# Reinforcement learning Episode 4

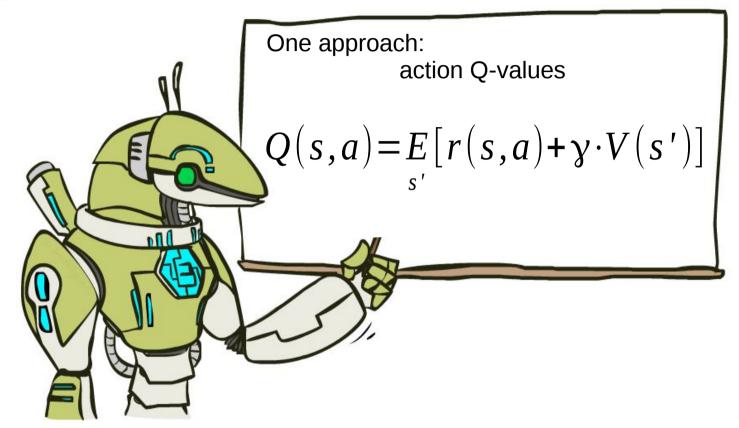
# Approximate reinforcement learning







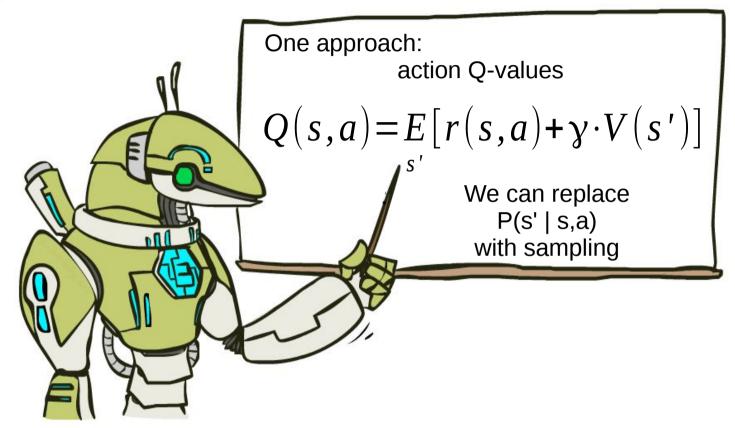
# Recap: Q-learning



**Action value Q(s,a)** is the expected total reward **G** agent gets from state **s** by taking action **a** and following policy  $\pi$  from next state.

$$\pi(s)$$
:  $argmax_a Q(s,a)$ 

# Recap: Q-learning



$$Q(s_t, a_t) \leftarrow \alpha \cdot (r_t + \gamma \cdot max_{a'} Q(s_{t+1}, a')) + (1 - \alpha) Q(s_t, a_t)$$

 $\pi(s)$ :  $argmax_a Q(s,a)$ 

Given <**s**,**a**,**r**,**s**'> minimize

$$L = [Q(s_t, a_t) - Q^{true}(s_t, a_t)]^2$$

$$L \approx [Q(s_t, a_t) - (r_t + \gamma \cdot max_{a'}Q(s_{t+1}, a'))]^2$$

## How to optimize?

Given <**s**,**a**,**r**,**s**'> minimize

$$L = [Q(s_t, a_t) - Q^{true}(s_t, a_t)]^2$$

$$L \approx [Q(s_t, a_t) - (r_t + \gamma \cdot max_{a'}Q(s_{t+1}, a'))]^2$$

For tabular Q(s,a)

$$\nabla L = 2 \cdot [Q(s_t, a_t) - (r_t + \gamma \cdot max_{a'}Q(s_{t+1}, a'))]$$

Given <**s**,**a**,**r**,**s**'> minimize

$$L = [Q(s_t, a_t) - Q^{true}(s_t, a_t)]^2$$

$$L \approx [Q(s_t, a_t) - (r_t + \gamma \cdot max_{a'}Q(s_{t+1}, a'))]^2$$

For tabular Q(s,a)

$$\nabla L \approx 2 \cdot [Q(s_t, a_t) - (r_t + \gamma \cdot max_a, Q(s_{t+1}, a'))]$$

Something's sooo wrong!

Given <**s**,**a**,**r**,**s**'> minimize

$$L = [Q(s_t, a_t) - Q^{true}(s_t, a_t)]^2$$
 const

$$L \approx [Q(s_t, a_t) - (r_t + \gamma \cdot max_{a'}Q(s_{t+1}, a'))]^2$$

const

For tabular Q(s,a)

$$\nabla L \approx 2 \cdot [Q(s_t, a_t) - (r_t + \gamma \cdot max_{a'}Q(s_{t+1}, a'))]$$

### For tabular Q(s,a)

$$L \approx [Q(s_t, a_t) - (r_t + \gamma \cdot max_a, Q(s_{t+1}, a'))]^2$$

$$\nabla L \approx 2 \cdot [Q(s_t, a_t) - (r_t + \gamma \cdot max_a, Q(s_{t+1}, a'))]$$

### Gradient descent step:

$$Q(s,a) := Q(s,a) - \alpha \cdot 2[Q(s_t,a_t) - (r_t + \gamma \cdot max_{a'}Q(s_{t+1},a'))]$$

### For tabular Q(s,a)

$$L \approx [Q(s_t, a_t) - (r_t + \gamma \cdot max_{a'}Q(s_{t+1}, a'))]^2$$

$$\nabla L \approx 2 \cdot [Q(s_t, a_t) - (r_t + \gamma \cdot max_a, Q(s_{t+1}, a'))]$$

### Gradient descent step:

$$Q(s,a) := Q(s,a)(1-2\alpha)+2\alpha(r_t+\gamma \cdot max_{a'}Q(s_{t+1},a'))$$

For tabular Q(s,a)

