

Introduction to Naïve Bayes



Course Overview

You are here...

| Term | CDF | GCD | GCDAI | PGPDSAI |
|---------|-------------------------------|--|--|--|
| Term 1 | Data Analytics with Python | Data Analytics with Python | Data Analytics with Python | Data Analytics with Python |
| Term 2 | Data Visualization Techniques | Data Visualization Techniques | Data Visualization Techniques | Data Visualization Techniques |
| Term 3 | EDA & Data Storytelling | EDA & Data Storytelling | EDA & Data Storytelling | EDA & Data Storytelling |
| | | Minor Project | Minor Project | Minor Project |
| Term 4 | | Machine Learning Foundation | Machine Learning Foundation | Machine Learning Foundation |
| Term 5 | | Machine Learning Intermediate | Machine Learning Intermediate | Machine Learning Intermediate |
| Term 6 | | Machine Learning Advanced (Mandatory) | Machine Learning Advanced (Mandatory) | Machine Learning Advanced (Mandatory) |
| | | Data Visualization with Tableau (Elective - I) | Data Visualization with Tableau (Elective - I) | Data Visualization with Tableau (Elective - I) |
| | | Data Analytics with R (Elective - II) | Data Analytics with R (Elective - II) | Data Analytics with R (Elective - II) |
| | | Capstone Project | Capstone Project | Capstone Project |
| Term 7 | | Bonus: Industrial ML (ML – 4 & 5) | Basics of AI, TensorFlow, and Keras | Basics of AI, TensorFlow, and Keras |
| Term 8 | | | Deep Learning Foundation | Deep Learning Foundation |
| Term 9 | | | NPL – I/CV – I | CV – I |
| Term 10 | | | NLP – II/CV – II | NLP – I |
| | | | Capstone Project | Capstone Project |
| Term 11 | | | | CV – II |
| Term 12 | | | | NLP – II |
| | | | | NLP – III + CV – III |
| | | | | AutoVision & AutoNLP |
| | | | | Building AI product |

Term Context

- Decision Tree
- Random Forest
- Principal Component Analysis
- Naïve Bayes Classifier ← You are here...

Agenda

1. What is Naïve Bayes?

Baye's Thm

Naya hai waha

2. Why it is called Naïve?

3. Bayes Theorem & Example

4. Naïve Bayes In Working

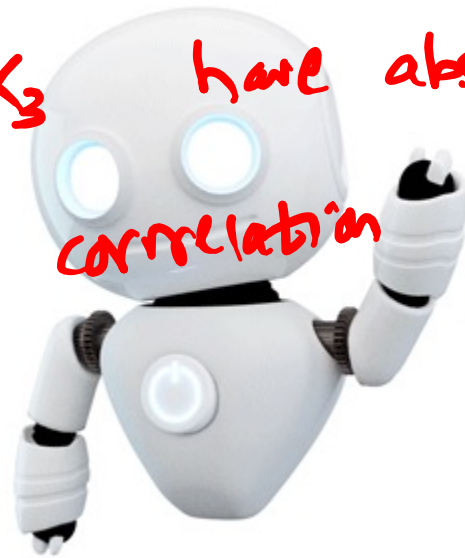
5. Application of Naïve Bayes

6. Pros/Cons of Naïve Bayes

What is Naïve Bayes?

- A family of simple "probabilistic classifiers".
- Based on applying Bayes' theorem with strong (naïve) independence assumptions between the features.

$X_1, X_2, X_3 \perp y \rightarrow$ N.B. algo. will give fantastic results iff
 $X_1, X_2 \& X_3$ have absolutely no correlation or
marginal correlation b/w each other.



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2. Why it is called Naïve?

