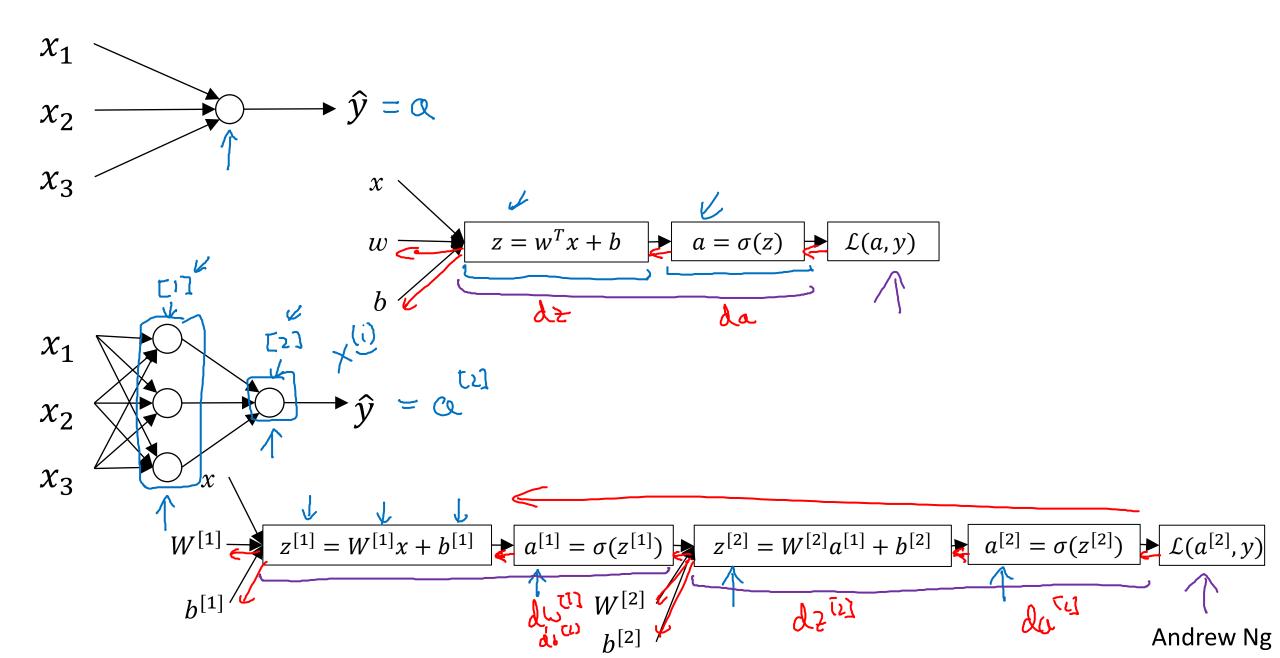


## One hidden layer Neural Network

# Neural Networks Overview

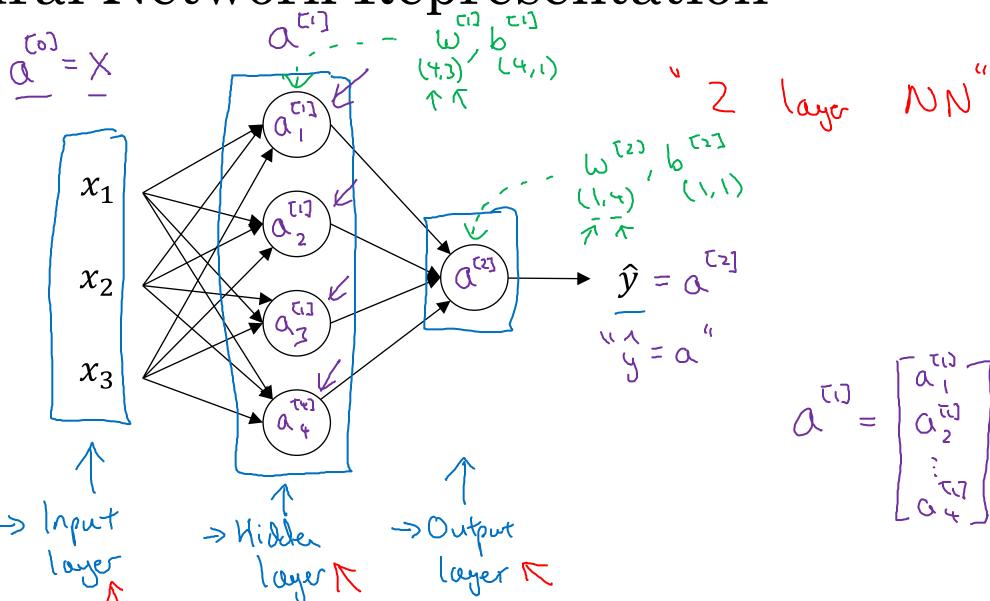
### What is a Neural Network?





## One hidden layer Neural Network

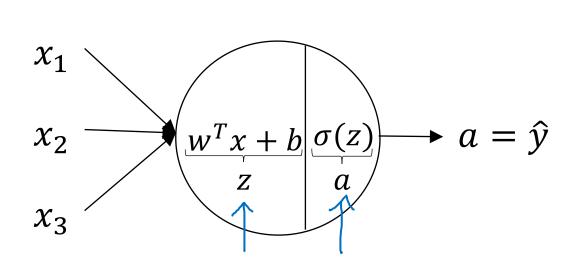
Neural Network Representation



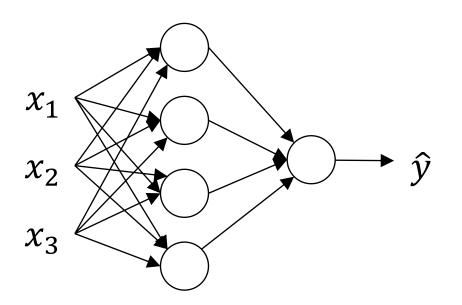


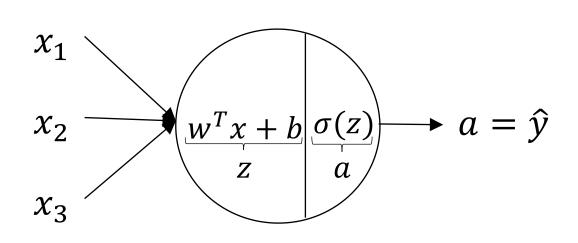
## One hidden layer Neural Network

Computing a Neural Network's Output

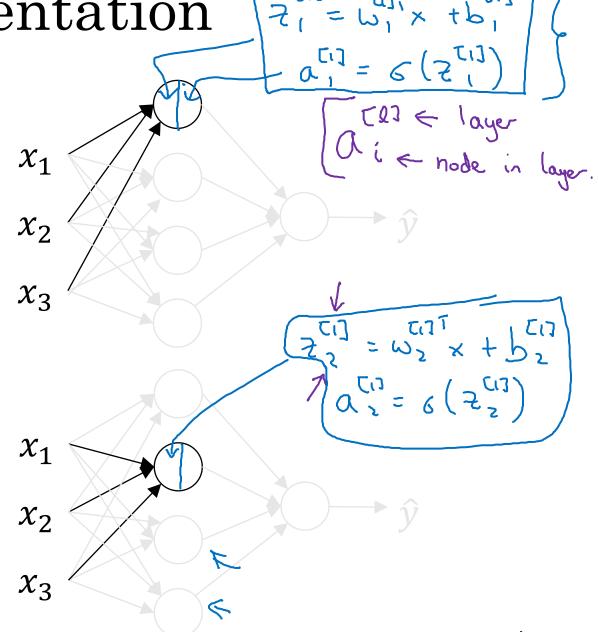


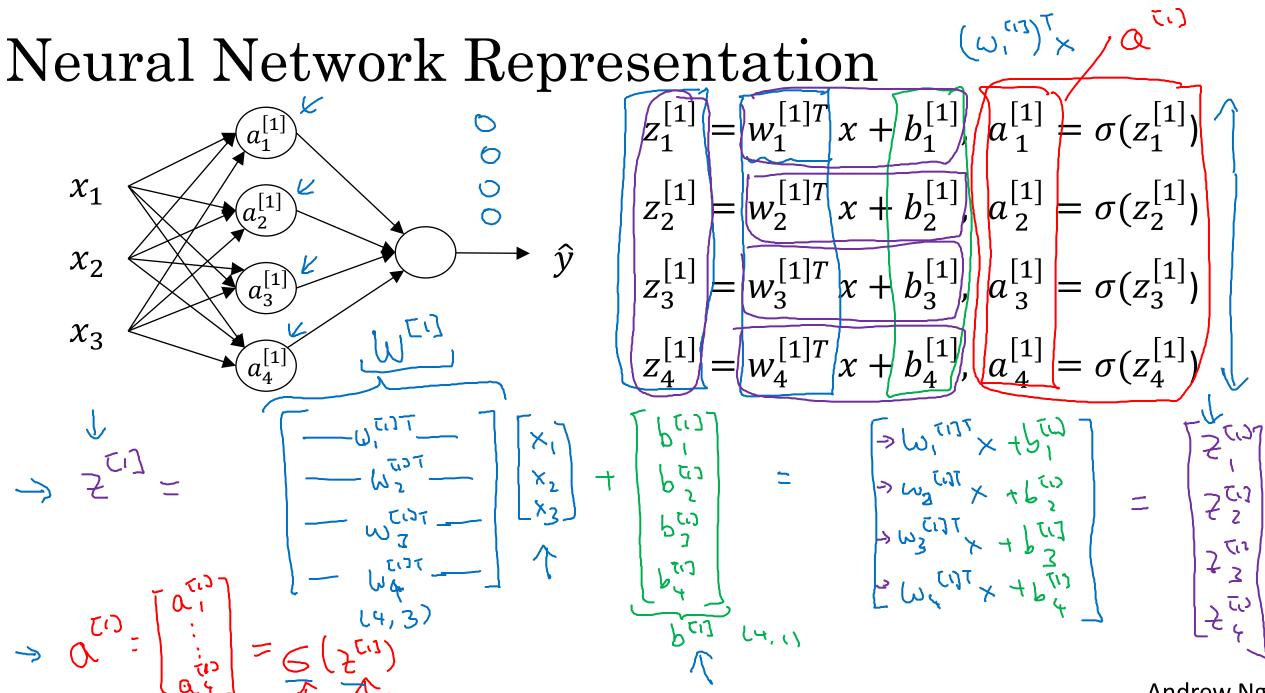
$$z = w^T x + b$$
$$a = \sigma(z)$$





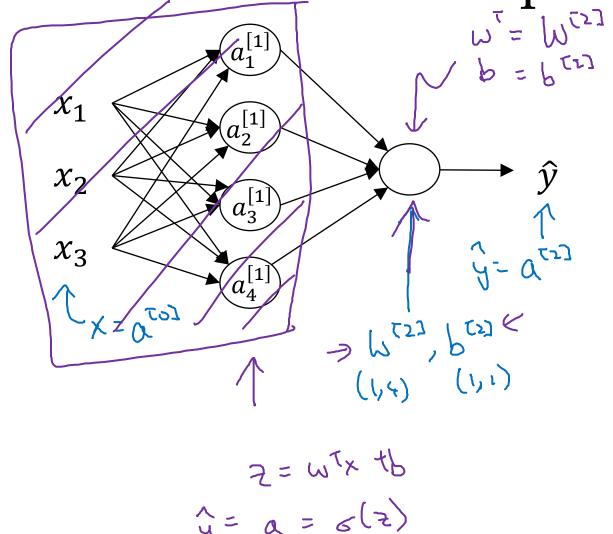
$$z = w^T x + b$$
$$a = \sigma(z)$$





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Neural Network Representation learning



Given input x:

$$z^{[1]} = W^{[1]} + b^{[1]}$$

$$a^{[1]} = \sigma(z^{[1]})$$

$$a^{[1]} = w^{[2]} a^{[1]} + b^{[2]}$$

$$a^{[2]} = w^{[2]} a^{[1]} + b^{[2]}$$

$$a^{[2]} = \sigma(z^{[2]})$$

$$a^{[2]} = \sigma(z^{[2]})$$

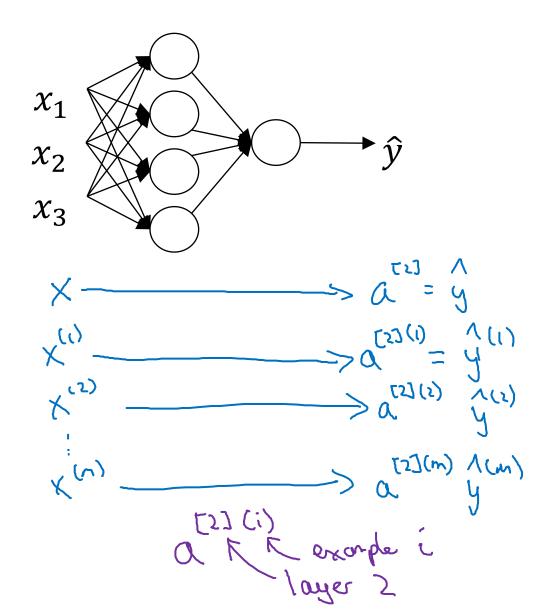
$$a^{[2]} = \sigma(z^{[2]})$$

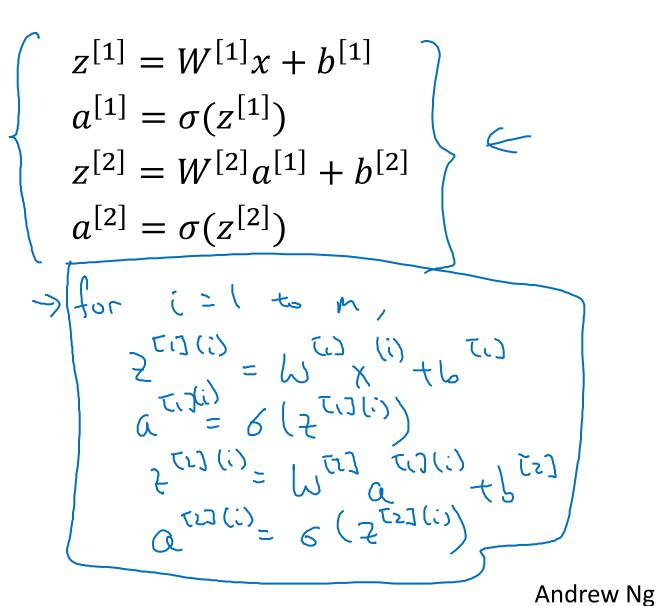


## One hidden layer Neural Network

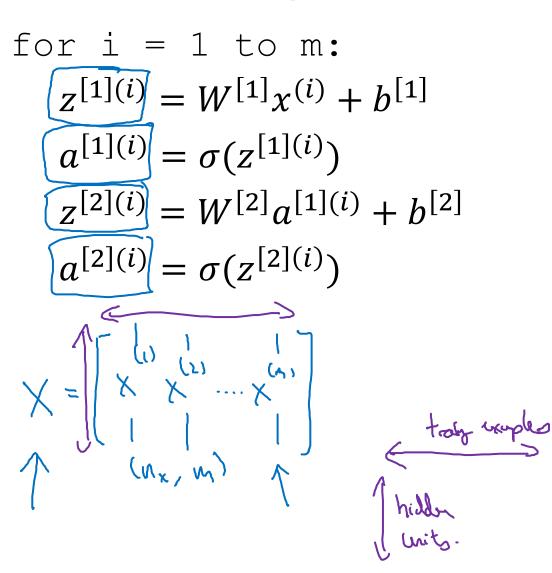
Vectorizing across multiple examples

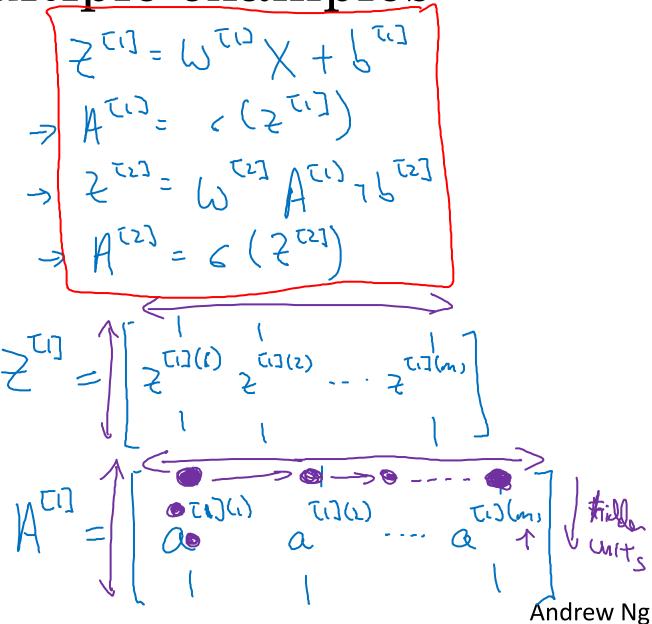
### Vectorizing across multiple examples





Vectorizing across multiple examples



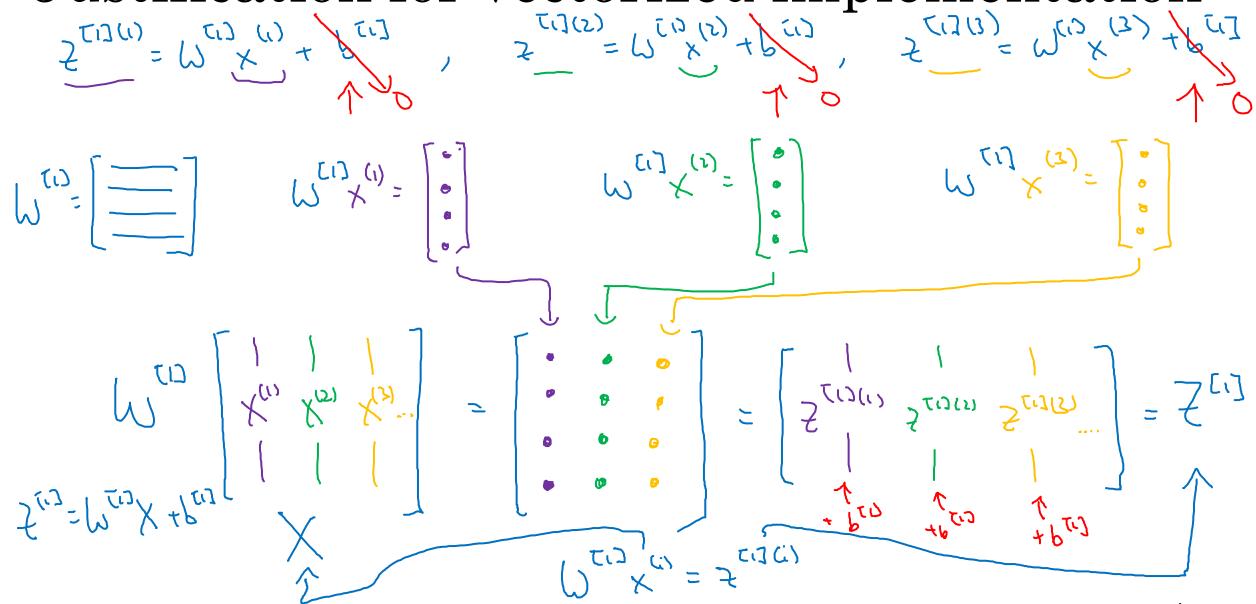




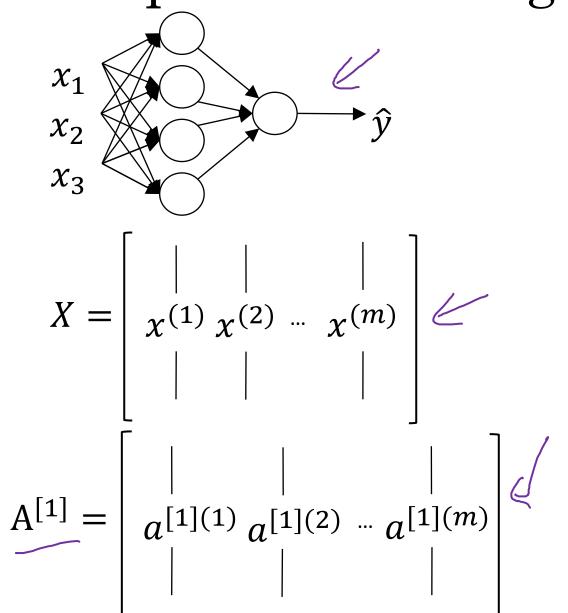
## One hidden layer Neural Network

Explanation for vectorized implementation

Justification for vectorized implementation



### Recap of vectorizing across multiple examples



```
for i = 1 to m
    + z^{[1](i)} = W^{[1]}x^{(i)} + b^{[1]}
    \Rightarrow a^{[1](i)} = \sigma(z^{[1](i)})
   \Rightarrow z^{[2](i)} = W^{[2]}a^{[1](i)} + b^{[2]}
   \Rightarrow a^{[2](i)} = \sigma(z^{[2](i)})
                        A^{[0]} \times = a^{[0]} \times (i) = a^{[0](i)}
Z^{[1]} = W^{[1]}X + b^{[1]} \leftarrow W^{[1]}X^{(0)} + b^{[1]}
A^{[1]} = \sigma(Z^{[1]})
Z^{[2]} = W^{[2]}A^{[1]} + b^{[2]}
A^{[2]} = \sigma(Z^{[2]})
```



## One hidden layer Neural Network

### Activation functions

### Activation functions

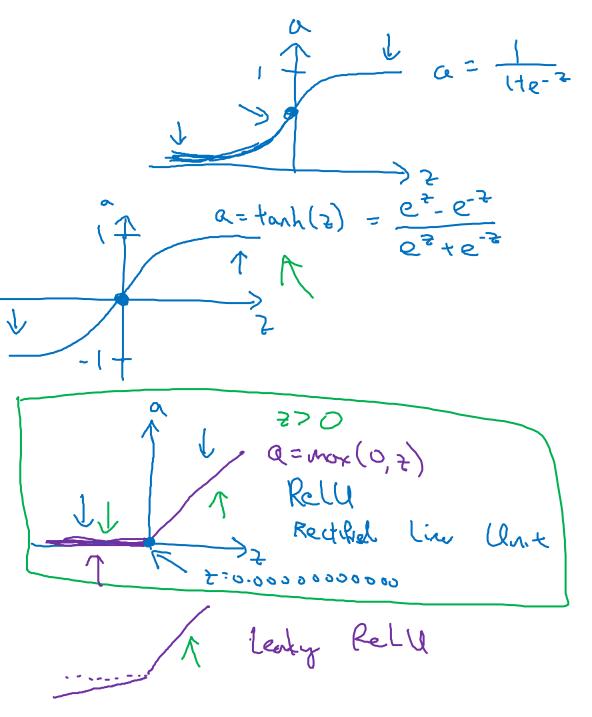
Given x:

$$z^{[1]} = W^{[1]}x + b^{[1]}$$

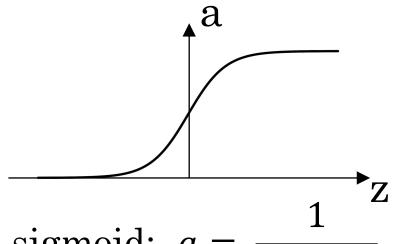
$$z^{[2]} = W^{[2]}a^{[1]} + b^{[2]}$$

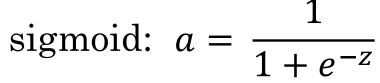
$$z^{[2]} = w^{[2]}a^{[1]} + b^{[2]}$$

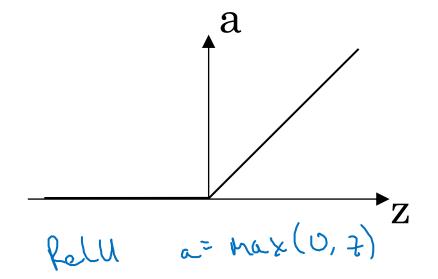
$$a^{[2]} = \sigma(z^{[2]}) \quad \sigma^{[2]} = \sigma(z^{[2]})$$

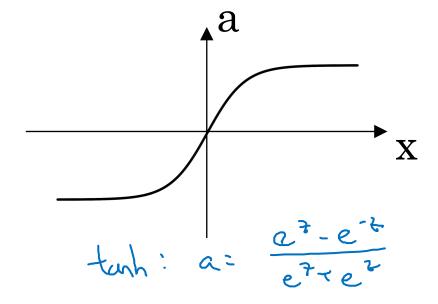


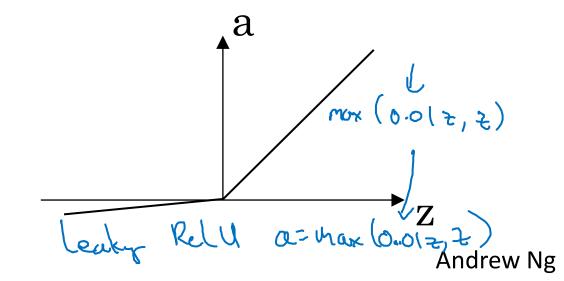
### Pros and cons of activation functions









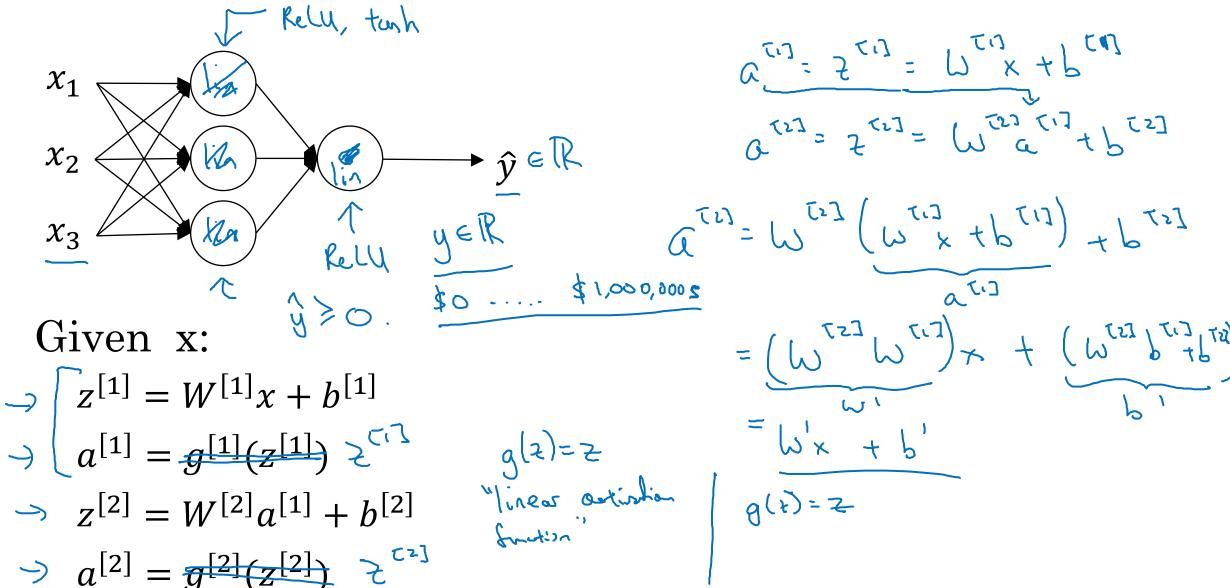




## One hidden layer Neural Network

Why do you need non-linear activation functions?

### Activation function





## One hidden layer Neural Network

# Derivatives of activation functions

### Sigmoid activation function

$$g(z) = \frac{1}{1 + e^{-z}}$$

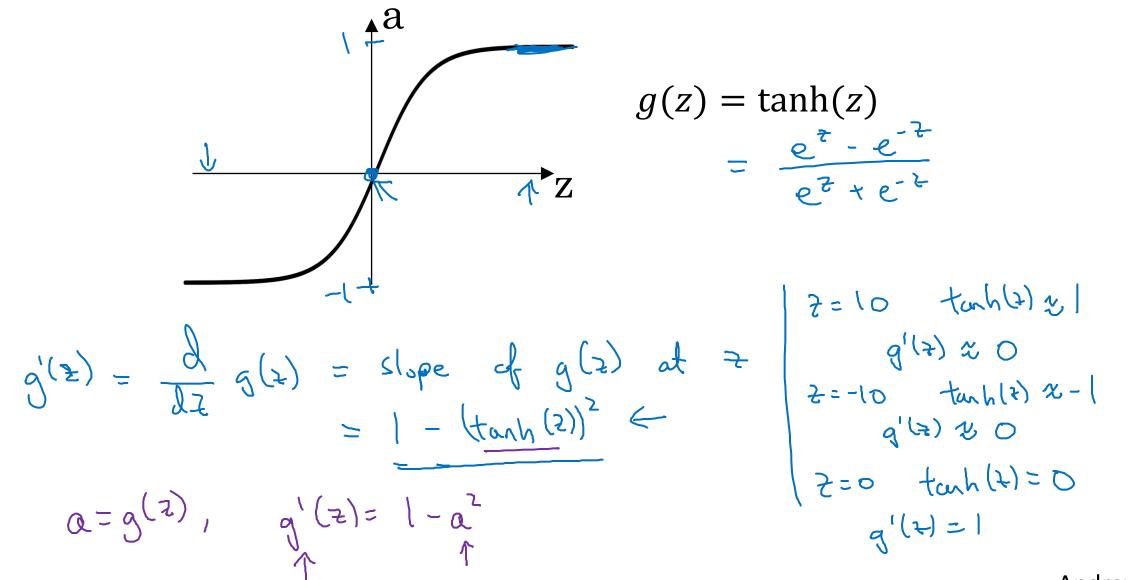
$$g(z) = \frac{1}{1 + e^{-z}}$$

$$a = g(z) = \frac{1}{1 + e^{-z}}$$

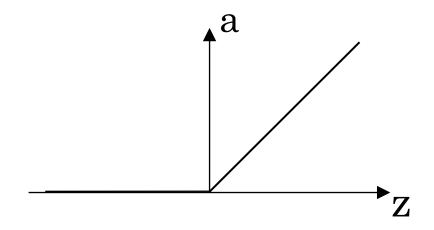
$$\frac{1}{1 + e^{-z}}$$

$$\frac{1}{$$

### Tanh activation function



### ReLU and Leaky ReLU



#### ReLU

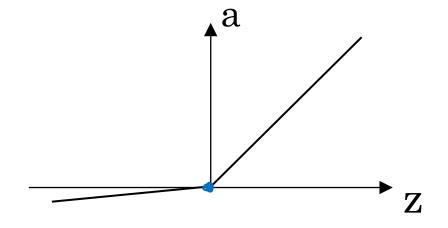
$$g(t) = mox(0, 2)$$

$$\Rightarrow g'(t) = \begin{cases} 0 & \text{if } 2 < 0 \\ 1 & \text{if } t \geq 0 \end{cases}$$

$$\Rightarrow g'(t) = \begin{cases} 0 & \text{if } t \geq 0 \end{cases}$$

$$\Rightarrow g'(t) = \begin{cases} 0 & \text{if } t \geq 0 \end{cases}$$

$$\Rightarrow g'(t) = \begin{cases} 0 & \text{if } t \geq 0 \end{cases}$$



#### Leaky ReLU

$$g(z) = \max(0.01z, z)$$
  
 $g'(z) = \{0.01 \text{ if } z < 0\}$ 



## One hidden layer Neural Network

Gradient descent for neural networks

Formulas for computing derivatives

Formal babagain;
$$\begin{cases}
\zeta_{13} = \Omega_{13}(\zeta_{13}) = C(\zeta_{13}) \\
\zeta_{13} = \Omega_{23}(\zeta_{13}) \\
\zeta_{13} = \Omega_{23}(\zeta_{13}) \\
\zeta_{13} = \Omega_{23}(\zeta_{13}) \\
\zeta_{13} = \Omega_{23}(\zeta_{13})$$
Formal babagain;

Back propagation:

$$\begin{aligned}
&\mathcal{Z}^{[i]} = \mathcal{A}^{[i]} = \mathcal{A}^{[i]} \mathcal{A}^{[i]} \\
&\mathcal{A}^{[i]} = \mathcal{A}^{[i]} \mathcal{A}^{[i]} \end{aligned}$$

$$\begin{aligned}
&\mathcal{A}^{[i]} = \mathcal{A}^{[i]} \mathcal{A}^{[i]} \\
&\mathcal{A}^{[i]} = \mathcal{A}^{[i]} \mathcal{A}^{[i]} \end{aligned}$$

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$$\begin{aligned}
&\mathcal{A}^{[i]} = \mathcal{A}^{[i]} \mathcal{A}^{[i]} \\
&\mathcal{A}^{[i]} = \mathcal{A}^{[i]} \mathcal{A}^{[i]} \end{aligned}$$

$$\end{aligned}$$

$$\begin{aligned}
&\mathcal{A}^{[i]} = \mathcal{A}^{[i]} \mathcal{A}^{[i]} \\
&\mathcal{A}^{[i]} = \mathcal{A}^{[i]} \mathcal{A}^{[i]} \end{aligned}$$

$$\end{aligned}$$

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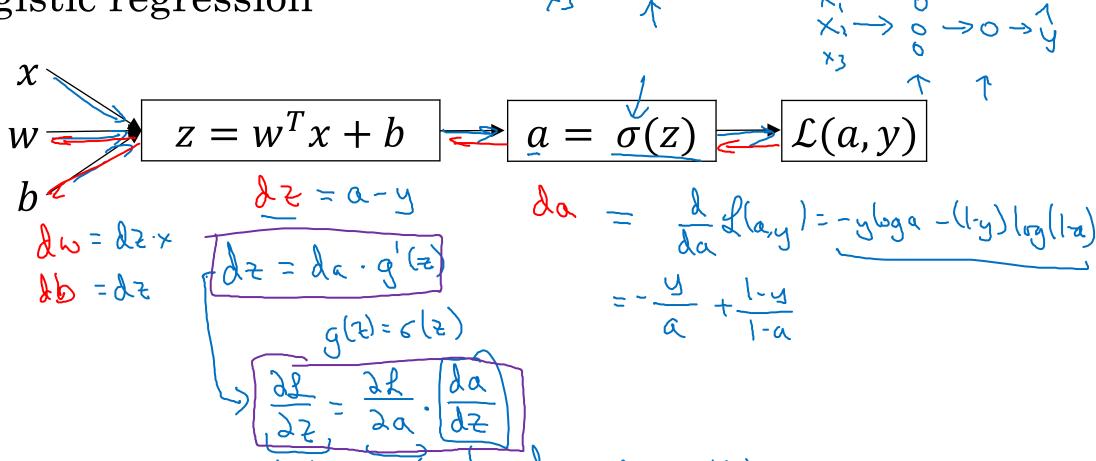


## One hidden layer Neural Network

Backpropagation intuition (Optional)

### Computing gradients

Logistic regression



Neural network gradients  $z^{[2]} = W^{[2]}x + b^{[2]}$ du = de a Tos > db (s) = dz [s] K  $\left( \begin{array}{cccc} n^{T\lambda^{2}} & n^{Li_{2}} \end{array} \right)$ 

### Summary of gradient descent

$$dz^{[2]} = a^{[2]} - y$$
 $dW^{[2]} = dz^{[2]}a^{[1]^T}$ 
 $db^{[2]} = dz^{[2]}$ 
 $dz^{[1]} = W^{[2]T}dz^{[2]} * g^{[1]'}(z^{[1]})$ 
 $dW^{[1]} = dz^{[1]}x^T$ 
 $db^{[1]} = dz^{[1]}$ 

Vectorized Implementation:

$$Z^{(1)} = \omega^{(1)} \times + b^{(1)}$$

$$Z^{(1)} = g^{(1)}(Z^{(1)})$$

$$Z^{(1)} = \left[ Z^{(1)}(Z^{(1)}) + Z^{(1)}(Z^{(1)}) \right]$$

$$Z^{(1)} = \omega^{(1)} \times + b^{(1)}$$

$$Z^{(1)} = g^{(1)}(Z^{(1)})$$

$$Z^{(1)} = g^{(1)}(Z^{(1)})$$

### Summary of gradient descent

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$$dz^{[1]} = W^{[2]T}dz^{[2]} * g^{[1]'}(z^{[1]})$$

$$dz^{[1]} = W^{[2]T}dz^{[2]} * g^{[1]'}(z^{[1]})$$

$$dw^{[1]} = dz^{[1]}x^T$$

$$db^{[1]} = dz^{[1]}$$

$$db^{[1]} = dz^{[1]}$$

$$dz^{[1]} = w^{[2]T}dz^{[2]} * g^{[1]'}(z^{[1]})$$

$$dz^{[1]} = w^{[2]T}dz^{[1]}x^T$$

$$dw^{[1]} = \frac{1}{m}dz^{[1]}x^T$$

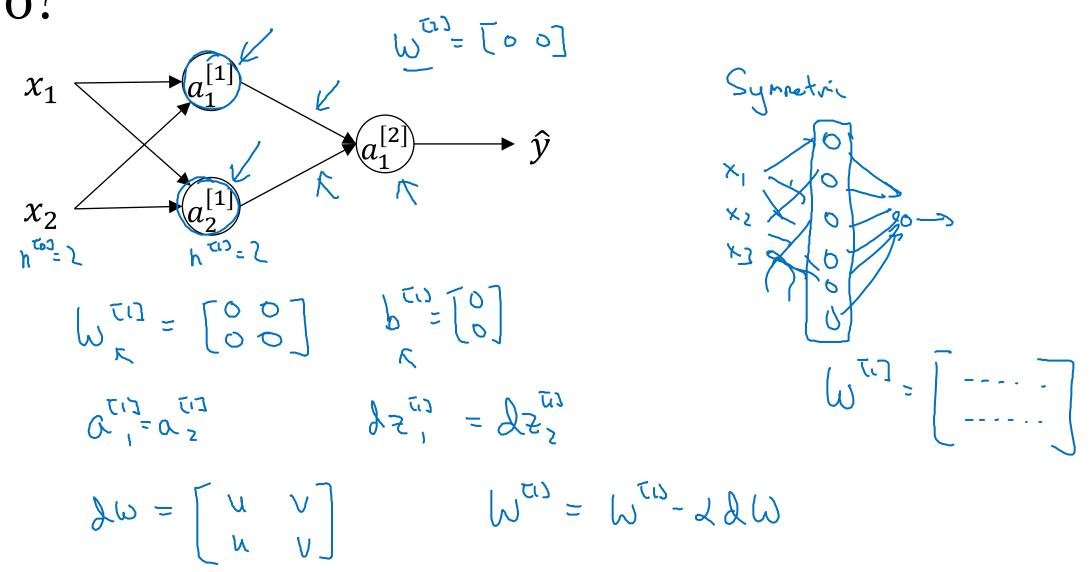
$$db^{[1]} = dz^{[1]}$$



## One hidden layer Neural Network

### Random Initialization

## What happens if you initialize weights to zero?



### Random initialization