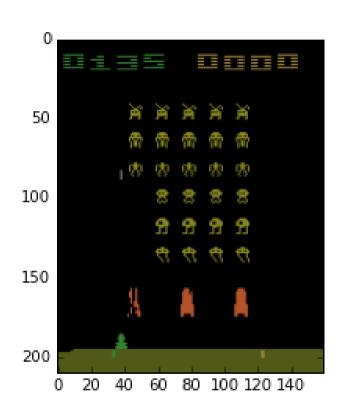
$$L \approx [Q(s_t, a_t) - (r_t + \gamma \cdot max_{a'}Q(s_{t+1}, a'))]^2$$

$$\nabla L \approx 2 \cdot [Q(s_t, a_t) - (r_t + \gamma \cdot max_a, Q(s_{t+1}, a'))]$$

Gradient descent step:

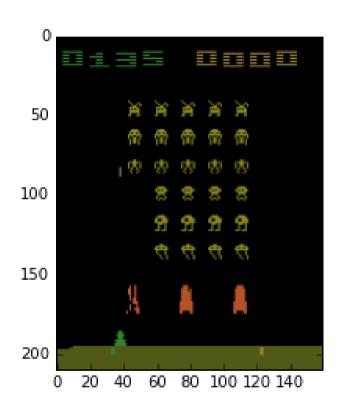
$$Q(s,a) := Q(s,a)(1-2\alpha) + 2\alpha(r_t + \gamma \cdot max_{a'}Q(s_{t+1},a'))$$

## Real world



How many states are there? approximately

## Real world



$$|S| \approx 2^{8.210.160} = 729179546432630...$$

80917 digits:)

#### **P**roblem:

# State space is usually large, sometimes continuous.

And so is action space;

However, states do have a structure, similar states have similar action outcomes.

#### **P**roblem:

# State space is usually large, sometimes continuous.

And so is action space;

#### Two solutions:

- Binarize state space (last week)
- Approximate agent with a function (crossentropy method)

#### **P**roblem:

# State space is usually large, sometimes continuous.

And so is action space;

#### Two solutions:

- Approximate agent with a function
   Let's pick this one

## From tables to approximations

- Before:
  - For all states, for all actions, remember Q(s,a)
- Now:
  - Approximate Q(s,a) with some function
  - e.g. linear model over state features

$$argmin_{w,b}(Q(s_t,a_t)-[r_t+\gamma\cdot max_{a'}Q(s_{t+1},a')])^2$$

Trivia: should we use classification or regression model? (e.g. logistic regression Vs linear regression)

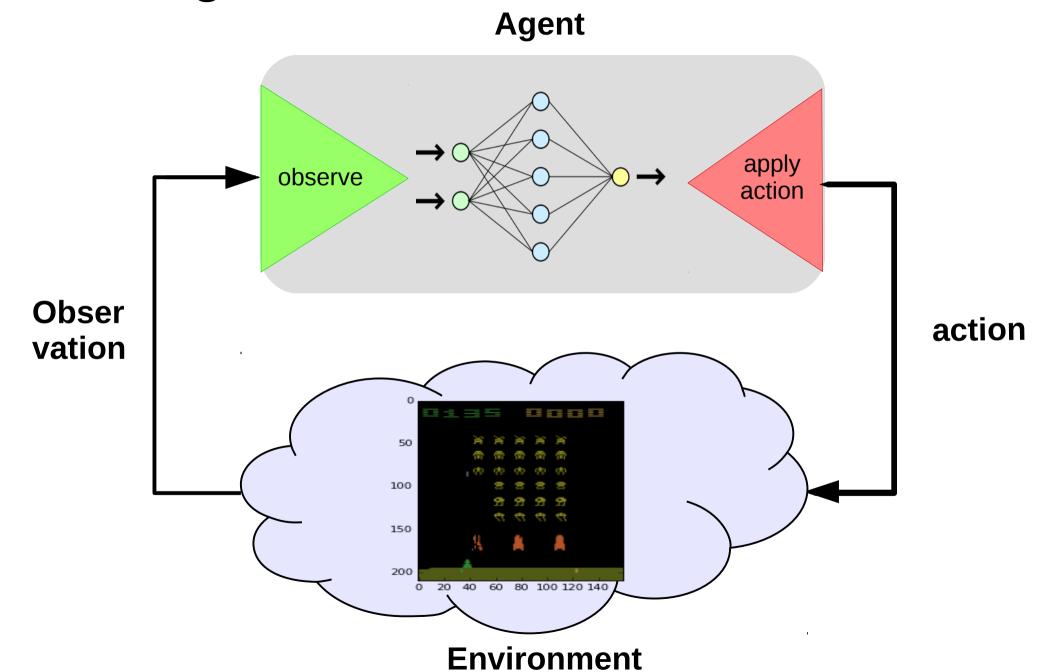
## From tables to approximations

- Before:
  - For all states, for all actions, remember Q(s,a)
- Now:
  - Approximate Q(s,a) with some function
  - e.g. linear model over state features

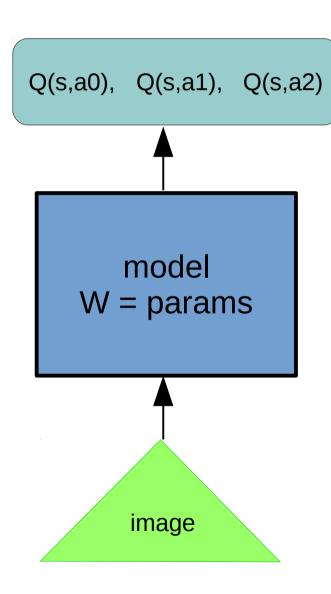
$$argmin_{w,b}(Q(s_t,a_t)-[r_t+\gamma\cdot max_{a'}Q(s_{t+1},a')])^2$$

• Solve it as a **regression** problem!

# MDP again



# Approximate Q-learning



#### **Q-values:**

$$\hat{Q}(s_t, a_t) = r + \gamma \cdot max_{a'} \hat{Q}(s_{t+1}, a')$$

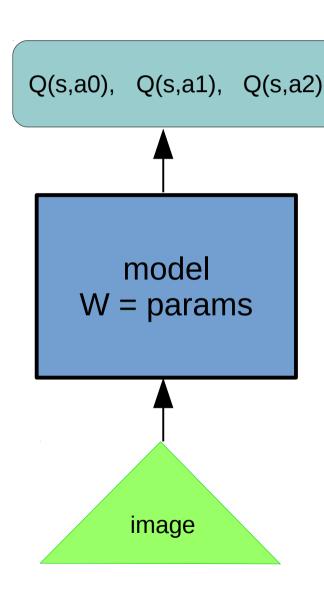
#### **Objective:**

$$L = (Q(s_t, a_t) - [r + \gamma \cdot max_{a'} Q(s_{t+1}, a')])^2$$

#### **Gradient step:**

$$w_{t+1} = w_t - \alpha \cdot \frac{\delta L}{\delta w}$$

# Approximate Q-learning



#### **Q-values:**

$$\hat{Q}(s_t, a_t) = r + \gamma \cdot max_{a'} \hat{Q}(s_{t+1}, a')$$

#### **Objective:**

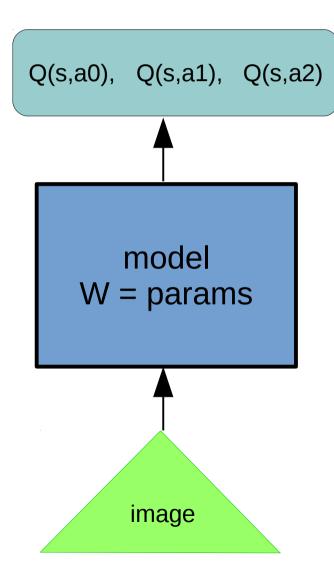
$$L = (Q(s_t, a_t) - [r + \gamma \cdot \max_{a'} Q(s_{t+1}, a')])^2$$
consider const

#### **Gradient step:**

$$\mathbf{w}_{t+1} = \mathbf{w}_t - \alpha \cdot \frac{\partial L}{\partial \mathbf{w}_t}$$

## Approximate SARSA

#### **Objective:**



$$L = (Q(s_t, a_t) - \hat{Q}(s_t, a_t))^2$$
consider const

#### **Q-learning:**

$$\hat{Q}(s_t, a_t) = r + \gamma \cdot \max_{a'} Q(s_{t+1}, a')$$

#### **SARSA:**

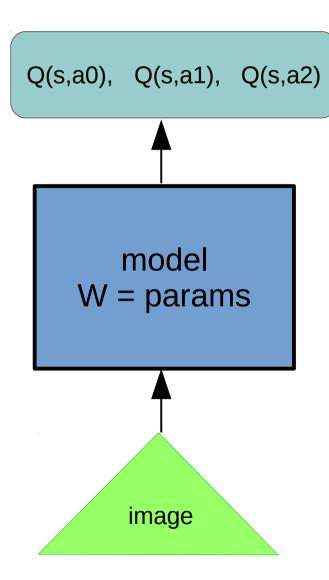
$$\hat{Q}(s_t, a_t) = r + \gamma \cdot Q(s_{t+1}, a_{t+1})$$

