



دانشگاه صنعتی اصفهان

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### Q1)

A)  $LR(0) \subset LALR(1) \subset LR(2) \subset LR(1)$

wrong,  $LR(2)$  is more powerful than  $LR(1)$

for example, the grammar below is not  $LR(1)$  but it is  $LR(2)$

$$\begin{aligned} S &\rightarrow A1 B x \mid A2 B y \\ A1 &\rightarrow a \\ A2 &\rightarrow a \\ B &\rightarrow b \end{aligned}$$

B) any CFG can be parsed in  $O(n^3)$

correct, all CFGs can be parsed using CYK in  $O(n^3)$

C) all unambiguous grammars can be parsed using  $LR(1)$

wrong, the grammar  $A \rightarrow aAa \mid \varepsilon$  is not ambiguous but also can't be parsed using  $LR(1)$  because of conflict

### Q2)

Power:

$$SLR(1) \subset LALR(1) \subset LR(1)$$

Number of states:

$$LR(1) > LALR(1) = SLR(1)$$

SLR table									
State	ACTION					GOTO			
	a	q	b	c	\$	S	A	B	C
0	s2	r <sub>2</sub>	r <sub>2</sub>	r <sub>2</sub>	r <sub>2</sub>		1		
1		r <sub>4</sub>	s4	r <sub>4</sub>	r <sub>4</sub>			3	
2		s5							
3				s7	r <sub>6</sub>				6
4		r <sub>4</sub>	s4	r <sub>4</sub>	r <sub>4</sub>			8	
5	s2	r <sub>2</sub>	r <sub>2</sub>	r <sub>2</sub>	r <sub>2</sub>		9		
6					acc				
7				s7	r <sub>6</sub>				10
8		s11							
9		r <sub>1</sub>	r <sub>1</sub>	r <sub>1</sub>	r <sub>1</sub>				
10					r <sub>5</sub>				
11	s2	r <sub>2</sub>	r <sub>2</sub>	r <sub>2</sub>	r <sub>2</sub>		12		
12		r <sub>3</sub>		r <sub>3</sub>	r <sub>3</sub>				

B) **parse** the following input and show the step-by-step status of **stack**, **input line** and **actions taken**

*a q b q c c \$*

Trace			
Step	Stack	Input	Action
1	0	a q b q c c \$	s2
2	0 2	q b q c c \$	s5
3	0 2 5	b q c c \$	r <sub>2</sub>
4	0 2 5	b q c c \$	9
5	0 2 5 9	b q c c \$	r <sub>1</sub>
6	0	b q c c \$	1
7	0 1	b q c c \$	s4
8	0 1 4	q c c \$	r <sub>4</sub>
9	0 1 4	q c c \$	8
10	0 1 4 8	q c c \$	s11
11	0 1 4 8 11	c c \$	r <sub>2</sub>
12	0 1 4 8 11	c c \$	12
13	0 1 4 8 11 12	c c \$	r <sub>3</sub>
14	0 1	c c \$	3
15	0 1 3	c c \$	s7
16	0 1 3 7	c \$	s7
17	0 1 3 7 7	\$	r <sub>6</sub>
18	0 1 3 7 7	\$	10
19	0 1 3 7 7 10	\$	r <sub>5</sub>
20	0 1 3 7	\$	10
21	0 1 3 7 10	\$	r <sub>5</sub>
22	0 1 3	\$	6
23	0 1 3 6	\$	acc

