## Mathematics in DSA Curriculum

### Comprehensive Problem Set

### April 17, 2025

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### 1 Week 1: Number Theory (GCD, LCM, Primes)

- 1.1 Easy (5)
- 1. GCD of Two Numbers (LeetCode 1071)
- 2. LCM of Two Numbers (GFG)
- 3. Check if a Number is Prime (LeetCode 204)
- 4. Ugly Number (Primes 2,3,5) (LeetCode 263)
- 5. Sieve of Eratosthenes (LeetCode 204)
- 1.2 Medium (10)
- 1. Prime Factorization
- 2. Count Primes in Range (LeetCode 204)
- 3. GCD of Array (LeetCode 1979)
- 4. LCM of Array
- 5. Ugly Number II (Dynamic Programming) (LeetCode 264)
- 6. Super Ugly Number (LeetCode 313)
- 7. Largest Coprime Divisor
- 8. Sum of GCD of Pairs
- 9. Euler's Totient Function
- 10. Modular Multiplicative Inverse
- 1.3 Hard (10)
- 1. Number of Divisors in Range
- 2. Prime Pairs (Goldbach Conjecture) (LeetCode 2761)
- 3. Closest Prime Numbers in Range (LeetCode 2523)
- 4. GCD of Subarrays
- 5. LCM of Subarrays
- 6. Prime Substrings (LeetCode 2762)
- 7. Bezout's Identity (Extended GCD)
- 8. Chinese Remainder Theorem
- 9. Prime Counting Function (Legendre's Formula) (LeetCode 204)
- 10. Sum of Primes in Range (Segmented Sieve)

# 2 Week 2: Modular Arithmetic and Exponentiation

- 2.1 Easy (5)
- 1. Modular Addition
- 2. Power of Two (LeetCode 231)
- 3. Power of Three (LeetCode 326)
- 4. Modular Subtraction
- 5. Fast Exponentiation (Iterative)
- 2.2 Medium (10)
- 1. Modular Multiplication
- 2. Modular Division
- 3. Binary Exponentiation (Recursive)
- 4. Matrix Exponentiation
- 5. Super Pow (Modular Exponentiation) (LeetCode 372)
- 6. Geometric Series Sum (Mod Inverse)
- 7. Fermat's Little Theorem
- 8. Wilson's Theorem
- 9. Euler's Theorem
- 10. Discrete Logarithm (Baby-Step Giant-Step)
- 2.3 Hard (10)
- 1. Modular Square Root (Tonelli-Shanks)
- 2. Chinese Remainder Theorem (Non-Coprime Moduli)
- 3. Lucas Theorem (Combinatorics Mod Prime)
- 4. Pollard's Rho Algorithm (Factorization)
- 5. RSA Algorithm (Encryption/Decryption)
- 6. Diffie-Hellman Key Exchange
- 7. Modular Log (Baby-Step Giant-Step)

- 8. Primitive Root Modulo N
- 9. Carmichael Function
- 10. Quadratic Residues

# 3 Week 3: Combinatorics (Factorials, Combinations, Catalan Numbers)

- 3.1 Easy (5)
- 1. Factorial of a Number
- 2. Combinations (nCr) (LeetCode 77)
- 3. Pascal's Triangle (LeetCode 118)
- 4. Pascal's Triangle II (LeetCode 119)
- 5. Catalan Numbers
- 3.2 Medium (10)
- 1. Permutations (nPr) (LeetCode 46)
- 2. Unique Paths (Grid) (LeetCode 62)
- 3. Unique Paths II (Obstacles) (LeetCode 63)
- 4. Count Derangements
- 5. Count Binary Strings Without Consecutive 1s
- 6. Count Valid Parentheses (Catalan) (LeetCode 22)
- 7. Count Ways to Reach Nth Stair (LeetCode 70)
- 8. Count Ways to Tile a Board
- 9. Count Palindromic Subsequences (LeetCode 730)
- 10. Count Inversions (Merge Sort) (LeetCode 315)
- 3.3 Hard (10)
- 1. Count Permutation Sequences (LeetCode 60)
- 2. Count Valid Permutations (Dice) (LeetCode 1155)
- 3. Count Ways to Distribute Candies (LeetCode 135)
- 4. Count Ways to Partition a Set (Bell Numbers)
- 5. Count Ways to Color a Graph (LeetCode 256)
- 6. Count Ways to Place Houses (LeetCode 2320)
- 7. Count Ways to Build Rooms (LeetCode 1916)

- 8. Count Ways to Arrange Balls (LeetCode 2403)
- 9. Count Ways to Make Fair Array (LeetCode 1664)
- 10. Count Ways to Split a String (LeetCode 1573)