#### **Expected Value SARSA:**

$$\hat{Q}(s_t, a_t) = ???$$

## Approximate SARSA

#### **Objective:**



$$L = (Q(s_t, a_t) - \hat{Q}(s_t, a_t))^2$$
consider const

#### **Q-learning:**

$$\hat{Q}(s_t, a_t) = r + \gamma \cdot \max_{a'} Q(s_{t+1}, a')$$

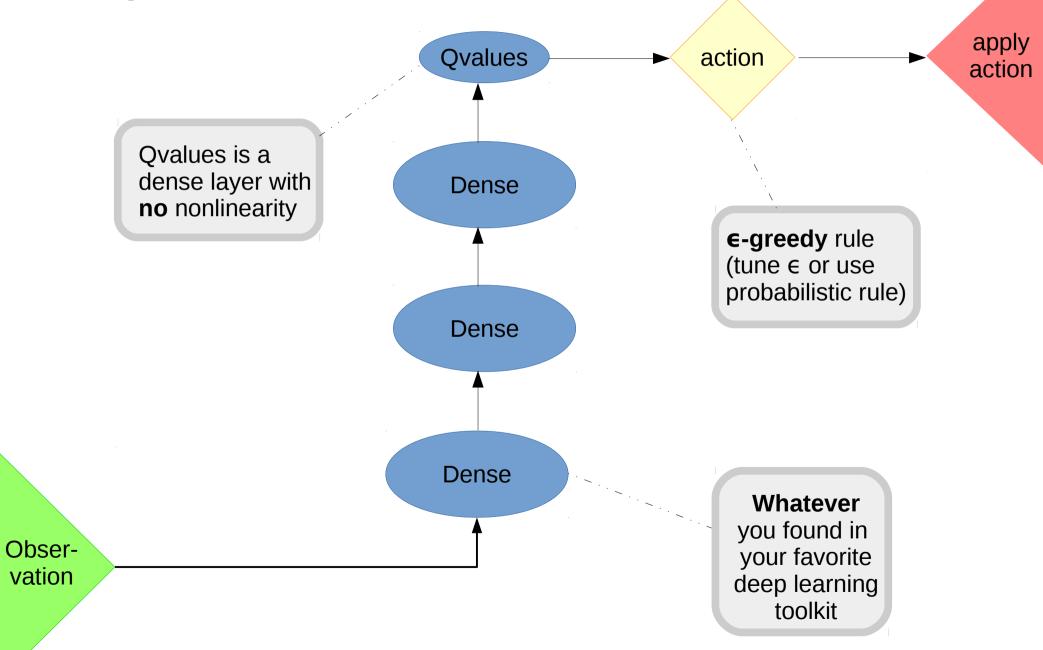
#### **SARSA:**

$$\hat{Q}(s_t, a_t) = r + \gamma \cdot Q(s_{t+1}, a_{t+1})$$

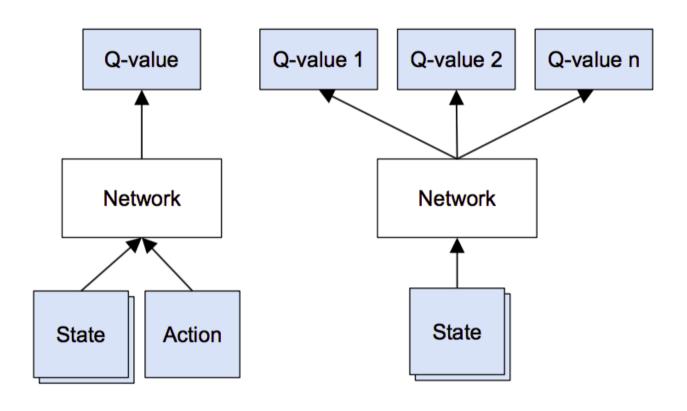
#### **Expected Value SARSA:**

$$\hat{Q}(s_t, a_t) = r + \gamma \cdot E_{a' \sim \pi(a|s)} Q(s_{t+1}, a')$$

# Deep RL 101

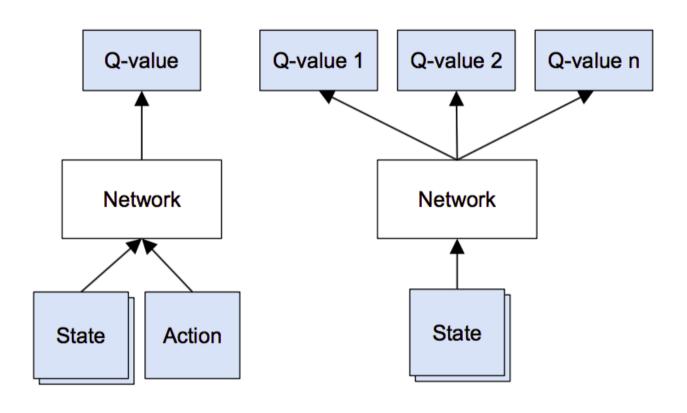


## Architectures



Given **(s,a)** Predict Q(s,a) Given **s** predict all q-values Q(s,a0), Q(s,a1), Q(s,a2)

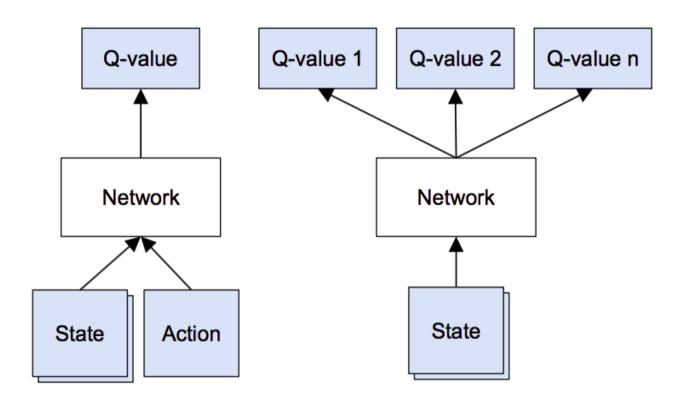
## Architectures



Given **(s,a)** Predict Q(s,a) Given **s** predict all q-values Q(s,a0), Q(s,a1), Q(s,a2)

**Trivia:** in which situation does **left** model work better? And right?

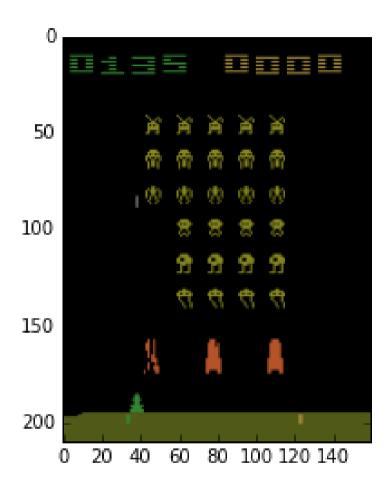
## Architectures



Needs one forward pass for **each action** 

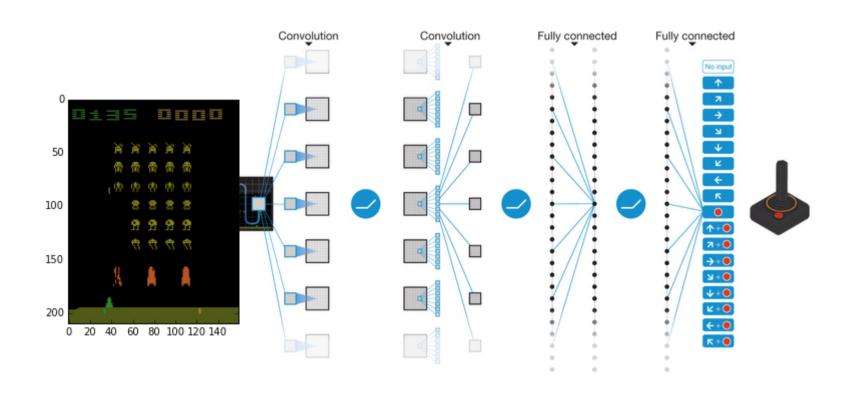
Works if action space is large efficient when not all actions are available from each state