**Q4) consider the following grammar**

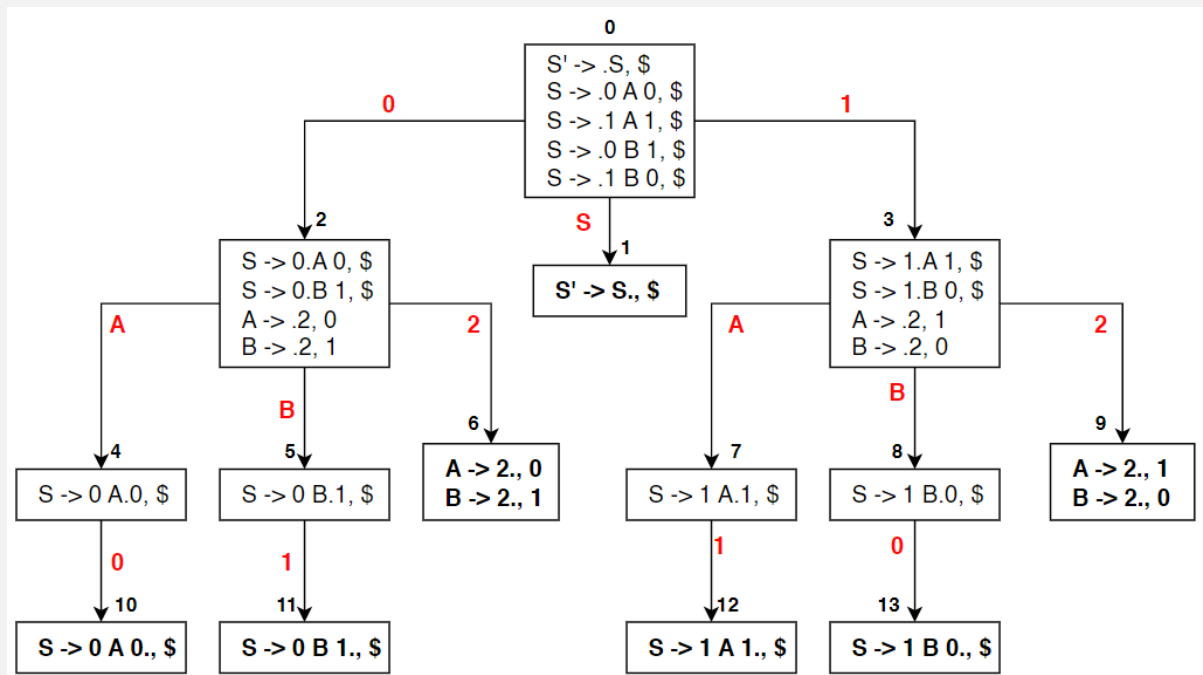
$$S' \rightarrow S$$

$$S \rightarrow 0A0 \mid 1A1 \mid 0B1 \mid 1B0$$

$$A \rightarrow 2$$

$$B \rightarrow 2$$

**A) draw the *LR(1)* state automata**



B) build the **LR(1) parsing table** of this grammar

LR table								
State	ACTION				GOTO			
	0	1	2	\$	S'	S	A	B
0	s2	s3				1		
1				acc				
2			s6				4	5
3			s9				7	8
4	s10							
5		s11						
6	r <sub>5</sub>	r <sub>6</sub>						
7		s12						
8	s13							
9	r <sub>6</sub>	r <sub>5</sub>						
10				r <sub>1</sub>				
11				r <sub>3</sub>				
12				r <sub>2</sub>				
13				r <sub>4</sub>				

C) is this grammar **LALR(1)**?

If not, briefly describe **why**, otherwise combine states from part A to build the **LALR(1) automata**.

In order to construct the **LALR(1)** automata of this grammar, we need to combine states 6 and 9, which results in a reduce/reduce conflict of r<sub>5</sub> and r<sub>6</sub>

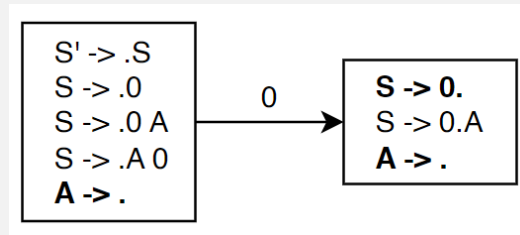
**Q5) Over the alphabet {0}, provide a grammar that...**

A)

has **exactly one** shift/reduce conflict and **exactly one** reduce/reduce conflict in **SLR(1)**. Also, provide the sets and GOTO transitions of **state automata (starting from set 0)** that reaches those conflicts (you don't need to draw the whole automata)

$$S \rightarrow 0 \mid 0A \mid A0$$

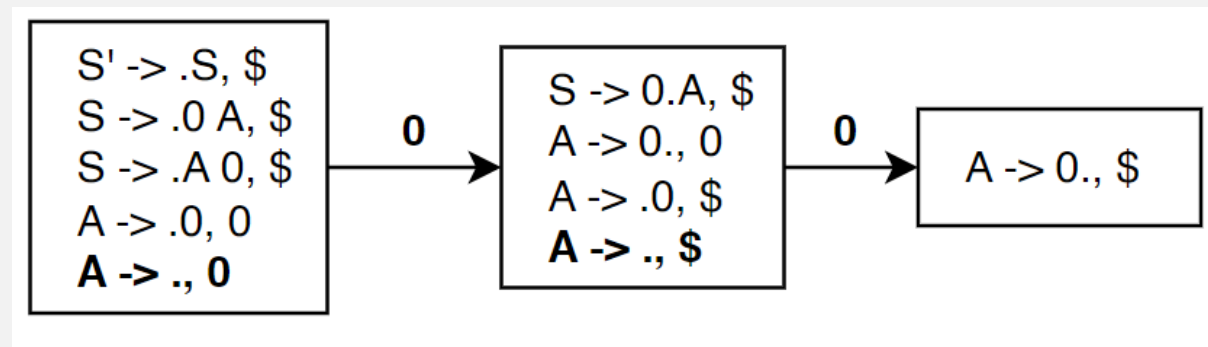
$$A \rightarrow \epsilon$$



B)