3. Bayes Theorem & Example

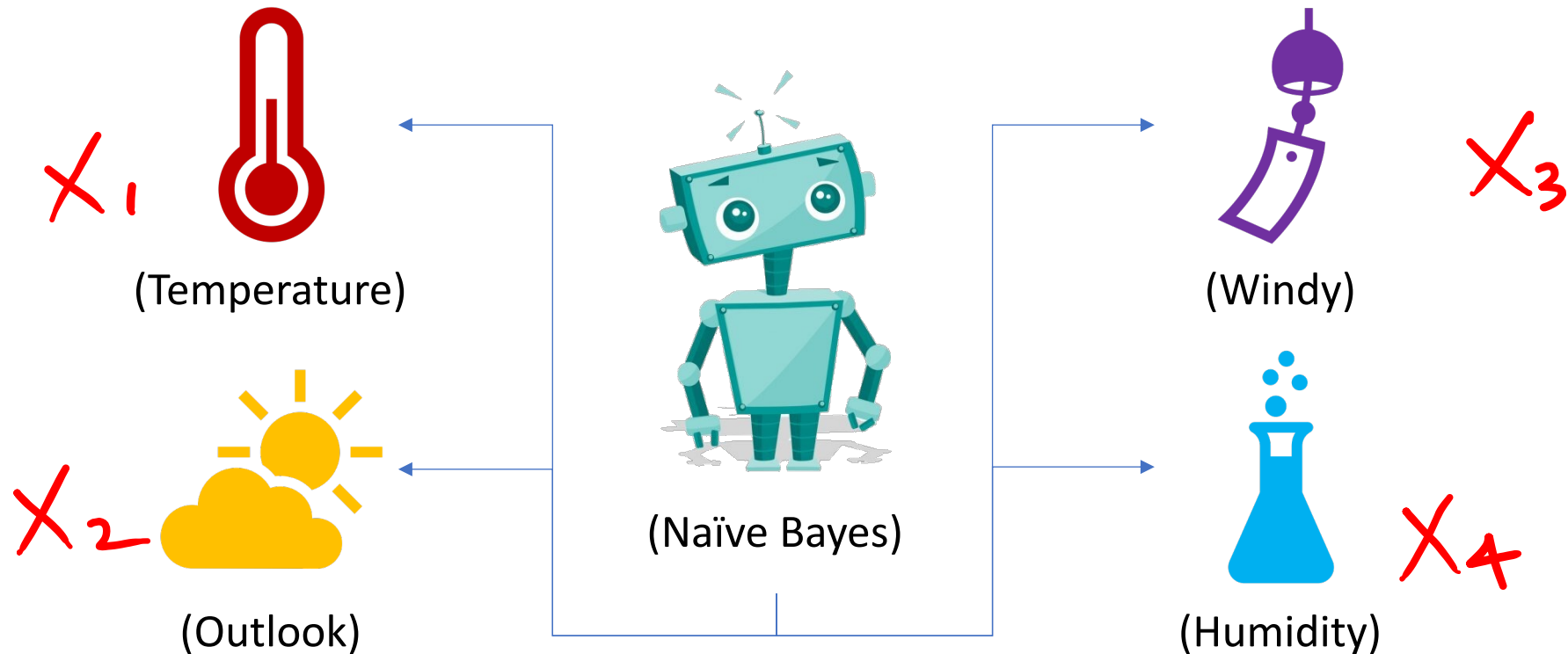
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Why it is called Naïve?

- It assume all attributes to be conditionally independent.
- **Example:** Features describing whether it is a good day to play golf or not.



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Bayes Theorem & Example

- It was named after **Reverend Thomas Bayes**.
- It describes the probability of an **event** happening.
- It is based on **prior knowledge** of conditions that might be related to the event.



$$P(A|B) = \frac{P(B|A) \cdot P(A)}{P(B)}$$

- A, B = Events
- $P(A|B)$ = Probability of A given B is true
- $P(B|A)$ = Probability of B given A is true
- $P(A), P(B)$ = Independent probabilities of A and B

Bayes Theorem & Example

$p(\text{Fire})$

$p(\text{Smoke})$

- Let us say dangerous fires are rare (1%), but smoke is fairly common (10%) due to barbecues,
- We add a condition that 90% of dangerous fires make smoke.

