

# “Mathematical Modelling of Myeloproliferative Neoplasms and Hematopoietic Stem Cells”

## Ph.D.-defense

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- Background on mathematical modelling and blood cancers

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- ▶ Background on mathematical modelling and blood cancers
- ▶ Three particular mathematical models

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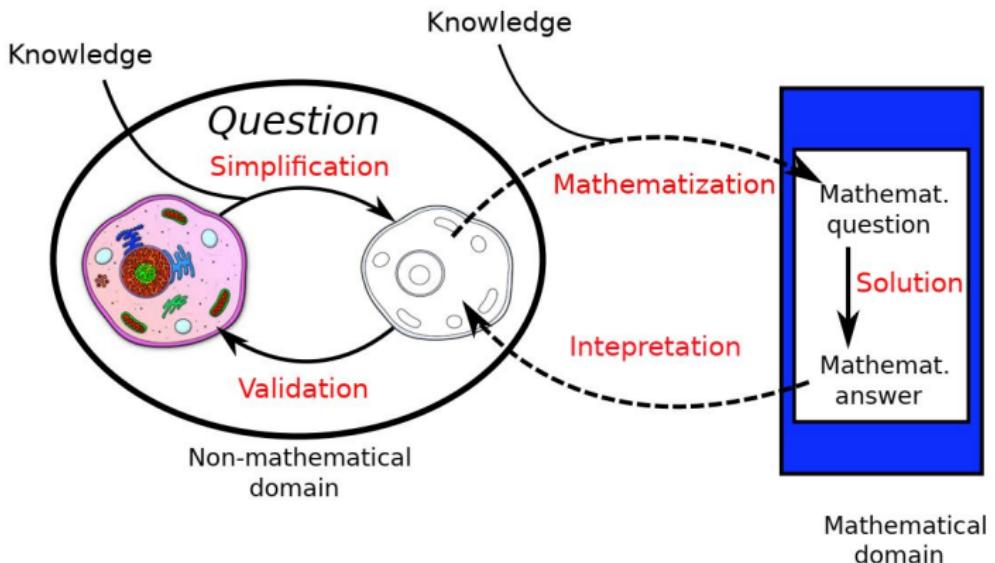
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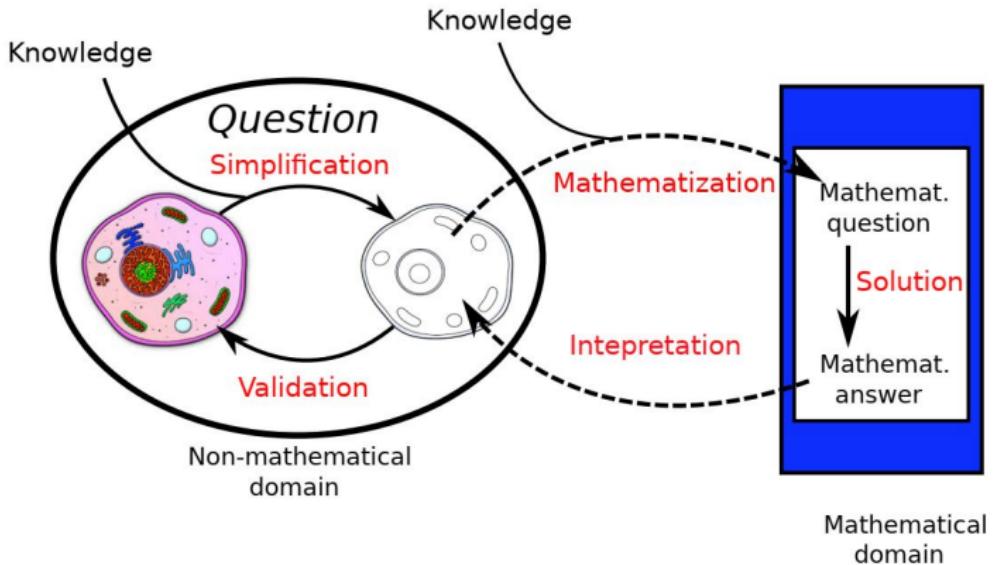
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The modelling cycle, taken from (Hansen & Ottesen, 2020)

# Mathematical Modelling



The modelling cycle, taken from (Hansen & Ottesen, 2020)

“If you want to be successful, pick a cancer and work on that”

- Doron Levy (University of Maryland), CIRM Math-Cancer workshop, summer 2018

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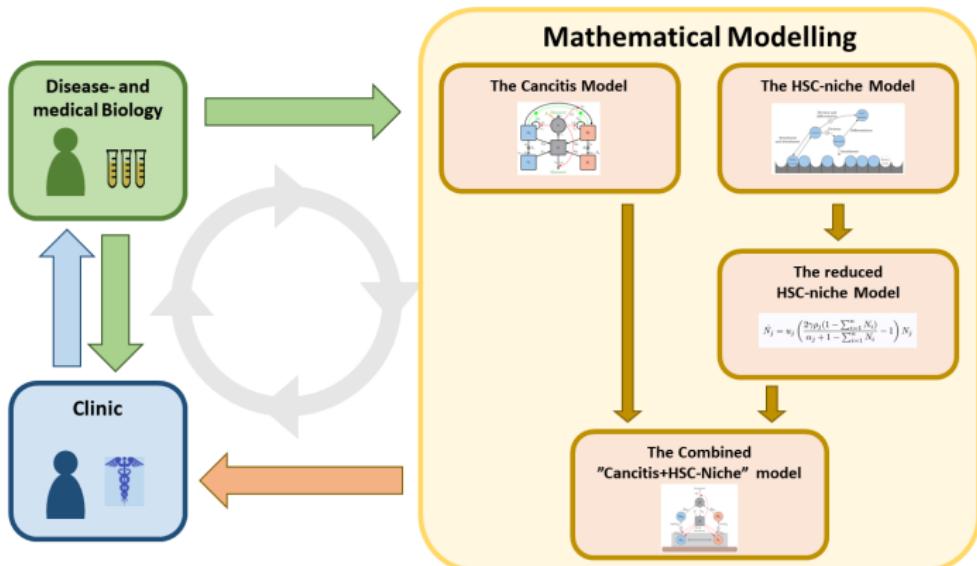
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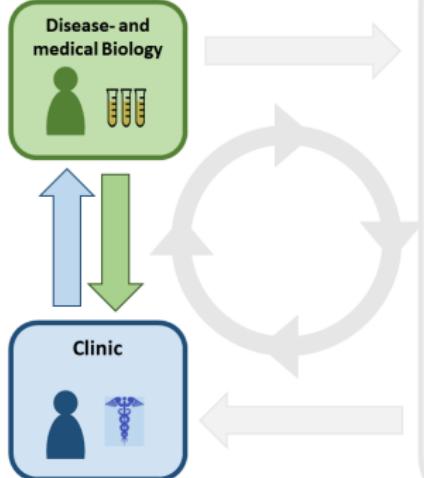
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## Mathematical Modelling

### The Cancitis Model



### The HSC-niche Model



### The reduced HSC-niche Model

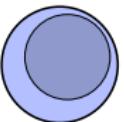
$$\dot{N}_I = \omega_I \left( \frac{2\eta p_I (1 - \sum_{i=1}^{N_H} N_i)}{\alpha_I + 1 - \sum_{i=1}^{N_H} N_i} - 1 \right) N_I$$

### The Combined "Cancitis+HSC-Niche" model



# The blood system and MPNs

- ▶ **HSC:** Hematopoietic Stem Cells. Produces progenitor cells.



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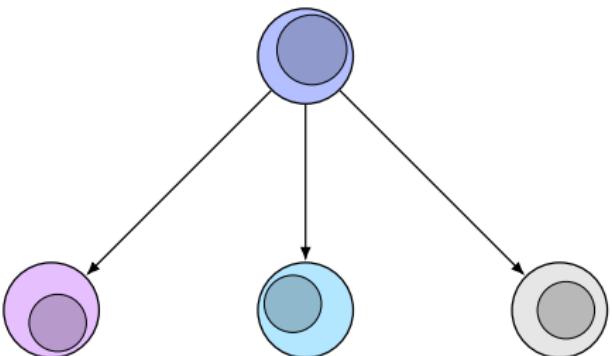
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# The blood system and MPNs

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- ▶ **Progenitors:** Produces blood cells.



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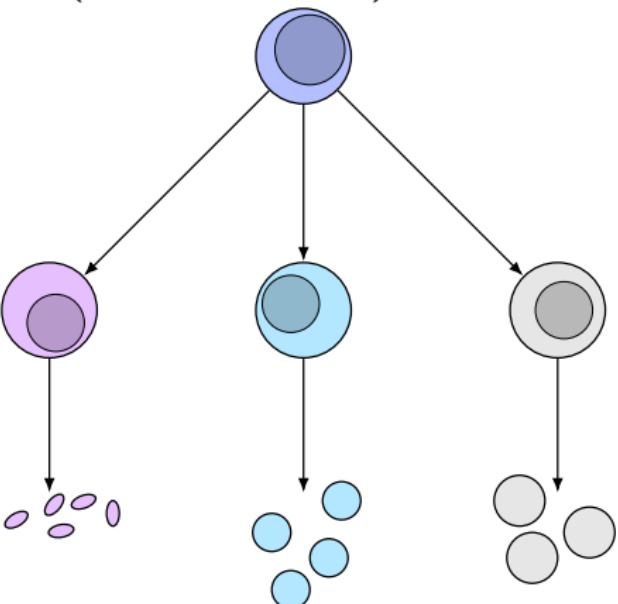
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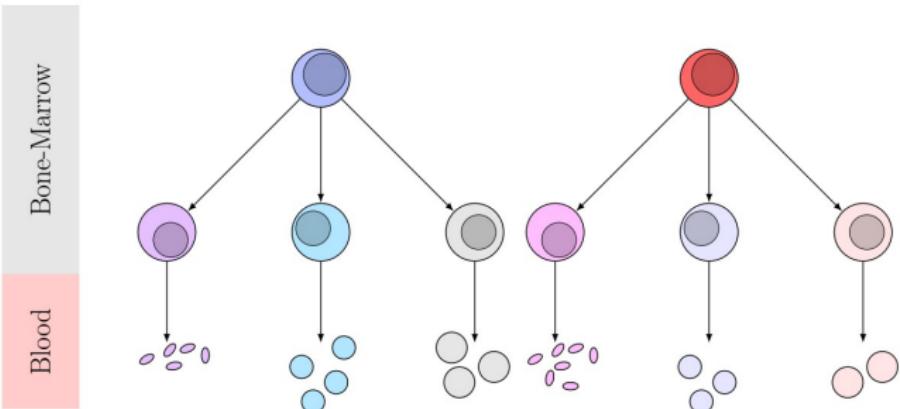
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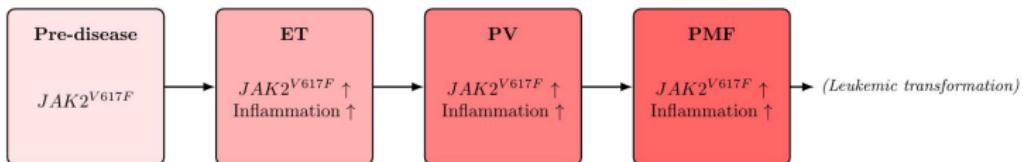
- ▶ **HSC:** Hematopoietic Stem Cells. Produces progenitor cells.
- ▶ **Progenitors:** Produces blood cells.
- ▶ **Blood-cells:** e.g. Thrombocytes (platelets) and Leukocytes (white blood cells).
- ▶ **HSC mutation:** Affects some part of HSC behaviour.
- ▶ **MPNs:** Myeloproliferative Neoplasms Group of diagnoses, e.g.
  - ▶ Essential Thrombocythemia (ET)
  - ▶ Polycythemia Vera (PV)
  - ▶ Primary Myelofibrosis (PMF)

Characterised by positive JAK2<sup>V617F</sup> mutation and heightened blood-cell counts.

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Characterised by positive JAK2<sup>V617F</sup> mutation and heightened blood-cell counts.

(Note: We do not consider CML, and focus only on the Philadelphia-chromosome-negative MPNs)

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- Phase III clinical trial comparing Interferon-alfa2a (IFN) and Hydroxyurea (HU)

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- ▶ Phase III clinical trial comparing Interferon-alfa2a (IFN) and Hydroxyurea (HU)
- ▶ ≈ 200 Danish MPN patients

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- ▶ Phase III clinical trial comparing Interferon-alfa2a (IFN) and Hydroxyurea (HU)
- ▶ ≈ 200 Danish MPN patients
- ▶ 63 with IFN mono-treatment through whole study

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- ▶ Phase III clinical trial comparing Interferon-alfa2a (IFN) and Hydroxyurea (HU)
- ▶ ≈ 200 Danish MPN patients
- ▶ 63 with IFN mono-treatment through whole study
- ▶ Data from a wide range of clinical measures

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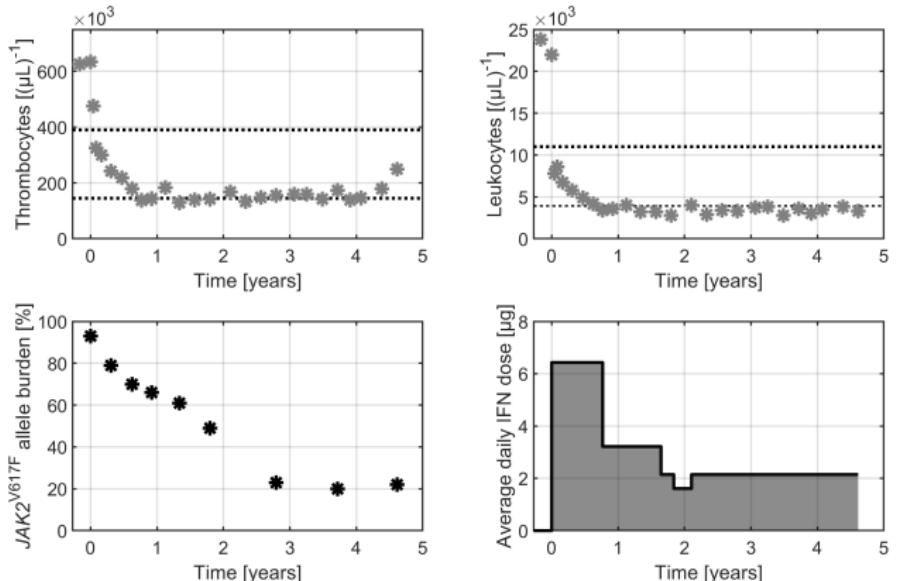
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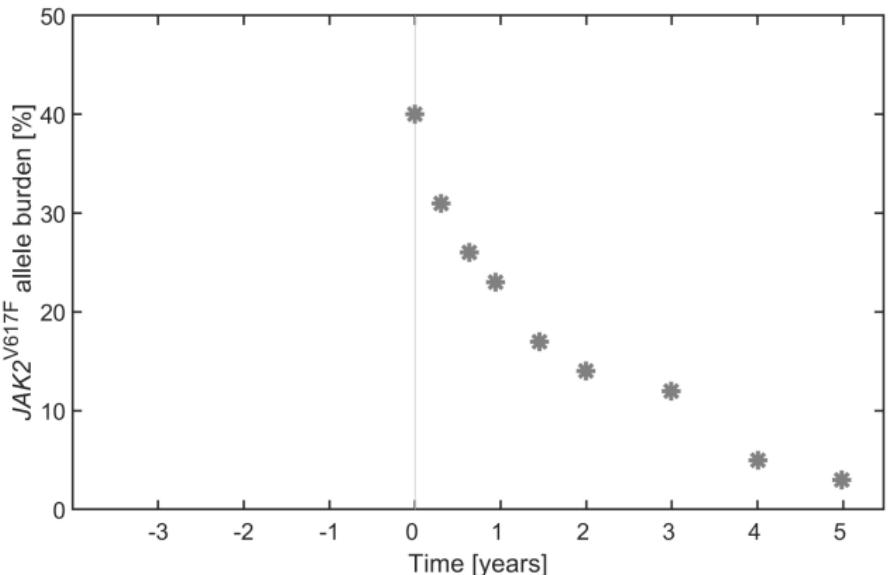
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For details, see chapter 3 or Pedersen et al (2020)

