

$$1) \cos \theta = \frac{\vec{U} \cdot \vec{V}}{|\vec{U}| |\vec{V}|} = \frac{-2+8-3}{\sqrt{4} \sqrt{21}}$$

$$\boxed{\theta = 71.92^\circ}$$

$$2) \begin{vmatrix} 0 & 1 & 1 \\ x & 3 & 0 \\ x & y & 1 \end{vmatrix} = (-x) + xy - 3x = 0$$

$$x(y-4) = 0$$

$$\boxed{x=0 \mid y=4}$$

$$3) \alpha = \cos^{-1} \left(\frac{1}{|A|} \right) = 74.5^\circ$$

$$\beta = \cos^{-1} \left(\frac{2}{|A|} \right) = 57.1^\circ$$

$$\gamma = \cos^{-1} \left(\frac{3}{|A|} \right) = 36.1^\circ$$

$$4) \vec{AB} = (6, 2, 3)$$

$$\vec{AC} = (2, -2, 1)$$

$$\begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ 6 & 2 & 3 \\ 2 & -2 & 1 \end{vmatrix} = 18\hat{i} + 16\hat{k}$$

$$\sqrt{64+256} = 8\sqrt{5}/2$$

$$\boxed{4\sqrt{5}}$$

$$5) \begin{vmatrix} 1 & 2 & 3 \\ -3 & 1 & 4 \\ 1 & 2 & 1 \end{vmatrix} = 1(-7) - 2(-7) + 3(-7) \\ = -7(2) = |-14| = 14 //$$

$$6) \begin{vmatrix} 2 & -1 & 3 \\ 0 & 2 & -5 \\ 1 & -1 & -2 \end{vmatrix} = 2(-9) + 5 + 3(-2) = -19 //$$

$$7) \vec{u} \times \vec{v} = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ 1 & -4 & 1 \\ 2 & 3 & 0 \end{vmatrix} = -3\hat{i} + 2\hat{j} + 11\hat{k} = \frac{-3, 2, 11}{\sqrt{134}}$$

$$\vec{u} = -0.26\hat{i} + 0.17\hat{j} + 0.95\hat{k} //$$

$$8) d = \cos^{-1} \left(\frac{2+12+6}{3 \cdot 7} \right) = 17.75^\circ //$$

$$9) \vec{c} = \frac{(5, 0, 0) + 3(-1, 2, 2)}{2} \times (5, 0, 0)$$

$$\vec{c} = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ 1 & 3 & 3 \\ 5 & 0 & 0 \end{vmatrix} = 0 + 15\hat{j} - 15\hat{k} = 15(\hat{j} - \hat{k}) //$$

$$10) \begin{matrix} AB = (1, -6, 4) \\ AC = (-1, -1, 0) \end{matrix} \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ 1 & -6 & 4 \\ -1 & -1 & 0 \end{vmatrix} = 4\hat{i} - 4\hat{j} + 7\hat{k}$$

$$\sqrt{16+16+49} = 9 \Rightarrow \boxed{\text{Area} = 4.5} //$$