Competitive Programming Library

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September 27, 2019

Contents

1	Dat	a Structure	4			
	1.1	Fenwick Tree (1D)	4			
	1.2	Fenwick Tree (2D)	6			
	1.3	Segment Tree (1D)	8			
	1.4		10			
	1.5		13			
	1.6		15			
	1.7		17			
	1.1	ino s riigoriumii On Tree	11			
2	Gra	nnh	22			
_	2.1	±	${22}$			
	2.2	y	24			
	2.3	- *	26			
	$\frac{2.3}{2.4}$		28			
		1 0				
	2.5	v C I	30			
	2.6		37			
	2.7	Maximum Bipartite Matching	40			
9	C4•		11			
3	Stri	o a contract of the contract o	44			
	3.1	0	44			
	3.2		47			
	3.3		49			
	3.4	8	50			
	3.5		53			
	3.6	Suffix Array Emax	56			
	3.7	Suffix Array $O(n \log n)$	59			
4						
	4.1	Number Theory	61			
	4.2	Rho Pollard Sieve	64			
	4.3	Big Integer	67			
	4.4		76			
	4.5	Lagrange Interpolation	79			
	4.6		81			
	4.7		83			
	4.8		86			
	4.9		89			
	4.9	Dig meger wumphcarion Osing FFT	09			
5	Geo	ometry	93			
0	5.1		93			
	5.1	Convex Hull				
	5.2	Convex Hun	UU			
6	Dynamic Programming 102					
J	6.1	Bit Mask DP Sample				
	-	•				
	6.2	Digit DP Sample				
	6.3	Sum Over Submasks DP (IUT IUPC Code)	.U7 .10			
	h /l	Sum Liver Sunmacke DP	111			

	6.5	Tree DP Sample	. 112		
7	Miscellaneous				
	7.1	Common Template Code	. 114		
	7.2	GP Hash Table Samples	. 118		
	7.3	Matrix Exponentiation	. 120		

1 Data Structure

1.1 Fenwick Tree (1D)

```
struct BIT{
    vll bit1;
    vll bit2;
    11 N;
    BIT(ll n)
        N=n;
        bit1.assign(n+1,0);
        bit2.assign(n+1,0);
    BIT(vll v) : BIT(v.size())
        for(ll i=0;i<v.size();i++)</pre>
            add(i+1, i+1, v[i]);
    }
    ll sum1(ll idx)
        ll ret=0;
        for (; idx > 0; idx -= idx & -idx)
            ret += bit1[idx];
        return ret;
    }
    11 sum2(11 idx)
        ll ret=0;
        for (; idx > 0; idx -= idx & -idx)
            ret += bit2[idx];
        return ret;
    }
    ll prefix_sum(ll idx)
        return sum1(idx)*idx - sum2(idx);
    11 sum(11 1, 11 r)
        return prefix_sum(r) - prefix_sum(1-1);
    }
```

```
void add1(ll idx, ll val)
        for (; idx <= N; idx += idx & -idx)</pre>
             bit1[idx] += val;
    }
    void add2(ll idx, ll val)
        for (; idx <= N; idx += idx & -idx)</pre>
             bit2[idx] += val;
    }
    void add(ll l, ll r, ll val)
        add1(1,val);
        add1(r+1,-val);
        add2(1,val*(1-1));
        add2(r+1,-val*r);
    }
};
int main()
{
    11 n,m,t,i,j,k,a,b,c,cs=1;
    cin>> n;
    vll v(n);
    for(i=0;i<n;i++) cin>> v[i];
    BIT bit(v);
    cin>> m;
    while(m--){
        cin>> t;
        if(t==1){
             cin>> a >> b;
             cout << "Sum: " << bit.sum(a,b) << "\n";</pre>
        }
        else{
             cin>> a >> b >> c;
             bit.add(a,b,c);
        }
    }
    return 0;
}
```

1.2 Fenwick Tree (2D)

```
struct BIT_2D {
    vvl bit;
    11 n, m;
    BIT_2D(11 N, 11 M)
    {
        n=N, m=M;
        vll v;
        v.assign(m,0);
        bit.assign(n,v);
    }
    BIT_2D(vvl val) : BIT_2D(val.size(), val[0].size())
        for(ll i=0;i<val.size();i++)</pre>
             for(ll j=0;j<val[i].size();j++)</pre>
                 add(i,j,val[i][j]);
    }
    11 sum(11 x, 11 y)
        11 \text{ ret} = 0;
        for (11 i = x; i \ge 0; i = (i & (i + 1)) - 1)
             for (11 j = y; j >= 0; j = (j & (j + 1)) - 1)
                 ret += bit[i][j];
        return ret;
    }
    void add(ll x, ll y, ll delta)
        for (ll i = x; i < n; i = i | (i + 1))
             for (ll j = y; j < m; j = j | (j + 1))
                bit[i][j] += delta;
    }
};
int main()
    ll n,m,t,i,j,k,a,b,c,cs=1;
    cin>> n >> m >> t;
    vvl val(n);
    for(i=0;i<n;i++){
        vll v(m);
```

```
for(j=0;j<m;j++)</pre>
             cin>> v[j];
        val[i]=v;
    }
    BIT_2D bit(val);
    while(t--){
        cin>> cs;
         if(cs==1){
             cin>> a >> b >> c;
             a--,b--;
             bit.add(a,b,c);
        }
        \verb"else" \{
             cin>> a >> b >> i >> j;
             a--,b--,i--,j--;
             11 x=0,res;
             res=bit.sum(i,j);
             if(b-1>=0)
                 res-=bit.sum(i,b-1);
             if(a-1>=0)
                 res-=bit.sum(a-1,j);
             if (a-1>=0 \text{ and } b-1>=0)
                 res+=bit.sum(a-1,b-1);
             cout << res << "\n";
        }
    }
    return 0;
}
```

1.3 Segment Tree (1D)

```
class Segment_Tree{
    11 N;
    struct Node{
        11 prop,sum;
        Node() {}
        Node(ll p, ll s)
             prop=p,sum=s;
    };
    vector < Node > val;
public:
    Segment_Tree(ll n)
        Node nd(0,0);
        N=(n+5)*4;
        val.assign(N,nd);
    }
    Segment_Tree(vll arr) : Segment_Tree(arr.size())
        for(ll i=0;i<arr.size();i++)</pre>
             update(1,1,N,i+1,i+1,arr[i]);
    }
    void update(ll id, ll b, ll e, ll i, ll j, ll x)
    {
        if (i > e || j < b)
             return;
        if (b >= i && e <= j)</pre>
             val[id].sum += ((e - b + 1) * x);
             val[id].prop += x;
             return;
        }
        ll Left = id << 1;</pre>
        11 Right = (id << 1) + 1;</pre>
        ll mid = (b + e) >> 1;
        update(Left, b, mid, i, j, x);
```

```
update(Right, mid + 1, e, i, j, x);
        val[id].sum = val[Left].sum + val[Right].sum + (e - b + 1)*val[id].prop;
    }
    11 query(11 id, 11 b, 11 e, 11 i, 11 j, 11 carry = 0)
        if (i > e \mid \mid j < b)
             return 0;
        if (b \ge i \text{ and } e \le j)
             return val[id].sum + carry * (e - b + 1);
        11 Left = id << 1;</pre>
        11 Right = (id << 1) + 1;</pre>
        11 \text{ mid} = (b + e) >> 1;
        11 p1 = query(Left, b, mid, i, j, carry + val[id].prop);
        11 p2 = query(Right, mid + 1, e, i, j, carry + val[id].prop);
        return p1 + p2;
    }
};
```

1.4 Segment Tree (2D)

```
11 tree[4*MX][4*MX], val[MX][MX];
void buildY(ll nodex, ll lx, ll rx, ll nodey, ll ly, ll ry, ll n, ll m)
    if(ly==ry){
        if(lx==rx)
            tree[nodex][nodey]=val[lx][ly];
        else
            tree[nodex][nodey]=tree[nodex*2][nodey]+tree[nodex*2+1][nodey];
    }
    else{
        11 \text{ midy}=(1y+ry)/2;
        buildY(nodex,lx,rx,nodey*2,ly,midy,n,m);
        buildY(nodex,lx,rx,nodey*2+1,midy+1,ry,n,m);
        tree[nodex][nodey]=tree[nodex][nodey*2]+tree[nodex][nodey*2+1];
    }
}
void buildX(ll nodex, ll lx, ll rx, ll n, ll m)
    if(lx!=rx){
        ll\ midx=(lx+rx)/2;
        buildX(nodex*2,lx,midx,n,m);
        buildX(nodex*2+1,midx+1,rx,n,m);
    buildY(nodex,lx,rx,1,1,m,n,m);
}
ll sumY(11 nodex, 11 nodey, 11 tly, 11 try1, 11 ly, 11 ry, 11 n, 11 m)
    if (ly > ry)
        return 0;
    if (ly==tly and try1==ry)
        return tree[nodex][nodey];
    11 \text{ midy} = (tly + try1)/2;
    11 ret = sumY(nodex, nodey*2, tly, midy, ly, min(ry, midy), n , m)
                + sumY(nodex, nodey*2+1, midy+1, try1, max(ly, midy+1), ry, n, m);
    return ret;
}
ll sumX(11 nodex, 11 tlx, 11 trx, 11 lx, 11 rx, 11 ly, 11 ry, 11 n, 11 m)
{
    if(lx>rx)
        return 0;
```

```
if(lx==tlx and rx==trx)
        return sumY(nodex, 1, 1, m, ly, ry, n, m);
    ll midx = (tlx+trx)/2; //if(!midx)midx++;
    11 ret = sumX(nodex*2,tlx,midx,lx,min(rx,midx),ly,ry,n,m)
        + sumX(nodex*2+1,midx+1,trx,max(lx,midx+1),rx,ly,ry,n,m);
    return ret;
}
void updateY(ll nodex, ll lx, ll rx, ll nodey, ll ly,
        11 ry, 11 x, 11 y, 11 new_val, 11 n, 11 m)
{
    if (ly == ry) {
        if (lx == rx)
            tree[nodex][nodey] = new_val;
        else
            tree[nodex][nodey] = tree[nodex*2][nodey] + tree[nodex*2+1][nodey];
    } else {
        11 \text{ my} = (1y + ry) / 2;
        if (y <= my)
            updateY(nodex, lx, rx, nodey*2, ly, my, x, y, new_val, n, m);
        else
            updateY(nodex, lx, rx, nodey*2+1, my+1, ry, x, y, new_val, n, m);
        tree[nodex][nodey] = tree[nodex][nodey*2] + tree[nodex][nodey*2+1];
    }
}
void updateX(11 nodex, 11 lx, 11 rx, 11 x, 11 y, 11 new_val, 11 n, 11 m)
    if (lx != rx) {
        11 mx = (1x + rx) / 2;
        if (x \le mx)
            updateX(nodex*2, lx, mx, x, y, new_val, n, m);
        else
            updateX(nodex*2+1, mx+1, rx, x, y, new_val, n, m);
    updateY(nodex, lx, rx, 1, 1, m, x, y, new_val, n, m);
}
int main()
    ll n,m,t,i,j,k,a,b,c,d,cs=1;
    cin >> n >> m;
    for(i=1;i<=n;i++)
        for(j=1;j<=m;j++)
            cin>> val[i][j];
```

```
buildX(1,1,n,n,m);

cin>> t;
while(t--){
    cin>> cs;
    if(!cs){
        cin>> a >> b >> c >> d;
        cout<< sumX(1,1,n,a,b,c,d,n,m) << endl;
    }
    else{
        cin>> a >> b >> c;
        updateX(1,1,n,a,b,c,n,m);
    }
}

return 0;
}
```

1.5 Maximum Bracket Sequence Using Segment Tree

```
/** Maximum correct bracket subsequence in a Range **/
struct info{
    11 maxBrac,unFB,unSB;
};
string str;
info tree[MX*3];
void init(ll node, ll b, ll e)
    stack<char>Q;
    for(ll i=b;i<=e;i++){</pre>
         if(str[i]=='(')
             Q.push(str[i]);
         else{
             if(Q.empty())
                 tree[node].unSB++;
             else{
                 Q.pop();
                 tree[node].maxBrac+=2;
        }
    }
    tree[node].unFB=Q.size();
    if (b == e) {
        return;
    ll Left = node * 2;
    ll Right = node * 2 + 1;
    11 \text{ mid} = (b + e) / 2;
    init(Left, b, mid);
    init(Right, mid + 1, e);
info query(ll node, ll b, ll e, ll i, ll j)
    info tmp;
    tmp.maxBrac=tmp.unFB=tmp.unSB=0;
    if (i > e \mid \mid j < b)
        return tmp;
    if (b >= i && e <= j)</pre>
        return tree[node];
```

```
11 Left = node * 2;
    11 Right = node * 2 + 1;
    11 \text{ mid} = (b + e) / 2;
    info p1 = query(Left, b, mid, i, j);
    info p2 = query(Right, mid + 1, e, i, j);
    tmp.maxBrac = p1.maxBrac+p2.maxBrac;
    tmp.maxBrac += min(p1.unFB,p2.unSB)*2;
    tmp.unFB = p1.unFB+p2.unFB-min(p1.unFB,p2.unSB);
    tmp.unSB = p1.unSB+p2.unSB-min(p1.unFB,p2.unSB);
    return tmp;
}
int main()
{
    fast_io;
    11 n,m,t,i,j,k,a,b,c,cs=1;
    //freopen(input.txt, r, stdin);
    //freopen(output.txt, w, stdout);
    cin>> str;
    cin>> m;
    init(1,0,str.size()-1);
    while(m--){
        cin>> a >> b;
        info res=query(1,0,str.size()-1,--a,--b);
        cout << res.maxBrac << endl;</pre>
    }
    return 0;
}
```

1.6 MO's Algorithm

```
const 11 block=320;
struct Query
    11 1,r,id;
    Query() {}
    Query(ll a, ll b, ll c)
        l=a, r=b, id=c;
    bool operator< (const Query &rhs)</pre>
        ll block_a = 1/block, block_b = rhs.1/block;
        if(block_a==block_b)
             return (r<rhs.r)^(block_a&1);</pre>
        return block_a < block_b;</pre>
    }
};
ll l=0,r=-1,res=0;
11 cnt[MX];
vll val;
void add(ll x)
    if(!cnt[val[x]])
        res++;
    cnt[val[x]]++;
}
void remove(ll x)
    if(cnt[val[x]]==1)
        res--;
    cnt[val[x]]--;
}
int main()
    FIO;
//
      IN;
//
      OUT;
    11 N;
```

```
cin>> N;
    val.resize(N);
    for(ll i=0; i<N; i++)</pre>
        cin>> val[i];
    11 Q;
    cin>> Q;
    11 ans[Q];
    vector < Query > qq(Q);
    for(ll i=0; i<Q; i++)</pre>
        cin>> qq[i].1 >> qq[i].r, qq[i].id=i, qq[i].1--, qq[i].r--;
    sort(all(qq));
    for(11 i=0; i<Q; i++)</pre>
        while(1 > qq[i].1) add(--1);
        while(r < qq[i].r) add(++r);
        while(1 < qq[i].1) remove(1++);</pre>
         while(r > qq[i].r) remove(r--);
         ans[qq[i].id]=res;
    }
    for(ll i=0;i<Q;i++) cout<< ans[i] << "\n";</pre>
}
```