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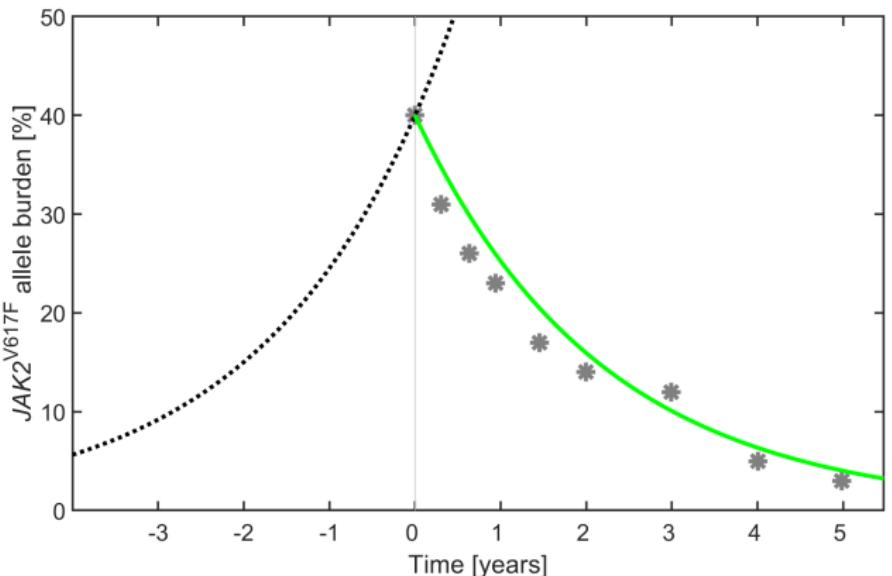
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# Comments on empirical approach

- The “what”, not the “why”

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- ▶ The “what”, not the “why”
- ▶ Blood-cells are not considered

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- ▶ The “what”, not the “why”
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- ▶ Standard-of-care vs. actual IFN-dose

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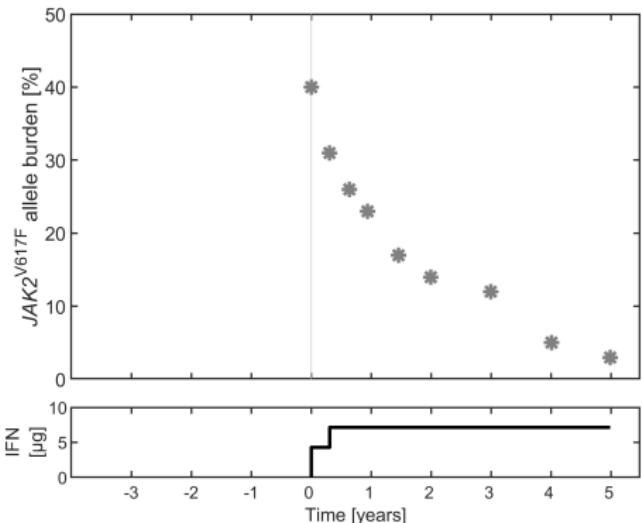
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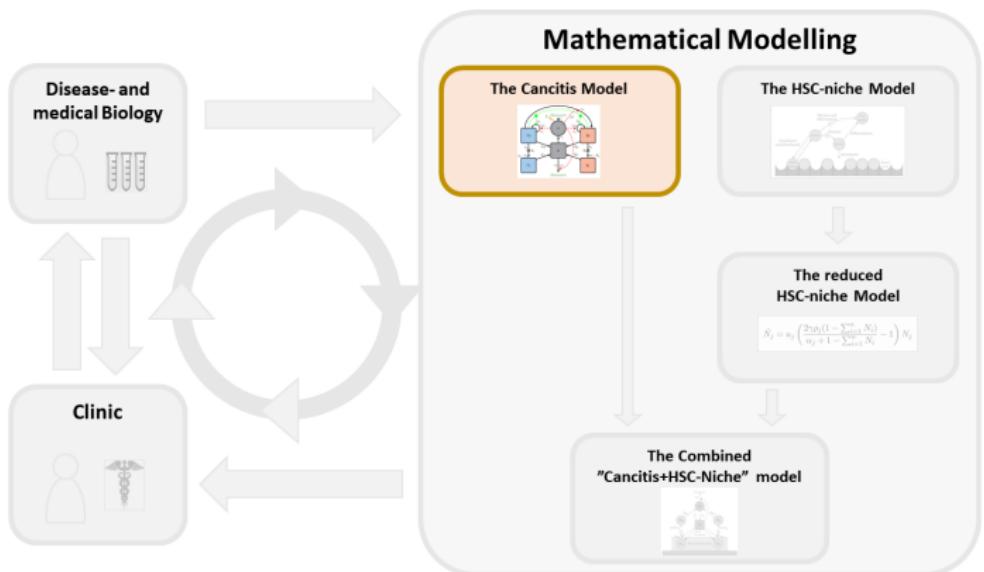
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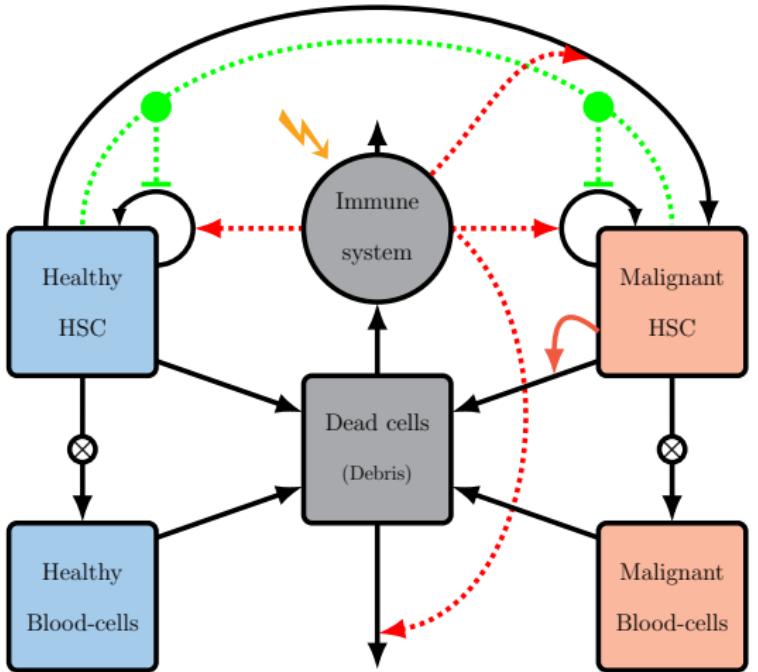
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For details, see chapter 5, figure 5.1 or Andersen et al (2017)

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$$\begin{aligned}\dot{x}_0 &= (r_x \phi_x(x_0, y_0) s - d_{x_0} - a_x) x_0 - r_m s x_0 \\ \dot{y}_0 &= \left( r_y \phi_y(x_0, y_0) s - \hat{d}_{y_0} - \tilde{d}_{y_0} y_0 - a_y \right) y_0 + r_m s x_0 \\ \dot{x}_1 &= a_x A_x x_0 - d_{x_1} x_1 \\ \dot{y}_1 &= a_y A_y y_0 - d_{y_1} y_1 \\ \dot{a} &= d_{x_0} x_0 + d_{x_1} x_1 + \left( \hat{d}_{y_0} + \tilde{d}_{y_0} y_0 \right) y_0 + d_{y_1} y_1 - e_a a s \\ \dot{s} &= r_s a - e_s s + I\end{aligned}$$

where  $\cdot$  denotes the time-derivative. The functions  $\phi_x(x_0, y_0)$  and  $\phi_y(x_0, y_0)$  are defined as:

$$\phi_x(x_0, y_0) = \frac{1}{1 + c_{xx} x_0 + c_{xy} y_0}$$

$$\phi_y(x_0, y_0) = \frac{1}{1 + c_{yx} x_0 + c_{yy} y_0}$$

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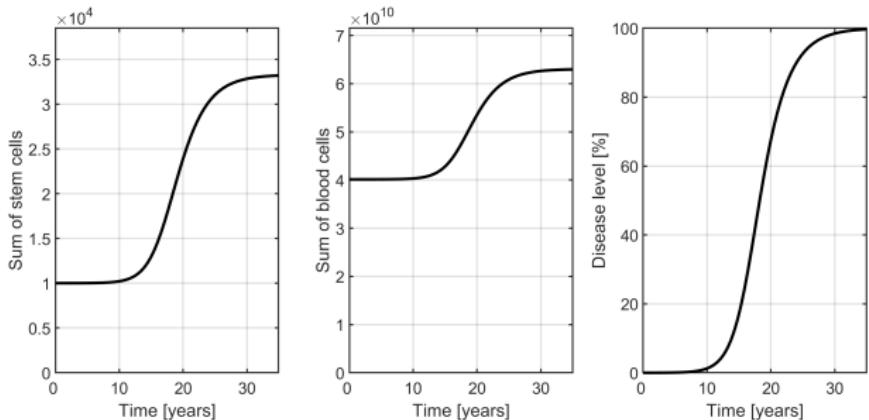
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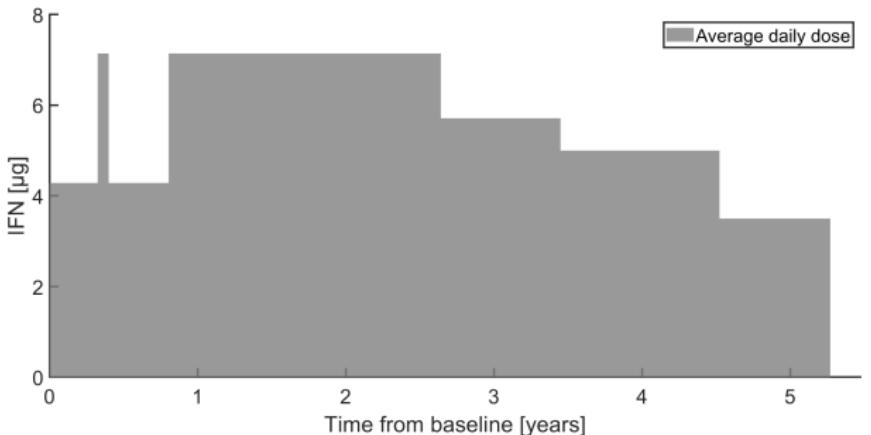
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What happens when the drug is injected?



