

# Cryptography Notes

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Note that these notes are based on the 2023v3 version of the cryptography book.

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# Curriculum

This is an excerpt of useful information from the professor on the exam, for this semester.

## Background material:

Chapters 2+3 (preliminary probability theory and math), Section 5.4 (optimistic results on key exchange), Section 6.3 (diff and lin analysis), Proof of Theorem 7.8 (if you can get the secret exponent you can factor), Section 7.6.1 (factoring algorithms), Section 9.6 (discrete log algorithms).

## Grading:

Your grade is based on an overall assessment of your performance at the exam and your hand-in exercises (which count for 20%) .

Here are some details on what you might for instance cover in each the exam subject. But do not misunderstand this in the sense that you have to follow the templates below, they really are just examples...

## Information theory and Cryptography:

Definition of perfect secret security, why you need as many keys as plaintexts to have perfect security. Definition of entropy, and proof of some of the inequalities properties it satisfies. Unicity distance (but be careful, this may take a lot of time, so test this beforehand)

## Symmetric (secret-key) cryptography:

What a crypto-system is (the three algorithms) You can describe DES or AES - but you can also just give a high-level description of what a block cipher is. Definitions of PRF and CPA security. Specification of CBC or CTR modes (or both), proofs of CPA security for CBC or CTR mode (or both). Perhaps a brief talk about stream ciphers and how to make one from a block cipher.

## Public-key cryptography from Factoring:

What a public-key cryptosystem is. Basic spec of RSA, maybe proof that decryption works. Then some selection of the following: How to make RSA be CPA secure (the PCRSA scheme, and the result that computing the least significant bit is as hard as inverting RSA). How to generate keys and Miller-Rabin primality testing, how to get CCA security: OAEP and the intuition on why it works.

## Public-key cryptography based on discrete log and LWE:

The DL, DH and DDH problems, and how they relate. The El Gamal cryptosystem and proof that it is secure if DDH is hard. Then some example of groups we can use, can be a subgroup of  $\mathbb{Z}_p^*$ , or you can talk about elliptic curves. You can also put less emphasis on El Gamal, for instance skip the example groups and go to LWE instead, define the problem and the cryptosystem and do the proof from the exercise that decryption works under a certain assumption about the noise distribution.

## Symmetric authentication and hash functions:

Definition of collision-intractable hash functions. Then a selection of: construction from discrete log, proof that collision-intractable implies one-way, construction and proof that we can get any size input from fixed size input. Finally, MAC schemes, definition of CMA security, CBCMAC and EMAC security result for EMAC. Maybe a brief mention of HMAC.

## Signature schemes:

Definition of signatures schemes and of CMA security. The Schnorr signature scheme, you can do many details here, such as the proof that you cannot cheat the underlying interactive game with better than  $1/q$  probability, and the full story on how you derive the signature scheme from the interactive game. Or you can just do the spec of the scheme, giving you time for something else, such as RSA+hash signatures and the proof that secure hash + secure signature scheme is secure. Or you can do the one-time signatures based on hash functions and the proof that they are secure.

## Information theory and Cryptography (Chapter 5)

### Disposition (Kirk)

- Perfect Security
- Entropy
- Unicity Distance

### Disposition (Berg)

#### Notes

#### Perfect Security

Below we have the definition for perfect security:

**Definition 5.1:** A cryptosystem has perfect security if for all  $x \in \mathcal{P}$  and  $y \in \mathcal{C}$ , it holds that  $P[x|y] = P[x]$ .

**TLDR:** Information about the ciphertext gives you *no* information about the plaintext.

# Symmetric (secret-key) cryptography (Chapter 4.1 + 6)

## Disposition (Kirk)

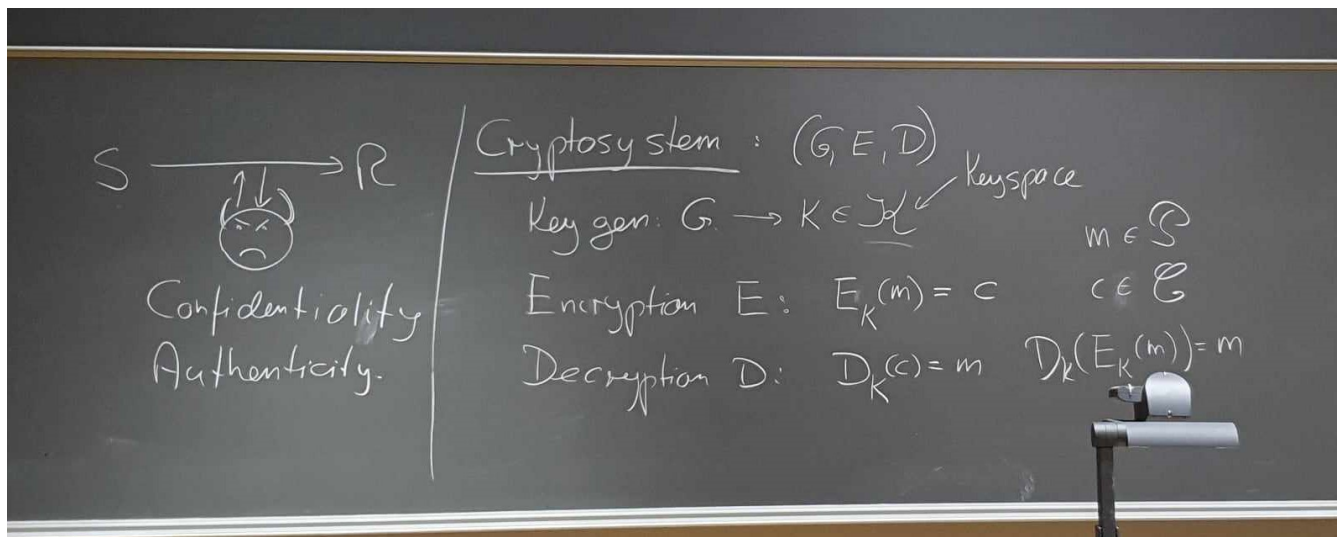
- Definitely AES
- PRF and CPA security
- CBC/CTR
- CPA security proof for CBC/CTR
- At least understand the block cipher...

## Disposition (Berg)

- Symmetric Cryptosystem definition (chap 4.1)
- DES definition
  - Feistel ciphers
- AES definition
- (High level definition of Block Ciphers)
- PRF security
- CPA security
- CBC mode
- CTR mode
- Stream ciphers
- (Differential & Linear Cryptanalysis)

## Notes

### Symmetric Cryptosystems



(Optionally something related to confidentiality and authenticity)

For a symmetric system, there are 3 finite sets given; the key.

## Public-key cryptography from Factoring (Chapter 7 & 8)

Disposition (Kirk)

Disposition (Berg)

Notes

Public-key cryptography based on discrete log and LWE (Chapter 9 & 10, definition of CPS security in chapter 8)

Disposition (Kirk)

Disposition (Berg)

Notes

## Symmetric authentication and hash functions (Chapter 11)

Disposition (Kirk)

Disposition (Berg)

Notes

## Signature schemes (Chapter 12)

Disposition (Kirk)

Disposition (Berg)

Notes