coming 2 weeks:

Manuel

1) Search for origin extra electrons: B(D) decays, photon conv., **fakes**

Search for origin extra muons: B-decays ?

Alexander

→ Study dependence on Pt (objects) and jet-type  
Disentangle parameters

→ Check FullSim Ttbar estimate (Pt, eta) versus Egamma estimate

→ Redo our study with medium electrons

→ Run over di-jet sample from Egamma group

3) Study difference TTbar Fast/Full Simulation

Some things CAN be modelled correctly others CAN NOT

4) Decide if we need separate FullSim QCD sample  $\sim 300k$  ?

Martijn