1.7 MO's Algorithm On Tree

```
Count on a tree II
                 LCA, MO, DFS
                 how many different integers that represent
                 the weight of nodes there are on the path from u to v
11 block=200;
struct Query
    11 1,r,id;
    11 type;
    Query() {}
    Query(ll a, ll b, ll c)
        l=a, r=b, id=c;
    bool operator < (const Query &rhs)
        11 block_a = 1/block, block_b = rhs.1/block;
        if(block_a==block_b)
            return (r<rhs.r)^(block_a&1);</pre>
        return block_a < block_b;</pre>
    }
};
11 1=0,r=-1,res=0;
ll cur=-1;
11 val[3*MX], cnt[MX], node[MX], vcnt[MX];
bool vis[MX];
vll G[MX];
pll somoy[MX];
11 level[MX],sparse[MX][22],par[MX];
inline void BFS(11 s)
{
    memset(vis, false, sizeof vis);
    queue < 11 > Q;
    Q.push(s);
    par[s]=s;
    vis[s]=true;
    while(!Q.empty()){
        11 u=Q.front();
        Q.pop();
```

```
for(auto v:G[u]){
             if(vis[v])
                 continue;
             par[v]=u;
             vis[v]=true;
             Q.push(v);
             level[v]=level[u]+1;
        }
    }
}
inline void LCA_InIt(ll N, ll root)
    BFS(root);
    memset(sparse, -1, sizeof sparse);
    for(ll i=1;i<=N;i++)</pre>
        sparse[i][0]=par[i];
    for(ll j=1;(1<<j)<=N;j++)</pre>
        for(ll i=1;i<=N;i++)</pre>
             if(sparse[i][j-1]!=-1)
                 sparse[i][j]=sparse[sparse[i][j-1]][j-1];
}
inline 11 LCA_query(11 N, 11 u, 11 v)
    if(level[u] < level[v])</pre>
        swap(u,v);
    ll log=1;
    while(true){
        11 next=log+1;
        if((1<<next)>level[u])
             break;
        log++;
    }
    for(ll i=log;i>=0;i--)
        if(level[u]-(1<<i)>=level[v])
             u=sparse[u][i];
    if(u==v)
        return u;
    for (ll i = log; i >= 0; i--)
        if (sparse[u][i] != -1 && sparse[u][i] != sparse[v][i])
```

```
u = sparse[u][i], v = sparse[v][i];
    return par[u];
}
void DFS(11 u)
    somoy[u].ff=++cur;
    val[cur]=u;
    vis[u]=true;
    for(auto v:G[u]){
        if(!vis[v])
            DFS(v);
    somoy[u].ss=++cur;
    val[cur]=u;
}
inline void add(ll x)
    cnt[val[x]]++;
    if(cnt[val[x]]==2){
        vcnt[node[val[x]]]--;
        if(!vcnt[node[val[x]]]) res--;
    }
    else{
        vcnt[node[val[x]]]++;
        if(vcnt[node[val[x]]]==1) res++;
    }
}
inline void remove(ll x)
    cnt[val[x]]--;
    if(cnt[val[x]]==1){
        vcnt[node[val[x]]]++;
        if(vcnt[node[val[x]]]==1) res++;
    }
    else{
        vcnt[node[val[x]]]--;
        if(!vcnt[node[val[x]]]) res--;
    }
}
int main()
//
      IN;
```

```
//
      OUT;
    11 N,Q;
    while(scanf("%1ld %1ld",&N,&Q)!=EOF){
        memset(cnt,0,sizeof cnt);
        memset(vcnt,0,sizeof vcnt);
        memset(sparse,-1,sizeof sparse);
        for(ll i=0;i<MX;i++) G[i].clear();</pre>
        cur=-1, res=0;
        1=0, r=-1;
        ordered_set ost;
        for(ll i=1; i<=N; i++)</pre>
             scanf("%lld",&node[i]),ost.insert(node[i]);
        for(ll i=1;i<=N;i++) node[i]=ost.order_of_key(node[i]);</pre>
        for(ll i=0;i<N-1;i++){
            11 u,v;
            scanf("%lld %lld",&u,&v);
            G[u].push_back(v);
            G[v].push_back(u);
        }
        block=sqrt(N)+1;
        DFS(1);
        LCA_InIt(N,1);
        11 ans[Q];
        vector < Query > qq(Q);
        for(ll i=0; i<Q; i++){
            11 u, v;
            qq[i].id=i;
            scanf("%lld %lld",&u,&v);
            if(somoy[u].ff>somoy[v].ff) swap(u,v);
            11 lca=LCA_query(N,u,v);
            if(lca==u)
                 qq[i].l=somoy[u].ff,qq[i].r=somoy[v].ff,qq[i].type=0;
            else
                 qq[i].l=somoy[u].ss,qq[i].r=somoy[v].ff,qq[i].type=lca;
        }
        sort(all(qq));
        for(ll i=0; i<Q; i++)</pre>
            while(1 > qq[i].1) add(--1);
            while(r < qq[i].r) add(++r);
            while (1 < qq[i].1) remove (1++);
```

2 Graph

2.1 Dijkstra

```
struct comp{
    bool operator() (const pii(ll,ll) &a, const pii(ll,ll) &b)
        return a.sd > b.sd;
    }
};
priority_queue<pii(l1,l1), vctr(pii(l1,l1)), comp>Q;
vctr(pii(l1,l1)) edg[MX];
11 dis[MX];
bool vis[MX];
int main()
    ll n,m,a,b,c,t,i,j,k,beg;
    string s;
    cin>> n >> m;
    while(m--){
        cin>> a >> b >> c;
        edg[a].pb(mkpr(b,c));
        edg[b].pb(mkpr(a,c));
    }
    beg=1;
    loop(i,n)
        dis[i]=INF, vis[i]=false;
    dis[beg]=0;
    Q.in(mkpr(beg,0));
    while(!Q.empty()){
        11 a=Q.top().ft;
        Q.out();
        if(vis[a])
            continue;
        k=edg[a].size();
        loop(i,k){
            b=edg[a][i-1].ft;
            c=edg[a][i-1].sd;
            if(!vis[b] && dis[b]>dis[a]+c){
                dis[b]=dis[a]+c;
                Q.in(mkpr(b,dis[b]));
            }
```

```
}
    vis[a]=true;
}

cout<< dis[n] << endl;

loop(i,n)
    edg[i].clear();
while(!Q.empty())Q.out();

return 0;
}</pre>
```

2.2 Minimum Spanning Tree-Krushkal

```
struct edge{
    11 u, v, w;
    bool operator < (const edge& a) const
        return w < a.w;</pre>
    }
};
vctr(edge) ed;
11 par[MX];
11 find(ll n)
    if(n==par[n])
        return par[n];
    return par[n]=find(par[n]);
}
11 MST(11 n)
    11 i,j;
    sort(ed.begin(),ed.end());
    loop(i,n)
        par[i]=i;
    11 cnt=0,s=0,m=(11)ed.size();
    for(i=0;i<m;i++){</pre>
        11 u=find(ed[i].u);
        11 v=find(ed[i].v);
        if(u!=v){
             par[u]=v;
             cnt++;
             s+=ed[i].w;
             if(cnt==n-1)
                 break;
        }
    }
    return s;
}
int main()
```

```
{
    ll n,m,a,b,c,t,i,j,k;
    string s;

    cin>> n >> m;

    while(m--){
        cin>> a >> b >> c;

        edge tmp;
        tmp.u=a,tmp.v=b,tmp.w=c;
        ed.pb(tmp);
}

cout << MST(n);

return 0;
}</pre>
```

2.3 Strongly Connected Component

```
#define WHITE 1
#define GRAY 2
vector<11>edge[MX],revEdge[MX],components[MX];
11 color[MX], mark;
stack<11>Q;
bool visited[MX];
void DFS1(ll node)
    color[node] = GRAY;
    for(auto u: edge[node])
        if(color[u] == WHITE)
             DFS1(u);
    Q.push(node);
void DFS2(11 node, 11 mark)
    components[mark].pb(node);
    visited[node]=true;
    cout << node << endl;</pre>
    for(auto u: revEdge[node])
        if(!visited[u])
             DFS2(u,mark);
}
void findSSC(ll nodes)
{
    11 i;
    while(!Q.empty())
         Q.pop();
    for(i=0;i<MX;i++)</pre>
         visited[i]=false,color[i]=WHITE;
    for(i=0;i<MX;i++)</pre>
         components[i].clear();
    for(i=1;i<=nodes;i++)</pre>
         if(color[i] == WHITE)
             DFS1(i);
```

```
while(!Q.empty()){
        11 u=Q.top();
        Q.pop();
         if(!visited[u]){
             mark++;
             DFS2(u,mark);
    }
}
int main()
{
    ll n,m,t,i,j,k,a,b,c,cs=1;
    //freopen("input.txt", "r", stdin);
    //freopen("output.txt", "w", stdout);
    cin>> n >> m;
    for(i=0;i<m;i++){</pre>
        cin>> a >> b;
        a++,b++;
        edge[a].pb(a);
        revEdge[a].pb(b);
    }
    mark=0;
    findSSC(n);
    for(i=1;i<=mark;i++){</pre>
        for(auto x:components[i])
             cout << x << " ";
        cout << components[i].size() << "\n";</pre>
    cout << endl;</pre>
    return 0;
}
```

2.4 Topological Sort

```
vctr(ll) edge[MX];
11 inDegree[MX];
bool compare(ll a, ll b)
    return inDegree[a] < inDegree[b];</pre>
}
vctr(ll) TopSort(ll n)
    vctr(ll) node,ans;
    for(ll i=1;i<=n;i++)</pre>
        node.pb(i);
    sort(node.begin(),node.end(),compare);
    queue<11>q;
    for(ll i=0;i<n;i++){</pre>
        if(inDegree[node[i]])
             break;
        q.push(node[i]);
    }
    while(!q.empty()){
        11 u=q.front();
        q.pop();
        ans.pb(u);
        11 x=edge[u].size();
        for(11 i=0;i<x;i++){</pre>
             ll v=edge[u][i];
             inDegree[v]--;
             if(!inDegree[v])
                 q.push(v);
        }
    }
    return ans;
}
int main()
    ll n,m,a,b,c,t,i,j,k;
    string s;
```

```
cin>> n >> m;

for(i=0;i<m;i++){
    cin>> a >> b;
    edge[a].pb(b);
    inDegree[b]++;
}

vctr(ll) ans=TopSort(n);

for(i=0;i<ans.size();i++)
    cout<< ans[i] << ' ';

return 0;
}</pre>
```

2.5 Heavy Light Decomposition

```
class Segment_Tree{
    11 N;
    struct Node{
        11 prop,sum;
        Node() {}
        Node(ll p, ll s)
            prop=p,sum=s;
    };
    vector < Node > val;
public:
    Segment_Tree(ll n)
        Node nd(0,0);
        N=(n+5)*4;
        val.assign(N,nd);
    }
    Segment_Tree(vll arr) : Segment_Tree(arr.size())
    {
        for(ll i=0;i<arr.size();i++)</pre>
            update(1,1,N,i+1,i+1,arr[i]);
    void update(ll id, ll b, ll e, ll i, ll j, ll x)
        if (i > e || j < b)
            return;
        if (b >= i && e <= j)
            val[id].sum = x;
            return;
        }
        ll Left = id << 1;</pre>
        11 Right = (id << 1) + 1;</pre>
        11 \text{ mid} = (b + e) >> 1;
        update(Left, b, mid, i, j, x);
        update(Right, mid + 1, e, i, j, x);
        val[id].sum = max( val[Left].sum , val[Right].sum );
```

```
}
    ll query(ll id, ll b, ll e, ll i, ll j)
        if (i > e \mid \mid j < b)
             return -INF;
         if (b \ge i \text{ and } e \le j)
             return val[id].sum;
        ll Left = id << 1;</pre>
        11 Right = (id << 1) + 1;</pre>
        11 \text{ mid} = (b + e) >> 1;
        ll p1 = query(Left, b, mid, i, j);
        11 p2 = query(Right, mid + 1, e, i, j);
        return max( p1 , p2 );
    }
};
vector<pair<pl1,11> > G[MX];
vll root;
bool vis[MX];
11 par[MX],level[MX],sparse[MX][22];
11 heavy[MX],subsize[MX];
11 chain_heads[MX*2];
11 base_array[MX*2];
11 edge_counted;
ll chain_size;
Segment_Tree seg(MX);
struct treeNode{
    11 par;
    11 depth;
    11 subtree;
    11 pos_seg;
    ll chain;
}node[MX];
struct Edge{
    ll weight;
    11 deep_node;
}edge[MX];
void DFS(ll u, ll p, ll lvl)
```

```
{
    vis[u]=true;
    par[u]=p,level[u]=lvl;
    subsize [u]=1, heavy [u]=-1;
    11 mx=0;
    for(auto x:G[u]){
        11 v=x.ff.ff;
        if(!vis[v]){
            DFS(v,u,lvl+1);
             subsize[u]+=subsize[v];
            if(subsize[v]>mx) mx=subsize[v],heavy[u]=v;
        }
    }
    node[u].par=p;
    node[u].depth=lvl;
    node[u].subtree=subsize[u];
}
void LCA_Build(ll N)
    memset(vis,false,sizeof vis);
    for(auto r:root) if(!vis[r]) DFS(r,-1,0);
    memset(sparse, -1, sizeof sparse);
    for(ll i=1;i<=N;i++) sparse[i][0]=par[i];</pre>
    for(ll log=1;(1<<log)<=N;log++)</pre>
        for(ll i=1;i<=N;i++)
            if(sparse[i][log-1]!=-1)
                 sparse[i][log]=sparse[sparse[i][log-1]][log-1];
}
11 LCA_Query(11 N, 11 u, 11 v)
    if(level[u] < level[v]) swap(u,v);</pre>
    11 log=1;
    while(true){
        11 next=log+1;
        if((1<<next)>level[u]) break;
        log++;
    }
    for(11 i=log;i>=0;i--)
        if(level[u]-(1<<i)>=level[v])
            u=sparse[u][i];
```

```
if(u==v) return u;
    for (ll i=log;i>=0;i--)
        if (sparse[u][i]!=-1 and sparse[u][i]!=sparse[v][i])
           u=sparse[u][i], v=sparse[v][i];
    return par[u];
}
11 kth_Parent(ll N, ll u, ll K)
    if(level[u] < K) return -1;</pre>
    if(!K) return u;
    11 x;
    for(ll i=0;(1<<i)<=N;i++){</pre>
        if(sparse[u][i]!=-1 and (1<<i)>K)
            break;
        x=i;
    }
    return kth_Parent(N,sparse[u][x],K-(1<<x));</pre>
}
void HLD(ll cur_node, ll cost)
{
    vis[cur_node]=true;
    if (chain_heads[chain_size] == -1) chain_heads[chain_size] = cur_node;
    node[cur_node].chain=chain_size;
    node[cur_node].pos_seg=edge_counted;
    base_array[edge_counted]=cost;
    11 cc;
    for(auto x:G[cur_node]){
        if(x.ff.ff==heavy[cur_node]){
            cc=x.ff.ss;
            edge[x.ss].deep_node=heavy[cur_node];
            edge[x.ss].weight=x.ff.ss;
        }
    }
    if(heavy[cur_node]!=-1) ++edge_counted, HLD(heavy[cur_node],cc);
    for(auto x:G[cur_node]){
        11 v=x.ff.ff;
```

```
if(!vis[v] and v!=heavy[cur_node]){
            ++edge_counted,++chain_size;
            HLD(v,x.ff.ss);
            edge[x.ss].deep_node=v;
            edge[x.ss].weight=x.ff.ss;
        }
    }
}
ll crawl_tree(ll u, ll v)
    11 chain_u,chain_v=node[v].chain,ans=-INF;
    if(level[u] < level[v]) swap(u,v);</pre>
    while(true){
        chain_u=node[u].chain;
        if(chain_u==chain_v){
            11 cur=seg.query(1,1,edge_counted,node[v].pos_seg+1,node[u].pos_seg);
            if(u!=v) ans=max(ans,cur);
            break;
        }
        ll cur=seg.query(1,1,edge_counted,
                        node[chain_heads[chain_u]].pos_seg,node[u].pos_seg);
        ans=max(ans,cur);
        u=node[chain_heads[chain_u]].par;
    }
    return ans;
}
void change(ll edge_no, ll val)
    11 pos=node[edge[edge_no].deep_node].pos_seg;
    11 cur=edge[edge_no].weight;
    seg.update(1,1,edge_counted,pos,pos,val);
        edge[edge_no].weight = val;
}
ll max_edge(ll u, ll v, ll N)
    11 lca=LCA_Query(N,u,v);
    return max(crawl_tree(u,lca),crawl_tree(v,lca));
}
```

```
void setup(ll N)
    LCA_Build(N);
    memset(vis,false,sizeof vis);
    for(auto r:root) HLD(r,-1);
    for(ll i=1;i<=edge_counted;i++) seg.update(1,1,edge_counted,i,i,base_array[i]);</pre>
}
void reset()
    for(ll i=0;i<MX;i++) G[i].clear();</pre>
    memset(chain_heads,-1,sizeof chain_heads);
    root.clear();
    edge_counted=1,chain_size=1;
}
int main()
//
      FIO;
      IN;
      OUT;
    11 T;
    scanf("%lld",&T);
    while(T--){
        11 N;
        scanf("%lld",&N);
        reset();
        root.push_back(1);
        for(ll i=1;i<=N-1;i++){</pre>
            ll u, v, w;
             scanf("%11d %11d %11d",&u,&v,&w);
            G[u].push_back({{v,w},i});
            G[v].push_back({{u,w},i});
        }
        setup(N);
        char str[10];
        while(true){
             scanf("%s",str);
             if(str[0] == 'D') break;
```