has **exactly 2** shift/reduce conflicts and **no** reduce/reduce conflict in **LR(1)**. Also, provide the sets and GOTO transitions of **state automata (starting from set 0)** that reaches those conflicts (you don't need to draw the whole automata)

$S \rightarrow 0A|A0$   
 $A \rightarrow 0 | \epsilon$



**Q6) Below is the *SLR(1)* parsing table of a grammar, along with the size of each production. find the whole grammar, explain with detail.**

SLR table											
State	ACTION						GOTO				
	0	1	a	b	c	\$	S'	S	A	B	C
0			s4		s3			1	2		
1					acc						
2	s5										
3					r <sub>2</sub>						
4	r <sub>4</sub>		s4						6		
5				s8						7	
6	r <sub>3</sub>										
7		s9		s10							
8		r <sub>6</sub>		r <sub>6</sub>							
9					s12						11
10		r <sub>5</sub>		r <sub>5</sub>							
11					r <sub>1</sub>						
12					r <sub>7</sub>						

#	LHS	Size of RHS
0	S'	1
1	S	5
2	S	1
3	A	2
4	A	1
5	B	2
6	B	1
7	C	1

Terminals: 0 1 a b c \$

Non terminals: S A B C

start symbol: S'

based on GOTO(0,S) = 1 and acc in state 1, we can fill #0 rule:

$$S' \rightarrow S$$

With that rule found, if we try to compute the closure in state 0, we get S rules

$$S' \rightarrow .S$$

$$S \rightarrow .X$$

$$S \rightarrow .XXXXX$$



The GOTO functions for these rules are as follow:

$\text{GOTO}(0,A) = 2$        $\text{GOTO}(0,c) = 3$        $\text{GOTO}(0,a) = 4$

if we look at state 3, we can see reduction with rule #2, combined with the  $\text{GOTO}(0,c) = 3$ , we can fill rule #2:

$$S \rightarrow c$$

Based on the fact that we have two GOTOs remaining, but one rule, we can come to conclusion that the first symbol of the remaining rule is A, so we get another closure and hence, we can find the other GOTO function:

$$\begin{aligned} S' &\rightarrow .S \\ S &\rightarrow .c \\ S &\rightarrow .AXXXX \\ A &\rightarrow .XX \\ A &\rightarrow .X \end{aligned}$$

Based on the only remining  $\text{GOTO}(0,a) = 4$ , we can fill the blanks (also, state 4 has reduction with rule 4, that's also another clue!):

$$\begin{aligned} S' &\rightarrow .S \\ S &\rightarrow .c \\ S &\rightarrow .AXXXX \\ A &\rightarrow .aX \\ A &\rightarrow .a \end{aligned}$$

Let's go to state 4, we have shift 4 (recursion) and also  $\text{GOTO}(0,A) = 6$ , we also have reduction with rule 3 in state 6, so that fills rule #3

$$A \rightarrow aA$$

let's go to state 2, in which we have the following kernel:

$$S \rightarrow A.XXXX$$

The only action in this state is shift to state 5 with symbol 0, so that's the next symbol.

Let's go to state 5, we get the following kernel:

$$S \rightarrow A0.XXX$$

In this state, we have  $\text{GOTO}(5,B) = 7$ , that gives us the next symbol. Now we compute the closure for state 5:

$$\begin{aligned} S &\rightarrow A0.BXX \\ B &\rightarrow .XX \\ B &\rightarrow .X \end{aligned}$$