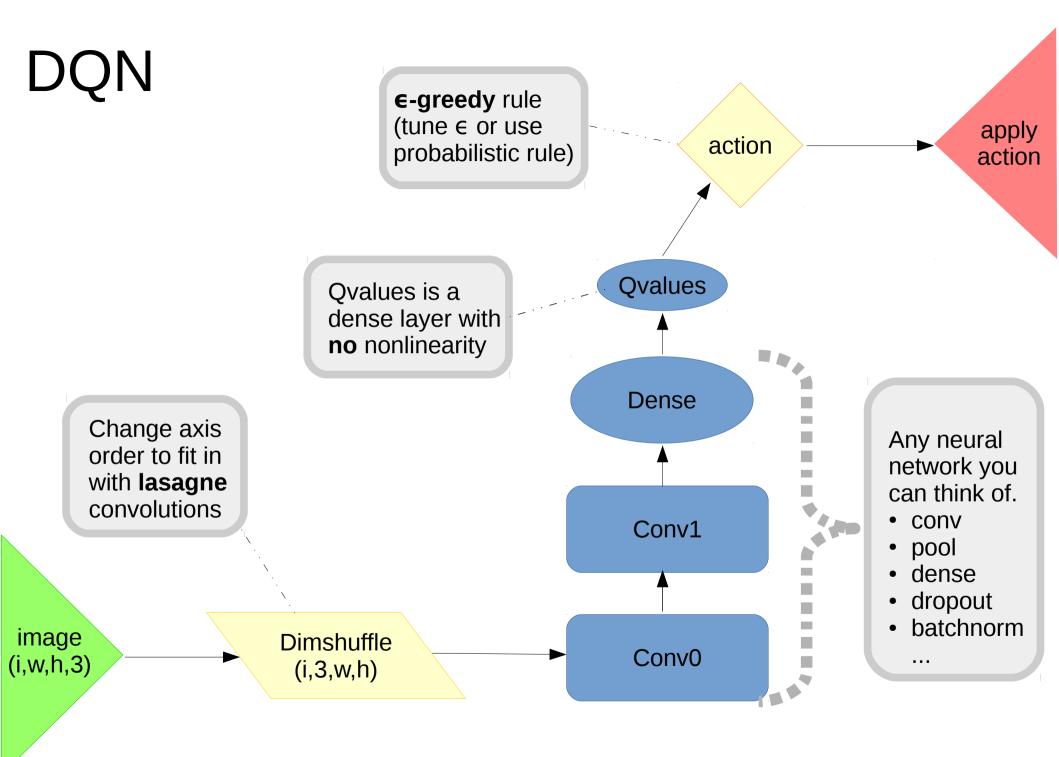
Needs one forward pass for **all actions** (faster)

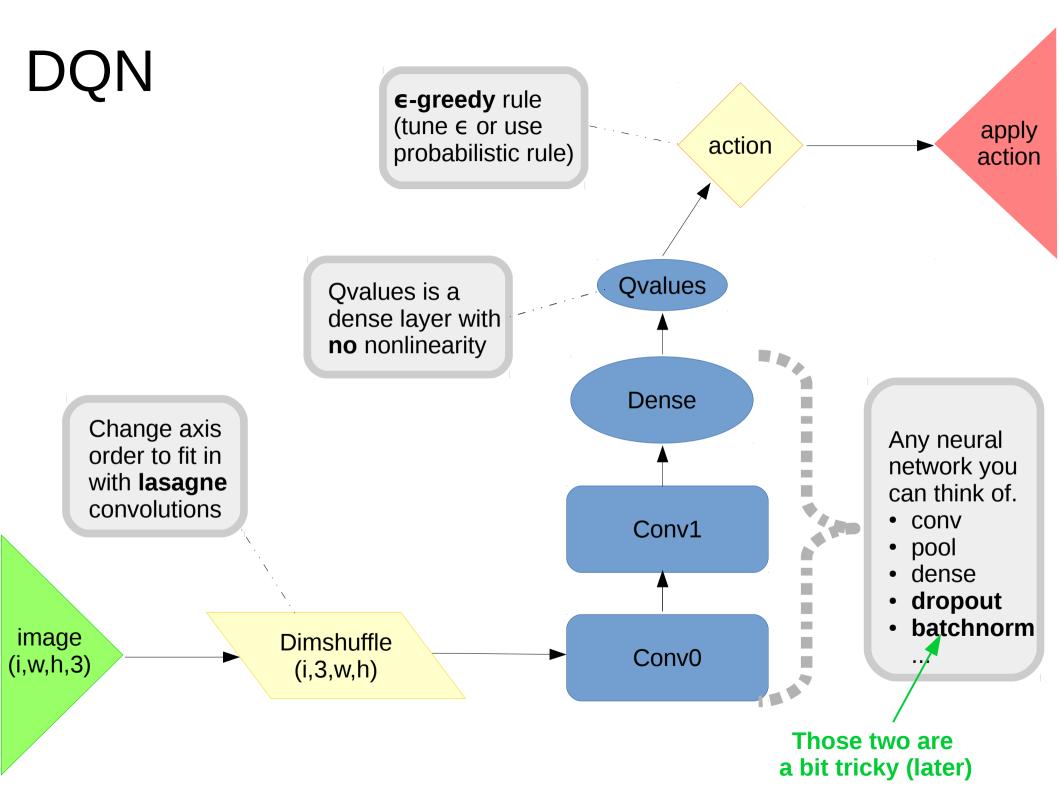


What kind of network digests images well?