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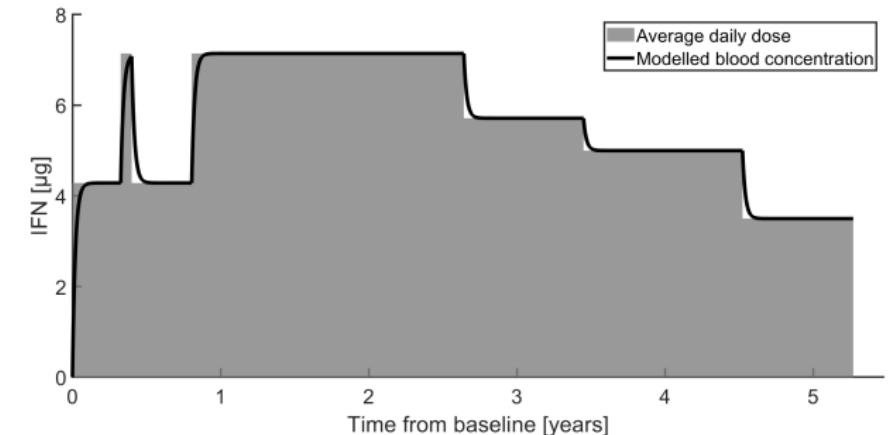
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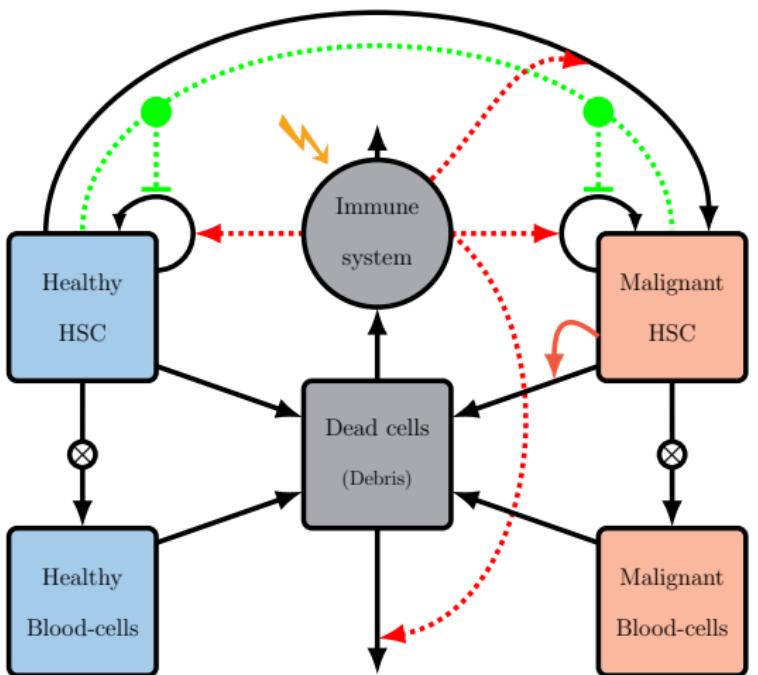
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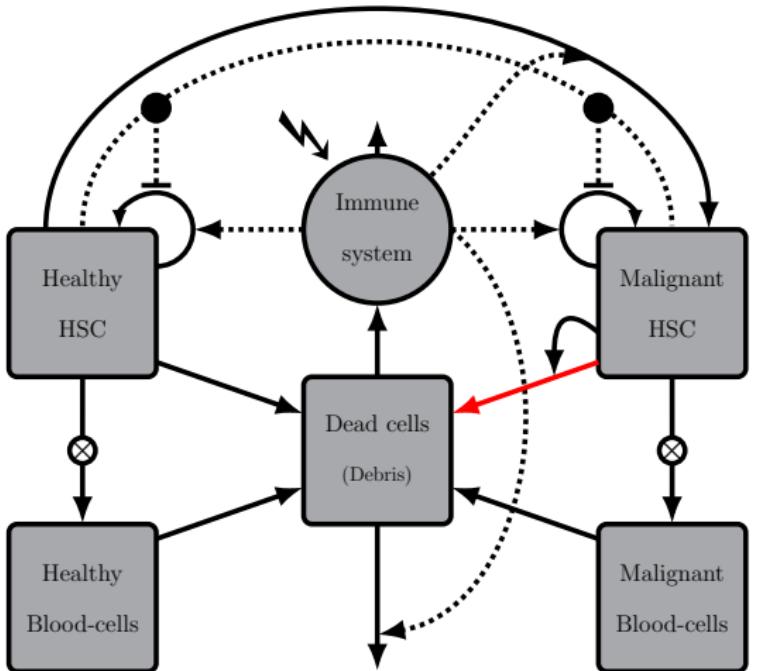
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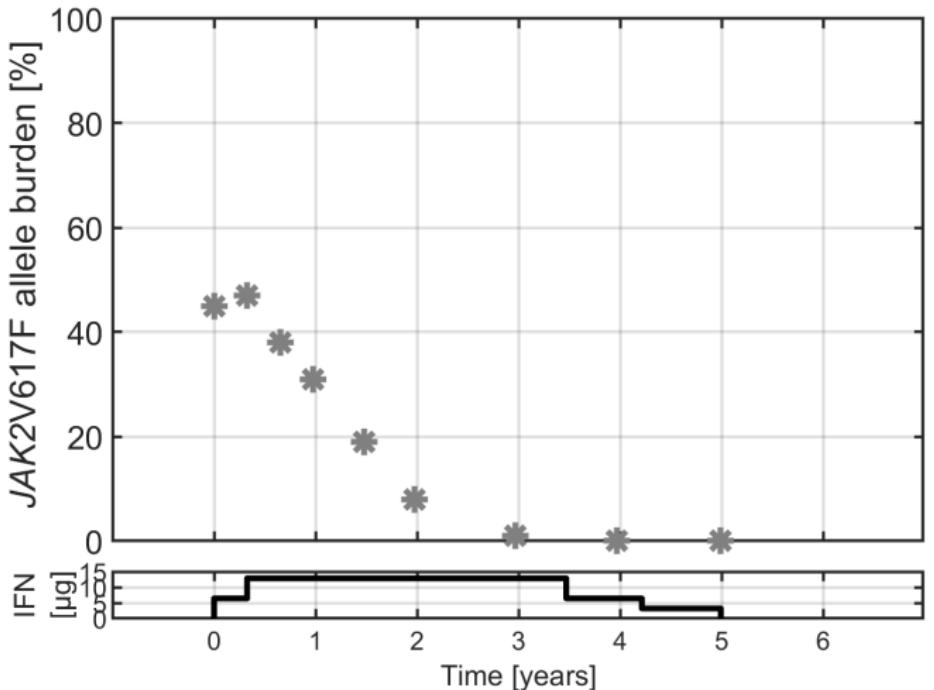
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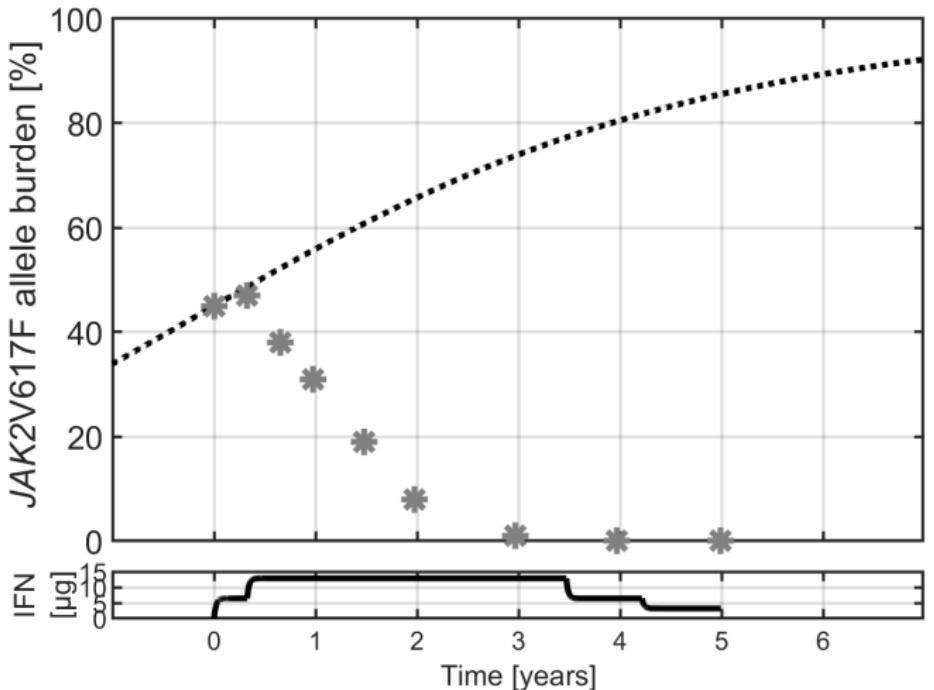
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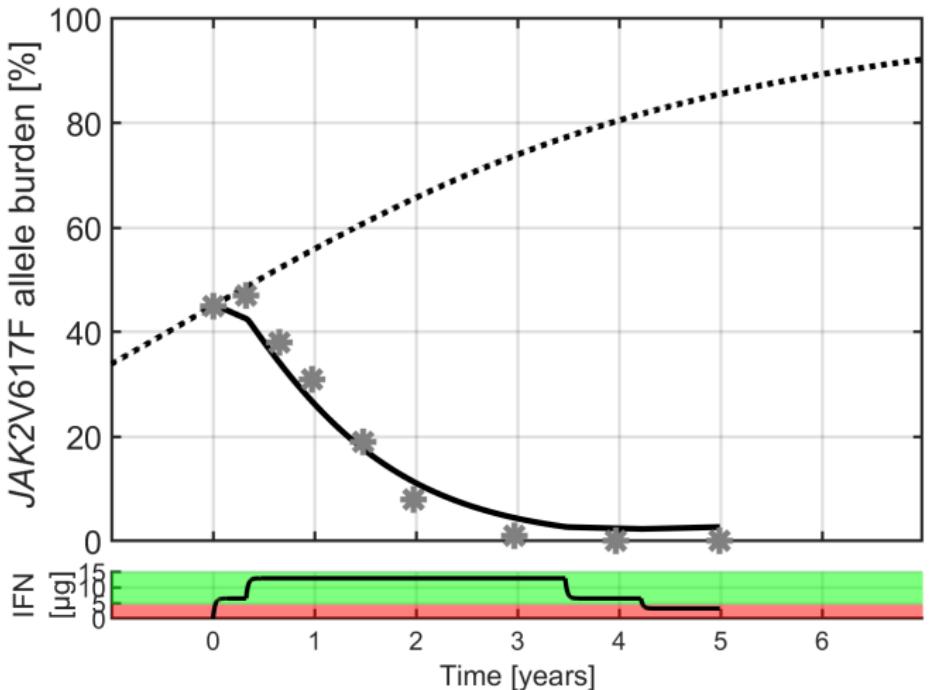
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- ▶ IFN-induced death of malignant stem cells appears a reasonable hypothesis.

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- ▶ IFN-induced death of malignant stem cells appears a reasonable hypothesis.
- ▶ 80% increased death of malignant stem cells causes steady state stability to change, leading to long-term healthy of the patient.

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- ▶ IFN-induced death of malignant stem cells appears a reasonable hypothesis.
- ▶ 80% increased death of malignant stem cells causes steady state stability to change, leading to long-term healthy of the patient.
- ▶ For many of the DALIAH patients, this was attained with  $5\mu\text{g}$  IFN daily ( $35\mu\text{g}$  weekly)

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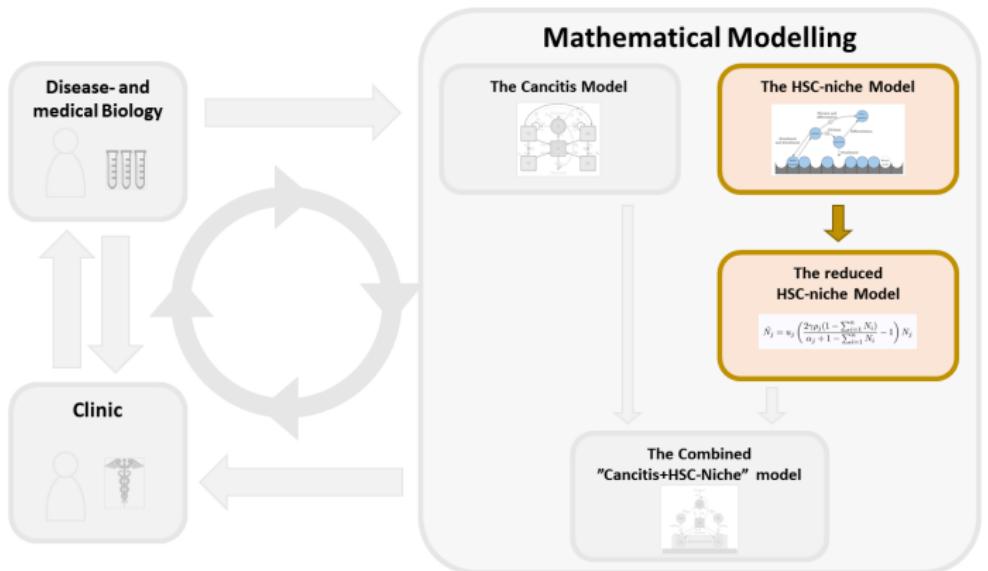
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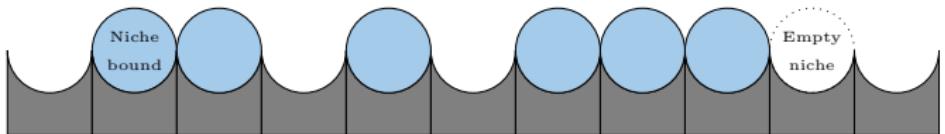
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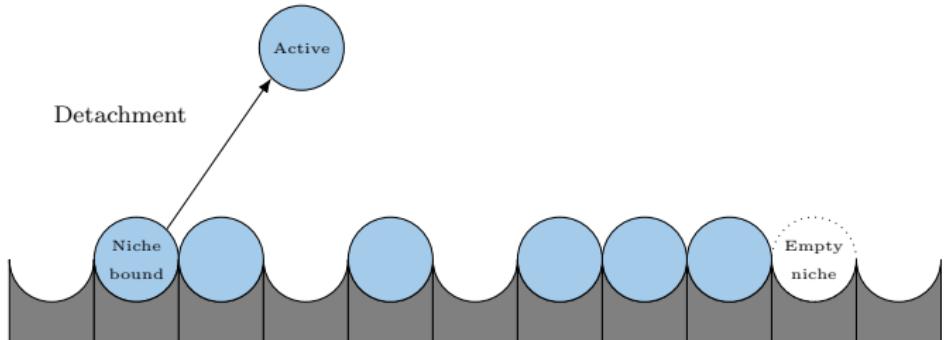
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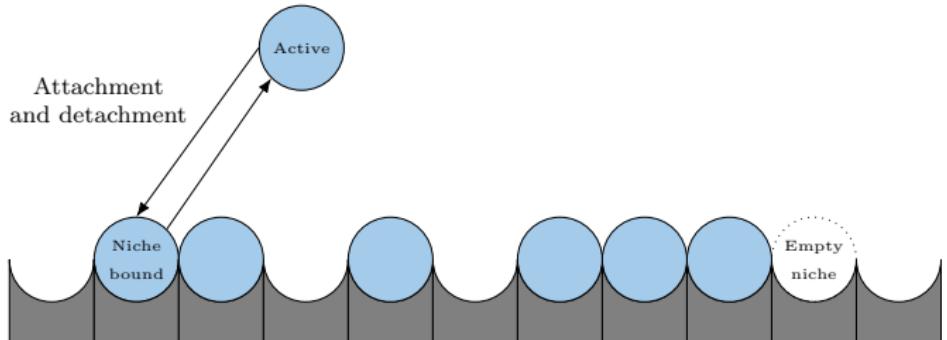
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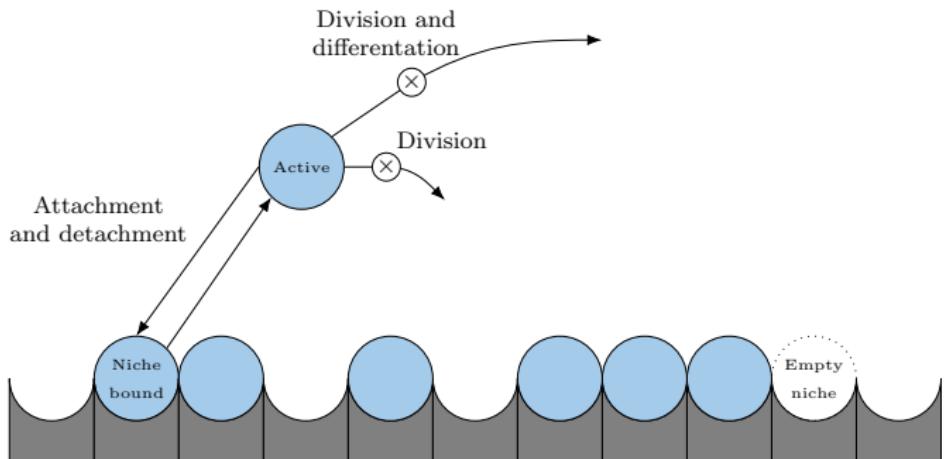
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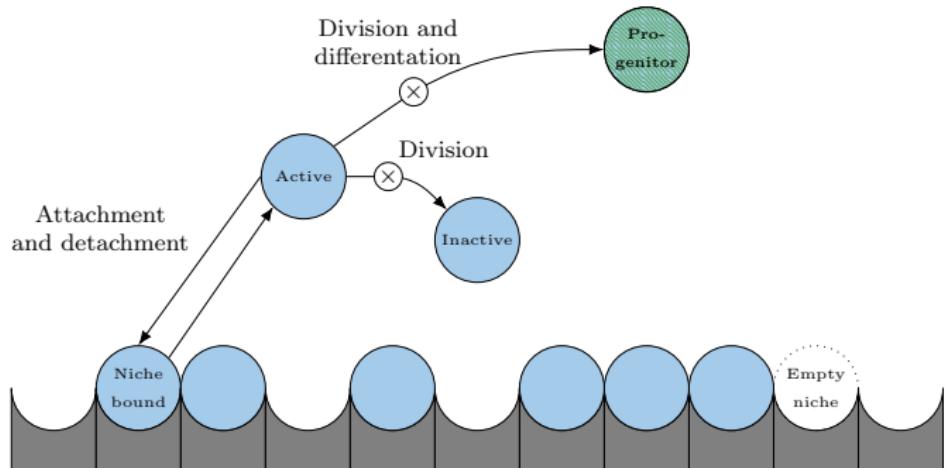
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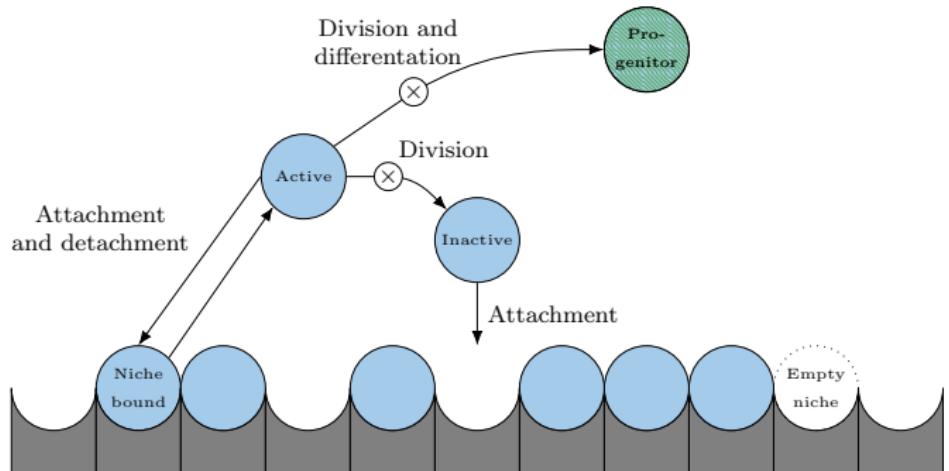
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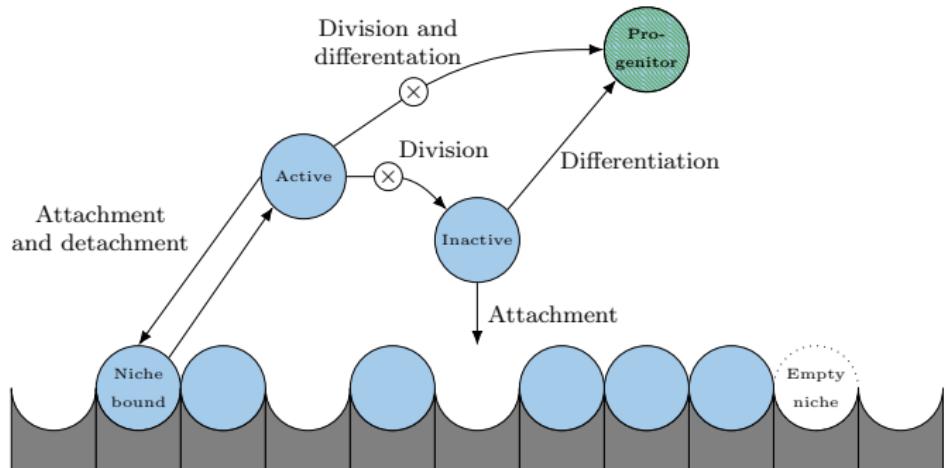
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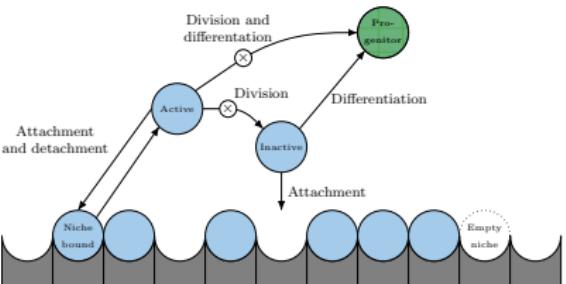
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$$\dot{N} = b_I(K - N)I + b_A(K - N)A - uN$$