$\uparrow p(\text{Smoke} | \text{Fire})$

- $P(\text{Fire})$ = how often there is fire
- $P(\text{Smoke})$ = how often we see smoke
- $P(\text{Fire} | \text{Smoke})$ = how often there is fire when we see smoke
- $P(\text{Smoke} | \text{Fire})$ = how often we see smoke when there is fire



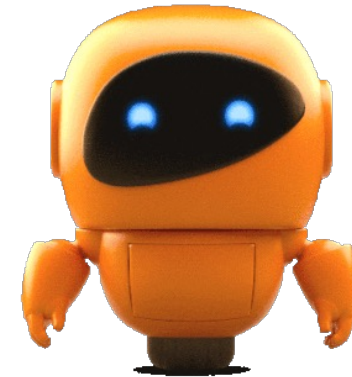
Bayes Theorem & Example

- We can then discover the probability of **dangerous Fire** when there is **Smoke**:

$$P(\text{Fire}|\text{Smoke}) = \frac{P(\text{Smoke}|\text{Fire}) \cdot P(\text{Fire})}{P(\text{Smoke})}$$

$$P(\text{Fire}|\text{Smoke}) = \frac{90\% \cdot 1\%}{10\%}$$

$$P(\text{Fire}|\text{Smoke}) = \underline{\underline{9\%}}$$



- So it is still **worth checking** out for any **smoke** as a **precaution**.

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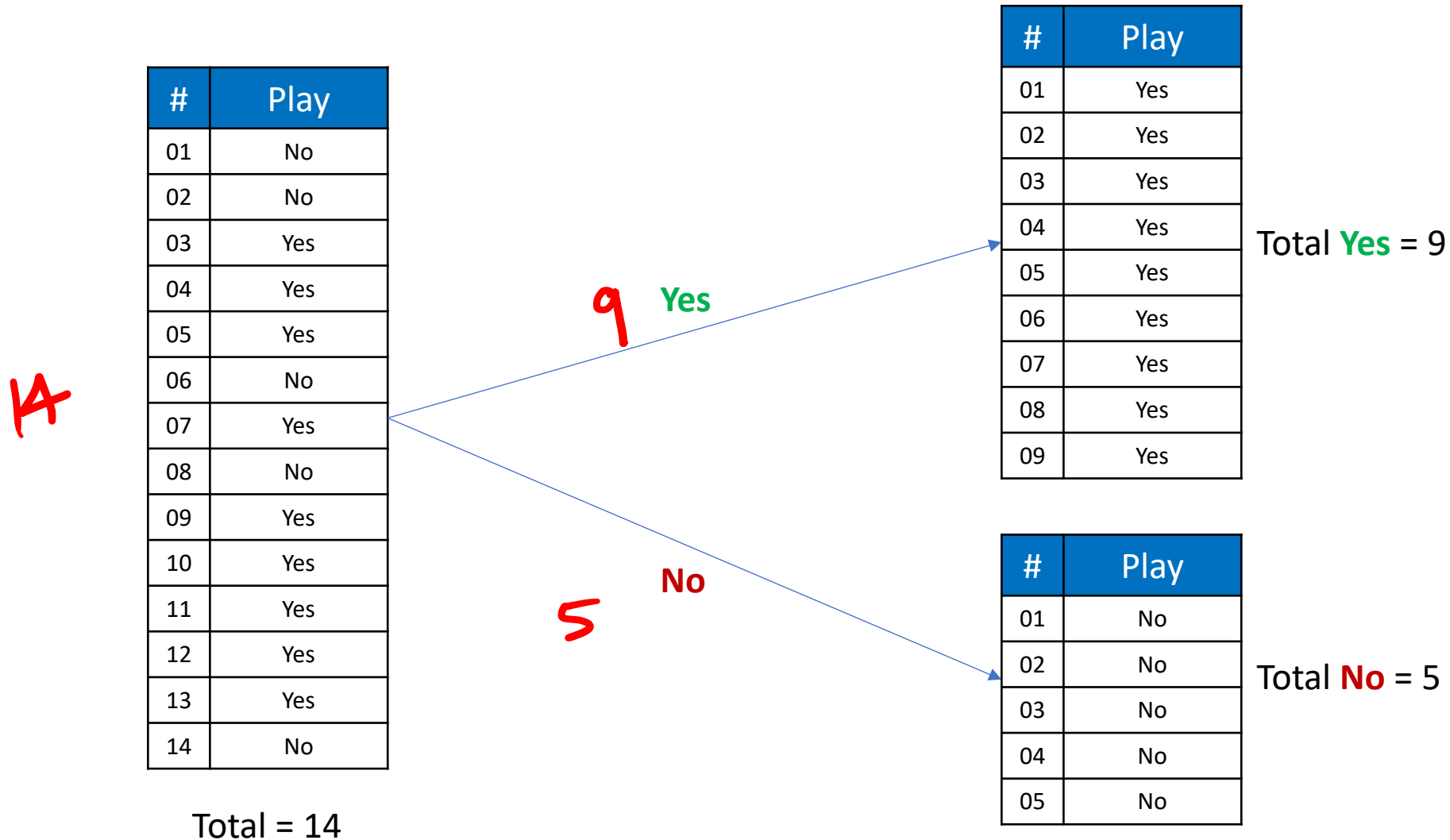
Naïve Bayes In Working