#### 4 Week 4: Fibonacci and Recurrence Relations

- $4.1 \quad \text{Easy} (5)$
- 1. Fibonacci Number (LeetCode 509)
- 2. Climbing Stairs (LeetCode 70)
- 3. Tribonacci Number (LeetCode 1137)
- 4. House Robber (LeetCode 198)
- 5. Min Cost Climbing Stairs (LeetCode 746)
- 4.2 Medium (10)
- 1. House Robber II (LeetCode 213)
- 2. Decode Ways (LeetCode 91)
- 3. Unique Binary Search Trees (LeetCode 96)
- 4. K-th Symbol in Grammar (LeetCode 779)
- 5. Tiling a Rectangle with Squares (LeetCode 1240)
- 6. Domino and Tromino Tiling (LeetCode 790)
- 7. Knight Dialer (LeetCode 935)
- 8. Number of Dice Rolls With Target Sum (LeetCode 1155)
- 9. Count Vowels Permutation (LeetCode 1220)
- 10. Number of Ways to Stay in the Same Place (LeetCode 1269)
- 4.3 Hard (10)
- 1. Split Array Largest Sum (LeetCode 410)
- 2. Minimum Cost to Merge Stones (LeetCode 1000)
- 3. Minimum Falling Path Sum (LeetCode 931)
- 4. Maximum Height by Stacking Cuboids (LeetCode 1691)
- 5. Number of Music Playlists (LeetCode 920)
- 6. Count All Possible Routes (LeetCode 1575)
- 7. Number of Ways to Reorder Array (LeetCode 1569)
- 8. Count Ways to Build Rooms (LeetCode 1916)
- 9. Number of Ways to Separate Numbers (LeetCode 1977)
- 10. Count Number of Special Subsequences (LeetCode 1955)

### 5 Week 5: Bit Manipulation Techniques

- 5.1 Easy (5)
- 1. Single Number (LeetCode 136)
- 2. Number of 1 Bits (LeetCode 191)
- 3. Hamming Distance (LeetCode 461)
- 4. Power of Two (LeetCode 231)
- 5. Missing Number (LeetCode 268)
- 5.2 Medium (10)
- 1. Single Number II (LeetCode 137)
- 2. Single Number III (LeetCode 260)
- 3. Reverse Bits (LeetCode 190)
- 4. Subsets (Bitmask) (LeetCode 78)
- 5. Gray Code (LeetCode 89)
- 6. Divide Two Integers (Bit Shifts) (LeetCode 29)
- 7. Sum of Two Integers (Bitwise) (LeetCode 371)
- 8. Maximum Product of Word Lengths (LeetCode 318)
- 9. Find the Difference (LeetCode 389)
- 10. Binary Watch (LeetCode 401)
- 5.3 Hard (10)
- 1. Minimum Flips to Make a OR b Equal to c (LeetCode 1318)
- 2. Find XOR Sum of All Pairs (LeetCode 1835)
- 3. Count Pairs With XOR in Range (LeetCode 1803)
- 4. Minimum Number of Flips to Convert Binary Matrix (LeetCode 1284)
- 5. Maximum XOR of Two Numbers in an Array (LeetCode 421)
- 6. Repeated DNA Sequences (Bitmask) (LeetCode 187)
- 7. Minimum Number of Operations to Make Array Continuous (LeetCode 2009)
- 8. Find K-th Smallest Pair Distance (LeetCode 719)
- 9. Count Unique Characters of All Substrings (LeetCode 828)
- 10. Number of Wonderful Substrings (LeetCode 1915)

### 6 Week 6: Probability Basics and Expected Value Problems

- 6.1 Easy (5)
- 1. Flipping a Coin (Simulation) (LeetCode 519)
- 2. Rolling a Dice (Simulation) (LeetCode 1223)
- 3. Probability of Drawing a Red Ball
- 4. Probability of Two Dice Sum
- 5. Expected Value of a Dice Roll
- 6.2 Medium (10)
- 1. New 21 Game (DP + Probability) (LeetCode 837)
- 2. Knight Probability in Chessboard (LeetCode 688)
- 3. Random Pick with Weight (LeetCode 528)
- 4. Random Pick Index (Reservoir Sampling) (LeetCode 398)
- 5. Generate Random Point in a Circle (LeetCode 478)
- 6. Probability of Winning a Game
- 7. Expected Number of Trials
- 8. Monty Hall Problem
- 9. Birthday Paradox
- 10. Gambler's Ruin Problem
- 6.3 Hard (10)
- 1. Dice Roll Simulation (DP) (LeetCode 1223)
- 2. Number of Dice Rolls With Target Sum (DP) (LeetCode 1155)
- 3. Soup Servings (DP + Probability) (LeetCode 808)
- 4. Random Flip Matrix (Reservoir Sampling) (LeetCode 519)
- 5. Random Point in Non-overlapping Rectangles (LeetCode 497)
- 6. Expected Value of a Binomial Distribution
- 7. Expected Value of a Geometric Distribution

- 8. Markov Chains (Weather Prediction)
- 9. Bayes' Theorem (Medical Testing)
- 10. Chebyshev's Inequality

### 7 Additional Notes

#### About This Curriculum

- **Problem Sources:** Each problem is linked to its source (LeetCode or GeeksforGeeks).
- Difficulty Progression: Problems are organized from Easy to Medium to Hard within each topic.
- Topic Coverage: Each week focuses on a core mathematical concept essential for DSA with practical coding problems.
- Completion Tracking: All problems are marked as completed in this document.