$$\dot{I} = 2\gamma rA - b_I(K - N)I - d_I I$$

$$\dot{A} = uN - b_A(K - N)A - rA - d_AA$$

$$N_E = K - N$$

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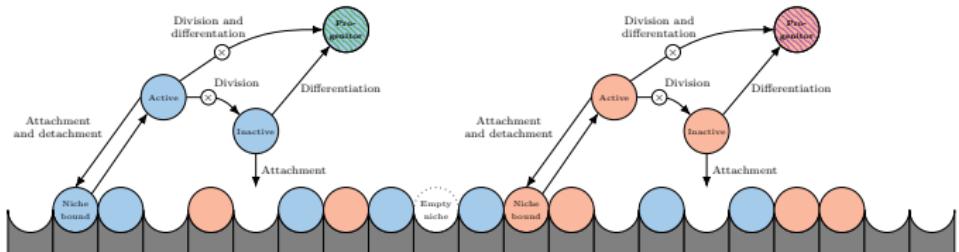
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$$\dot{N}_j = b_{I_j} \left( K - \sum_{i=1}^n N_i \right) I_j + b_{A_j} \left( K - \sum_{i=1}^n N_i \right) A_j - u_j N_j$$

$$\dot{I}_j = 2\gamma r_j A_j - b_{I_j} \left( K - \sum_{i=1}^n N_i \right) I_j - d_{I_j} I_j$$

$$\dot{A}_j = u_j N_j - b_{A_j} \left( K - \sum_{i=1}^n N_i \right) A_j - r_j A_j - d_{A_j} A_j$$

$$N_E = K - \sum_{i=1}^n N_i$$

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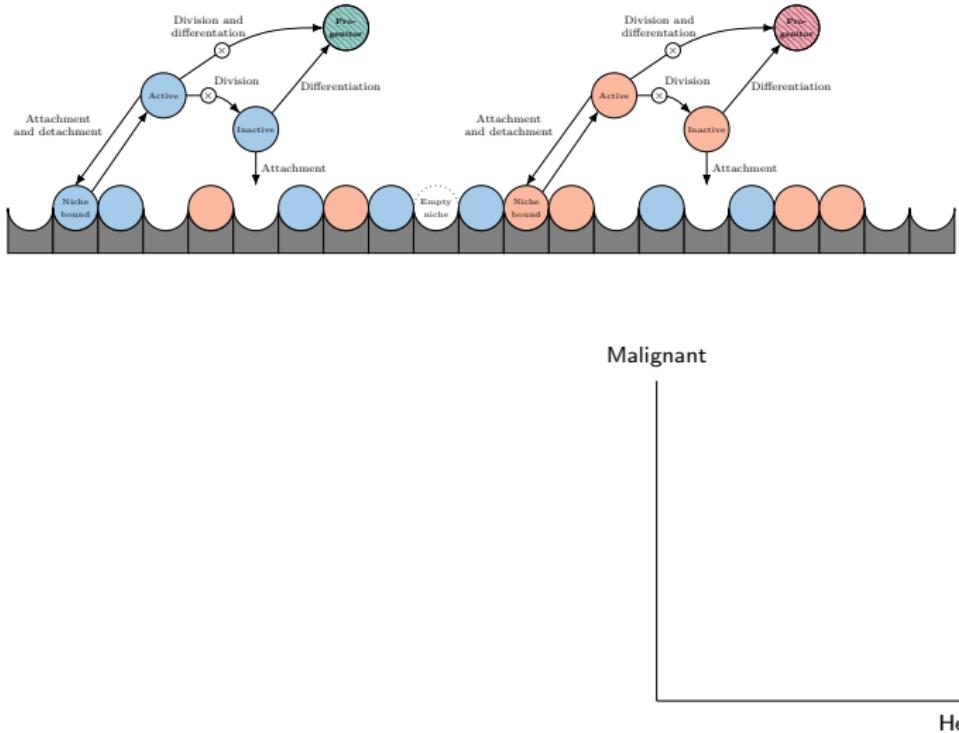
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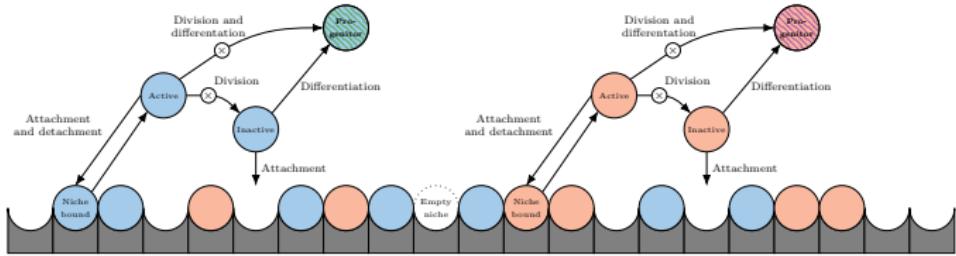
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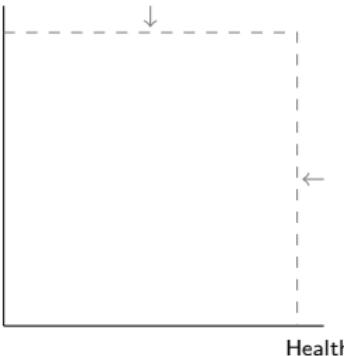
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## ► Attractive trapping region

Malignant



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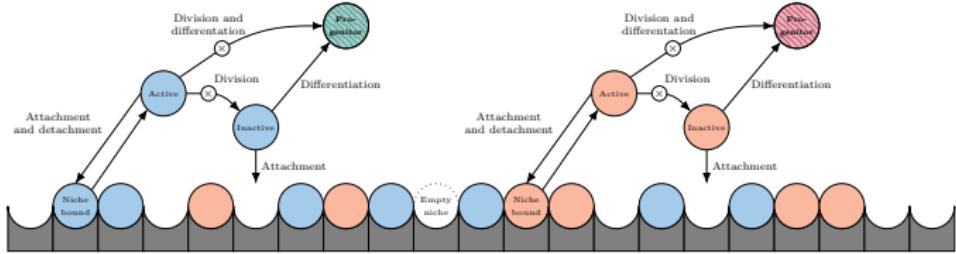
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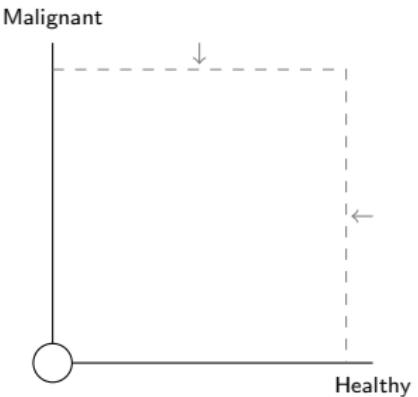
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- ▶ Attractive trapping region
- ▶ Steady states:
  - ▶ No cells (Exhaustion)



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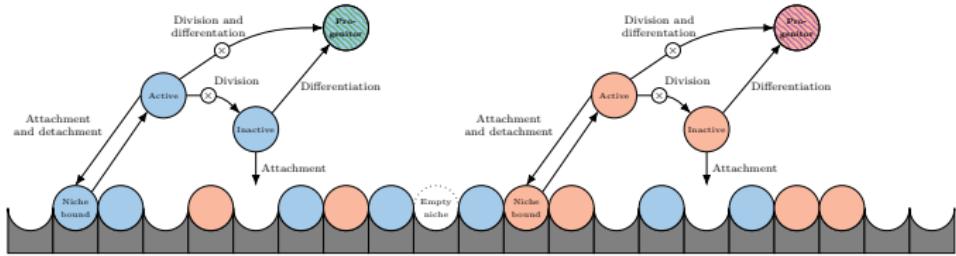
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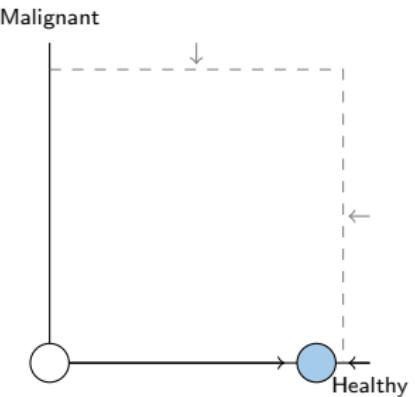
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- ▶ Attractive trapping region
- ▶ Steady states:
  - ▶ No cells (Exhaustion)
  - ▶ Only healthy



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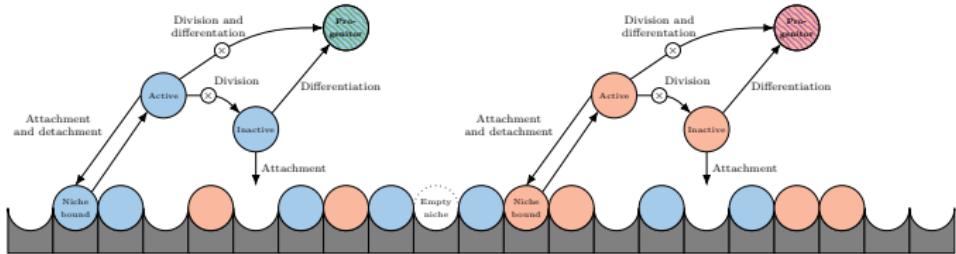
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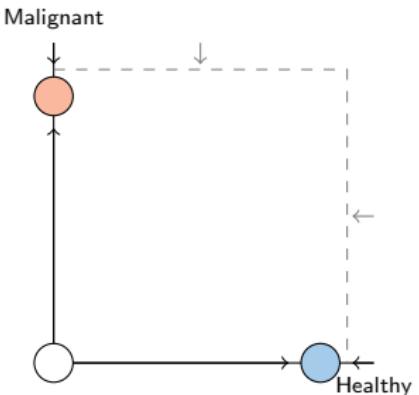
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- ▶ Attractive trapping region
- ▶ Steady states:
  - ▶ No cells (Exhaustion)
  - ▶ Only healthy
  - ▶ Only malignant



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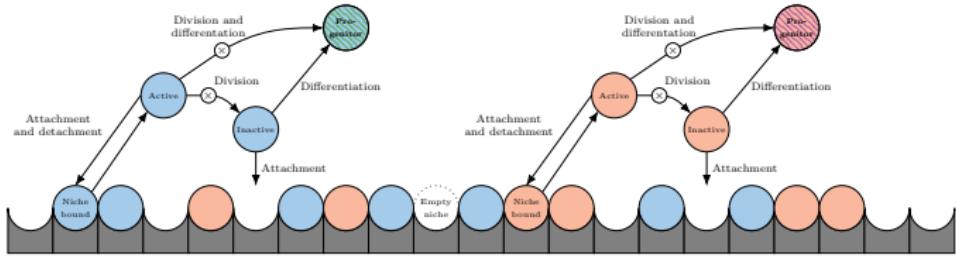
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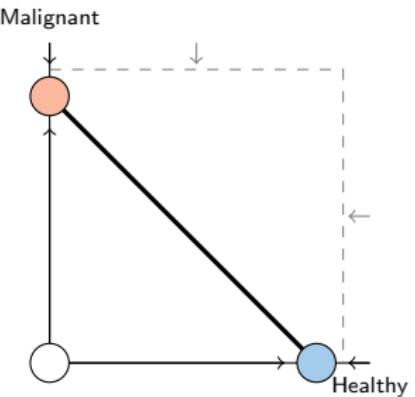
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- ▶ Attractive trapping region
- ▶ Steady states:
  - ▶ No cells (Exhaustion)
  - ▶ Only healthy
  - ▶ Only malignant
  - ▶ Co-existence