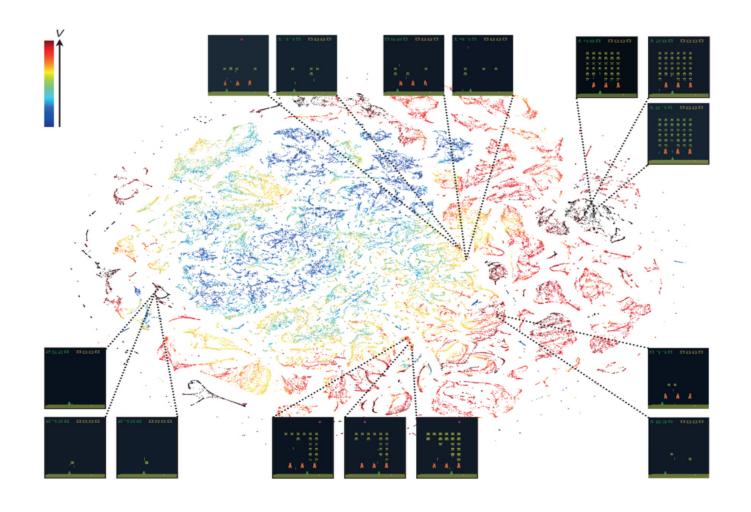
## Deep learning approach: DQN



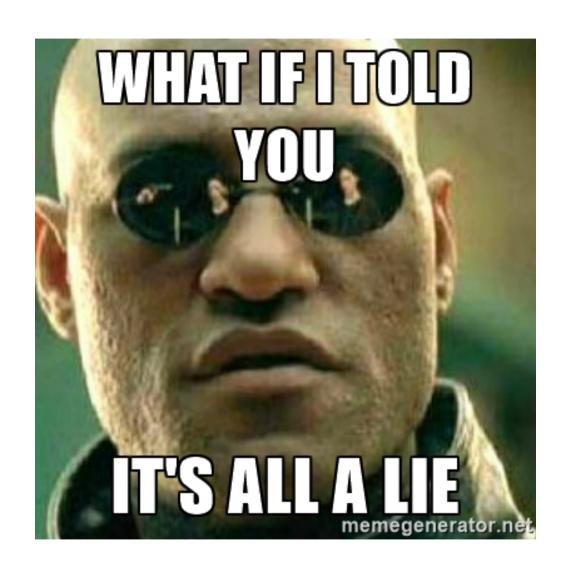


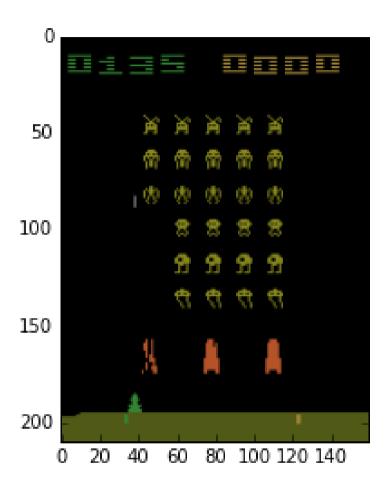


## TSNE makes every slide 40% better



- Embedding of pre-last layer activations
- Color =  $V(s) = max \ a \ Q(s,a)$

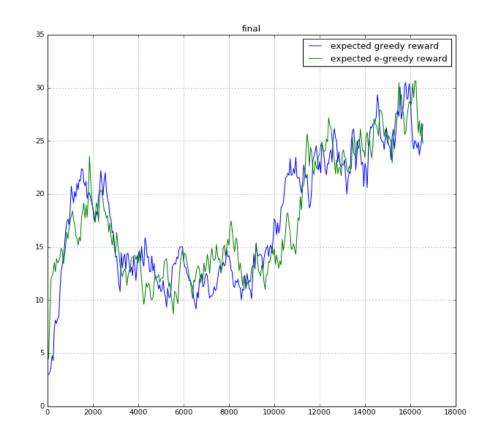




How bad it is if agent spends next 1000 ticks under the left rock? (while training)

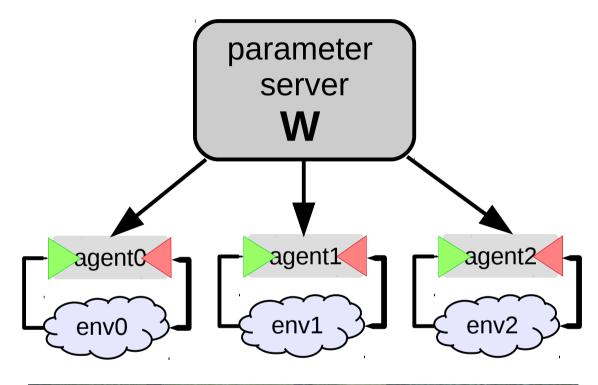
## Problem

- Training samples are not "i.i.d",
- Model forgets parts of environment it hasn't visited for some time
- Drops on learning curve
- Any ideas?



# Multiple agent trick

**Idea:** Throw in several agents with shared **W**.



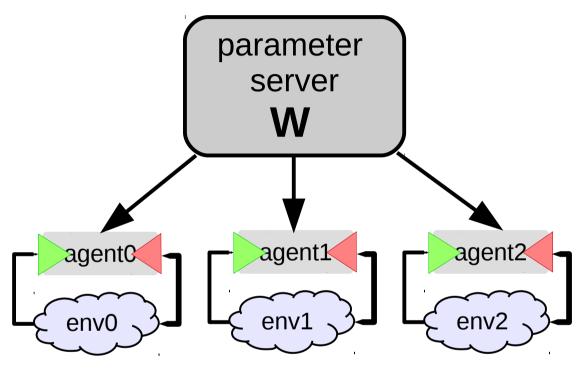


## Multiple agent trick

**Idea:** Throw in several agents with shared **W**.

- Chances are, they will be exploring different parts of the environment,
- More stable training,
- Requires a lot of interaction

**Trivia:** your agent is a real robot car. Any problems?

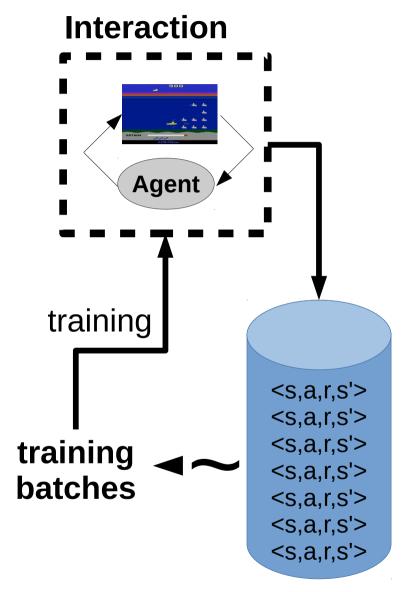




## Experience replay

Idea: store several past interactions <s,a,r,s'>
Train on random subsamples

Any +/- ?