- Let's say we have the following data using which we want to **predict** whether to **play golf** or **not**.

| | X_1 | X_2 | X_3 | X_4 | |
|----|----------|-------------|----------|-------|------|
| # | Outlook | Temperature | Humidity | Windy | Play |
| 01 | Sunny | Hot | High | False | No |
| 02 | Sunny | Hot | High | True | No |
| 03 | Overcast | Hot | High | False | Yes |
| 04 | Rainy | Mild | High | False | Yes |
| 05 | Rainy | Cool | Normal | False | Yes |
| 06 | Rainy | Cool | Normal | True | No |
| 07 | Overcast | Cool | Normal | True | Yes |
| 08 | Sunny | Mild | High | False | No |
| 09 | Sunny | Cool | Normal | False | Yes |
| 10 | Rainy | Mild | Normal | False | Yes |
| 11 | Sunny | Mild | Normal | True | Yes |
| 12 | Overcast | Mild | High | True | Yes |
| 13 | Overcast | Hot | Normal | False | Yes |
| 14 | Rainy | Mild | High | True | No |

$n=14$
Yes 9
No 5

Naïve Bayes In Working



Naïve Bayes In Working

- First we need to identify the probability of **Play = Yes** and **Play = No**.

| # | Play | P(Yes/No) |
|----|-----------------|-------------|
| 01 | Yes 9 | $9 \div 14$ |
| 02 | No 5 | $5 \div 14$ |
| 03 | Total 14 | 100% |

- X₁:** Now we need to calculate **probability** of **each features** with respect to **Play Feature**.

| # | Outlook Calculation | | | | |
|----|---------------------|-----|----|------------|------------|
| | Outlook | Yes | No | P(Yes) | P(No) |
| 01 | Sunny | 2 | 3 | $2 \div 9$ | $3 \div 5$ |
| 02 | Overcast | 4 | 0 | $4 \div 9$ | $0 \div 5$ |
| 03 | Rainy | 3 | 2 | $3 \div 9$ | $2 \div 5$ |
| 04 | Total | 9 | 5 | 100% | 100% |

X₂:

| # | Temperature Calculation | | | | |
|----|-------------------------|-----|----|------------|-------------------|
| | Temperature | Yes | No | P(Yes) | P(No) |
| 01 | Hot | 2 | 2 | $2 \div 9$ | 2 $\div 5$ |
| 02 | Mild | 4 | 2 | $4 \div 9$ | $2 \div 5$ |
| 03 | Cool | 3 | 1 | $3 \div 9$ | $1 \div 5$ |
| 04 | Total | 9 | 5 | 100% | 100% |

