

CSC 503 Homework Assignment 5

Out: September 11, 2015

Due: September 18, 2015

MISSING-ID

In using the Fitch macros to typeset proofs in first order logic, one introduces a dummy variable x by means of the command `\open[x]`.

1. [10 points] Using only the basic natural deduction rules, find a proof for

$$\forall x(P(x) \rightarrow Q(x)) \vdash \forall xP(x) \rightarrow \forall xQ(x).$$

2. [20 points] Using only the basic natural deduction rules, find a proof for

$$\forall x\forall yP(x, y) \vdash \forall u\forall vP(u, v).$$

3. [35 points] Using only the basic natural deduction rules, find a proof for

$$\exists x(\neg P(x) \vee Q(x)) \vdash \exists x\neg(P(x) \wedge \neg Q(x)).$$

4. [35 points] Using only the basic natural deduction rules, find a proof for

$$\forall x\forall y\forall z[S(x, y) \wedge S(y, z) \rightarrow S(x, z)], \forall x\neg S(x, x) \vdash \forall x\forall y[S(x, y) \rightarrow (\neg S(y, x) \vee S(x, x))]$$