2.6 Maximum Flow

```
// Adjacency list implementation of FIFO push relabel maximum flow
// with the gap relabeling heuristic. This implementation is
// significantly faster than straight Ford-Fulkerson. It solves
// random problems with 10000 vertices and 1000000 edges in a few
// seconds, though it is possible to construct test cases that
// achieve the worst-case.
//
// Running time:
      0(|V|^3)
//
// INPUT:
//
       - graph, constructed using AddEdge()
//
       - source
//
       - sink
//
// OUTPUT:
       - maximum flow value
//
       - To obtain the actual flow values, look at all edges with
//
         capacity > 0 (zero capacity edges are residual edges).
struct Edge {
    ll from, to, cap, flow, index;
    Edge(ll from, ll to, ll cap, ll flow, ll index) :
    from(from), to(to), cap(cap), flow(flow), index(index) {}
};
struct PushRelabel {
    11 N;
    vector<vector<Edge> > G;
    vector<ll> excess;
    vector<ll> dist, active, count;
    queue <11> Q;
    PushRelabel(11 N): N(N), G(N), excess(N), dist(N), active(N), count(2*N) {}
    void AddEdge(ll from, ll to, ll cap) {
        G[from].push_back(Edge(from, to, cap, 0, G[to].size()));
        if (from == to) G[from].back().index++;
        G[to].push_back(Edge(to, from, 0, 0, G[from].size() - 1));
    void Enqueue(ll v) {
        if (!active[v] && excess[v] > 0) { active[v] = true; Q.push(v); }
    void Push(Edge &e) {
```

```
11 amt = ll(min(excess[e.from], ll(e.cap - e.flow)));
    if (dist[e.from] <= dist[e.to] || amt == 0) return;</pre>
    e.flow += amt;
    G[e.to][e.index].flow -= amt;
    excess[e.to] += amt;
    excess[e.from] -= amt;
    Enqueue(e.to);
void Gap(ll k) {
    for (11 v = 0; v < N; v++) {
        if (dist[v] < k) continue;</pre>
        count[dist[v]]--;
        dist[v] = max(dist[v], N+1);
        count[dist[v]]++;
        Enqueue(v);
    }
}
void Relabel(ll v) {
    count[dist[v]]--;
    dist[v] = 2*N;
    for (ll i = 0; i < G[v].size(); i++)</pre>
        if (G[v][i].cap - G[v][i].flow > 0)
    dist[v] = min(dist[v], dist[G[v][i].to] + 1);
    count[dist[v]]++;
    Enqueue(v);
}
void Discharge(ll v) {
    for (11 i = 0; excess[v] > 0 && i < G[v].size(); i++) Push(G[v][i]);
    if (excess[v] > 0) {
        if (count[dist[v]] == 1)
        Gap(dist[v]);
            else
        Relabel(v);
    }
}
11 GetMaxFlow(ll s, ll t) {
    count[0] = N-1;
    count[N] = 1;
    dist[s] = N;
    active[s] = active[t] = true;
    for (ll i = 0; i < G[s].size(); i++) {</pre>
        excess[s] += G[s][i].cap;
        Push(G[s][i]);
    }
```

```
while (!Q.empty()) {
          11 v = Q.front();
          Q.pop();
          active[v] = false;
          Discharge(v);
       }
       11 totflow = 0;
       for (ll i = 0; i < G[s].size(); i++) totflow += G[s][i].flow;
       return totflow;
   }
};
// BEGIN CUT
int main()
   11 n,m;
   cin>> n >> m;
   PushRelabel pr(n);
   for(11 i=0;i<m;i++){</pre>
       ll a,b,c;
       cin>> a >> b >> c;
       if(a==b)
          continue;
       pr.AddEdge(a-1,b-1,c);
       pr.AddEdge(b-1,a-1,c);
   cout << pr.GetMaxFlow(0,n-1);</pre>
   return 0;
}
```

2.7 Maximum Bipartite Matching

```
// Adjacency list implementation of FIFO push relabel maximum flow
// with the gap relabeling heuristic. This implementation is
// significantly faster than straight Ford-Fulkerson. It solves
// random problems with 10000 vertices and 1000000 edges in a few
// seconds, though it is possible to construct test cases that
// achieve the worst-case.
//
// Running time:
      0(|V|^3)
//
// INPUT:
//
       - graph, constructed using AddEdge()
//
       - source
//
       - sink
//
// OUTPUT:
       - maximum flow value
//
       - To obtain the actual flow values, look at all edges with
//
         capacity > 0 (zero capacity edges are residual edges).
struct Edge {
    ll from, to, cap, flow, index;
    Edge(ll from, ll to, ll cap, ll flow, ll index) :
    from(from), to(to), cap(cap), flow(flow), index(index) {}
};
struct PushRelabel {
    11 N;
    vector<vector<Edge> > G;
    vector<ll> excess;
    vector<ll> dist, active, count;
    queue <11> Q;
    PushRelabel(11 N): N(N), G(N), excess(N), dist(N), active(N), count(2*N) {}
    void AddEdge(ll from, ll to, ll cap) {
        G[from].push_back(Edge(from, to, cap, 0, G[to].size()));
        if (from == to) G[from].back().index++;
        G[to].push_back(Edge(to, from, 0, 0, G[from].size() - 1));
    void Enqueue(ll v) {
        if (!active[v] && excess[v] > 0) { active[v] = true; Q.push(v); }
    void Push(Edge &e) {
```

```
11 amt = ll(min(excess[e.from], ll(e.cap - e.flow)));
    if (dist[e.from] <= dist[e.to] || amt == 0) return;</pre>
    e.flow += amt;
    G[e.to][e.index].flow -= amt;
    excess[e.to] += amt;
    excess[e.from] -= amt;
    Enqueue(e.to);
void Gap(ll k) {
    for (11 v = 0; v < N; v++) {
        if (dist[v] < k) continue;</pre>
        count[dist[v]]--;
        dist[v] = max(dist[v], N+1);
        count[dist[v]]++;
        Enqueue(v);
    }
}
void Relabel(11 v) {
    count[dist[v]]--;
    dist[v] = 2*N;
    for (ll i = 0; i < G[v].size(); i++)</pre>
        if (G[v][i].cap - G[v][i].flow > 0)
    dist[v] = min(dist[v], dist[G[v][i].to] + 1);
    count[dist[v]]++;
    Enqueue(v);
}
void Discharge(ll v) {
    for (11 i = 0; excess[v] > 0 && i < G[v].size(); i++) Push(G[v][i]);
    if (excess[v] > 0) {
        if (count[dist[v]] == 1)
        Gap(dist[v]);
            else
        Relabel(v);
    }
}
11 GetMaxFlow(ll s, ll t) {
    count[0] = N-1;
    count[N] = 1;
    dist[s] = N;
    active[s] = active[t] = true;
    for (ll i = 0; i < G[s].size(); i++) {</pre>
        excess[s] += G[s][i].cap;
        Push(G[s][i]);
    }
```

```
while (!Q.empty()) {
             11 v = Q.front();
            Q.pop();
             active[v] = false;
            Discharge(v);
        }
        11 \text{ totflow} = 0;
        for (ll i = 0; i < G[s].size(); i++) totflow += G[s][i].flow;
        return totflow;
    }
};
// BEGIN CUT
// The following code solves SPOJ problem #4110: Fast Maximum Flow (FASTFLOW)
struct info{
    11 age,height,divocee;
};
int main()
{
    fast_io;
    ll n,m,t,i,j,k,a,b,c,cs=1;
    //freopen(input.txt, r, stdin);
    //freopen(output.txt, w, stdout);
    cin>> t;
    for(cs=1;cs<=t;cs++){
        cin>> n >> m;
        PushRelabel pr(n+m+2);
        vector < info > man(n), woman(m);
        for(i=0;i<n;i++)
             cin>> man[i].height >> man[i].age >> man[i].divocee;
        for(i=0;i<m;i++)</pre>
             cin>> woman[i].height >> woman[i].age >> woman[i].divocee;
        for(i=0;i<n;i++){
             for(j=0;j<m;j++){
                 if(fabs(man[i].height-woman[j].height) <= 12 and</pre>
                         fabs(man[i].age-woman[j].age) <= 5 and</pre>
                         man[i].divocee==woman[j].divocee){
```

```
pr.AddEdge(i+1,j+1+n,1);
                     //pr.AddEdge(j+1+n,i+1,1);
                 }
             }
        }
        for(i=0;i<n;i++){
             pr.AddEdge(0,i+1,1);
             pr.AddEdge(i+1,0,1);
        for(i=0;i<m;i++){</pre>
             pr.AddEdge(i+1+n,n+m+1,1);
             pr.AddEdge(n+m+1,i+1+n,1);
        }
         /*for(i=0;i < m;i++){}
             cin >> a >> b >> c;
             if(a==b)
                 continue;
             pr.AddEdge(a-1,b-1,c);
             pr.AddEdge(b-1,a-1,c);
        }*/
        cout << "Case " << cs << ": ";
        cout << pr.GetMaxFlow(0,n+m+1) << "\n";</pre>
    }
    return 0;
}
```

3 String

3.1 Hashing

```
#include <bits/stdc++.h>
using namespace std;
#define pb push_back
typedef long long int 11;
typedef pair < int,int > PII;
typedef pair < 11,11 > PLL;
#define F first
#define S second
ostream& operator << (ostream & os, PLL h)
        return os << "( " << h.F << ", " << h.S << " )" << endl;
PLL operator+ (PLL a, ll x)
                                 \{\text{return } \{\text{a.F} + x, \text{a.S} + x\} ;\}
                                 {return {a.F - x, a.S - x} ;}
PLL operator- (PLL a, ll x)
PLL operator* (PLL a, ll x)
                                 {return {a.F * x, a.S * x} ;}
PLL operator+(PLL x, PLL y) { return {x.F + y.F,x.S + y.S} ;}
PLL operator-(PLL x,PLL y) { return {x.F - y.F, x.S - y.S} ;}
PLL operator*(PLL x,PLL y) { return {x.F * y.F , x.S * y.S} ;}
PLL operator%(PLL x,PLL y) { return {x.F % y.F, x.S % y.S} ;}
PLL base = \{37,41\};
PLL M = \{1000000021, 1e9 + 9 \};
int const MX = 2e6 + 10;
PLL P[MX];
PLL h[MX] ;
map < PLL, int > mp;
PLL Hash(string &s)
    PLL hh = \{0,0\};
    for(int i = 0; i < s.size(); i++)</pre>
        hh = (hh * base + (s[i] - 'a' + 1)) \% M ;
    //cout << hh << endl;
    return hh ;
}
```

```
PLL sub(int 1,int r)
    return ( (h[r] - (h[l-1]*P[r-l+1])) % M + M ) % M;
int main()
    ios::sync_with_stdio(false);
    cin.tie(0);
    P[0] = \{1,1\};
    for(int i = 1; i < MX; i++)</pre>
        P[i] = (P[i-1] * base) % M;
    int n,k;
    cin >> n >> k;
    string s;
    cin >> s;
    s += s;
    h[0] = \{0,0\};
    for(int i = 0; i < s.size(); i++){</pre>
        h[i+1] = (h[i] * base + (ll)(s[i] - 'a' + 1))% M;
    }
    int g;
    cin >> g;
    for(int i = 0; i < g; i++)
        string s;
        cin >> s;
        //cout << Hash(s) << endl;
        mp[Hash(s)] = i+1;
    vector < int > ans;
    vector < bool > vis(g+1,0);
    bool f = 0;
    for(int i = 1; i <= k && !f ; i++){
        ans.clear();
        int cnt = 0;
        for(int j = i,cnt = 1; j + k - 1 \le s.size() and cnt \le n; j += k, cnt++){
```

```
PLL tempHash = sub(j,j+k-1);
              //cout << tempHash << endl;</pre>
               \  \  \  \  \  if (mp.count(tempHash) \ \ and \ \ !vis[mp[tempHash]]) \{ \\
                  ans.pb(mp[tempHash]);
                  vis[mp[tempHash]] = 1;
              }
         }
         if(ans.size() == n){
              f = 1;
              break;
         for(int i =0 ; i < ans.size(); i++)</pre>
              vis[ans[i]] = 0;
    }
    if(!f){
         return cout << "NO", 0 ;</pre>
    cout << "YES" << '\n';
    for(auto x: ans)
         cout << x << " ";
    cout << endl;</pre>
    return 0;
}
```