Naïve Bayes In Working

X₃:

| # | Humidity Calculation | | | | |
|----|----------------------|-----|----|------------|------------|
| | Humidity | Yes | No | P(Yes) | P(No) |
| 01 | High | 3 | 4 | $3 \div 9$ | $4 \div 5$ |
| 02 | Normal | 6 | 1 | $6 \div 9$ | $1 \div 5$ |
| 03 | Total | 9 | 5 | 100% | 100% |

X₄:

| # | Windy Calculation | | | | |
|----|-------------------|-----|----|------------|------------|
| | Windy | Yes | No | P(Yes) | P(No) |
| 01 | False | 6 | 2 | $6 \div 9$ | $2 \div 5$ |
| 02 | True | 3 | 3 | $3 \div 9$ | $3 \div 5$ |
| 03 | Total | 9 | 5 | 100% | 100% |

- We have finally **obtained** all the **values** that are required to a **predict a new value.**
- Let's say we have a new instance as following:

Unseen
Data →

| # | Outlook | Temperature | Humidity | Windy | Play |
|----|---------|-------------|----------|-------|------|
| 01 | Sunny | Cool | High | True | ? |



Naïve Bayes In Working

- Now we need to estimate the **probability** that we can **play game** or **not** using those **lookup tables**.

| Lookup Table | | | | | |
|--------------|--------------|-----|----|--------|-------|
| | Categories | Yes | No | P(Yes) | P(No) |
| Outlook | ☑ Sunny | 2 | 3 | 2 ÷ 9 | 3 ÷ 5 |
| | Overcast | 4 | 0 | 4 ÷ 9 | 0 ÷ 5 |
| | Rainy | 3 | 2 | 3 ÷ 9 | 2 ÷ 5 |
| | Total | 9 | 5 | 100% | 100% |
| Temperature | Hot | 2 | 2 | 2 ÷ 9 | 3 ÷ 5 |
| | Mild | 4 | 2 | 4 ÷ 9 | 2 ÷ 5 |
| | ☑ Cool | 3 | 1 | 3 ÷ 9 | 1 ÷ 5 |
| | Total | 9 | 5 | 100% | 100% |
| Humidity | ☑ High | 3 | 4 | 3 ÷ 9 | 4 ÷ 5 |
| | Normal | 6 | 1 | 6 ÷ 9 | 1 ÷ 5 |
| | Total | 9 | 5 | 100% | 100% |
| Windy | False | 6 | 2 | 6 ÷ 9 | 2 ÷ 5 |
| | ☑ True | 3 | 3 | 3 ÷ 9 | 3 ÷ 5 |
| | Total | 9 | 5 | 100% | 100% |

Probability that we can play a game:

- $P(\text{Outlook} = \text{Sunny} \mid \text{Play} = \text{Yes}) = 2 \div 9$
- $P(\text{Temperature} = \text{Cool} \mid \text{Play} = \text{Yes}) = 3 \div 9$
- $P(\text{Humidity} = \text{High} \mid \text{Play} = \text{Yes}) = 3 \div 9$
- $P(\text{Windy} = \text{True} \mid \text{Play} = \text{Yes}) = 3 \div 9$
- $P(\text{Play} = \text{Yes}) = 9 \div 14$

Naïve Bayes In Working

- Now we need to estimate the **probability** that we can **play game** or **not** using those **lookup tables**.