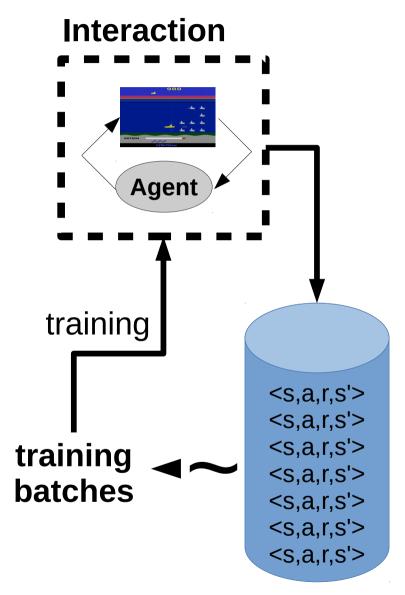
Replay buffer

## Experience replay

Idea: store several past interactions <s,a,r,s'>
Train on random subsamples

- Atari DQN: >10^5 interactions
- Closer to i.i.d pool contains several sessions
- Older interactions were obtained under weaker policy

Better versions coming next week



## Summary so far

to make data closer to i.i.d.

Use one or several of

- experience replay
- multiple agents
- Infinitely small learning rate :)

advanced stuff coming next lecture

## An important question

- You approximate Q(s,a) with a neural network
- You use experience replay when training

Trivia: which of those algorithms will fail?

- Q-learning
- SARSA

- CEM
- Expected Value SARSA

## An important question

- You approximate Q(s,a) with a neural network
- You use experience replay when training

Agent trains off-policy on an older version of him

Trivia: which of those algorithms will fail?

Off-policy methods work, On-policy is super-slow (fail)

Q-learning

- CEM

- SARSA

Expected Value SARSA

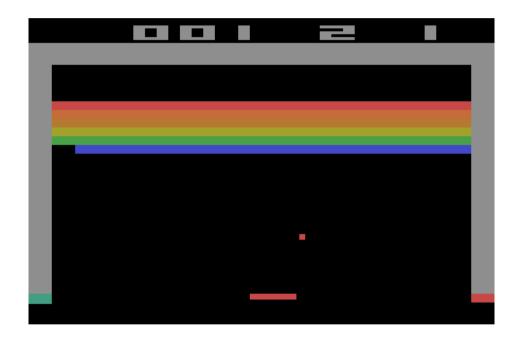
### When training with on-policy methods,

- use no (or small) experience replay
- compensate with parallel game sessions

## Deep learning meets MDP

- Dropout, noize
  - Used in experience replay only: like the usual dropout
  - Used when interacting: a special kind of exploration
  - You may want to decrease p over time.
- Batchnorm
  - Faster training but may break moving average
  - Experience replay: may break down if buffer is too small
  - Parallel agents: may break down under too few agents
     <same problem of being non i.i.d.>

# Final problem



Left or right?

#### **P**roblem:

Most practical cases are partially observable:

Agent observation does not hold all information about process state (e.g. human field of view).

Any ideas?

#### **Problem:**

Most practical cases are partially observable:

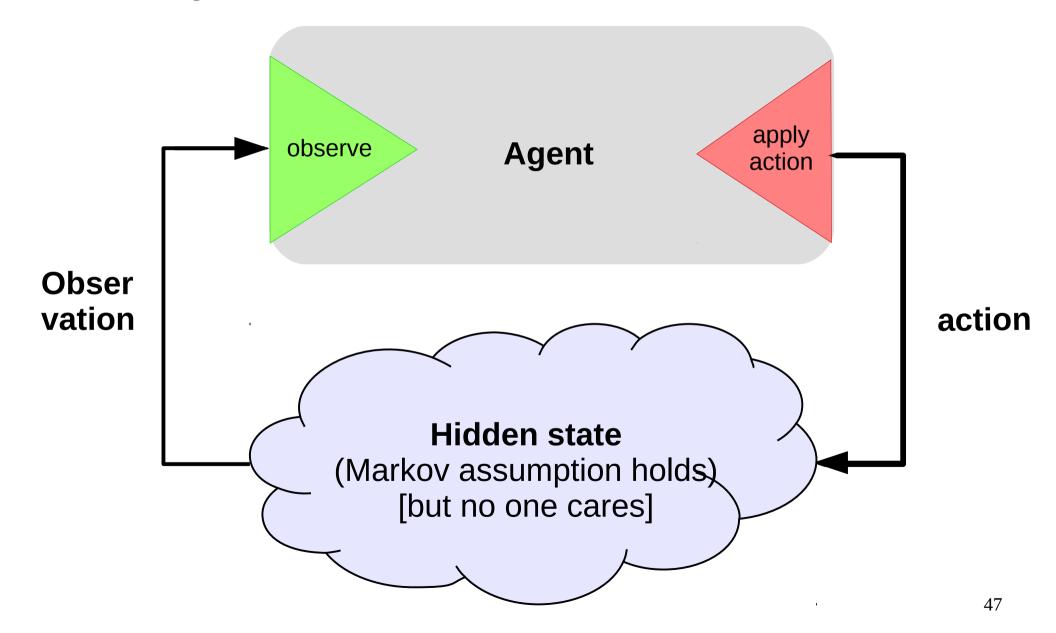
Agent observation does not hold all information about process state (e.g. human field of view).

 However, we can try to infer hidden states from sequences of observations.

$$s_t \simeq m_t : P(m_t | o_t, m_{t-1})$$

Intuitively that's agent memory state.