3.2 Knuth-Moriss-Pitt

```
vll pref_func(string str)
    11 n=str.size();
    vll v(n);
    v[0]=0;
    for(ll i=1,j=0;i<n;i++){</pre>
         while(j>0 and str[i]!=str[j])
             j = v[j-1];
         if(str[i]==str[j])
             j++;
        v[i]=j;
    }
    return v;
}
int main()
    11 n,m,t,i,j,k,a,b,c,cs=1;
    string text, str;
    cin>> text >> str;
    vll pf=pref_func(str);
    vll res;
    for(i=0,j=0;i<text.size();i++){</pre>
        while(j>0 and text[i]!=str[j])
                  j=pf[j-1];
         if(str[j]==text[i])
             j++;
         if(j==str.size()){
             res.pb(i-j);
             j=pf[j-1];
        }
    }
    if(j==str.size())
        res.pb(i-j);
    cout << res.size() << endl;</pre>
    for(i=0;i<res.size();i++)</pre>
         cout << res[i] +1 << ' ';
    cout << endl;</pre>
```

```
return 0;
}
```

3.3 Z Function

```
vll z_func(string str)
    11 n=str.size();
    vll z(n);
    z[0]=0;
    for(ll i=1,l=0,r=0;i<n;i++){</pre>
        if(i<=r)
             z[i]=min(r-i+1,z[i-1]);
        while(i+z[i] \le n and str[z[i]] = str[i+z[i]])
             z[i]++;
        if(i+z[i]-1>r)
             l=i,r=i+z[i]-1;
    }
    return z;
}
int main()
    fast_io;
    11 n,m,t,i,j,k,a,b,c,cs=1;
    //freopen(input.txt, r, stdin);
    //freopen(output.txt, w, stdout);
    string str;
    cin>> str;
    vll zf=z_func(str);
    for(i=0;i<str.size();i++)</pre>
        cout << zf[i] << ' ';
    cout << endl;</pre>
    return 0;
}
```

3.4 Xor Maximization Using Trie Tree

```
const 11 K=2;
struct Node{
    11 next[K];
    bool leaf=false;
    Node()
        memset(next, -1, sizeof next);
};
vector < Node > tr(1);
void add_String(string str)
    11 v=0;
    for(auto ch: str)
        11 c=ch-'0';
        if(tr[v].next[c]==-1){
            tr[v].next[c]=tr.size();
            tr.emplace_back();
        v=tr[v].next[c];
    tr[v].leaf=true;
}
11 find_max_xor(string s)
    11 root=0;
    11 val=0;
    for(ll i=0;i<s.size();i++){</pre>
        if(s[i]=='0'){
            if(tr[root].next[1]!=-1){
                 val=val*2+1;
                 root=tr[root].next[1];
            else if(tr[root].next[0]!=-1){
                 val=val*2;
                root=tr[root].next[0];
            else
```

```
val=val*2;
        }
        else{
             if(tr[root].next[0]!=-1){
                 val=val*2+1;
                 root=tr[root].next[0];
             else if(tr[root].next[1]!=-1){
                 val=val*2;
                 root=tr[root].next[1];
             }
             else
                 val=val*2;
        }
    }
    return val;
}
string make(ll n)
    string str;
    while(n){
        str+=n%2+48;
        n/=2;
    for(ll i=str.size();i<32;i++)</pre>
        str+=48;
    reverse(str.begin(),str.end());
    //cout << str << endl;</pre>
    return str;
}
int main()
    fast_io;
    ll n,m,t,i,j,k,a,b,c,cs=1;
    //freopen(input.txt, r, stdin);
    //freopen(output.txt, w, stdout);
    cin>> n;
    for(i=0;i<n;i++){</pre>
        cin>> a;
        string str=make(a);
```

```
add_String(str);
}

cin>> k;
string str=make(k);
cout<< find_max_xor(str);
return 0;
}</pre>
```

3.5 Aho Corasik

```
ll leaf_node[MX];
string text;
const 11 K = 26;
struct Vertex {
    11 next[K];
    bool leaf = false;
    11 p = -1;
    char pch;
    11 link = -1;
    ll go[K];
    vll pos;
    vll exit_link;
    11 cnt=0;
    bool check=false;
    Vertex(ll p=-1, char ch='$') : p(p), pch(ch) {
        fill(begin(next), end(next), -1);
        fill(begin(go), end(go), -1);
};
vector<Vertex> t(1);
void add_string(string const& s, ll pos) {
    11 v = 0;
    for (char ch : s) {
        11 c = ch - 'a';
        if (t[v].next[c] == -1) {
            t[v].next[c] = t.size();
            t.emplace_back(v, ch);
        v = t[v].next[c];
    t[v].pos.push_back(pos);
    t[v].leaf = true;
    leaf_node[pos]=v;
}
11 go(ll v, char ch);
ll get_link(ll v) {
    if (t[v].link == -1) {
        if (v == 0 || t[v].p == 0)
            t[v].link = 0;
```

```
else
            t[v].link = go(get_link(t[v].p), t[v].pch);
    return t[v].link;
}
11 go(ll v, char ch) {
    ll c = ch - 'a';
    if (t[v].go[c] == -1) {
        if (t[v].next[c] != -1)
            t[v].go[c] = t[v].next[c];
        else
            t[v].go[c] = v == 0 ? 0 : go(get_link(v), ch);
    }
    return t[v].go[c];
}
void DFS(ll pos, ll node)
    if(pos==text.size()) return;
    11 c = text[pos] - 'a';
    if(t[node].next[c]!=-1){
        t[t[node].next[c]].cnt++;
        DFS(pos+1,t[node].next[c]);
    else if(node) DFS(pos,get_link(node));
}
ll calc_count(ll node)
    if(t[node].check) return t[node].cnt;
    t[node].check=true;
    for(auto x:t[node].exit_link) t[node].cnt+=calc_count(x);
    return t[node].cnt;
}
int main()
//
      FIO;
//
      IN;
//
      OUT;
```

```
11 T;
    cin>> T;
    for(ll cs=1;cs<=T;cs++){</pre>
         11 n;
         cin>> n >> text;
         t.clear();
         t.push_back(Vertex());
         for(ll i=0;i<n;i++){</pre>
             string s;
             cin>> s;
             add_string(s,i);
         }
         for(ll i=0;i<t.size();i++){</pre>
             t[get_link(i)].exit_link.push_back(i);
         DFS(0,0);
         cout << "Case " << cs << ":\n";
         for(11 i=0;i<n;i++){</pre>
             cout << calc_count(leaf_node[i]) << "\n";</pre>
    }
}
```

3.6 Suffix Array Emax

```
vll sort_cyclic_shifts(string const& s)
    11 n=s.size();
    const 11 alp=256;
    vll p(n),c(n),cnt(max(alp,n),0);
    ll i,j,k,h;
    for(i=0;i<n;i++)
        cnt[s[i]]++;
    for(i=1;i<alp;i++)</pre>
        cnt[i]+=cnt[i-1];
    for(i=0;i<n;i++)
        p[--cnt[s[i]]]=i;
    11 classes=1;
    c[p[0]]=0;
    for(i=1;i<n;i++){
        if(s[p[i]]!=s[p[i-1]])
            classes++;
        c[p[i]]=classes-1;
    }
    vll pn(n),cn(n);
    for(h=0;(1<<h)<n;h++){
        for(i=0;i<n;i++){
            pn[i]=p[i]-(1<<h);
            if(pn[i]<0)
                 pn[i]+=n;
        }
        fill(cnt.begin(),cnt.begin()+classes,0);
        for(i=0;i<n;i++)
            cnt[c[pn[i]]]++;
        for (i=1;i<classes;i++)</pre>
            cnt[i]+=cnt[i-1];
        for (i=n-1;i>=0;i--)
            p[--cnt[c[pn[i]]]]=pn[i];
        cn[p[0]]=0;
        classes=1;
        for(i=1;i<n;i++){
            pll cur={c[p[i]],c[(p[i]+(1<<h))%n]};</pre>
            pll prev={c[p[i-1]],c[(p[i-1]+(1<<h))%n]};
            if(cur!=prev)
```

```
classes++;
            cn[p[i]]=classes-1;
        c.swap(cn);
    return p;
}
vll build_suffix_array(string s)
{
    s+='$';
    vll res=sort_cyclic_shifts(s);
    res.erase(res.begin());
    return res;
}
vll lcp_construction(string const& s, vll const& p) {
    ll n = s.size();
    vll rank(n, 0);
    for (11 i = 0; i < n; i++)
        rank[p[i]] = i;
    11 k = 0;
    vll lcp(n-1, 0);
    for (11 i = 0; i < n; i++) {
        if (rank[i] == n - 1) {
            k = 0;
            continue;
        ll j = p[rank[i] + 1];
        while (i + k < n && j + k < n && s[i+k] == s[j+k])
            k++;
        lcp[rank[i]] = k;
        if (k)
            k--;
    return lcp;
}
11 uniqueSubstrings(string str)
    11 n=str.size();
    vll sa=build_suffix_array(str);
    vll lcp=lcp_construction(str,sa);
    11 res=n-sa[0];
```

```
for(ll i=1;i<n;i++)</pre>
        res+=(n-sa[i])-lcp[i-1];
    res++;
    return res;
}
int main()
{
    ll n,m,t,i,j,k,a,b,c,cs=1;
    string str;
    cin>> str;
    vll res=build_suffix_array(str);
    for(i=0;i<res.size();i++)</pre>
        cout << res[i] << ' ';
    cout << endl;</pre>
    cout << uniqueSubstrings(str) << endl;</pre>
    return 0;
}
```

3.7 Suffix Array $O(n \log n)$

```
#include < bits / stdc++.h>
using namespace std;
string str;
11 N, m, SA [MX], LCP [MX];
ll x [MX], y [MX], w [MX], c [MX];
inline bool cmp (const ll a, const ll b, const ll l)
        return (y [a] == y [b] && y [a + 1] == y [b + 1]);
void Sort () {
    for (ll i = 0; i < m; ++i) w [i] = 0;
    for (ll i = 0; i < N; ++i) ++w [x [y [i]]];
    for (ll i = 0; i < m - 1; ++i) w [i + 1] += w [i];
    for (ll i = N - 1; i >= 0; --i) SA [--w [x [y [i]]]] = y [i];
}
void DA () {
    ++N;
    for (ll i = 0; i < N; ++i) x [i] = str [i], y[i] = i;
    Sort ();
    for (ll i, j = 1, p = 1; p < N; j \iff 1, m = p) {
        for (p = 0, i = N - j; i < N; i++) y [p++] = i;
        for (ll k = 0; k < N; ++k) if (SA [k] >= j) y [p++] = SA [k] - j;
        Sort ();
        for (swap (x, y), p = 1, x [SA [0]] = 0, i = 1; i < N; ++i)
                 x [SA [i]] = cmp (SA [i - 1], SA [i], j) ? p - 1 : p++;
    for (ll i = 1; i < N; ++i) SA[i - 1] = SA[i]; --N;
void kasaiLCP () {
    for (ll i = 0; i < N; ++i) c [SA [i]] = i;
    LCP [0] = 0;
    for (ll i = 0, h = 0; i < N; ++i) if (c[i] > 0) {
            11 j = SA [c [i] - 1];
            while (i + h < N \&\& j + h < N \&\& str [i + h] == str [j + h]) ++h;
            LCP[c[i]] = h;
            if (h > 0) --h;
        }
}
void suffixArray () {
    m = 256;
```

4 Math

4.1 Number Theory

```
#define MX 10000005
#define mod 100000007
#define INF 1000000000000
bool marked[MX];
vll primes;
void sieve()
    int i,j;
    marked[0]=marked[1]=true;
    for(i=2;i*i<=MX-1;i++){</pre>
        if(marked[i] == false){
             for(j=i*i;j<=MX-1;j+=i){</pre>
                 marked[j]=true;
        }
    }
    loop(i,MX-1)
        if(!marked[i]){
             primes.pb(i);
             //cout << i << ' ';
        }
}
vll primeFactors(ll N)
        vll factors;
        11 pf_id=0,pf=primes[pf_id];
        while(pf*pf<=N){
        while (N\%pf == 0) {
             N/=pf;
             factors.pb(pf);
        }
        pf=primes[++pf_id];
        if(N!=1)
        factors.pb(N);
    return factors;
}
```

```
11 numPF(11 N)
         11 pf_id=0,pf=primes[pf_id],ans=0;
         while(pf*pf<=N){</pre>
         while (N\%pf == 0) {
             N/=pf;
             ans++;
         pf=primes[++pf_id];
         if(N!=1)
         ans++;
    return ans;
}
11 numDiv(11 N)
         11 pf_id=0,pf=primes[pf_id],ans=1;
         while(pf*pf<=N){</pre>
         11 power=0;
         while (N\%pf == 0) {
             N/=pf;
             power++;
         ans*=(power+1);
         pf=primes[++pf_id];
         }
         if(N!=1)
         ans*=2;
    return ans;
}
11 sumDiv(11 N)
         11 pf_id=0,pf=primes[pf_id],ans=1;
         while(pf*pf<=N){</pre>
         11 power=0;
         while (N\%pf == 0) {
             N/=pf;
             power++;
         ans *= ((11) pow((double) pf, power +1.0) -1)/(pf-1);
         pf=primes[++pf_id];
         }
         if(N!=1)
         ans*=((11)pow((double)N,2.0)-1)/(N-1);;
```

```
return ans;
}
int main()
{
    ll n,m,a,b,c,t,i,j,k;
    string s;
    sieve();
    return 0;
}
```

4.2 Rho Pollard Sieve

```
_sieve _prime_factorize
Program to print prime factorisation of a number in the range [1, 1e18].
Input: an integer denoting the value of n
Output: prime factors of n in ascending order, separated by '*' character
Sample Input: 546534813485312
Sample Output: 5*1373*89533*13216567543
Time Complexity: O(1e7)
Space Complexity: O(1e6)
Stack\ \textit{Overflow Problem Link: https://stackoverflow.com/questions/50251565}
#include <iostream>
#include <vector>
#include <algorithm> // __gcd()
#include <cstring> // memset()
#include <cassert> // assert()
using namespace std;
#define int long long
typedef long double dbl;
const int N=2e6+10;
int np, prime[N];
bool isp[N];
void sieve(int N) {
    memset(isp, true, sizeof isp);
    isp[0] = isp[1] = false;
    for(int i=2; i<N; i++) if(isp[i]) {</pre>
        prime[++np]=i;
        for(int j=2*i; j<N; j+=i) {</pre>
            isp[j]=false;
        }
    }
}
inline int mul(int a, int b, int m) {
        a\%=m; if (a<0) a+=m;
        b\%=m; if (b<0) b+=m;
        int q = ((dbl)a * (dbl)b) / (dbl)m;
        int r = a*b - q*m;
        return (r<0 ? r+m:r);
inline int pwr(int a, int n, int m) {
```

```
int ans(1);
    while(n) {
        if(n & 1) ans = mul(ans, a, m);
        if(n >>= 1) a = mul(a, a, m);
    return ans%m;
int myrand(int n) {
        return rand()%n*rand()%n*rand()%n;
bool ispmiller(int p) { // O(30*logp)
        if(p<2) return false;</pre>
        if(p==2) return true;
        if(p%2==0) return false;
        int s=p-1; s>>=__builtin_ctzll(s);
        for(int i=0; i<60; i++) {
                 int val=pwr(myrand(p-1)+1,s,p), temp=s;
                 while (temp!=p-1 \text{ and } 1 < val \text{ and } val < p-1) {
                         val=mul(val,val,p);
                         temp < <= 1;
                 if(val!=p-1 and temp%2==0) return false;
        return true;
}
inline int pollardrho(int n) { // O(n^0.25)
        if(n==1) return 1;
        if(n%2==0) return 2;
        int c=myrand(n-1)+1, x=myrand(n-2)+2, y=x;
        int d=1; while(d==1) {
                 x=mul(x,x,n)+c; if(x>=n) x-=n;
                 y=mul(y,y,n)+c; if(y>=n) y-=n;
                 y=mul(y,y,n)+c; if(y>=n) y-=n;
                 d=_gcd(abs(x-y),n);
                 if(d==n) return (ispmiller(n) ? n:pollardrho(n));
        return d;
}
#undef int
int main() {
#define int long long
    int n; cin >> n;
    if(ispmiller(n)) {
        cout << n << '\n'; // input \ n \ is \ prime, output as it \ is
        return 0;
    }
```

```
vector<int> factors; // holds the prime factorisation of input n
    sieve(1e6);
    for(int i=1; i<np and prime[i]*prime[i]<=n; i++) {</pre>
        if(n\%prime[i]==0) { // n is divisible by prime[i] (<= 1e6)}
                 while(n%prime[i]==0) {
                         n /= prime[i];
                         factors.push_back(prime[i]);
                }
        }
    if(ispmiller(n)) {
        factors.push_back(n);
    else if(n>1) { // n still has some prime factors > 1e6
        int x = pollardrho(n);
        assert(x > 1e6);
        factors.push_back(x);
        factors.push_back(n/x);
    }
    // Print the factorisation
    for(int i=0; i<(int)factors.size()-1; i++) cout << factors[i] << '*';</pre>
        cout << (factors.empty() ? 1 : factors.back()) << '\n';</pre>
    return 0;
}
```

