



Figure 3. Cauchy's quadric for an *indefinite dielectric media*, where eigenvalues of $\hat{\epsilon}$ are not all the same sign. The quadric consists of a two-sheeted hyperboloid and an one-sheeted one. Asymptotic cone, that divides the space into two regions, is also shown.

\bar{u}_1 axis, respectively, it is easily shown that:

$$\tan \psi = -\frac{|\varepsilon_3|}{\varepsilon_1} \tan \phi \quad (16)$$

Our proposed alternative method attains the same result (16), by using Cauchy's quadric section given by:

$$\varepsilon_1 x_1^2 - |\varepsilon_3| x_3^2 = -1$$

3. RAY TRACING IN RHM AND LHM INDEFINITE MEDIA WITH DIELECTRIC ANISOTROPY

In [22], it was shown that in uniaxial right-handed media, vector $\bar{\varepsilon}_n$ is collinear with the extraordinary ray direction.

In uniaxial left-handed media, $\bar{\varepsilon}_n$ also lies in the same plane that $\bar{\nu}$, $\bar{\varepsilon}_\nu$ and \bar{n} . Since the angle between \bar{E} and \bar{D} is the same as the angle between \bar{t} and \bar{n} and Cauchy's theorem [22] states that $\bar{\varepsilon}_n \cdot \bar{\nu}$ ($= \bar{n} \cdot \bar{\varepsilon}_\nu$) also vanishes, vector $\bar{\varepsilon}_n$ is collinear with \bar{t} , but may be antiparallel.

Our method is applied to four media with dielectric anisotropy and magnetic isotropy [4] with the following material parameters:

This kind of media are named *indefinite* because the eigenvalues of their permittivity tensors are not all the same sign.

Figure 3 shows the plot of the two shells (double-sheeted and one-sheeted hyperboloids) of Cauchy's quadric for dielectric parameters of