## Partially observable MDP



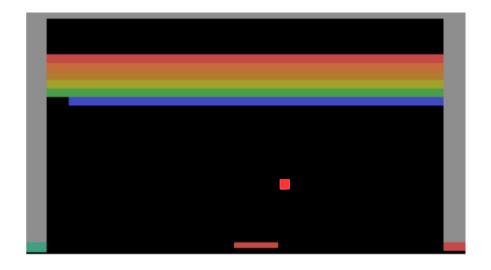
## N-gram heuristic

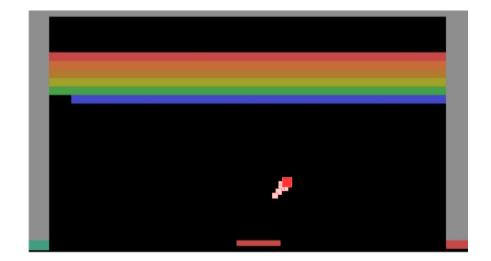
#### Idea:

$$s_t \neq o(s_t)$$

$$s_t \approx (o(s_{t-n}), a_{t-n}, ..., o(s_{t-1}), a_{t-1}, o(s_t))$$

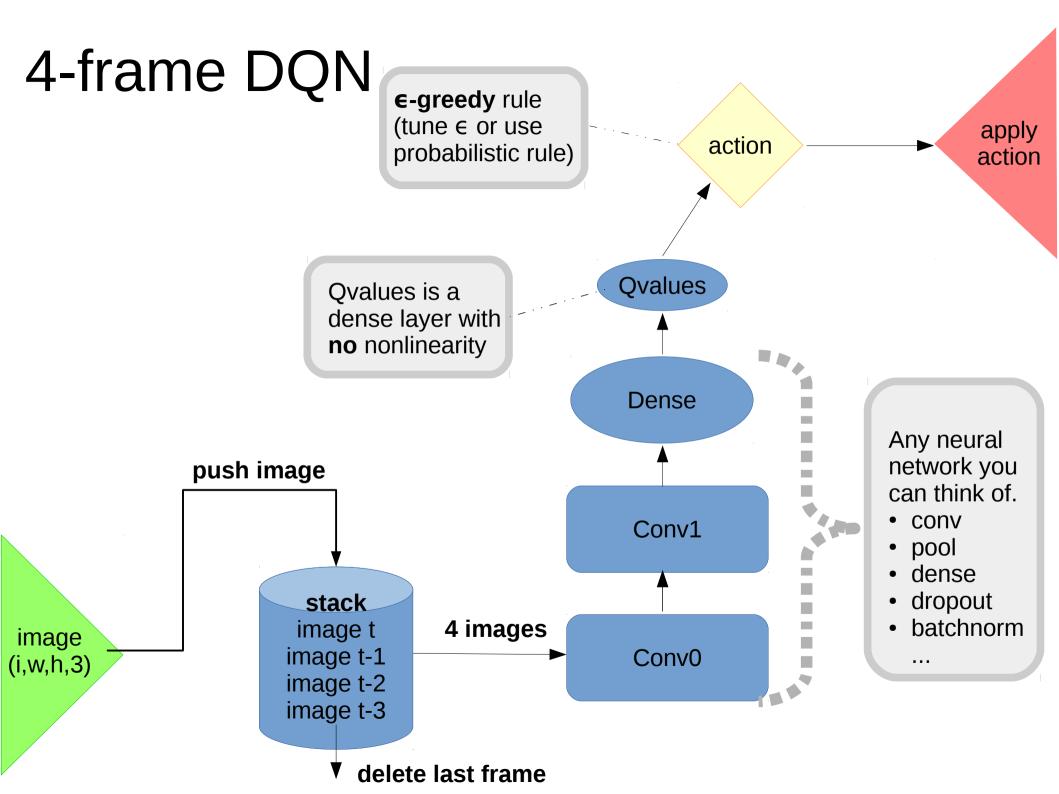
e.g. ball movement in breakout





· One frame

· Several frames 48



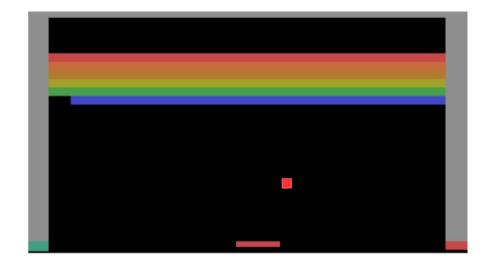
## N-gram heuristic

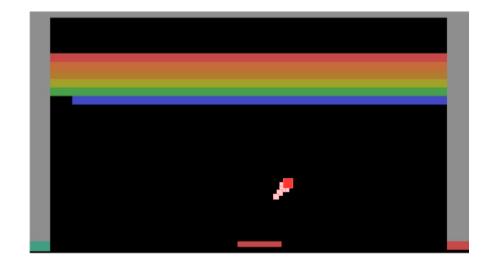
#### Idea:

$$s_t \neq o(s_t)$$

$$s_t \approx (o(s_{t-n}), a_{t-n}, ..., o(s_{t-1}), a_{t-1}, o(s_t))$$

e.g. ball movement in breakout





· One frame

· Several frames 50

### **Alternatives**

### **Ngrams:**

- Nth-order markov assumption
- Works for velocity/timers
- Fails for anything longer that N frames
- Impractical for large N

### **Alternative approach:**

- Infer hidden variables given observation sequence
- · Kalman Filters, Recurrent Neural Networks
- · More on that in a few lectures

### Seminar



### Autocorrelation

• Reference is based on predictions

$$r + \gamma \cdot max_{a'}Q(s_{t+1}, a')$$

- Any error in Q approximation is propagated to neighbors
- If some Q(s,a) is mistakenly over-exaggerated, neighboring qvalues will also be increased in a cascade
- Worst case: divergence
- Any ideas?

### Target networks

**Idea:** use older network snapshot to compute reference

$$L = (Q(s_t, a_t) - [r + \gamma \cdot max_a' Q^{old}(s_{t+1}, a')])^2$$

- Update Q old periodically
  - Slows down training

## Target networks

**Idea:** use older network snapshot to compute reference

$$L = (Q(s_t, a_t) - [r + \gamma \cdot max_a' Q^{old}(s_{t+1}, a')])^2$$

- Update Q old periodically
  - Slows down training
- Smooth version:
  - use moving average

$$\theta^{old} := (1 - \alpha) \cdot \theta^{old} + \alpha \cdot \theta^{new}$$

•  $\Theta$  = weights