

35. Naive Bayes

- These are classification algorithm which work on **conditional probability basis**
- Naive Bayes is a classification algorithm based on Bayes' theorem.
- which is a probability theory that describes the probability of an event, based on prior knowledge of conditions that might be related to the event
- **Naive**: It is called Naive b/c it assumes that the occurrence of a certain feature is independent of the occurrence of other features.
- **Bayes**: It is called Bayes b/c it depends on the principle of Bayes' Theorem.

Conditional Probability

$$P(E) = \frac{\text{favourable outcome(s)}}{\text{total outcomes}}$$

$$0 \leq P(E) \leq 1$$

Example: A bag contains 3 red balls and 2 blue balls.

$$P(\text{red balls}) = \frac{3}{3+2} = 0.60$$

Conditional Probability has 2 more types:

1. Independent Probability
2. Dependent Probability

1. Independent Probability

- Rolling a dice can have following events: {1,2,3,4,5,6}
- For single event the probability will be 1/6
- The preceding event and following event both are not dependents on each other

2. Dependent Probability

- It is also called **Conditional Probability**
- In above balls example, the probability of $P(\text{red balls}) = 3/5$.
- But condition is that when you take the ball out, then do not put it back to the bag.
- so if we have taken one red ball from the bag, then there will be 2 red balls left and 4 total balls,
- In such circumstance, probability of blue ball is 2/4
- Hence the probability of blue ball is depending upon the probability of red balls

- so we can express this as:

$$P(\text{Blue Balls}) = P\left(\frac{\text{Blue Balls}}{\text{Red Balls}}\right) = P\left(\frac{B}{R}\right)$$

Also can be written as:

$$P(R \text{ or } B) = P(R) * P\left(\frac{B}{R}\right)$$

OR

$$P(R \text{ or } B) = P(B/R) * P(R)$$

Bayes' Theorem:


$$P(A \cap B) = P(B/A) * P(A)$$

as

$$P(A \cap B) = P(B \cap A)$$

so

$$P(B \cap A) = P(A/B) * P(B)$$

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As

$$P(A \cap B) = P(B \cap A)$$

So

$$P(B/A) * P(A) = P(A/B) * P(B)$$

To find P(A/B)

$$P(A/B) = \frac{P(B/A) * P(A)}{P(B)}$$

The above formula is called **Bayes' Theorem**

- This formula states that when event B is occurred, then what are chances of event A to come

Bayes' Theorem


- **Bayes' Theorem** is also known as Bayes' Rule or Bayes' law.
- which is used to determine the probability of a hypothesis with prior knowledge.


- It depends on the conditional probability.
- It is expressed as:

$$P(A/B) = \frac{P(B/A) * P(A)}{P(B)}$$

Where:

- **P(A/B) is Posterior Probability:** Probability of hypothesis A on the observed event B.
- **P(B/A) is Likelihood Probability:** Probability of hypothesis B when event A is occurring. Probability of the evidence given that the probability of a hypothesis is true.
- **P(A) is Prior Probability:** Probability of hypothesis before observing the evidence.
- **P(B) is Marginal Probability:** Probability of evidence.

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Types of Naive Bayes Model

There are three types of Naive Bayes Model:

1. Gaussian
2. Multinomial
3. Bernoulli

1. Gaussian Naive Bayes:

- Assumes that continuous features follow a Gaussian (normal) distribution
- Suitable for features that are continuous and have a normal distribution

2. Bernoulli Naive Bayes:

- Assumes that features are binary (Boolean) variables
- Suitable for data that can be represented as binary features, such as document classification problems where each term is either present or absent

3. Multinomial Naive Bayes:

- Assumes that features follow a multinomial distribution
- Typically used for discrete data, such as text data, where each feature represents the frequency of a term.

In []: