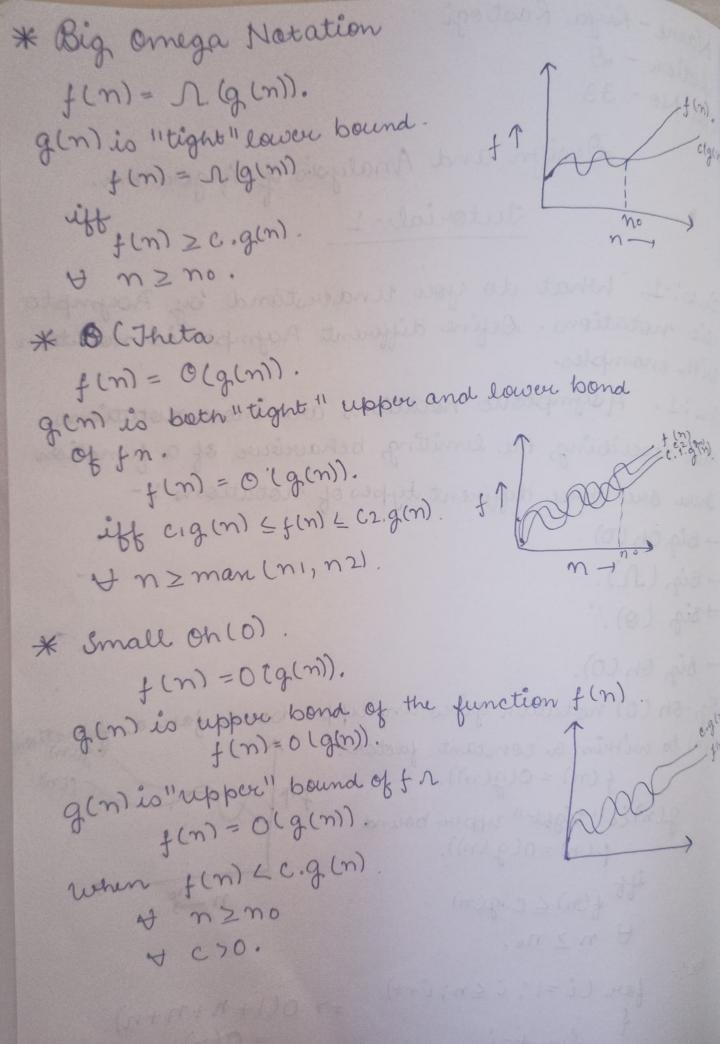
Name-Riya Rastogi Action - D Coll No - 33. Design and Analysis of Algorithm. Jutorial - 1 aus: 1. What do you understand by Asympto tic notation. Define different Asymptotic notation Ano: 1. A symptotic notations are those notations that describing the limiting behaviour of a function There are three different types of notations: - Big Oh (0). - Big (IL). → Big (0). - Big on (0). *Sig-on (0) notation gives an upper bond for a function sign-on (0) notant factor.

f(n) to within a constant factor.

f(n) = O(g(n)). q(n)is "tight" upper bound of f(n) = O(q(n)). ift f(m) < c.g(m) Hnzno.

ex:- for $(i=1; i \le n; i+1)$. => O(1+n+n+n)= O(n).



* Small omega (w) fin) = wigin). gent is dower bound of fr f(n) = wg(n)). when ten) > c.g(n). せ かつかの 4 & C>0 aus: 2 What Should be time complexity for (i=1 ton) {i=i*23. for (i=1 to n) 11 i=1,2,4,8 di=i*23 11 0(1). => £ 1+2+4+0+---+n. Kth term of GP=> TR = CL91K-1. n= 2x-1 n = 2K 2n = 2K log2 (2n) = K (log22)

 $2^{n} = 2^{n}$ $\log_{2}(2^{n}) = K(\log_{2}2)$ $K = \log_{2}(2^{n})$ $K = \log_{2}2 + \log_{2}n$ $K = 1 + \log_{2}n$ $K \neq 1 + \log_{2}n$ $0(\log_{2}n)$ $0(\log_{2}n)$

```
Ques: -3
     T(n) = {3T(n-1) if n>0, otherwise 1}
 T(n) = 3T(n-1).
    = 3 (3T(n-2)).
      = 32 T (n-2)
      = 3^3 T (n-3)
      =3^n T(n-n)
       = 377(0).
        = 37.
    =>0(3^n).
Oues: - 4
     T(n)={27(n-1)-1 if n>0,0therwise 13.
        T(n) = 27(n-1)-1
             - 2(2T(n-2)-1)-1
             =2^{2}(\tau(n-2))-2-1
              - 22 (2T(n-3)-1)-2-1
             =2^3 T(n-3) -2^2-2^1-2^0
            = 2^{n} - (n-n) - 2^{n-1} - 2^{n-2} - 2^{n-3}
              ---- 2<sup>2</sup>-2'-2°.
            = 2n - 2n - 1 - 2n - 2 n - 3
              --- 22-21-20
              - 2n - (2n-1).
         T(n)=1.
```

=>0(1).

```
aus: - 5 what should be the time complexity
    int i = 1, 5=1;
   while (SC=n) &
   i++;
    S= Sti;
  printf ("#");
 i=1,2,3,4,5,6,----K
 S=2+3+8+15----K.
 when 5 >= n, then loop will slopat Kth iterations
   => S>=n
      S=n.
  - 2+2+3+4+ --+ K=n
   = 1+(K*(K+1)) 2=n
   = K^2 = \eta
   K=In
   = 0 (m).
 Oues: - 6 Time complenity of.
  void function (int n).
       inti, count=0.
     forli=1°, i*iL=n;i++)
          count ++°. 110(1).
      as i² L=n.
         i L=Tr
    i=1,2,3,4,-5n

  \[
  \left( \frac{1}{2} + 2 + 3 + - - - + 5 \text{m}.
  \]
```

$$T(n) = \int n \times (\int n + 1)$$

$$T(n) = \int n \int n$$

$$T(n) = o(n)$$

Ours: -7 void function (int m) {

ent i, j, K, court = 0;

for (i=n|2; i<=n; i++).

for (j=1; j<=n; j=j*2)

for (K=1; K=n; K=K*2).

for K= K*2 K=1,2,4,8,---n. G.P=7 a=1, N=2

```
=7 1 (2K-1)
     n=> 2K
      legn=K.
      logn logn*logn
      logn logn *logn
      logn logn* logn.
      => O(n*logn*longn).
       => 0(n log2n).
Ø: 8.
      funtion (int n)
         int (n==1)
     for li=1 ton)
       per (j=1 ton).
       question (n-3),
       T(n) = T(n|3) + n^2
          a=1, b=3, f(n)=n2
            c=log31=0
               n°=1 > (fln)=n2)
             T(n) = O(n2).
```

```
& void function (int n)
           for li= 1 to n)
             for(j=1', j <=n', j=j+1).
              y trint f (" * ")
    for i=1=) j=1,2,3,4,---n.
    for i=2 => j= 1,3,5,7,---n
for i=3 => j= 1,4,7,---n.
        for i=n => j=1 ---
  =7 \leq n+1/2+n/3+n/4+---+1.
  => < n[1+112+113+114+----1]n].
       => \ \ n[logn]
        => T(n) = (n log n)
            T(n) = O[n logn]
Ques' .- 10
          as given nx & cn
         rulation blw n 2 ch is
                 mr = o(cn).
                             as nx < cn
                  y n≥no and some constant a>0
            for no = 1
          => 1k \ (a2)
             => mo=1 & C=2.
```