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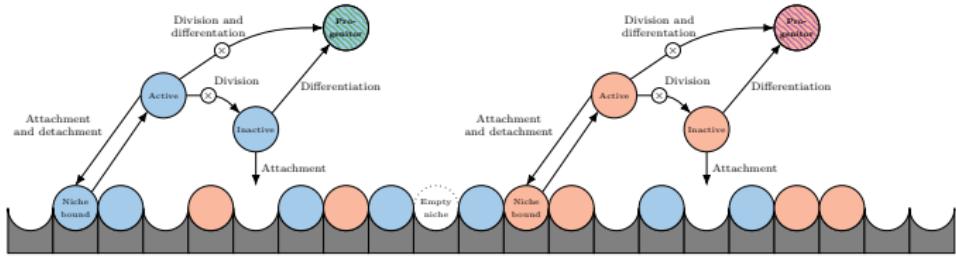
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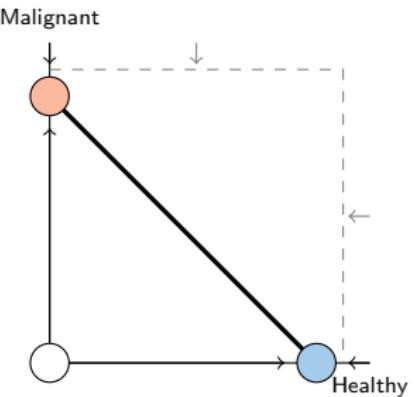
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- ▶ Attractive trapping region
- ▶ Steady states:
  - ▶ No cells (Exhaustion)
  - ▶ Only healthy
  - ▶ Only malignant
  - ▶ Co-existence
- ▶ HSC fitness:

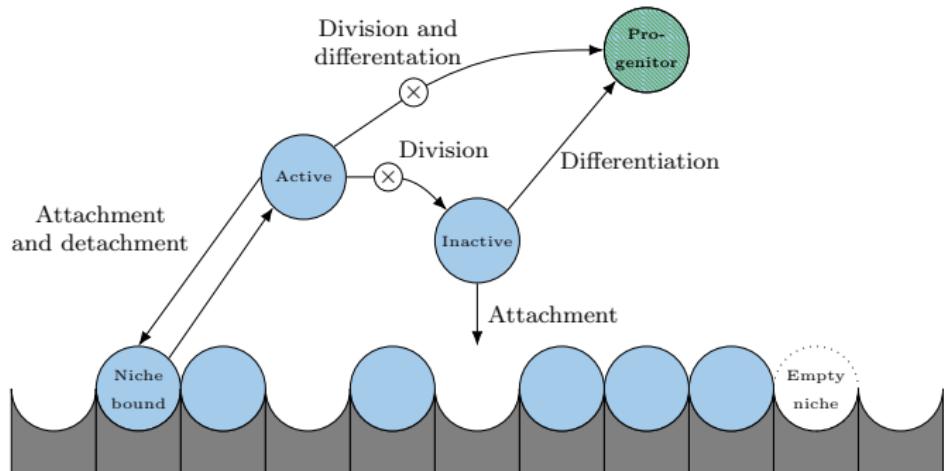
$$F_j = \frac{b_{I_j} ((2\gamma - 1)r_j - d_{A_j})}{d_{I_j}(r_j + d_{A_j})}$$



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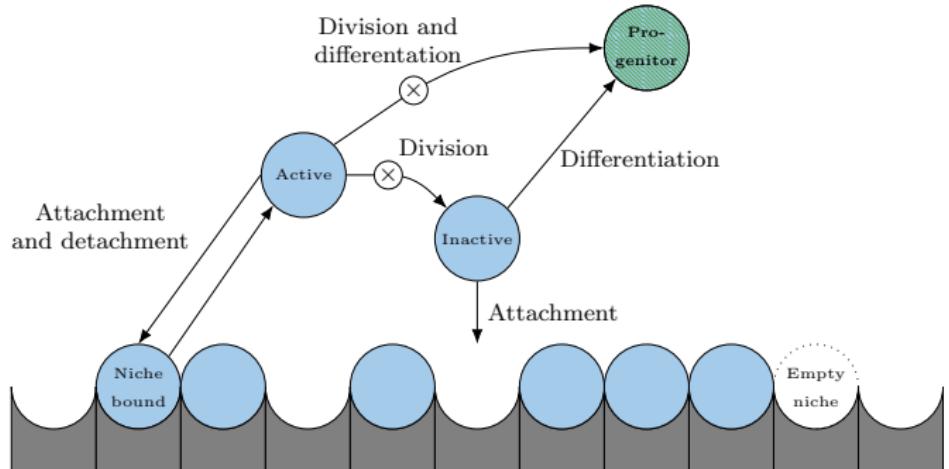
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- ▶ **Assumption** Most HSC niches are occupied

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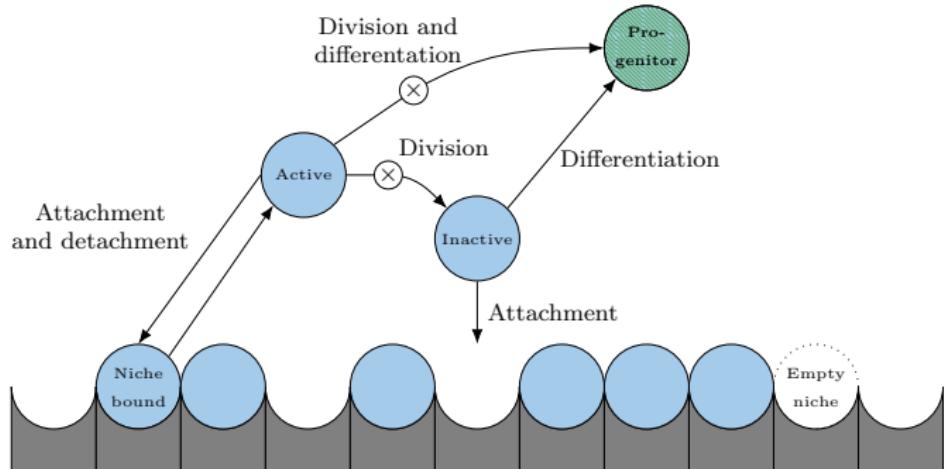
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- ▶ **Assumption** Most HSC niches are occupied
- ▶ **Assumption** Most HSCs are niche-bound

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- ▶ **Assumption** Most HSC niches are occupied
- ▶ **Assumption** Most HSCs are niche-bound

Consequences:

- ▶ No need to keep track of free HSC.

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- ▶ **Assumption** Most HSC niches are occupied
- ▶ **Assumption** Most HSCs are niche-bound

Consequences:

- ▶ No need to keep track of free HSC.
- ▶ Only three parameters per HSC-type:  $\rho$ ,  $\alpha$  and  $u$

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- ▶ **Assumption** Most HSC niches are occupied
- ▶ **Assumption** Most HSCs are niche-bound

Consequences:

- ▶ No need to keep track of free HSC.
- ▶ Only three parameters per HSC-type:  $\rho$ ,  $\alpha$  and  $u$
- ▶

$$\dot{N}_j = u_j \left( \frac{2\gamma\rho_j(1 - \sum_{i=1}^n N_i)}{\alpha_j + 1 - \sum_{i=1}^n N_i} - 1 \right) N_j$$

where  $\rho_j = \frac{r_j}{r_j+d_{A_j}}$  and  $\alpha_j = \frac{d_{I_j}}{b_{I_j}K}$ .

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- ▶ **Assumption** Most HSC niches are occupied
- ▶ **Assumption** Most HSCs are niche-bound

Consequences:

- ▶ No need to keep track of free HSC.
- ▶ Only three parameters per HSC-type:  $\rho$ ,  $\alpha$  and  $u$
- ▶

$$\dot{N}_j = u_j \left( \frac{2\gamma\rho_j(1 - \sum_{i=1}^n N_i)}{\alpha_j + 1 - \sum_{i=1}^n N_i} - 1 \right) N_j$$

where  $\rho_j = \frac{r_j}{r_j+d_{A_j}}$  and  $\alpha_j = \frac{d_{I_j}}{b_{I_j}K}$ .

- ▶ Only minor changes to dynamics.

# The HSC niche Model, reduction

MM of MPNs and  
HSC

- ▶ **Assumption** Most HSC niches are occupied
- ▶ **Assumption** Most HSCs are niche-bound

Consequences:

- ▶ No need to keep track of free HSC.
- ▶ Only three parameters per HSC-type:  $\rho$ ,  $\alpha$  and  $u$
- ▶

$$\dot{N}_j = u_j \left( \frac{2\gamma\rho_j(1 - \sum_{i=1}^n N_i)}{\alpha_j + 1 - \sum_{i=1}^n N_i} - 1 \right) N_j$$

where  $\rho_j = \frac{r_j}{r_j+d_{A_j}}$  and  $\alpha_j = \frac{d_{I_j}}{b_{I_j}K}$ .

- ▶ Only minor changes to dynamics.
- ▶ Importantly, concept of HSC fitness still exists:

$$f_j = \frac{2\gamma\rho_j - 1}{\alpha_j}$$

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If there are only two types of HSC, and they are very similar ( $f_1 \approx f_2$ ), we can reduce further.

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If there are only two types of HSC, and they are very similar ( $f_1 \approx f_2$ ), we can reduce further.

$$\dot{C} = \phi(1 - C)C \quad (1)$$

$$\text{where } \phi = g_2(T_1^*) = u_2 \frac{\alpha_2}{\alpha_2 + f_1^{-1}} \left( \frac{f_2}{f_1} - 1 \right).$$

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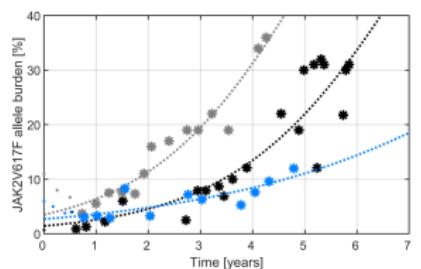
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(a)

$$\phi > 0$$

$$f_1 < f_2$$

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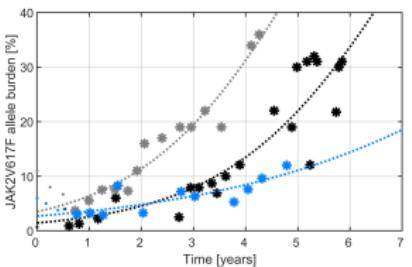
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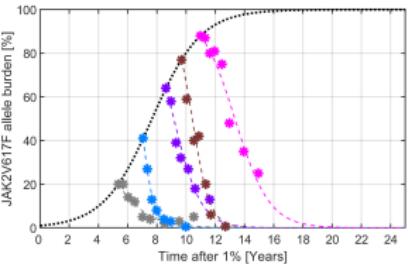
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(a)

$$\phi > 0$$

$$f_1 < f_2$$



(b)

$$\phi < 0$$

$$f_1 > f_2$$

# The HSC niche model, summing it up

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- ▶ A detailed description of an experimentally inaccessible system

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- ▶ A detailed description of an experimentally inaccessible system
- ▶ A notion of HSC fitness naturally arises

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- ▶ A detailed description of an experimentally inaccessible system
- ▶ A notion of HSC fitness naturally arises
- ▶ Biologically-grounded simplifications results in a simple logistic expression.

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- ▶ A detailed description of an experimentally inaccessible system
- ▶ A notion of HSC fitness naturally arises
- ▶ Biologically-grounded simplifications results in a simple logistic expression.

*Similar to the empirical modelling of the DALIAH trial data!*

# The HSC niche model, summing it up

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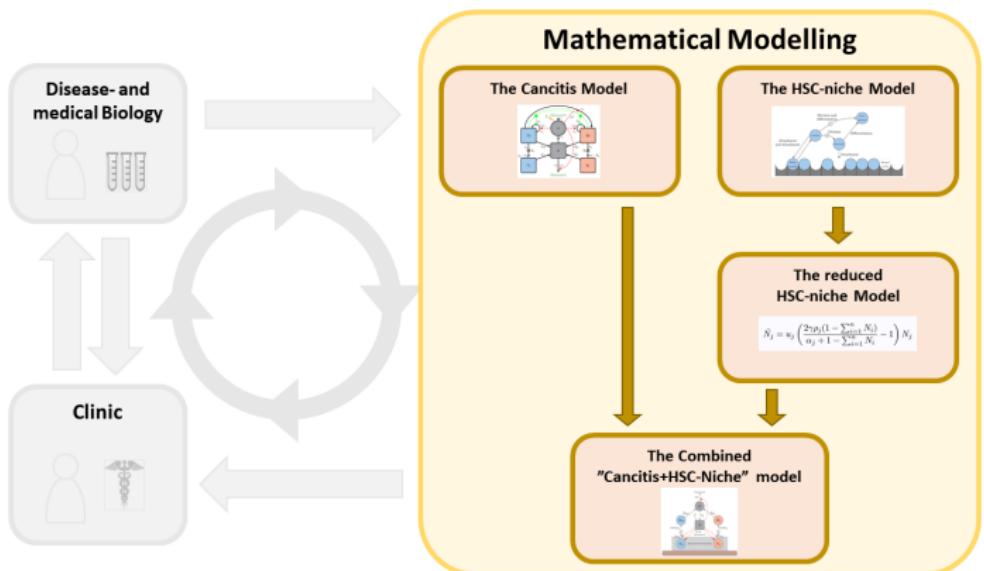
- ▶ A detailed description of an experimentally inaccessible system
- ▶ A notion of HSC fitness naturally arises
- ▶ Biologically-grounded simplifications results in a simple logistic expression.

