

Lambda Calculus

Instructions:

Solutions of the exercises are to be delivered before Wednesday, the 12th of April at 10:15AM.

Solutions should be placed in a separate folder with the name “**Assignment05**”.

Please submit answers to all the exercises in **one** text file.

Exercise 1 (2 points)

Consider the following λ -expressions. Indicate which occurrences of variables are bound and which ones are free in the expressions.

1. $(\lambda x. x) y (\lambda y. y x) x$

2. $((\lambda x. \lambda y. \lambda z. x y z) (\lambda x. y x) y) (\lambda x. z x)$

Exercise 2 (2 points)

Define boolean functions `and` and `or` in Lambda Calculus and show that `True and False = False` and `True or False = True` based on the definitions of `True` and `False` functions from the lecture hours.

Exercise 3 (2 points)

Reduce the following λ -expressions to their normal form where possible.

1. $(\lambda x. (\lambda z. z y) x) (\lambda x. x)$

2. $(\lambda x. x x y) (\lambda x. x x y)$