

Pop Andreea-Diana (Lector Dr.)

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Nota Sem: 10 dacă s-a obținut nr. med. de activ.  
(parte întreagă) sau mai mult  
ponderat:  $\text{nr. activ. obținute} / \text{nr. mediu}$

# Operații aritmetice de bază

## Adunarea

Ex:

în baza 10:

$$\begin{array}{r} 10+1+1 \leftarrow \\ 743_{(10)} + \\ \underline{59_{(10)}} \\ 802 \end{array}$$

$$\begin{aligned} (3+9) / 10 &= 1 \text{ rest } 2 \\ (4+5+1) / 10 &= 1 \text{ rest } 0 \\ (7+0+1) / 10 &= 0 \text{ rest } 7 \end{aligned}$$

$$\begin{array}{r} a_m a_{m-1} \dots a_1 a_0(p) \leftarrow \\ b_m b_{m-1} \dots b_1 b_0(p) \\ \hline c_k c_{k-1} \dots c_1 c_0(p) \end{array}$$

$$i = 0, \max(m, n)$$

$$k = \max(m, n) + 1 \text{ dacă } \star_{\max(m, n)} \neq 0$$

$$x_0 = 0$$

$$(a_i + b_i + x_i) / p = x_{i+1} \text{ rest } c_i$$

baza 2

$$\begin{array}{r} 110010_{(2)} + \\ 10011_{(2)} \\ \hline 1000101_{(2)} \end{array}$$

baza 5

$$\begin{array}{r} 1234_{(5)} + \\ 340_{(5)} \\ \hline 2124_{(5)} \end{array}$$

baza 16

$$\begin{array}{r} 7E2A_{(16)} + \\ 3F2_{(16)} \\ \hline 821C_{(16)} \end{array}$$



Grindarea

Ex:  $\begin{array}{r} 2805_{(10)} \\ - 373_{(10)} \\ \hline 2432_{(10)} \end{array}$

$5 \geq 3 \quad 5 - 3 = 2$   
 $0 < 7 \quad 10 + 0 - 7 = 3$   
 $8 - 1 \geq 3 \quad 8 - 1 - 3 = 4$   
 $2 \geq 0 \quad 2 - 0 = 2$

$A \geq B$

$\begin{array}{r} a_n a_{n-1} \dots a_1 a_0 (p) \\ b_m b_{m-1} \dots b_1 b_0 (p) \\ \hline c_n c_{n-1} \dots c_1 c_0 (p) \end{array}$

$i = \overline{0, n}, x_0 = 0$

$$c_i = \begin{cases} a_i + x_i - b_i, & \text{dac\u0103 } a_i + x_i \geq b_i, x_{i+1} = 0 \\ p + a_i + x_i - b_i, & \text{altfel, } x_{i+1} = -1 \end{cases}$$

baza 2

$\begin{array}{r} 10110_{(2)} \\ - 1101_{(2)} \\ \hline 01001_{(2)} \end{array}$

$\begin{array}{r} 9A3CF_{(16)} \\ - BE5C_{(16)} \\ \hline 8E573_{(16)} \end{array}$

baza 8

$\begin{array}{r} 6240_{(8)} \\ - 2405_{(8)} \\ \hline 3633_{(8)} \end{array}$

$\begin{array}{r} 19 \\ - 14 \\ \hline 5 \end{array}$

$\begin{array}{r} 25 \\ - 11 \\ \hline 14 = E \end{array}$

## Înmulțirea cu o cifră

$$\begin{array}{r} \text{Ex: } \begin{matrix} +3 & +2 & +1 & \leftarrow \\ 5 & 4 & 0 & 12 \end{matrix} \end{array} \quad \begin{matrix} (10) \\ * \end{matrix}$$

$$\begin{array}{r} 7_{(10)} \\ \hline 378084_{(10)} \end{array}$$

$$7 * 2 = 14; 14 / 10 = 1 \text{ rest } 4 \quad (b * a_i + t_i) / p = t_{i+1} \text{ rest } c_i$$
$$(7 * 1 + 1) / 10 = 0 \text{ rest } 8$$
$$(7 * 0 + 0) / 10 = 0 \text{ rest } 0$$
$$(7 * 4 + 0) / 10 = 2 \text{ rest } 8$$
$$(7 * 5 + 2) / 10 = 3 \text{ rest } 7$$
$$c_{m+1} = t_{m+1}$$

$$\tau_{n+1} = \tau_{n+1}$$

$$\overline{a_n a_{n-1} \dots a_1 a_0(p)}^* \leftarrow \mathcal{O}(p)$$

$$\kappa_{m+1} \kappa_m \kappa_{m-1} \cdots \kappa_1 \kappa_0(p)$$

$$i = \overline{0, m}, t_0 = 0$$

$$\begin{array}{r} \text{+1} \quad \text{+1} \\ 20121(3) \times \\ \quad 2(3) \\ \hline 111012(3) \end{array}$$

$$2^2 \quad 2 \quad A \quad 3 \quad \star$$

B (16)

$$1001_{(16)}$$

$$33:16 = 2 \text{ R } 1$$

$$112:16 = 770$$

$$2^9:16 = 1 \rightarrow 13$$



### Împărțirea la o cifră

Ex:  $\rightarrow 2075_{(10)} : 6_{(10)} = 0345_{(10)} \text{ rest } 5_{(10)}$

$(0 \cdot 10 + 2) : 6 = 0 \text{ rest } 2$

$(2 \cdot 10 + 0) : 6 = 20 : 6 = 3 \text{ rest } 2$

$(2 \cdot 10 + 7) : 6 = 27 : 6 = 4 \text{ rest } 3$

$(3 \cdot 10 + 5) : 6 = 35 : 6 = 5 \text{ rest } 5$

$\rightarrow a_m a_{m-1} \dots a_1 a_0_{(p)} : b_{(p)} = r_m r_{m-1} \dots r_1 r_0_{(p)} \text{ rest } r_{(p)}$

$i = \overline{m, 0} \quad r_m = 0$

$(r_i \cdot p + a_i) / b = r_{i+1} \text{ rest } r_{i+1}$

$r_i = r_{i-1}$

baza 7:

$2163_{(7)} : 4_{(7)} = 0366_{(7)} \text{ rest } 0_{(7)}$

$2 : 4 = 0 \text{ rest } 2$

$(2 \cdot 7 + 1) : 4 = 15 : 4 = 3 \text{ rest } 3$

$(3 \cdot 7 + 6) : 4 = 27 : 4 = 6 \text{ rest } 3$

$(3 \cdot 7 + 3) : 4 = 24 : 4 = 6$

$2AC8_{(16)} : 6_{(16)} = 0721_{(16)} \text{ rest } 2_{(16)}$

$(32 + 10) / 6 = 42 / 6 = 7$