*Similar to the empirical modelling of the DALIAH trial data!*

- ▶ Possible explanation for *why* data looks the way it does

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# The combined model



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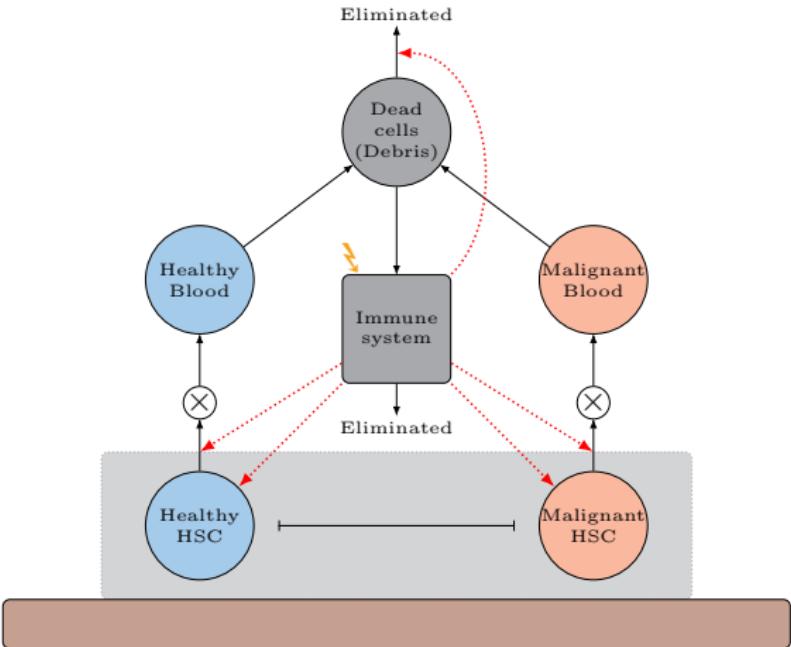
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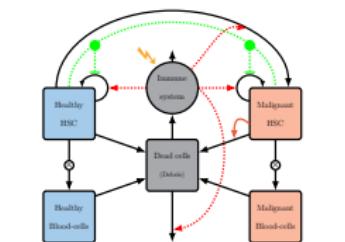
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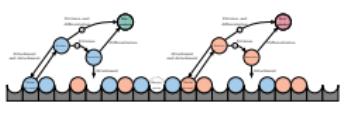
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$$\begin{aligned}\dot{x}_0 &= (r_x \phi_x(x_0, y_0)s - d_{x_0} - a_x)x_0 - r_m s x_0 \\ \dot{y}_0 &= (r_y \phi_y(x_0, y_0)s - \hat{d}_{y_0} - \tilde{d}_{y_0} y_0 - a_y)y_0 + r_m s x_0 \\ \dot{x}_1 &= a_x A_x x_0 - d_{x_1} x_1 \\ \dot{y}_1 &= a_y A_y y_0 - d_{y_1} y_1 \\ \dot{a} &= d_{x_0} x_0 + d_{x_1} x_1 + (\hat{d}_{y_0} + \tilde{d}_{y_0} y_0)y_0 + d_{y_1} y_1 - e_a a s \\ \dot{s} &= r_s a - e_s s + l\end{aligned}$$



$$\begin{aligned}\dot{N}_H &= u_H \left( \frac{2\gamma\rho_H(1 - N_H - N_L)}{\alpha_H + 1 - N_H - N_L} - 1 \right) N_H \\ \dot{N}_L &= u_L \left( \frac{2\gamma\rho_L(1 - N_H - N_L)}{\alpha_L + 1 - N_H - N_L} - 1 \right) N_L\end{aligned}$$

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$$\dot{N}_H = u_H S \left( \frac{2\gamma\rho_H (1 - N_H - N_L)}{\alpha_H + 1 - N_H - N_L} - 1 \right) N_H$$

$$\dot{N}_L = u_L S \left( \frac{2\gamma\rho_L (1 - N_H - N_L)}{\alpha_L + 1 - N_H - N_L} - 1 \right) N_L$$

$$\dot{M}_H = \omega_H i_{D_H} S - d_{M_H} M_H$$

$$\dot{M}_L = \omega_L i_{D_L} S - d_{M_L} M_L$$

$$\dot{D} = d_{M_H} M_H + d_{M_L} M_L - e_D D S$$

$$\dot{S} = r_S D - e_S S + I$$

Purple: Cancitis model, green: HSC-Niche model

# The combined Cancitis-niche Model

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$$\begin{aligned}\dot{N}_H &= u_H S \left( \frac{2\gamma\rho_H(1 - N_H - N_L)}{\alpha_H + 1 - N_H - N_L} - 1 \right) N_H \\ \dot{N}_L &= u_L S \left( \frac{2\gamma\rho_L(1 - N_H - N_L)}{\alpha_L + 1 - N_H - N_L} - 1 \right) N_L \\ \dot{M}_H &= \omega_H i_{D_H} S - d_{M_H} M_H \\ \dot{M}_L &= \omega_L i_{D_L} S - d_{M_L} M_L \\ \dot{D} &= d_{M_H} M_H + d_{M_L} M_L - e_D D S \\ \dot{S} &= r_S D - e_S S + I\end{aligned}$$

where  $i_{D_j} = \left( 2 - 2\rho_j + \frac{2\gamma\alpha_j\rho_j}{\alpha_j + 1 - N_H - N_L} \right) u_j K N_j$ . All parameters are non-negative. In addition,  $\rho_j \leq 1$  and  $\gamma \geq 1$ .

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MM of MPNs and HSC

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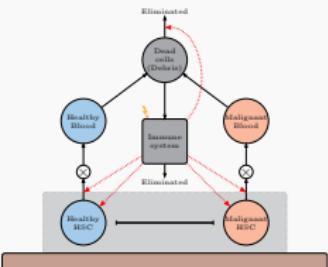
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- Feedback from blood to the HSC system: Increases HSC activation

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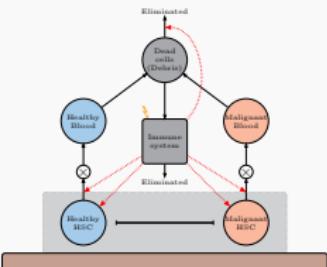
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- ▶ Feedback from blood to the HSC system: Increases HSC activation
- ▶ A refined description of HSC behaviour

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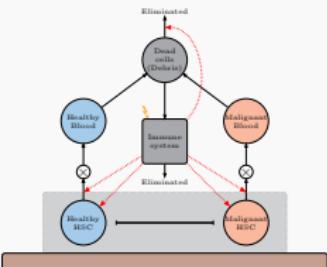
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- ▶ Feedback from blood to the HSC system: Increases HSC activation
- ▶ A refined description of HSC behaviour
- ▶ Same steady states as HSC niche model

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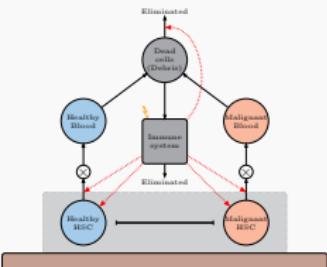
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- ▶ Feedback from blood to the HSC system: Increases HSC activation
- ▶ A refined description of HSC behaviour
- ▶ Same steady states as HSC niche model
  - ▶ No cells

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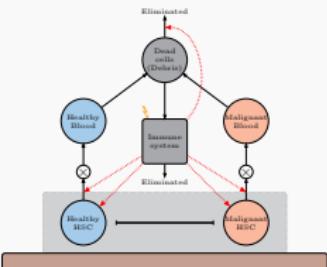
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- ▶ Feedback from blood to the HSC system: Increases HSC activation
- ▶ A refined description of HSC behaviour
- ▶ Same steady states as HSC niche model
  - ▶ No cells
  - ▶ Single-type steady state

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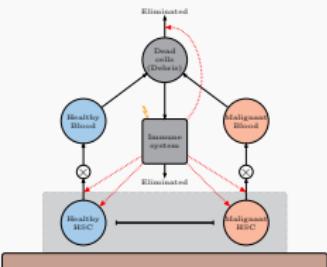
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- ▶ Feedback from blood to the HSC system: Increases HSC activation
- ▶ A refined description of HSC behaviour
- ▶ Same steady states as HSC niche model
  - ▶ No cells
  - ▶ Single-type steady state
  - ▶ Co-existence steady state

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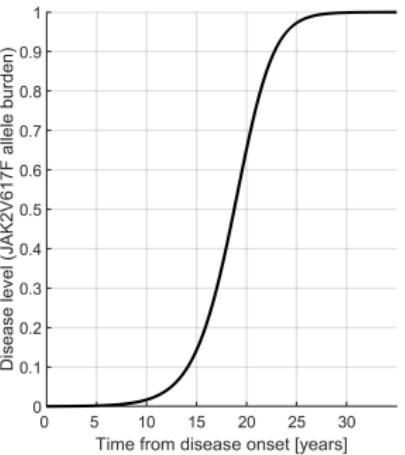
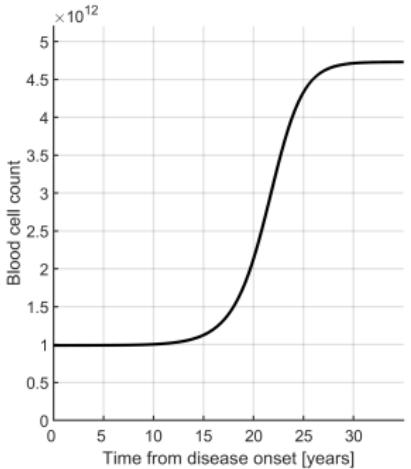
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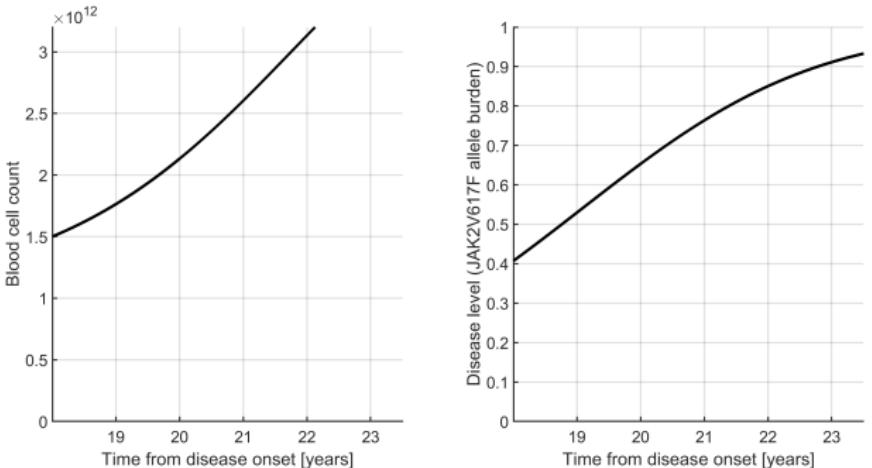
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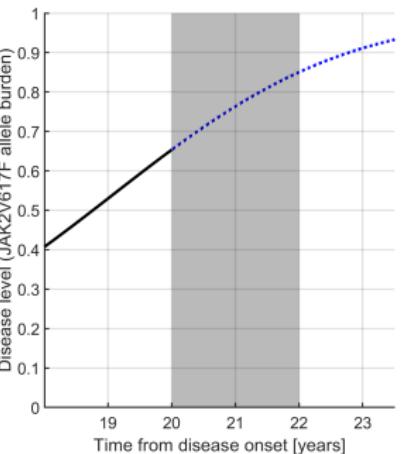
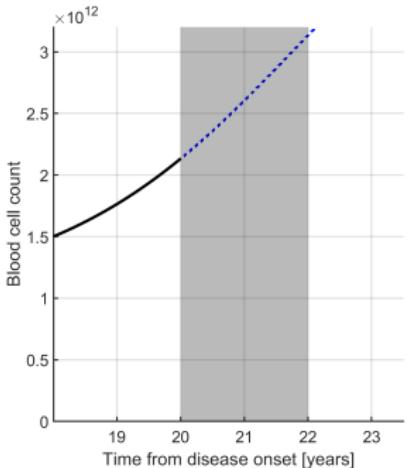
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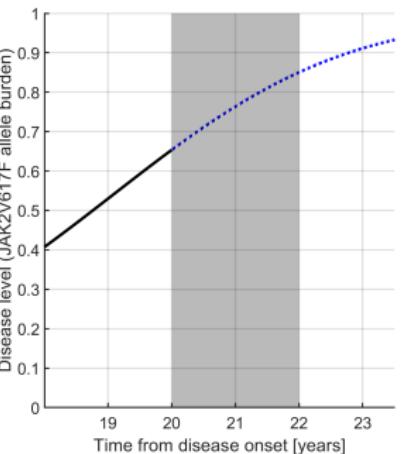
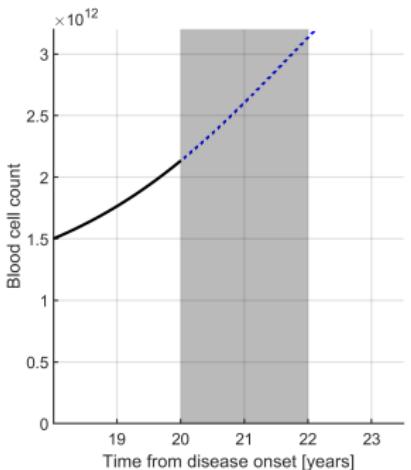
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(For the Cancitis model: Death of HSC)

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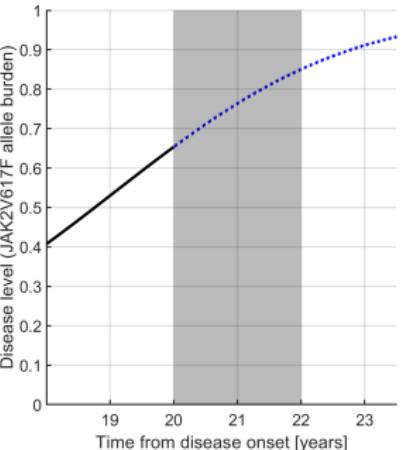
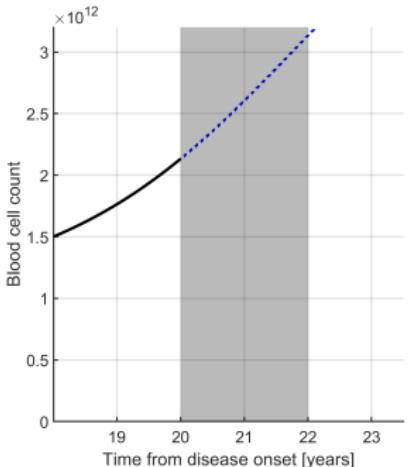
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For the combined model:

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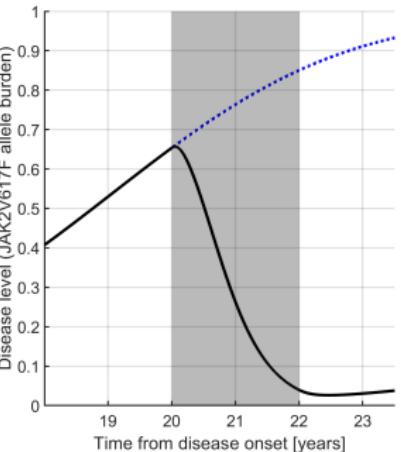
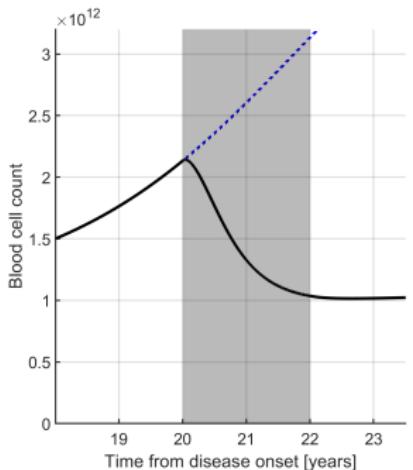
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For the combined model:

- Decreased self-renewal of mutated cells,  $\rho_L$

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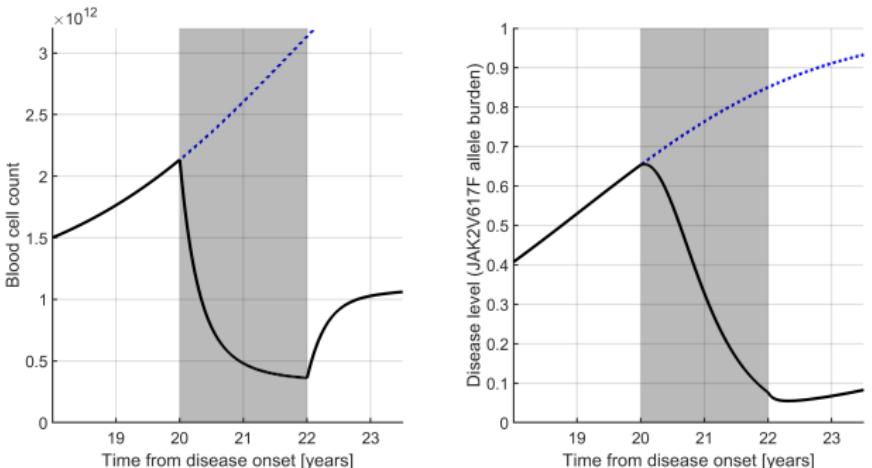
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For the combined model:

- Decreased self-renewal of mutated cells,  $\rho_L$
- Death of all actively dividing cells,  $\omega_H$  and  $\omega_L$

# Fitting the combined model to patient data

MM of MPNs and HSC

Rasmus Kristoffer Pedersen

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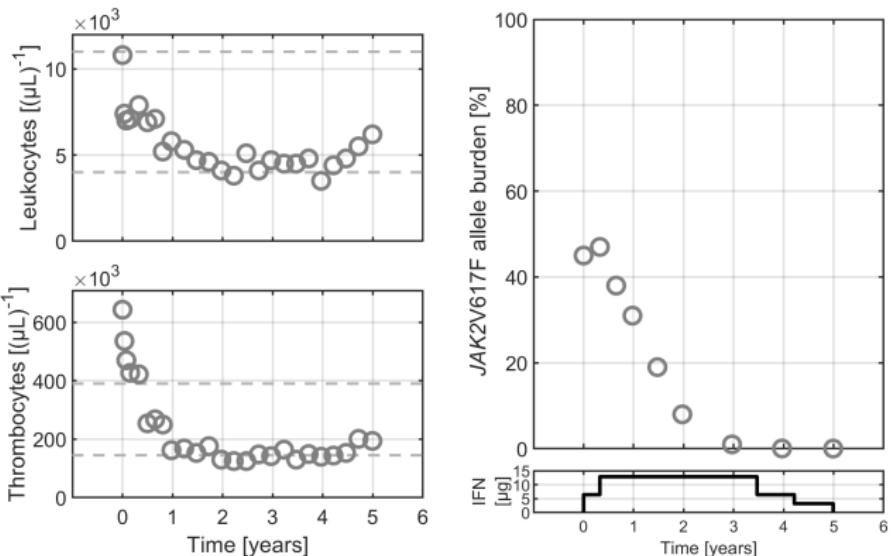
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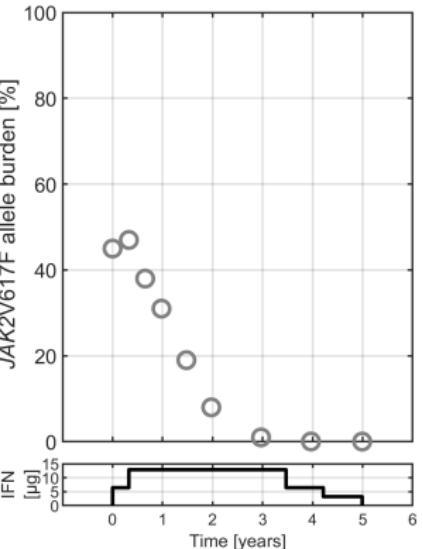
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Patient P198, Raw data



# Fitting the combined model to patient data

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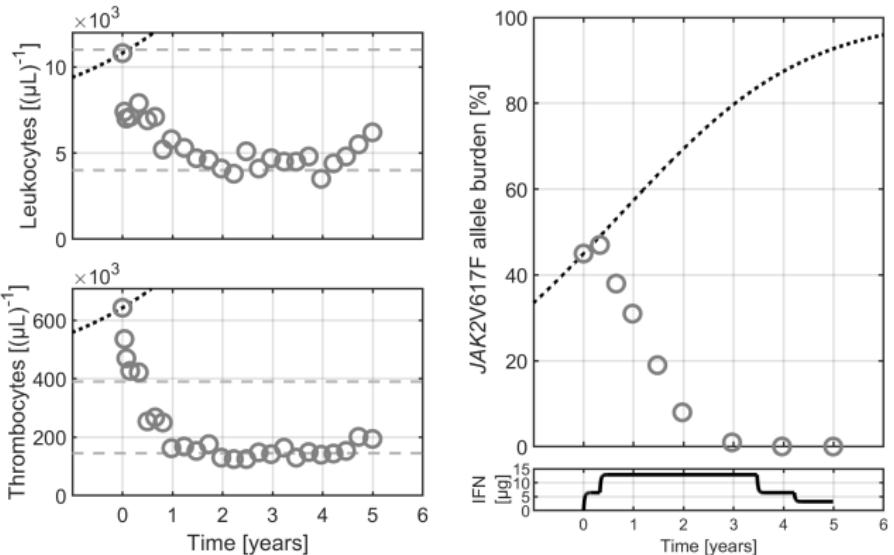
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Patient P198, Data, Growth and PK/PD-modelling

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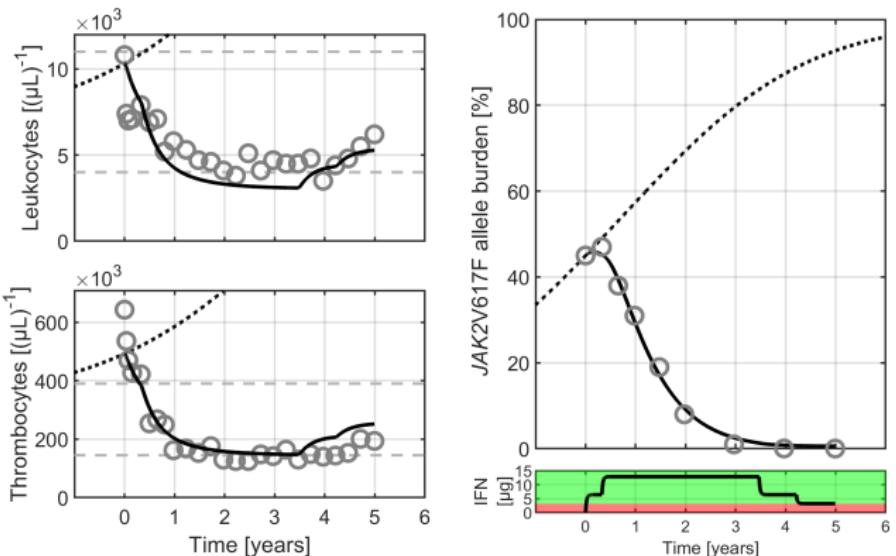
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Patient P198, IFN-dose dependent fitting of model-parameters

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Population modelling!

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Then what?

Population modelling!

Goal: To describe the effect of IFN on a population level, so expected outcome of treatment can be predicted (with estimated uncertainties of prediction)

# Proof-of-concept population modelling

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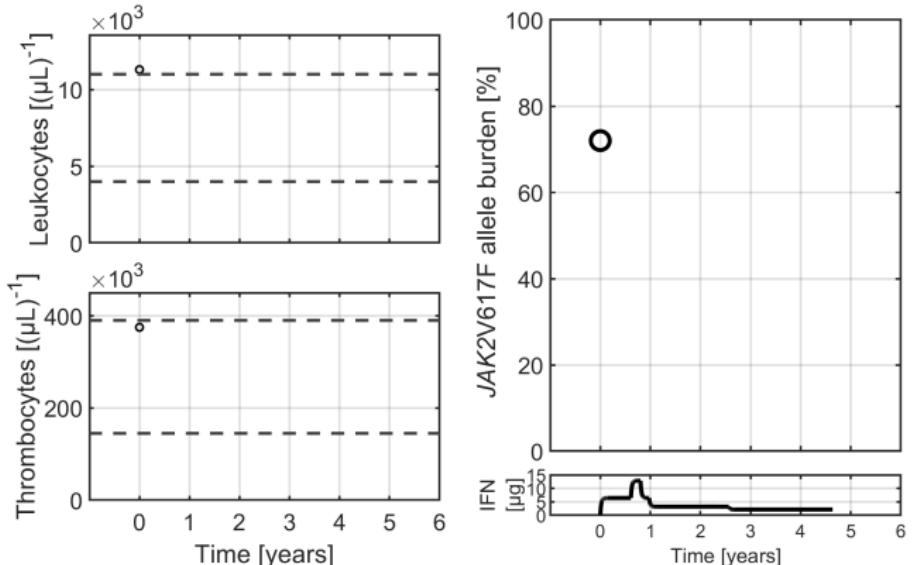
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Patient P082

# Proof-of-concept population modelling

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Rasmus Kristoffer Pedersen

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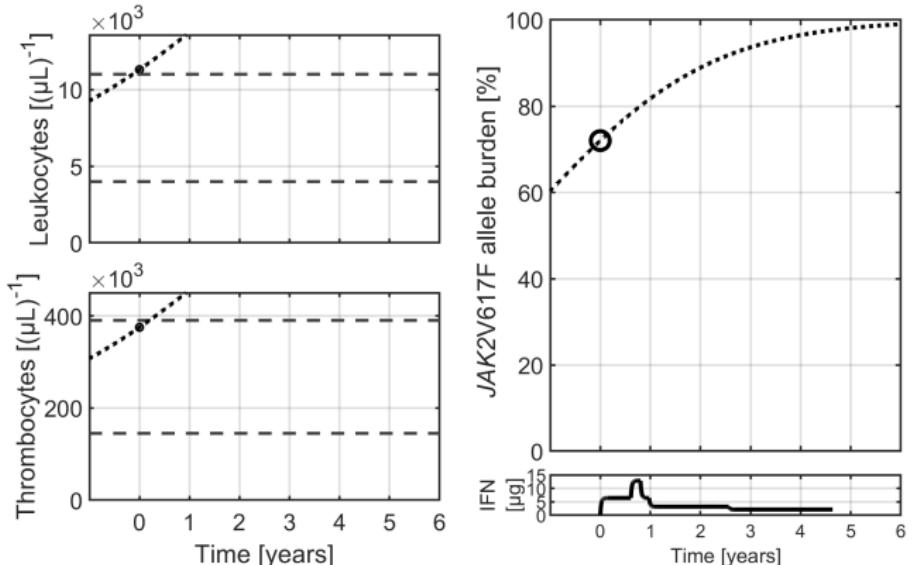
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Patient P082

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Rasmus Kristoffer Pedersen

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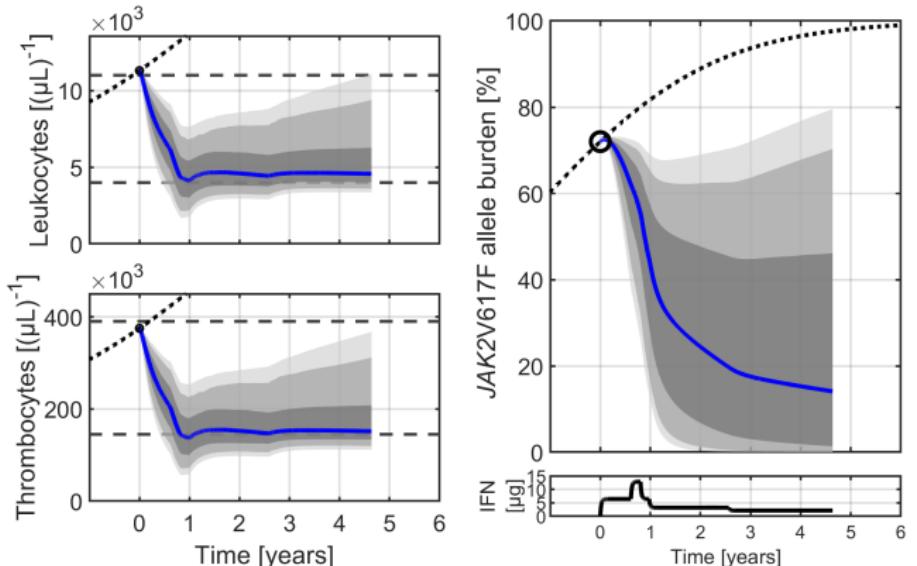
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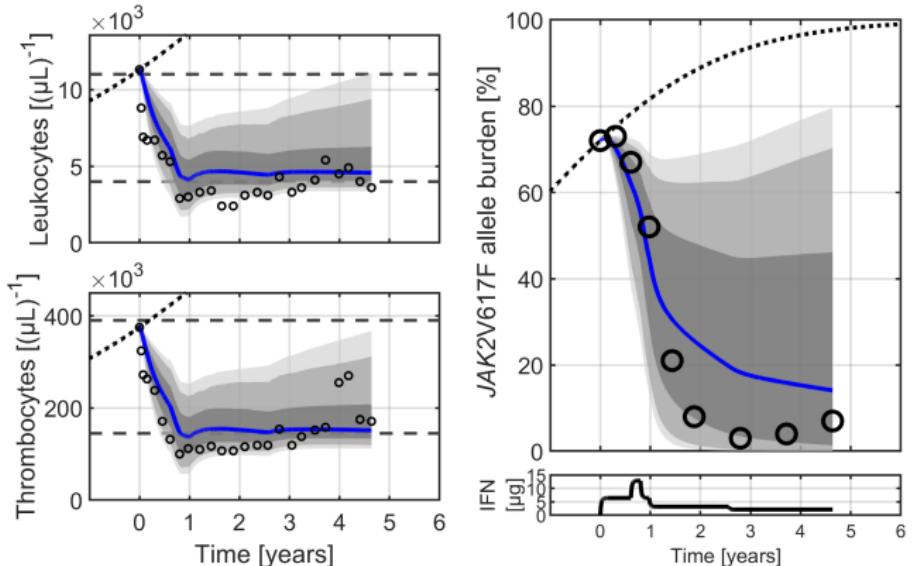
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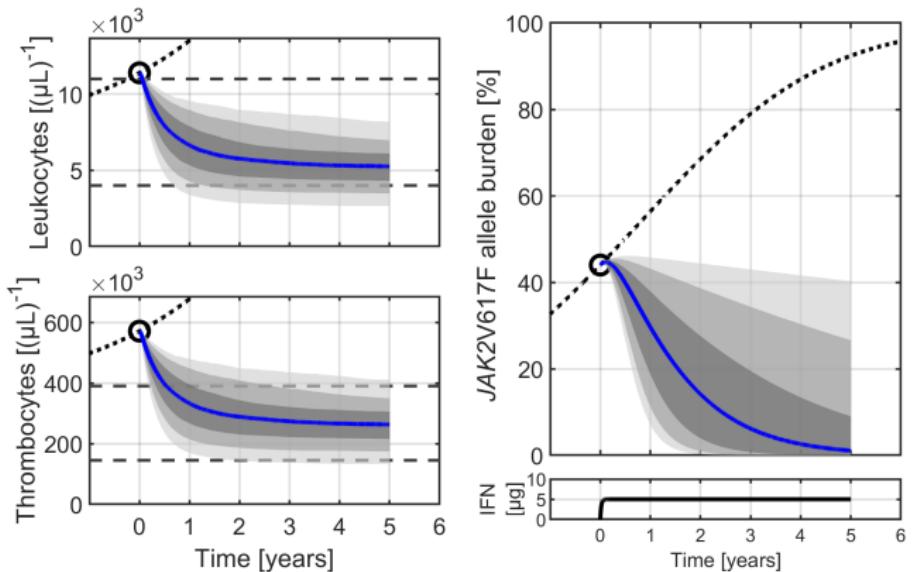
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# Proof-of-concept population modelling