4.3 Big Integer

```
#include <bits/stdc++.h>
using namespace std;
typedef long long 11;
typedef pair<11,11> 111;
typedef pair<ll,int> lli;
typedef pair<int,int> ii;
#define EL printf("\n")
#define OK printf("OK")
#define pb push_back
#define mp make_pair
#define ep emplace_back
#define X first
#define Y second
#define fillchar(a,x) memset(a, x, sizeof(a))
#define FOR(i,1,r) for (int i=1;i<=r;i++)</pre>
#define FORD(i,r,l) for (int i=r;i>=1;i--)
const int base = 1e9;
typedef vector<int> BigInt;
void Set(BigInt &a) {
    while (a.size() > 1 && a.back() == 0) a.pop_back();
}
void Print(BigInt a) {
    Set(a);
    printf("%d", (a.size() == 0) ? 0 : a.back());
    FORD(i,a.size()-2,0) printf("%09d", a[i]); EL;
}
BigInt Integer(string s) {
    BigInt ans;
    if (s[0] == '-') return ans;
    if (s.size() == 0) {ans.pb(0); return ans;}
    while (s.size()\%9 != 0) s = '0'+s;
    for (int i=0;i<s.size();i+=9) {</pre>
        int v = 0;
        for (int j=i; j<i+9; j++) v = v*10+(s[j]-'0');
        ans.insert(ans.begin(),v);
    Set(ans);
    return ans;
```

```
}
BigInt Integer(char c[]) {
    string s = "";
    FOR(i,0,strlen(c)-1) s = s + c[i];
    return Integer(s);
}
BigInt Integer(ll x) {
    string s = "";
    while (x > 0) s = char(x\%10+'0') + s, x /= 10;
    return Integer(s);
}
BigInt Integer(int x) {
    return Integer((11) x);
void operator >> (istream &in, BigInt &a) {
    string s;
    getline(cin, s);
    a = Integer(s);
}
void operator << (ostream &out, BigInt a) {</pre>
    Print(a);
}
bool operator < (BigInt a, BigInt b) {</pre>
    Set(a);
    Set(b);
    if (a.size() != b.size()) return (a.size() < b.size());</pre>
    FORD(i,a.size()-1,0)
        if (a[i] != b[i]) return (a[i] < b[i]);</pre>
    return false;
}
bool operator > (BigInt a, BigInt b) {
    return (b < a);
}
bool operator == (BigInt a, BigInt b) {
```

```
return (!(a < b) && !(b < a));
}
bool operator <= (BigInt a, BigInt b) {</pre>
    return (a < b || a == b);
bool operator >= (BigInt a, BigInt b) {
    return (b < a || b == a);
bool operator < (BigInt a, int b) {</pre>
    return (a < Integer(b));</pre>
}
bool operator > (BigInt a, int b) {
    return (a > Integer(b));
}
bool operator == (BigInt a, int b) {
    return (a == Integer(b));
}
bool operator >= (BigInt a, int b) {
    return (a >= Integer(b));
bool operator <= (BigInt a, int b) {</pre>
    return (a <= Integer(b));</pre>
}
BigInt max(BigInt a, BigInt b) {
    if (a > b) return a;
    return b;
}
BigInt min(BigInt a, BigInt b) {
    if (a < b) return a;
    return b;
}
BigInt operator + (BigInt a, BigInt b) {
    Set(a);
```

```
Set(b);
    BigInt ans;
    int carry = 0;
    FOR(i,0,max(a.size(), b.size())-1) {
        if (i < a.size()) carry += a[i];</pre>
        if (i < b.size()) carry += b[i];</pre>
        ans.pb(carry%base);
        carry /= base;
    }
    if (carry) ans.pb(carry);
    Set(ans);
    return ans;
}
BigInt operator + (BigInt a, int b) {
    return a + Integer(b);
BigInt operator ++ (BigInt &a) { // ++a
    a = a + 1;
    return a;
}
void operator += (BigInt &a, BigInt b) {
    a = a + b;
void operator += (BigInt &a, int b) {
    a = a + b;
}
BigInt operator - (BigInt a, BigInt b) {
    Set(a);
    Set(b);
    BigInt ans;
    int carry = 0;
    FOR(i,0,a.size()-1) {
        carry += a[i] - (i < b.size() ? b[i] : 0);</pre>
        if (carry < 0) ans.pb(carry+base), carry = -1;</pre>
        else ans.pb(carry), carry = 0;
    }
    Set(ans);
    return ans;
}
```

```
BigInt operator - (BigInt a, int b) {
    return a - Integer(b);
void operator -- (BigInt &a) { // --a
    a = a - 1;
}
void operator -= (BigInt &a, BigInt b) {
    a = a + b;
}
void operator -= (BigInt &a, int b) {
    a = a - b;
}
BigInt operator * (BigInt a, BigInt b) {
    Set(a);
    Set(b);
    BigInt ans;
    ans.assign(a.size()+b.size(), 0);
    FOR(i,0,a.size()-1) {
        11 carry = 011;
        for (int j=0; j< b.size() || carry > 0; j++) {
            11 s = ans[i+j] + carry + (11)a[i]*(j<b.size()?(11)b[j]:011);
            ans[i+j] = s\%base;
            carry = s/base;
        }
    }
    Set(ans);
    return ans;
}
BigInt operator * (BigInt a, int b) {
    return a * Integer(b);
}
void operator *= (BigInt &a, BigInt b) {
    a = a * b;
}
void operator *= (BigInt &a, int b) {
    a = a * b;
}
```

```
BigInt operator / (BigInt a, BigInt b) {
    Set(a);
    Set(b);
    if (b == Integer(0)) return Integer("-1");
    BigInt ans, cur;
    FORD(i,a.size()-1,0) {
        cur.insert(cur.begin(), a[i]);
        int x = 0, L = 0, R = base;
        while (L <= R) \{
            int mid = (L+R)>>1;
            if (b*Integer(mid) > cur) {
                x = mid;
                R = mid-1;
            }
            else
                L = mid+1;
        cur = cur - Integer(x-1)*b;
        ans.insert(ans.begin(),x-1);
    Set(ans);
    return ans;
}
BigInt operator / (BigInt a, int b) {
    Set(a);
    BigInt ans;
    11 cur = 011;
    FORD(i,a.size()-1,0) {
        cur = (cur*(l1)base + (l1)a[i]);
        ans.insert(ans.begin(),cur/b);
        cur %= b;
    }
    Set(ans);
    return ans;
}
void operator /= (BigInt &a, BigInt b) {
    a = a / b;
void operator /= (BigInt &a, int b) {
    a = a / b;
}
```

```
BigInt operator % (BigInt a, BigInt b) {
    Set(a);
    Set(b);
    if (b == Integer(0)) return Integer("-1");
    BigInt ans;
    FORD(i,a.size()-1,0) {
        ans.insert(ans.begin(), a[i]);
        int x = 0, L = 0, R = base;
        while (L \leq R) {
            int mid = (L+R)>>1;
            if (b*Integer(mid) > ans) {
                x = mid;
                R = mid-1;
            }
            else
                L = mid+1;
        }
        ans = ans - Integer(x-1)*b;
    Set(ans);
    return ans;
}
int operator % (BigInt a, int b) {
    Set(a);
    if (b == 0) return -1;
    int ans = 0;
    FORD(i,a.size()-1,0)
        ans = (ans*(base\%b) + a[i]\%b)\%b;
    return ans;
}
void operator %= (BigInt &a, BigInt b) {
    a = a \% b;
}
void operator %= (BigInt &a, int b) {
    a = a % Integer(b);
BigInt gcd(BigInt a, BigInt b) {
    Set(a);
    Set(b);
    while (b > Integer(0)) {
        BigInt r = a\%b;
        a = b;
        b = r;
```

```
}
    Set(a);
    return a;
}
BigInt lcm(BigInt a, BigInt b) {
    return (a*b/gcd(a,b));
BigInt sqrt(BigInt a) {
    BigInt x0 = a, x1 = (a+1)/2;
    while (x1 < x0) {
        x0 = x1;
        x1 = (x1+a/x1)/2;
    return x0;
}
BigInt pow(BigInt a, BigInt b) {
    if (b == Integer(0)) return Integer(1);
    BigInt tmp = pow(a, b/2);
    if (b\%2 == 0) return tmp * tmp;
    return tmp * tmp * a;
}
BigInt pow(BigInt a, int b) {
    return pow(a,(Integer(b)));
}
int log(int n, BigInt a) { // log_n(a)
    Set(a);
    int ans = 0;
    while (a > Integer(1)) {
        ans++;
        a /= n;
    return ans;
}
int main()
    BigInt B; cin >> B;
    BigInt A = Integer("123456789");
```

```
BigInt C = Integer(12345678911);
    int x; x = 123456789;
    if (B <= A) cout << A - B;</pre>
    else {
         cout << "-";
         cout << B - A;
    cout << A + B; Print(A + x);
    cout << A * B; Print(A * x);</pre>
    cout << A / B; Print(A / x);</pre>
    cout << A % B; printf("%d\n", A % x);</pre>
    C = ++A; ++B; C += B + x;
    Print(A); Print(B); Print(C);
    cout << max(A,B);</pre>
    cout << min(A,B);</pre>
    cout << gcd(A,B);</pre>
    cout << lcm(A,B);</pre>
    cout << sqrt(A);</pre>
    printf("%d %d %d\n", log(2,A), log(10,B), log(5,C));
    A = Integer(16); x = 12;
    cout << pow(A,B);</pre>
    cout << pow(A,x);</pre>
    return 0;
}
```

4.4 Gaussian Elimination

```
#include < bits / stdc++.h>
using namespace std;
#define fast_io ios_base::sync_with_stdio(0); //cin.tie(0);
#define ll long long
#define ld long double
#define pb push_back
#define ins insert
#define in push
#define out pop
#define loop(i,n) for(i=1;i<=n;i++)</pre>
#define loon(i,n) for(i=n;i>0;i--)
#define vctr(x) vector< x >
#define pii(x,y) pair< x,y >
#define mkpr(x,y) make_pair(x,y)
#define ft first
#define sd second
#define MX 1005
#define mod 100000007
#define INF 1000000000000
double mat[MX][MX],solution[MX];
11 N;
void swap_row(ll i, ll j)
{
        for (11 k=0; k \le N; k++)
                 double temp = mat[i][k];
                mat[i][k] = mat[j][k];
                mat[j][k] = temp;
        }
}
void print()
        for (ll i=0; i<N; i++, printf("\n")){
                 for (ll j=0; j \le N; j++)
                         printf("%f ", mat[i][j]);
            printf("\n");
    }
}
11 forwardElim()
        for (11 k=0; k<N; k++)
        {
```

```
ll i_max = k;
                for (ll i = k+1; i < N; i++)
                         if (fabs(mat[i][k]) > fabs(mat[i_max][k]))
                                 i_max = i;
                if (mat[i_max][k]==0){
                     //cout << i_max << endl;
                         return k;
                }
                if (i_max != k)
                         swap_row(k, i_max);
                 for (ll i=k+1; i<N; i++)</pre>
                         double f = mat[i][k]/mat[k][k];
                         for (ll j=k+1; j \le N; j++)
                                 mat[i][j] -= mat[k][j]*f;
                         mat[i][k] = 0;
                }
        }
        return -1;
}
void backSub()
{
        for (ll i = N-1; i >= 0; i--)
                 solution[i] = mat[i][N];
                for (int j=i+1; j<N; j++)
                         solution[i] -= mat[i][j]*solution[j];
                }
                 solution[i] = solution[i]/mat[i][i];
        }
        /*printf("\nSolution for the system:\n");
        for (int i=0; i < N; i++)
                printf("%f\n", solution[i]);*/
}
```

```
void gaussianElimination()
        11 singular_flag = forwardElim();
        if (singular_flag != -1)
                 printf("Singular Matrix.\n");
                 if (mat[singular_flag][N])
                         printf("Inconsistent System.\n");
                 else
                         printf("May have infinitely many "
                                  "solutions.\n");
                 return;
        }
        backSub();
}
int main()
    11 n,m,t,i,j,k,a,b,c,cs=1;
    //freopen(input.txt, r, stdin);
    //freopen(output.txt, w, stdout);
    cin>> N;
    for(i=0;i<N;i++)</pre>
        for(j=0;j<=N;j++)
            cin>> mat[i][j];
    gaussianElimination();
    print();
    for(i=0;i<N;i++)</pre>
        cout<< fixed << setprecision(10) << solution[i] << endl;</pre>
    return 0;
}
```

4.5 Lagrange Interpolation

```
Complexity O(n^2) for pre-computing
    O(n) per query
#include <bits/stdc++.h>
using namespace std;
// x and y are vectors of the points
// n is the number of points; degree of poly is n-1
// returns intermediate co-efficients
vector<double> lagrange_interpolate(vector<double> x, vector<double> y, int n) {
    vector<double> ret = y;
    for(int i=0; i<n; ++i) {</pre>
        for(int j=0; j<n; ++j) {
            if(i == j) continue;
            ret[i] /= (x[i] - x[j]);
        }
    }
    return ret;
}
int main() {
    // Number of points
    // therefor polynomial order is n-1
    int n;
    cin >> n;
    vector < double > x(n), y(n);
    for(int i=0; i<n; ++i) {</pre>
        cin >> x[i] >> y[i];
    vector<double> coef = lagrange_interpolate(x, y, n);
    // number of queries. How many x 's are there you want to know the y
    int q;
    cin >> q;
    while(q--) {
        double xx;
        cin >> xx;
        double mul = 1.0;
        for(int i=0; i<n; ++i) mul *= (xx - x[i]);</pre>
        bool input_point = false;
```

```
double sum = 0;
        for(int i=0; i<n; ++i) {</pre>
            double div = (xx - x[i]);
            if(div == 0) {
                // This means this is one of the input points
                // Answer it immediately
                cout << y[i] << "\n";
                input_point = true;
                break;
            }
            else {
                sum += (coef[i] / div);
            }
        if(input_point) continue;
        double res = mul * sum;
        cout << res << "\n";
    return 0;
}
```