We have  $GOTO(5,B) = 7$ , which gives us the next symbol for rule #5, and  $GOTO(5,b) = 8$ , and also have reduction with rule #6 in state 8, now we can fill rule #6:

$$B \rightarrow b$$

Let's go to state 7, in which we have:

$$S \rightarrow A0B.XX$$

$$B \rightarrow B.X$$

In this state, we have  $GOTO(7,1) = 9$  and  $GOTO(7,b) = 10$ , and we only have reduction with rule #5 in state 10, that gives us:

$$B \rightarrow Bb$$

Let's visit state 9:

$$S \rightarrow A0B1.X$$

Finally! We found non-terminal C in  $GOTO(9,C) = 11$ , that gives us this closure:

$$S \rightarrow A0B1.C$$

$$C \rightarrow .X$$

We have  $GOTO(9,c) = 12$  and reduction with rule #7 in state 12, that's the final missing piece

The whole answer put together is:

$$S' \rightarrow S$$

$$S \rightarrow A0B1C \mid c$$

$$A \rightarrow aA \mid a$$

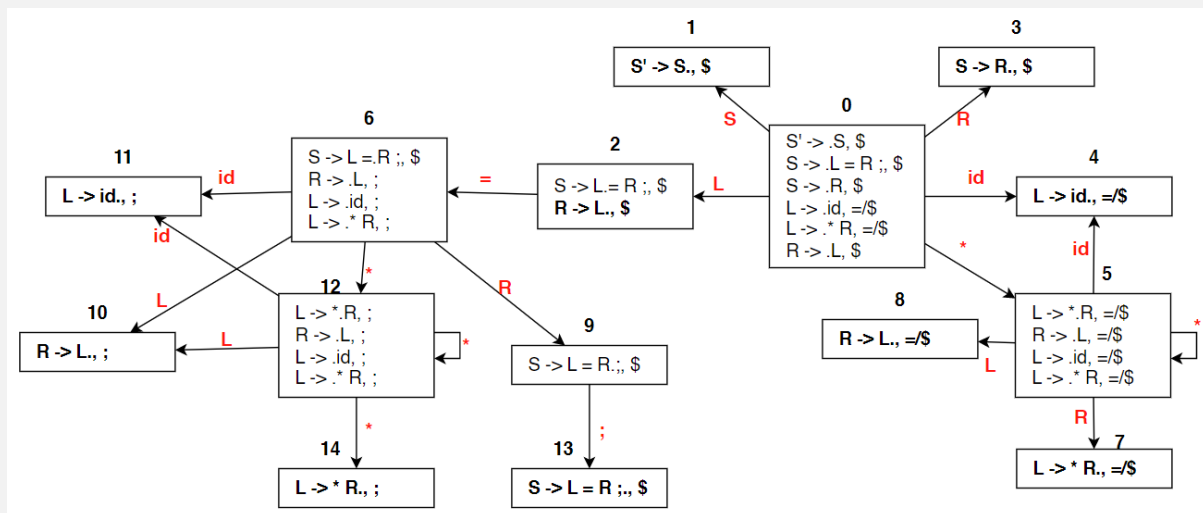
$$B \rightarrow Bb \mid b$$

$$C \rightarrow c$$

## Q7) Consider the following grammar

$$\begin{aligned}
 S' &\rightarrow S \\
 S &\rightarrow L = R ; \mid R \\
 L &\rightarrow id \mid * R \\
 R &\rightarrow L
 \end{aligned}$$

### A) draw its LR(1) state automata



### B) using the answer for part A, tell which states should be merged together to get to LALR(1)

States 8 and 10, States 7 and 14, States 5 and 12, States 4 and 11

### C) construct LALR(1) parsing table

LR table									
State	ACTION					GOTO			
	=	;	id	*	\$	S'	S	L	R
0			s4	s5			1	2	3
1					acc				
2	s6				r5				
3					r2				
4	r3	r3			r3				
5			s4	s5				8	7
6			s4	s5				8	9
7	r4	r4			r4				
8	r5	r5			r5				
9		s10							
10					r1				

D) **parse** the following input and show the step-by-step status of **stack**, **input line** and **actions taken**

*id = id ;*

Trace			
Step	Stack	Input	Action
1	0	id = id ; \$	s4
2	0 4	= id ; \$	r <sub>3</sub>
3	0	= id ; \$	2
4	0 2	= id ; \$	s6
5	0 2 6	id ; \$	s4
6	0 2 6 4	; \$	r <sub>3</sub>
7	0 2 6	; \$	8
8	0 2 6 8	; \$	r <sub>5</sub>
9	0 2 6	; \$	9
10	0 2 6 9	; \$	s10
11	0 2 6 9 10	\$	r <sub>1</sub>
12	0	\$	1
13	0 1	\$	acc

E) show that this grammar is **not SLR(1)**, you don't need to draw the whole state diagram, start from state 0 and reach a conflict.