MM of MPNs and HSC

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## A hypothetical “typical PV-diagnosed patient”



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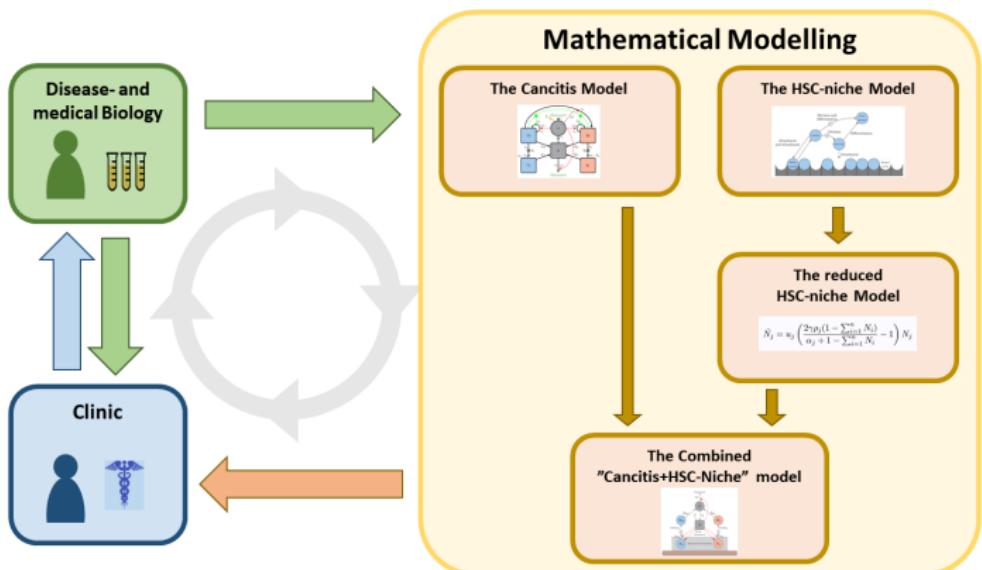
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Through mathematical modelling we have come up with:

- ▶ Hypotheses about the behaviour of HSC.

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Through mathematical modelling we have come up with:

- ▶ Hypotheses about the behaviour of HSC.
- ▶ Numerical estimates of efficient HSC treatment requires.

# Summing it up

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Through mathematical modelling we have come up with:

- ▶ Hypotheses about the behaviour of HSC.
- ▶ Numerical estimates of efficient HSC treatment requires.
- ▶ Biological interpretation of the effect of IFN, on a personalized level.

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Through mathematical modelling we have come up with:

- ▶ Hypotheses about the behaviour of HSC.
- ▶ Numerical estimates of efficient HSC treatment requires.
- ▶ Biological interpretation of the effect of IFN, on a personalized level.
- ▶ Population-level predictions about the expected response of newly diagnosed MPN patients.

# Where to go from here?

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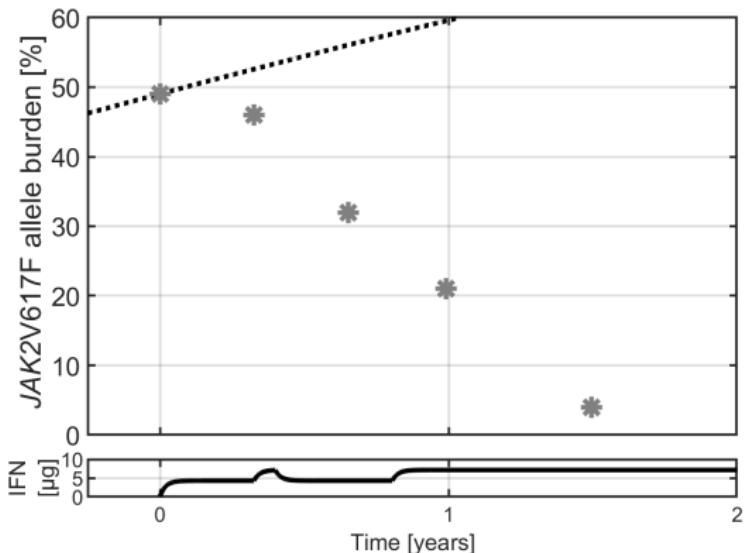
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- ▶ Additional model-validation and data-collection.

# Where to go from here?

- Additional model-validation and data-collection.  
*Particularly for the first year of treatment.*



Patient P002

MM of MPNs and HSC

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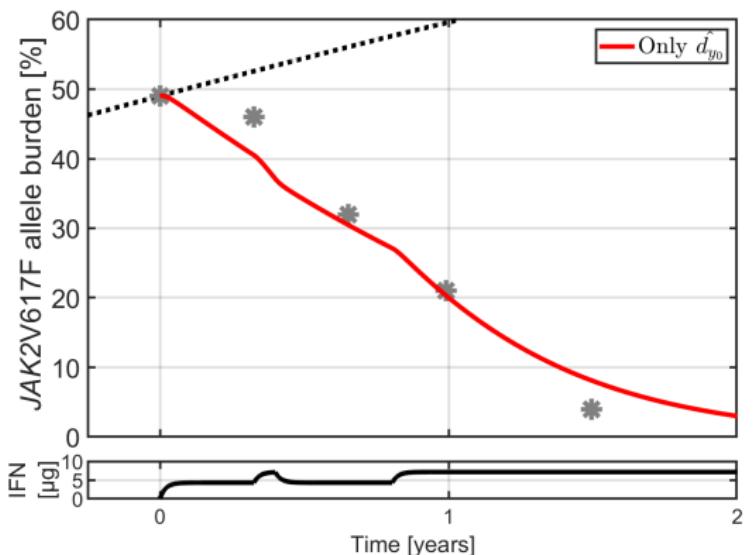
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# Where to go from here?

- Additional model-validation and data-collection.  
*Particularly for the first year of treatment.*



Patient P002

MM of MPNs and HSC

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- ▶ Additional model-validation and data-collection.
- ▶ Improved identification/stratification of patient sub-diagnoses.

# Where to go from here?

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- ▶ Additional model-validation and data-collection.
- ▶ Improved identification/stratification of patient sub-diagnoses.
- ▶ Consideration of other drugs (HU, Ruxo, Jakavi, Statins, etc.), and combination treatment.

# Where to go from here?

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- ▶ Additional model-validation and data-collection.
- ▶ Improved identification/stratification of patient sub-diagnoses.
- ▶ Consideration of other drugs (HU, Ruxo, Jakavi, Statins, etc.), and combination treatment.
- ▶ Including additional available data (Cytokine-level, smoking, age, etc.)

# Personalized Mathematical Modelling?

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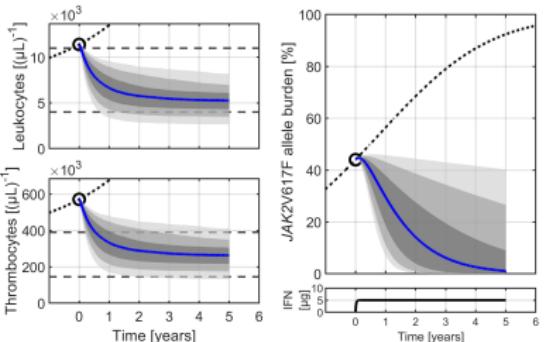
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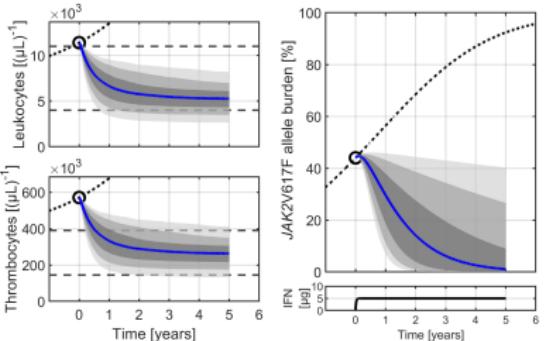
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Is mathematical modelling the primary clinical tool of tomorrow?



*“Completely irresponsible to let mathematical models make decisions...”*

# Personalized Mathematical Modelling?

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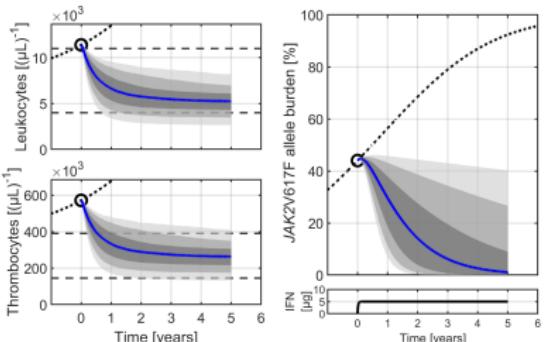
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Is mathematical modelling the primary clinical tool of tomorrow?



*“Completely irresponsible to let mathematical models make decisions, but even worse to ignore them”*  
- Johnny T. Ottesen

# Thank you for your time and attention!

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# Thank you for your time and attention!

And a big thanks to supervisors and collaborators:

- ▶ Johnny Ottesen, Morten Andersen and Hans Hasselbalch
- ▶ Thomas Stiehl
- ▶ Johanne Gudmand-Høyer, Zamra Sajid and Marc Dam
- ▶ Vibe Skov, Lasse Kjær and Trine Knudsen

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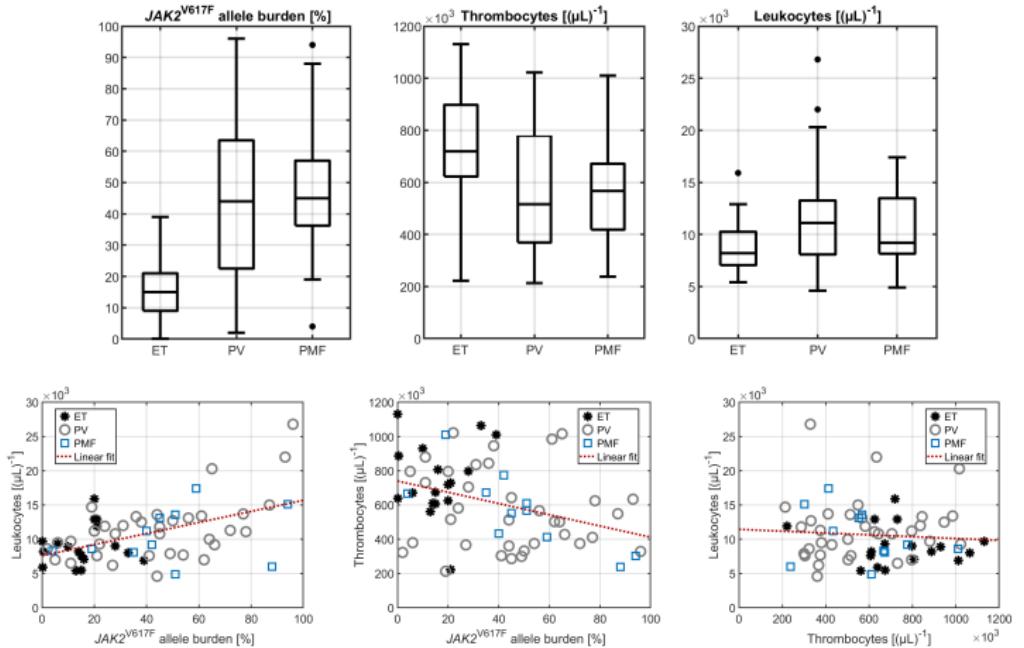
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# The framework of Brady & Enderling (2019)

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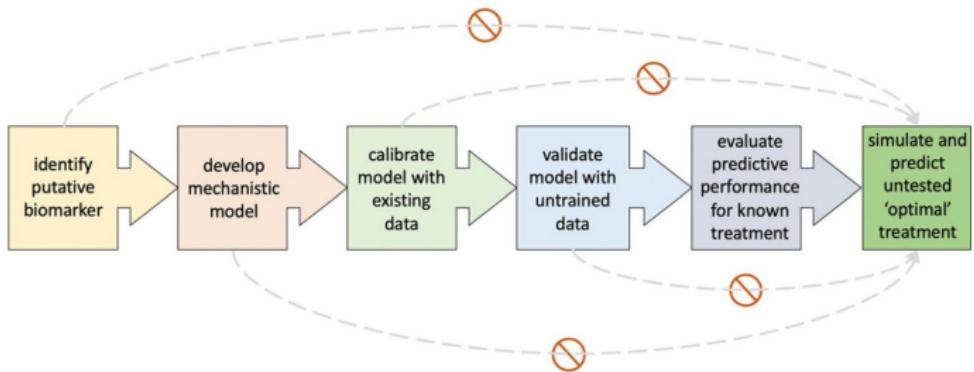


Figure from Brady & Enderling (2019)

# The effect of IFN, “hypothetical” consequences

MM of MPNs and  
HSC

Rasmus Kristoffer  
Pedersen

Assuming our guess of the IFN-effect is valid

( $\rho_L \downarrow$ ,  $\omega_H \downarrow$  and  $\omega_L \downarrow$ )

What are the consequences?

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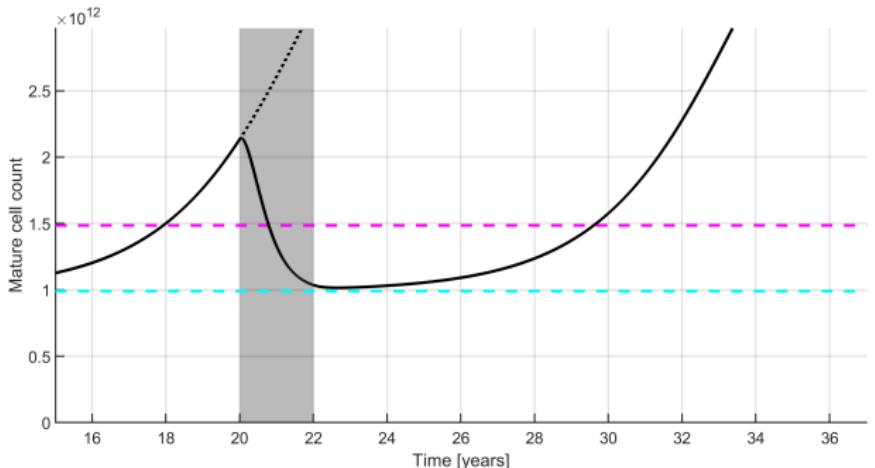
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# The effect of IFN, “hypothetical” consequences

Assuming our guess of the IFN-effect is valid  
( $\rho_L \downarrow$ ,  $\omega_H \downarrow$  and  $\omega_L \downarrow$ )  
What are the consequences?



(Here, only  $\rho_L$  was decreased)

MM of MPNs and HSC

Rasmus Kristoffer Pedersen

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