| Lookup Table | | | | | |
|--------------|------------|-----|----|------------|------------|
| | Categories | Yes | No | P(Yes) | P(No) |
| Outlook | ✓ Sunny | 2 | 3 | $2 \div 9$ | $3 \div 5$ |
| | Overcast | 4 | 0 | $4 \div 9$ | $0 \div 5$ |
| | Rainy | 3 | 2 | $3 \div 9$ | $2 \div 5$ |
| | Total | 9 | 5 | 100% | 100% |
| Temperature | Hot | 2 | 2 | $2 \div 9$ | $3 \div 5$ |
| | Mild | 4 | 2 | $4 \div 9$ | $2 \div 5$ |
| | ✓ Cool | 3 | 1 | $3 \div 9$ | $1 \div 5$ |
| | Total | 9 | 5 | 100% | 100% |
| Humidity | ✓ High | 3 | 4 | $3 \div 9$ | $4 \div 5$ |
| | Normal | 6 | 1 | $6 \div 9$ | $1 \div 5$ |
| | Total | 9 | 5 | 100% | 100% |
| Windy | False | 6 | 2 | $6 \div 9$ | $2 \div 5$ |
| | ✓ True | 3 | 3 | $3 \div 9$ | $3 \div 5$ |
| | Total | 9 | 5 | 100% | 100% |

Probability that we cannot play a game:

- $P(\text{Outlook} = \text{Sunny} \mid \text{Play} = \text{No}) = 3 \div 5$
- $P(\text{Temperature} = \text{Cool} \mid \text{Play} = \text{No}) = 1 \div 5$
- $P(\text{Humidity} = \text{High} \mid \text{Play} = \text{No}) = 4 \div 5$
- $P(\text{Windy} = \text{True} \mid \text{Play} = \text{No}) = 3 \div 5$
- $P(\text{Play} = \text{No}) = 5 \div 14$

Naïve Bayes In Working

- Next we will multiply all the probability for both the cases (being Yes or No) individually.

$$P(X \mid \text{Play} = \text{Yes}) \cdot P(\text{Play} = \text{Yes})$$

$$(2 \div 9) * (3 \div 9) * (3 \div 9) * (3 \div 9) * (9 \div 14)$$

0.0053



$$P(X \mid \text{Play} = \text{No}) \cdot P(\text{Play} = \text{No})$$

$$(3 \div 5) * (1 \div 5) * (4 \div 5) * (3 \div 5) * (5 \div 14)$$

0.0206



- Finally we need to divide both of the result by evidence P(X) to normalize.
- The **evidence** for both the equation is **same**.
- We can find the value from the Total column of the lookup table.

Naïve Bayes In Working

Unseen

- $P(X) = P(\text{Outlook} = \text{Sunny}) * P(\text{Temperature} = \text{Cool}) * P(\text{Humidity} = \text{High}) * P(\text{Windy} = \text{True})$
- $P(X) = (5 \div 14) * (4 \div 14) * (7 \div 14) * (6 \div 14)$
- $P(X) = 0.02186$
- Finally we will use this value to divide the probability of playing Yes and No.