4.6 Newton Interpolation

```
Complexity O(n^2) for pre-computing
    O(n) per query
#include <bits/stdc++.h>
using namespace std;
vector<double> divided_diff(vector<double> x, vector<double> y, int n) {
    vector < double > ret(n, 0);
    ret[0] = y[0];
    vector<double> last = y;
    for(int i=1; i<n; ++i) {</pre>
        vector<double> temp;
        for(int j=0; j+1<(int) last.size(); ++j) {</pre>
             double diff = last[j+1] - last[j];
            diff \neq (x[i+j] - x[j]);
            temp.push_back(diff);
        }
        last = temp;
        ret[i] = last[0];
    }
    return ret;
}
int main() {
    // Number of points
    // therefor polynomial order is n-1
    int n;
    cin >> n;
    vector<double> x(n), y(n);
    for(int i=0; i<n; ++i) {</pre>
        cin >> x[i] >> y[i];
    vector<double> coef = divided_diff(x, y, n);
    // number of queries. How many x 's are there you want to know the y
    int q;
    cin >> q;
    while(q--) {
        double xx;
```

```
cin >> xx;
        double mul = 1.0;
        double res = coef[0];
        for(int i=1; i<(int) coef.size(); ++i) {</pre>
            mul *= (xx - x[i-1]);
            res += (mul * coef[i]);
        cout << res << "\n";
    }
   return 0;
}
/*
4
5 12
6 13
9 14
11 16
1
10
*/
/*
5
5 150
7 392
11 1452
13 2366
21 9702
2
6
9
*/
```

4.7 Fast Fourier Transformation (Complex)

```
#define CD complex<double>
#define MX 10000005
#define mod 100000007
#define INF 1000000000000
#define EXP 0.00000001
const double PI = acos(-1.0);
ll rev(ll id, ll level)
    ll res=0;
    for(11 i=0;i<level;i++){</pre>
        if(id & (1<<i))</pre>
            res |=1<<(level-i-1);
    }
    return res;
void FFT(vector<CD>&PoC, bool inverse)
    11 len=PoC.size();
    11 level=0;
    while((1<<level)<len)
        level++;
    for(ll i=0;i<len;i++){</pre>
        if(i<rev(i,level))</pre>
             swap(PoC[i],PoC[rev(i,level)]);
    }
    for(11 1=2;1<=len;1<<=1){
         double ang=(2*PI*(inverse?-1:1))/1;
         CD wN(cos(ang),sin(ang));
         for(ll i=0;i<len;i+=1){</pre>
              CD w(1);
              for(11 j=0; j<1/2; j++){
                 CD u=PoC[i+j], v=PoC[i+j+1/2]*w;
                 PoC[i+j]=u+v;
                 PoC[i+j+1/2]=u-v;
                 w *= wN;
              }
         }
    }
    if(inverse){
```

```
for(CD &x:PoC)
             x/=len;
    }
}
vector<ll> multiplyTP(vector<ll>&A,vector<ll>&B)
    vector <CD>polA(A.begin(), A.end()), polB(B.begin(), B.end());
    ll n=1;
    while(n<A.size()+B.size())
        n*=2;
    polA.resize(n);
    polB.resize(n);
    FFT(polA,false);
    FFT(polB, false);
    for(ll i=0;i<n;i++)</pre>
         polA[i]*=polB[i];
    FFT(polA,true);
    vector<ll>ans(n);
    for(11 i=0;i<n;i++)</pre>
         ans[i]=round(polA[i].real());
    return ans;
}
int main()
    ll n,m,t,i,j,k,a,b,c,cs=1;
    cin>> n >> m;
    vector<11>A(n),B(m),C;
    for(i=0;i<n;i++)
         cin>> A[i];
    for(i=0;i<m;i++)</pre>
        cin>> B[i];
    C=multiplyTP(A,B);
    for(i=0;i<C.size();i++)</pre>
         cout << C[i] << ' ';
    cout << endl;</pre>
```

```
return 0;
}
```

4.8 Fast Fourier Transformation (NTT)

```
#define MX 1000005
#define mod 100000007
#define INF 1000000000000
#define EXP 0.00000001
const double PI = acos(-1.0);
const 11 root_mod = 7340033;
const ll root = 5;
const ll root_1 = 4404020;
const ll root_pw = 1 << 20;</pre>
ll rev(ll id, ll level)
{
    ll res=0;
    for(11 i=0;i<level;i++){</pre>
        if(id & (1<<i))</pre>
            res|=1<<(level-i-1);
    }
    return res;
}
11 modPow(ll x, ll n, ll mood)
    if(n==0)
        return 1%mood;
    ll t=modPow(x,n/2,mood);
    t*=t;
    t%=mood;
    if(n%2)
        t*=x;
    t%=mood;
    return t;
}
void FFT(vector<ll>&PoC, bool inverse)
    11 len=PoC.size();
    11 level=0;
    while((1<<level)<len)
        level++;
    for(ll i=0;i<len;i++){</pre>
```

```
if(i<rev(i,level))</pre>
             swap(PoC[i],PoC[rev(i,level)]);
    }
    for(11 1=2;1<=len;1<<=1){
          11 wN=inverse?root_1:root;
          for(ll i=1;i<root_pw;i<<=1)</pre>
             wN=(wN*wN)%root_mod;
          for(ll i=0;i<len;i+=1){</pre>
              ll w=1;
              for(11 j=0; j<1/2; j++){
                 ll u=PoC[i+j], v=(PoC[i+j+1/2]*w)%root_mod;
                 PoC[i+j]=(u+v)%root_mod;
                 PoC[i+j+1/2] = (u-v+root_mod)%root_mod;
                 w *= wN;
                 w%=root_mod;
              }
         }
    }
    if(inverse){
         11 inv=modPow(len,root_mod-2,root_mod);
         for(ll &x:PoC)
             x = inv, x\% = root mod;
    }
}
vector<ll> multiplyTP(vector<ll>&A,vector<ll>&B)
    vector<11>polA(A.begin(), A.end()), polB(B.begin(), B.end());
    11 n=1;
    while(n<A.size()+B.size())</pre>
        n*=2;
    polA.resize(n);
    polB.resize(n);
    FFT(polA,false);
    FFT(polB, false);
    for(11 i=0;i<n;i++)</pre>
         polA[i]*=polB[i],polA[i]%=root_mod;
    FFT(polA,true);
    vector<ll>ans(n);
    for(11 i=0;i<n;i++)</pre>
         ans[i]=polA[i];
```

```
return ans;
}
int main()
{
    11 n,m,t,i,j,k,a,b,c,cs=1;
    cin>> n >> m;
    vector<11>A(n),B(m),C;
    for(i=0;i<n;i++)
        cin>> A[i];
    for(i=0;i<m;i++)
        cin>> B[i];
    C=multiplyTP(A,B);
    for(i=0;i<C.size();i++)</pre>
        cout << C[i] << ' ';
    cout << endl;</pre>
    return 0;
}
```

4.9 Big Integer Multiplication Using FFT

```
#define EXP 0.00000001
const double PI = acos(-1.0);
const 11 root_mod = 7340033;
const ll root = 5;
const ll root_1 = 4404020;
const ll root_pw = 1 << 20;</pre>
ll rev(ll id, ll level)
    ll res=0;
    for(ll i=0;i<level;i++){</pre>
         if(id & (1<<i))</pre>
             res |=1<<(level-i-1);
    return res;
}
11 modPow(ll x, ll n, ll mood)
    if(n==0)
        return 1%mood;
    11 t=modPow(x,n/2,mood);
    t*=t;
    t%=mood;
    if(n%2)
        t*=x;
    t%=mood;
    return t;
}
void FFT(vector<ll>&PoC, bool inverse)
    11 len=PoC.size();
    11 level=0;
    while((1<<level)<len)</pre>
         level++;
    for(ll i=0;i<len;i++){</pre>
         if(i<rev(i,level))</pre>
```

```
swap(PoC[i],PoC[rev(i,level)]);
    }
    for(11 1=2;1<=len;1<<=1){
         11 wN=inverse?root_1:root;
         for(ll i=1;i<root_pw;i<<=1)</pre>
             wN=(wN*wN)%root_mod;
         for(11 i=0;i<len;i+=1){</pre>
              11 w=1;
              for (11 j=0; j<1/2; j++) {
                 ll u=PoC[i+j], v=(PoC[i+j+1/2]*w)%root_mod;
                 PoC[i+j]=(u+v)%root_mod;
                 PoC[i+j+1/2] = (u-v+root_mod)%root_mod;
                 w *= wN;
                 w%=root_mod;
              }
         }
    }
    if(inverse){
        11 inv=modPow(len,root_mod-2,root_mod);
        for(ll &x:PoC)
             x*=inv,x%=root_mod;
    }
}
vector<ll> multiplyTP(vector<ll>&A, vector<ll>&B)
    vector<11>polA(A.begin(), A.end()), polB(B.begin(), B.end());
    11 n=1;
    while(n<A.size()+B.size())
        n*=2;
    polA.resize(n);
    polB.resize(n);
    FFT(polA, false);
    FFT(polB, false);
    for(ll i=0;i<n;i++)</pre>
        polA[i]*=polB[i],polA[i]%=root_mod;
    FFT(polA,true);
    vector<ll>ans(n);
    for(ll i=0;i<n;i++)</pre>
        ans[i]=polA[i];
    return ans;
```

```
}
int main()
    11 n,m,t,i,j,k,a,b,c,cs=1;
    //freopen(input.txt, r, stdin);
    //freopen(output.txt, w, stdout);
    cin>> t;
    while(t--){
        string str1, str2, str3;
        cin>> str1 >> str2;
        vector<ll>A(str1.size()),B(str2.size()),C;
        for(i=str1.size()-1,j=0;i>=0;i--,j++)
             A[j]=str1[i]-48;
        for(i=str2.size()-1,j=0;i>=0;i--,j++)
             B[j]=str2[i]-48;
        C=multiplyTP(A,B);
        11 carry=0, mul=10;
        for(i=0;i<C.size();i++){</pre>
             11 digit=C[i]+carry;
             //ll digit=C[i];
             //cout << C[i] << ' ';
             str3+=digit%mul+48;
             carry=digit/mul;
        reverse(str3.begin(),str3.end());
        //cout << str3 << endl;
        bool ok=false;
        for(i=0;i<str3.size();i++){</pre>
             if(str3[i]!='0')
                 ok=true;
             if(ok)
                 cout << str3[i];</pre>
        }
        if(!ok)
             cout << 0;
        cout << endl;</pre>
    }
```

```
return 0;
}
```