$$P(\text{Play} = \text{Yes} \mid X) = 0.0053 \div 0.02186 = 0.2424 \checkmark$$

$$P(\text{Play} = \text{No} \mid X) = 0.0206 \div 0.02186 = 0.9421 \checkmark$$

$$0.9421 > 0.2424$$

- Given the final outcome **we cannot play Golf.**



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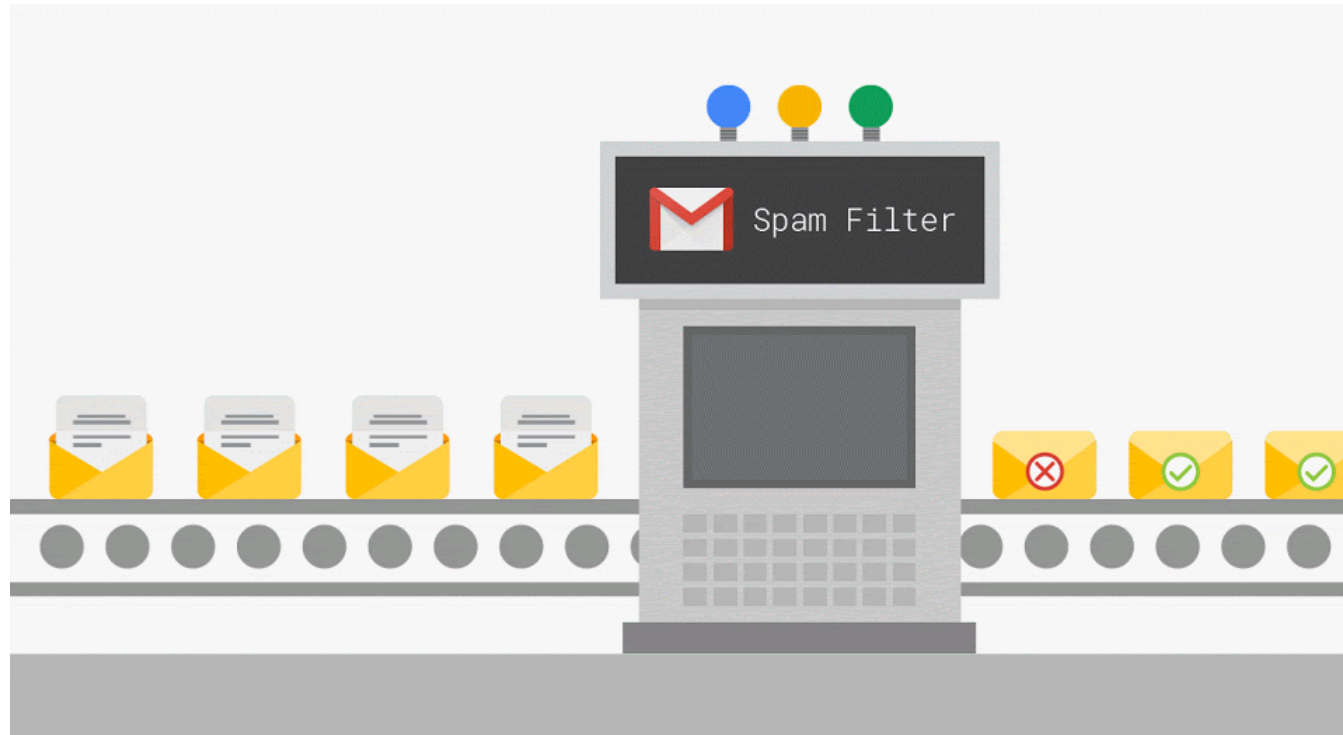
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Spam Filtration

- Naïve bayes can also be used to **identify** whether the mail is **spam free or not**.



Weather Prediction

- We can **forecast** the **weather condition** of specific **region** based on the pre historic data .
- It can **save resources** and **prepare** for the **changes** coming forth.



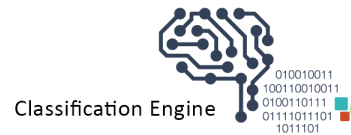
Face Recognition

- It is considered as automated approach to verify the identification of the human being.
- It is done based on characteristics such as fingerprint, iris pattern, or face.



Text Classification (NLP)

- Naïve Bayes have a higher success rate in terms of classifying text as compared to other algorithms.



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Pros/Cons of Naïve Bayes

Pros

- It requires less training data and handles both categorical and discrete data.
- It is very simple, fast and easy to implement even in real time.
- Highly scalable with number of data points.
- Not sensitive to irrelevant features.

Cons

- ✱ • Assumption of independent predictors, which is impossible in real life.
- Categories present in the test dataset, which was not observed in training (Also known as Zero Frequency).
- To handle zero frequency problem smoothing techniques are used which we will cover later on.

The background features several abstract, flowing blue lines. A prominent, thick, glossy blue line curves from the top left towards the bottom center. Other thinner, more translucent blue lines sweep across the lower half of the image, creating a sense of movement and depth. The overall aesthetic is clean and modern.

Thank You