5 Geometry

5.1 Geometry Library

/*Geom_Library*/ // C++ routines for computational geometry. double INF = 1e100; double EPS = 1e-12; struct PT { double x, y; PT() {} PT(double x, double y) : x(x), y(y) {} PT(const PT &p) : x(p.x), y(p.y) {} PT operator + (const PT &p) const { return PT(x+p.x, y+p.y); } PT operator - (const PT &p) const { return PT(x-p.x, y-p.y); } PT operator * (double c) const { return PT(x*c, PT operator / (double c) const { return PT(x/c, y*c); } y/c); } }; double dot(PT p, PT q) { return p.x*q.x+p.y*q.y; } double dist2(PT p, PT q) { return dot(p-q,p-q); } double cross(PT p, PT q) { return p.x*q.y-p.y*q.x; } ostream & operator << (ostream & os, const PT & p) { os << "(" << p.x << "," << p.y << ")"; } // rotate a point CCW or CW around the origin PT RotateCCW90(PT p) { return PT(-p.y,p.x); } PT RotateCW90(PT p) { return PT(p.y,-p.x); } PT RotateCCW(PT p, double t) { return PT(p.x*cos(t)-p.y*sin(t), p.x*sin(t)+p.y*cos(t)); } // project point c onto line through a and b // assuming a != b PT ProjectPointLine(PT a, PT b, PT c) { return a + (b-a)*dot(c-a, b-a)/dot(b-a, b-a); // project point c onto line segment through a and b PT ProjectPointSegment(PT a, PT b, PT c) { double r = dot(b-a,b-a);if (fabs(r) < EPS) return a; r = dot(c-a, b-a)/r;if (r < 0) return a; if (r > 1) return b;

```
return a + (b-a)*r;
}
// compute distance from c to segment between a and b
double DistancePointSegment(PT a, PT b, PT c) {
  return sqrt(dist2(c, ProjectPointSegment(a, b, c)));
}
// compute distance between point (x,y,z) and plane ax+by+cz=d
double DistancePointPlane(double x, double y, double z,
                          double a, double b, double c, double d)
  return fabs(a*x+b*y+c*z-d)/sqrt(a*a+b*b+c*c);
}
// determine if lines from a to b and c to d are parallel or collinear
bool LinesParallel(PT a, PT b, PT c, PT d) {
  return fabs(cross(b-a, c-d)) < EPS;</pre>
bool LinesCollinear(PT a, PT b, PT c, PT d) {
  return LinesParallel(a, b, c, d)
      && fabs(cross(a-b, a-c)) < EPS
      && fabs(cross(c-d, c-a)) < EPS;
}
// determine if line segment from a to b intersects with
// line segment from c to d
bool SegmentsIntersect(PT a, PT b, PT c, PT d) {
  if (LinesCollinear(a, b, c, d)) {
    if (dist2(a, c) < EPS || dist2(a, d) < EPS ||
      dist2(b, c) < EPS || dist2(b, d) < EPS) return true;
    if (dot(c-a, c-b) > 0 && dot(d-a, d-b) > 0 && dot(c-b, d-b) > 0)
      return false;
   return true;
  if (cross(d-a, b-a) * cross(c-a, b-a) > 0) return false;
  if (cross(a-c, d-c) * cross(b-c, d-c) > 0) return false;
  return true;
}
// compute intersection of line passing through a and b
// with line passing through c and d, assuming that unique
// intersection exists; for segment intersection, check if
// segments intersect first
PT ComputeLineIntersection(PT a, PT b, PT c, PT d) {
 b=b-a; d=c-d; c=c-a;
  assert(dot(b, b) > EPS \&\& dot(d, d) > EPS);
```

```
return a + b*cross(c, d)/cross(b, d);
}
// compute center of circle given three points
PT ComputeCircleCenter(PT a, PT b, PT c) {
  b=(a+b)/2;
  c=(a+c)/2;
  return ComputeLineIntersection(b, b+RotateCW90(a-b), c, c+RotateCW90(a-c));
}
// determine if point is in a possibly non-convex polygon (by William
// Randolph Franklin); returns 1 for strictly interior points, 0 for
// strictly exterior points, and 0 or 1 for the remaining points.
// Note that it is possible to convert this into an *exact* test using
// integer arithmetic by taking care of the division appropriately
// (making sure to deal with signs properly) and then by writing exact
// tests for checking point on polygon boundary
bool PointInPolygon(const vector<PT> &p, PT q) {
  bool c = 0;
  for (int i = 0; i < p.size(); i++){</pre>
    int j = (i+1)\%p.size();
    if ((p[i].y \le q.y \&\& q.y < p[j].y ||
      p[j].y \le q.y && q.y \le p[i].y) &&
      q.x < p[i].x + (p[j].x - p[i].x) * (q.y - p[i].y) / (p[j].y - p[i].y))
      c = !c;
  }
  return c;
}
// determine if point is on the boundary of a polygon
bool PointOnPolygon(const vector<PT> &p, PT q) {
  for (int i = 0; i < p.size(); i++)</pre>
    if (dist2(ProjectPointSegment(p[i], p[(i+1)%p.size()], q), q) < EPS)
      return true;
    return false;
}
// compute intersection of line through points a and b with
// circle centered at c with radius r > 0
vector<PT> CircleLineIntersection(PT a, PT b, PT c, double r) {
  vector<PT> ret;
  b = b-a;
  a = a-c;
  double A = dot(b, b);
  double B = dot(a, b);
  double C = dot(a, a) - r*r;
  double D = B*B - A*C;
  if (D < -EPS) return ret;</pre>
```

```
ret.push_back(c+a+b*(-B+sqrt(D+EPS))/A);
  if (D > EPS)
    ret.push_back(c+a+b*(-B-sqrt(D))/A);
  return ret;
}
// compute intersection of circle centered at a with radius r
// with circle centered at b with radius R
vector<PT> CircleCircleIntersection(PT a, PT b, double r, double R) {
  vector < PT > ret;
  double d = sqrt(dist2(a, b));
  if (d > r+R \mid \mid d+min(r, R) < max(r, R)) return ret;
  double x = (d*d-R*R+r*r)/(2*d);
  double y = sqrt(r*r-x*x);
  PT v = (b-a)/d;
  ret.push_back(a+v*x + RotateCCW90(v)*y);
  if (y > 0)
    ret.push_back(a+v*x - RotateCCW90(v)*y);
  return ret;
}
// This code computes the area or centroid of a (possibly nonconvex)
// polygon, assuming that the coordinates are listed in a clockwise or
// counterclockwise fashion. Note that the centroid is often known as
// the "center of gravity" or "center of mass".
double ComputeSignedArea(const vector<PT> &p) {
  double area = 0;
  for(int i = 0; i < p.size(); i++) {</pre>
    int j = (i+1) % p.size();
    area += p[i].x*p[j].y - p[j].x*p[i].y;
  return area / 2.0;
double ComputeArea(const vector<PT> &p) {
  return fabs(ComputeSignedArea(p));
}
PT ComputeCentroid(const vector < PT > &p) {
  PT c(0,0);
  double scale = 6.0 * ComputeSignedArea(p);
  for (int i = 0; i < p.size(); i++){</pre>
    int j = (i+1) % p.size();
    c = c + (p[i]+p[j])*(p[i].x*p[j].y - p[j].x*p[i].y);
  }
  return c / scale;
```

```
// tests whether or not a given polygon (in CW or CCW order) is simple
bool IsSimple(const vector<PT> &p) {
  for (int i = 0; i < p.size(); i++) {</pre>
    for (int k = i+1; k < p.size(); k++) {</pre>
      int j = (i+1) % p.size();
      int 1 = (k+1) % p.size();
      if (i == 1 || j == k) continue;
      if (SegmentsIntersect(p[i], p[j], p[k], p[l]))
        return false;
    }
  }
  return true;
int main() {
  // expected: (-5,2)
  cerr << RotateCCW90(PT(2,5)) << endl;</pre>
  // expected: (5,-2)
  cerr << RotateCW90(PT(2,5)) << endl;</pre>
  // expected: (-5,2)
  cerr << RotateCCW(PT(2,5),M_PI/2) << endl;</pre>
  // expected: (5,2)
  cerr << ProjectPointLine(PT(-5,-2), PT(10,4), PT(3,7)) << endl;</pre>
  // expected: (5,2) (7.5,3) (2.5,1)
  cerr << ProjectPointSegment(PT(-5,-2), PT(10,4), PT(3,7)) << " "</pre>
       << ProjectPointSegment(PT(7.5,3), PT(10,4), PT(3,7)) << " "</pre>
       << ProjectPointSegment(PT(-5,-2), PT(2.5,1), PT(3,7)) << endl;
  // expected: 6.78903
  cerr << DistancePointPlane(4,-4,3,2,-2,5,-8) << endl;</pre>
  // expected: 1 0 1
  cerr << LinesParallel(PT(1,1), PT(3,5), PT(2,1), PT(4,5)) << " "</pre>
       << LinesParallel(PT(1,1), PT(3,5), PT(2,0), PT(4,5)) << " "
       << LinesParallel(PT(1,1), PT(3,5), PT(5,9), PT(7,13)) << endl;</pre>
  // expected: 0 0 1
  cerr << LinesCollinear(PT(1,1), PT(3,5), PT(2,1), PT(4,5)) << " "</pre>
       << LinesCollinear(PT(1,1), PT(3,5), PT(2,0), PT(4,5)) << " "
       << LinesCollinear(PT(1,1), PT(3,5), PT(5,9), PT(7,13)) << endl;</pre>
  // expected: 1 1 1 0
  cerr << SegmentsIntersect(PT(0,0), PT(2,4), PT(3,1), PT(-1,3)) << " "
```

```
<< SegmentsIntersect(PT(0,0), PT(2,4), PT(4,3), PT(0,5)) << " "
     << SegmentsIntersect(PT(0,0), PT(2,4), PT(2,-1), PT(-2,1)) << " "
     << SegmentsIntersect(PT(0,0), PT(2,4), PT(5,5), PT(1,7)) << endl;
// expected: (1,2)
cerr << ComputeLineIntersection(PT(0,0), PT(2,4), PT(3,1), PT(-1,3)) << endl;
// expected: (1,1)
cerr << ComputeCircleCenter(PT(-3,4), PT(6,1), PT(4,5)) << endl;</pre>
vector<PT> v;
v.push_back(PT(0,0));
v.push back(PT(5,0));
v.push_back(PT(5,5));
v.push_back(PT(0,5));
// expected: 1 1 1 0 0
cerr << PointInPolygon(v, PT(2,2)) << " "</pre>
     << PointInPolygon(v, PT(2,0)) << " "
     << PointInPolygon(v, PT(0,2)) << " "
     << PointInPolygon(v, PT(5,2)) << " "
     << PointInPolygon(v, PT(2,5)) << endl;</pre>
// expected: 0 1 1 1 1
cerr << PointOnPolygon(v, PT(2,2)) << " "</pre>
     << PointOnPolygon(v, PT(2,0)) << " "
     << PointOnPolygon(v, PT(0,2)) << " "
     << PointOnPolygon(v, PT(5,2)) << " "
     << PointOnPolygon(v, PT(2,5)) << endl;</pre>
// expected: (1,6)
//
             (5,4) (4,5)
//
             blank line
//
             (4,5) (5,4)
//
             blank line
//
             (4,5) (5,4)
vector < PT > u = CircleLineIntersection(PT(0,6), PT(2,6), PT(1,1), 5);
for (int i = 0; i < u.size(); i++) cerr << u[i] << " "; cerr << endl;
u = CircleLineIntersection(PT(0,9), PT(9,0), PT(1,1), 5);
for (int i = 0; i < u.size(); i++) cerr << u[i] << " "; cerr << endl;
u = CircleCircleIntersection(PT(1,1), PT(10,10), 5, 5);
for (int i = 0; i < u.size(); i++) cerr << u[i] << " "; cerr << endl;
u = CircleCircleIntersection(PT(1,1), PT(8,8), 5, 5);
for (int i = 0; i < u.size(); i++) cerr << u[i] << " "; cerr << endl;
u = CircleCircleIntersection(PT(1,1), PT(4.5,4.5), 10, sqrt(2.0)/2.0);
for (int i = 0; i < u.size(); i++) cerr << u[i] << " "; cerr << endl;
u = CircleCircleIntersection(PT(1,1), PT(4.5,4.5), 5, sqrt(2.0)/2.0);
for (int i = 0; i < u.size(); i++) cerr << u[i] << " "; cerr << endl;
```

```
// area should be 5.0
// centroid should be (1.166666, 1.166666)
PT pa[] = { PT(0,0), PT(5,0), PT(1,1), PT(0,5) };
vector<PT> p(pa, pa+4);
PT c = ComputeCentroid(p);
cerr << "Area: " << ComputeArea(p) << endl;
cerr << "Centroid: " << c << endl;
return 0;
}</pre>
```

5.2 Convex Hull

```
struct PT {
  double x, y;
  PT() {}
  PT(double x, double y) : x(x), y(y) {}
  PT(const PT \&p) : x(p.x), y(p.y)
  PT operator + (const PT &p) const { return PT(x+p.x, y+p.y); }
  PT operator - (const PT &p) const { return PT(x-p.x, y-p.y); }
  PT operator * (double c) const { return PT(x*c, y*c ); }
PT operator / (double c) const { return PT(x/c, y/c ); }
};
bool cmp(PT a, PT b) {
    return a.x < b.x || (a.x == b.x && a.y < b.y);
}
bool cw(PT a, PT b, PT c) {
    return a.x*(b.y-c.y)+b.x*(c.y-a.y)+c.x*(a.y-b.y) < 0;
}
bool ccw(PT a, PT b, PT c) {
    return a.x*(b.y-c.y)+b.x*(c.y-a.y)+c.x*(a.y-b.y) > 0;
}
void convex_hull(vector<PT>& a) {
    if (a.size() == 1)
        return;
    sort(a.begin(), a.end(), &cmp);
    PT p1 = a[0], p2 = a.back();
    vector<PT> up, down;
    up.push_back(p1);
    down.push_back(p1);
    for (int i = 1; i < (int)a.size(); i++) {
        if (i == a.size() - 1 \mid\mid cw(p1, a[i], p2)) {
             while (up.size() >= 2 &&
                 !cw(up[up.size()-2], up[up.size()-1], a[i]))
                 up.pop_back();
            up.push_back(a[i]);
        }
        if (i == a.size() - 1 || ccw(p1, a[i], p2)) {
             while(down.size() >= 2 &&
                 !ccw(down[down.size()-2], down[down.size()-1], a[i]))
                 down.pop_back();
             down.push_back(a[i]);
        }
    }
```

```
a.clear();
    for (int i = 0; i < (int)up.size(); i++)</pre>
         a.push_back(up[i]);
    for (int i = down.size() - 2; i > 0; i--)
        a.push_back(down[i]);
}
inline double dist(const PT &a, const PT &b) {
         return hypot((double)(a.x-b.x), (double)(a.y-b.y));
}
int main()
{
    fast_io;
    ll n,m,t,i,j,k,a,b,c,cs=1;
    //freopen(input.txt, r, stdin);
    //freopen(output.txt, w, stdout);
    cin>> n;
    vector < PT > points(n);
    for(i=0;i<n;i++)</pre>
        cin>> points[i].x >> points[i].y;
    convex_hull(points);
    vector < PT > res = points;
    double convex_area=ComputeArea(res);
    cout << res.size() << endl;</pre>
    cout << convex_area << endl;</pre>
    for(i=0;i<res.size();i++)</pre>
         cout << res[i].x << ' ' << res[i].y << endl;</pre>
    return 0;
}
```

6 Dynamic Programming

6.1 Bit Mask DP Sample

```
ll weight[MX][MX],dp[1<<(MX-1)],n;</pre>
ll setBit(ll N, ll pos){ return N = N | (1 << pos); }
ll resetBit(ll N, ll pos){ return N = N & \sim(1<<pos); }
bool checkBit(ll N, ll pos){ return (bool)(N & (1<<pos)); }</pre>
11 bitMaskDP(ll mask)
    if(mask==(1<< n)-1)
        return 0;
    if(dp[mask]!=-1)
        return dp[mask];
    ll mn=1<<30;
    for(ll i=0;i<n;i++){</pre>
        if(!checkBit(mask,i)){
            ll price=weight[i][i];
            for(ll j=0; j< n; j++){
                 if(i!=j and checkBit(mask,j))
                     price+=weight[i][j];
            11 value=price+bitMaskDP(setBit(mask,i));
            mn=min(mn, value);
        }
    }
    dp[mask]=mn;
    return dp[mask];
}
int main()
    ll m,t,i,j,k,a,b,c,cs=1;
    //freopen("input.txt", "r", stdin);
    //freopen("output.txt", "w", stdout);
    cin>> t;
    while(t--){
        cin>> n;
        for(i=0;i<n;i++)
            for(j=0;j<n;j++)
```

6.2 Digit DP Sample

```
11 dp[MX][MX][3],total;
bool vis[MX][MX][3];
string str;
11 digitDP(ll pos, ll prev, ll ok)
{
    if(pos>=(ll)str.size()){
        return 1;
    if(vis[pos][prev][ok])
        return dp[pos][prev][ok];
    vis[pos][prev][ok]=true;
    11 low=0,up=9;
    if(prev==total)
        up=0;
    else if(ok==1)
        up=str[pos]-48;
    if(!pos)
        low=1;
    ll ans=0;
    if(ok==1){
        for(ll i=low;i<=up;i++){</pre>
            11 x=0;
            if(i)
                 x=1;
            if(i==up){
                 ans+=digitDP(pos+1,prev+x,ok);
            }
            else{
                 ans+=digitDP(pos+1,prev+x,3-ok);
        }
    }
    else{
        for(ll i=low;i<=up;i++){</pre>
            11 x=0;
            if(i)
                 x=1;
             ans+=digitDP(pos+1,prev+x,ok);
        }
    }
    //cout << ans << endl;
```

```
dp[pos][prev][ok]=ans;
    return dp[pos][prev][ok];
}
int main()
    11 n,m,t,i,j,k,a,b,c,cs=1;
    //freopen(input.txt, r, stdin);
    //freopen(output.txt, w, stdout);
    cin>> t;
    while(t--){
        string str1, str2;
        cin >> n >> m;
        n--;
        ll ans=0;
        total=3;
        if(n){
            memset(vis, false, sizeof vis);
            while(n){
                str1+=(char)(n\%10+48);
                n/=10;
            reverse(str1.begin(),str1.end());
            str="";
            11 tmp=0;
            for(i=1;i<=str1.size()-1;i++){</pre>
                str+='9';
                tmp+=digitDP(0,0,1);
                memset(vis, false, sizeof vis);
            }
            //cout << tmp << ' ';
            str=str1;
            tmp+=digitDP(0,0,1);
            //cout << tmp << endl;
            ans-=tmp;
```

```
}
        if(m){}
             memset(vis, false, sizeof vis);
             while(m){
                 str2+=(char)(m%10+48);
                 m/=10;
             reverse(str2.begin(),str2.end());
             str=str2;
             str="";
             11 tmp=0;
             for(i=1;i<=str2.size()-1;i++){</pre>
                 str+='9';
                 tmp+=digitDP(0,0,1);
                 memset(vis, false, sizeof vis);
             }
             //cout << tmp << ' ';
             str=str2;
             tmp+=digitDP(0,0,1);
             //cout << tmp << endl;</pre>
             ans+=tmp;
        }
        cout << ans << endl;</pre>
    }
    return 0;
}
```

6.3 Sum Over Subsets DP (IUT IUPC Code)

```
/* Power Puff Girls OF IUT IUPC 2019 */
            /* SOS DP */
            /* Sum of Over All Super-Set of a Sub-Set */
            /* Inclusion/Exclusion */
            /* Time: O((2^N)*N) */
             /* Memory: O((2^N)*N) */
11 N,v;
11 m1,m2,m3,m4;
ll cnt[1<<19];
ll F[5][1<<19];
ll res[1<<19];
ll bigMod(ll x, ll n)
    if(!n)
        return 1LL;
    ll temp=bigMod(x,n/2);
    temp=(temp*temp)%mod;
    if(n%2)
        temp=(temp*x)%mod;
    return temp;
}
void countF(ll id)
    ll dp[(1 << N)][N+1];
    memset(dp,0,sizeof dp);
    for(ll mask = (1 << N)-1; mask >= 0; --mask){
        dp[mask][0] = cnt[mask];
        for(11 i = 0; i < N; ++i){
             if(!(mask & (1<<i)))</pre>
                 dp[mask][i+1] = (dp[mask][i] + dp[mask^(1<<i)][i])%mod;</pre>
             else
                 dp[mask][i+1] = dp[mask][i];
        }
        F[id][mask] = dp[mask][N];
    for(ll mask = 0; mask<(1<<\mathbb{N}); mask++)
        res[mask] = (res[mask] * F[id][mask]) % mod;
}
void countRes()
    ll\ dp[(1<<N)][N+1];
```

```
memset(dp,0,sizeof dp);
    for(ll mask = (1 << N)-1; mask >= 0; --mask){
         dp[mask][0] = 0;
         for(ll i = 0;i < N; ++i){
             if(!(mask & (1<<i)))</pre>
                 dp[mask][i+1] = (dp[mask][i] +
                                   dp[mask^(1<<i)][i] + res[mask^(1<<i)])%mod;</pre>
             else
                 dp[mask][i+1] = dp[mask][i];
        res[mask] = (res[mask] - dp[mask][N] + mod)%mod;
    }
}
int main()
    fast_io;
    cin>> N;
    for(ll i=0; i<(1<<19); i++)
        res[i]=1;
    cin>> m1;
    memset(cnt,0,sizeof cnt);
    for(ll i=0; i<m1; i++)</pre>
        cin>> v,cnt[v]++;
    countF(0);
    cin >> m2;
    memset(cnt,0,sizeof cnt);
    for(11 i=0; i<m2; i++)</pre>
        cin>> v,cnt[v]++;
    countF(1);
    cin >> m3;
    memset(cnt,0,sizeof cnt);
    for(11 i=0; i<m3; i++)</pre>
        cin>> v,cnt[v]++;
    countF(2);
    cin >> m4;
    memset(cnt,0,sizeof cnt);
    for(11 i=0; i<m4; i++)</pre>
        cin>> v,cnt[v]++;
    countF(3);
```

```
countRes();

11 mul=(((m1*m2)%mod)*((m3*m4)%mod))%mod;
mul=bigMod(mul,mod-2);
for(ll i=0; i<(1<<N); i++)
{
    res[i]=(res[i]*mul)%mod;
    cout<< res[i] << "\n";
}
return 0;
}</pre>
```

6.4 Sum Over Submasks DP

```
Minimum sum of K Submask of a Mask
                         where All On Bits of the Mask exist
                         at least once in the K Submasks
                 **/
ll submask [(1<<16)][16];
int main()
    FIO;
      IN;
//
//
      OUT;
    11 N,K;
    cin >> N >> K;
    vector<pair<pl1,ll> >inp(N);
    for(ll i=0;i<N;i++) cin>> inp[i].ff.ff >> inp[i].ff.ss >> inp[i].ss;
    for(ll mask=0; mask<(1<<N); mask++){</pre>
        11 sum=0;
        11 h=0, w=0;
        11 cnt=0;
        for(ll i=0;i<N;i++){</pre>
             if((1 << i) \& mask) {
                 sum+=inp[i].ff.ff*inp[i].ff.ss*inp[i].ss;
                 h=max(h,inp[i].ff.ff);
                 w=max(w,inp[i].ff.ss);
                 cnt+=inp[i].ss;
            }
        }
        submask[mask][1]=h*w*cnt-sum;
    }
    for(11 k=2; k<=K; k++){
        for (ll mask=0; mask<(1<<N); ++mask){</pre>
             submask[mask][k]=INF;
            for (ll s=mask; s; s=(s-1)\&mask){
                 submask[mask][k]=min(submask[mask][k],
                                           submask[s][1]+submask[mask^s][k-1]);
                 submask[mask][k]=min(submask[mask][k],
                                           submask[s][k-1]+submask[mask^s][1]);
            }
        }
```

```
}
cout << submask [(1 << N) -1] [K];
}</pre>
```

6.5 Tree DP Sample

```
/**----End of Template----**/
                /** Maximum multiplication of sizes of connected
                 components of a Tree after removing some edges **/
vll G[MX];
11 sz[MX];
BigInt dp[MX][MX];
bool vis[MX];
BigInt temp[MX][MX];
void DFS(ll u, ll p)
{
    sz[u]=1;
    for(ll i=0;i<MX;i++) temp[u][i]=Integer(1);</pre>
    for(auto v:G[u]){
        if(v==p) continue;
        DFS(v,u);
        for(ll i=sz[u];i>=1;i--){
            for(ll j=sz[v]; j>=0; j--){
                temp[u][i+j]=max(temp[u][i]*dp[v][j],temp[u][i+j]);
        sz[u] += sz[v];
    for(ll i=1;i<=sz[u];i++)
        dp[u][i]=temp[u][i],temp[u][0]=max(temp[u][i]*i,temp[u][0]);
    dp[u][0]=temp[u][0];
}
int main()
{
    FIO;
    11 N;
    cin>> N;
    for(ll i=1;i<N;i++){</pre>
        11 u, v;
        cin>> u >> v;
        G[u].push_back(v);
        G[v].push_back(u);
    }
```

```
DFS(1,-1);
cout<< dp[1][0];
}</pre>
```

7 Miscellaneous

7.1 Common Template Code

```
#include < bits / stdc++.h>
using namespace std;
#include <ext/pb_ds/assoc_container.hpp>
#include <ext/pb_ds/tree_policy.hpp>
#include <ext/pb_ds/detail/standard_policies.hpp>
using namespace __gnu_pbds;
using namespace __gnu_cxx;
#define FIO
                   ios_base::sync_with_stdio(0); cin.tie(0); cout.tie(0);
#define IN
                   freopen("input.txt","r",stdin);
#define OUT
                   freopen("output.txt","w",stdout);
#define debug(x) cout << #x << " --> " << x << "\n";
#define NL
                   printf("\n");
#define case(x)
                  printf("Case %lld: ",x);
#define readI(x) scanf("%d",&x);
                   scanf("%lld",&x);
#define readL(x)
#define writeI(x) printf("%d",x);
#define writeL(X)
                   printf("%lld",x);
#define all(v)
                   v.begin(), v.end()
#define 11
               long long
#define ld
               long double
#define pb
               push_back
#define pii
               pair < int, int >
             pair< 11,11 >
#define pll
#define vii
              vector< int >
#define vll vector< 11 >
#define vss
               vector< string >
#define vdd vector< double >
#define vpi
             vector< pii >
#define vpl
              vector< pll >
#define vvi
               vector< vii >
#define vvl
               vector< vll >
#define PQ
               priority_queue
#define ff
               first
#define ss
               second
#define MX
               100005
#define mod
              1000000007
#define INF
               100000000000000000
#define EPS
               1e-12
/* Special functions:
               find_by_order(k) -->
```

```
returns iterator to the
                           kth largest element counting from O
                  order_of_key(val) -->
                           returns the number of items in a set
                           that are strictly smaller than our item
*/
typedef tree<
                 // type long long
11,
null_type,
less<11>,
rb_tree_tag,
tree_order_statistics_node_update>
ordered_set;
struct compare
    bool operator() (11 a, 11 b)
         return a>b;
};
const 11 p1=131,p2=137;
const 11 mod1=1000000009;
const 11 mod2=1000000007;
bool marked[MX];
vll primes;
inline ll bigMod(ll x, ll n)
    11 res=1;
    while(n){
         if (n\&1) res=(res*x)\%mod;
         x=(x*x)\mbox{\em mod};
         n=n>>1;
    }
    return res;
}
void sieve()
    marked[0] = marked[1] = true;
    for(11 i=2;i*i<MX;i++){</pre>
         if(marked[i] == false){
             \quad \text{for(ll } j = i*i; j < \texttt{MX}; j + = i) \{
```

```
marked[j]=true;
            }
        }
    }
    for(11 i=2;i<MX;i++)</pre>
        if(!marked[i]){
            primes.push_back(i);
        }
}
vpl primeFactors(ll N)
        vpl factors;
        11 pf_id=0,pf=primes[pf_id];
        while(pf*pf<=N){</pre>
        11 cnt=0;
                 while(N%pf==0) N/=pf,cnt++;
        if(cnt) factors.push_back({pf,cnt});
                pf=primes[++pf_id];
        }
        if(N!=1) factors.push_back({N,1});
    return factors;
}
struct pair_hash {
    template <class T1, class T2>
    size_t operator () (const pair<T1,T2> &p) const {
        auto h1 = hash < T1 > \{\}(p.first);
        auto h2 = hash<T2>{}(p.second);
        // Mainly for demonstration purposes, i.e. works but is overly simple
        // In the real world, use sth. like boost.hash_combine
        return h1 ^ h2;
};
struct chash {
        static uint64_t splitmix64(uint64_t x) {
                // http://xorshift.di.unimi.it/splitmix64.c
                x += 0x9e3779b97f4a7c15;
                x = (x ^ (x >> 30)) * 0xbf58476d1ce4e5b9;
                x = (x ^ (x >> 27)) * 0x94d049bb133111eb;
                return x ^(x >> 31);
        }
```

7.2 GP Hash Table Samples

```
#include <ext/pb_ds/assoc_container.hpp>
using namespace __gnu_pbds;
// For integer
gp_hash_table<int, int> table;
// Custom hash function approach is better
const int RANDOM = chrono::high_resolution_clock::now().time_since_epoch().count();
struct chash {
    int operator()(int x) const { return x ^ RANDOM; }
gp hash table<int, int, chash> table;
const ll TIME = chrono::high_resolution_clock::now().time_since_epoch().count();
const 11 SEED = (11)(new 11);
const 11 RANDOM = TIME ^ SEED;
const 11 \text{ MOD} = (int)1e9+7;
const ll MUL = (int)1e6+3;
 struct chash{
    11 operator()(11 x) const { return std::hash<11>{}((x ^ RANDOM) % MOD * MUL); }
gp_hash_table<11, int, chash> table;
unsigned hash_f(unsigned x) {
    x = ((x >> 16) ^ x) * 0x45d9f3b;
    x = ((x >> 16) ^x) * 0x45d9f3b;
    x = (x >> 16) ^ x;
    return x;
struct chash {
    int operator()(ll x) const { return hash_f(x); }
gp_hash_table<11, int, chash> table[N][N];
// so table [i][j][k] is storing an integer for corresponding k as hash
unsigned hash_combine(unsigned a, unsigned b) { return a * 31 + b; }
// For pairs
// The better the hash function, the less collisions
// Note that hash function should not be costly
struct chash {
    int operator()(pii x) const { return x.first* 31 + x.second; }
gp_hash_table<pii, int, chash> table;
// Another recommended hash function by neal on CF
struct custom hash {
    static uint64_t splitmix64(uint64_t x) {
```

```
// http://xorshift.di.unimi.it/splitmix64.c
        x += 0x9e3779b97f4a7c15;
        x = (x ^ (x >> 30)) * 0xbf58476d1ce4e5b9;
        x = (x ^ (x >> 27)) * 0x94d049bb133111eb;
        return x \hat{ } (x >> 31);
    size_t operator()(uint64_t x) const {
        static const uint64_t FIXED_RANDOM =
                chrono::steady_clock::now().time_since_epoch().count();
        return splitmix64(x + FIXED_RANDOM);
    }
};
gp_hash_table<11,int,custom_hash> safe_gp_hash_table;
unordered_map<ll,int,custom_hash> safe_umap;
typedef gp_hash_table<int, int, hash<int>,
equal_to<int>, direct_mod_range_hashing<int>, linear_probe_fn<>,
hash_standard_resize_policy < hash_prime_size_policy,
hash_load_check_resize_trigger < true >> true >>
gp;
gp Tree;
/\!/ Now Tree can probably be used for fenwick, indices can be long long
// S is an offset to handle negative value
// If values can be \geq -1e9, S=1e9+1
// maxfen is the MAXN in fenwick, this case it was 2e9+2;
// Note that it was okay to declare gp in integer as the values were
// still in the range of int.
void add(long long p, int v) {
    for (p += S; p < maxfen; p += p & -p)
        Tree[p] += v;
}
int sum(int p) {
    int ans = 0;
    for (p += S; p; p ^= p & -p)
        ans += Tree[p];
    return ans;
}
```

7.3 Matrix Exponentiation

```
ll mod;
class Matrix{
public:
    vvl mat;
    ll r,c;
    Matrix(ll r, ll c)
        this->r=r,this->c=c;
        vll v(c); for(ll i=0;i<r;i++) mat.push_back(v);</pre>
        for(ll i=0;i<r;i++)</pre>
             for(11 j=0;j<c;j++)</pre>
                 mat[i][j]=0;
    }
    Matrix(vvl ip)
        r=ip.size(),c=ip[0].size();
        for(ll i=0;i<r;i++)</pre>
             for(11 j=0; j < c; j++)
                 mat[i][j]=ip[i][j];
    }
    Matrix operator*(Matrix rhs)
        Matrix temp(r,rhs.c);
        for(11 i=0;i<r;i++){</pre>
             for(11 j=0; j<c; j++){
                 temp.mat[i][j]=0;
                 for(11 k=0;k<c;k++)</pre>
                      temp.mat[i][j]=(temp.mat[i][j]+mat[i][k]*rhs.mat[k][j])%mod;
             }
        }
        return temp;
    }
};
Matrix matPow(Matrix m, ll p)
{
    if(!p){
        Matrix temp(m.r,m.c);
```

```
for(ll i=0;i<m.r;i++) temp.mat[i][i]=1;</pre>
        return temp;
    }
    Matrix temp=matPow(m,p/2);
    temp=temp*temp;
    if(p%2) temp=temp*m;
    return temp;
}
/**
F(n) = a1*F(n-1) + a2*F(n-2) + a3*F(n-3) + .... + akF(n-k);
k*k Matrix:
10 0 0 . . . a1/
/1 0 0 . . . a2/
10 1 0 . . . a3/
. . . . . . . .
. . . . . . . .
|0 \ 0 \ . \ . \ . \ ak|
**/
int main()
{
//
      FIO;
//
      IN;
      OUT;
    11 T;
    cin>> T;
    for(ll cs=1;cs<=T;cs++){</pre>
        ll a,b,n,m;
        cin>> a >> b >> n >> m;
        Matrix mat(2,2);
        mat.mat[0][1]=mat.mat[1][0]=mat.mat[1][1]=1;
        mod=pow(10,m);
        if(n>1) mat=matPow(mat,n-1);
        11 res=(a*mat.mat[0][1]+b*mat.mat[1][1])%mod;
        if(n==0) res=a\%mod;
        else if(n==1) res=b%mod;
```

```
cout<< "Case " << cs << ": " << res << "\n";
}</pre>
```