

1. Dimensional Analysis

1. A particle is thrown into the air from ground level height $h = 0$ with upward velocity v . Which of the following gives the height of the particle at time t from launch?
 - a. $h(t) = v \cdot t - \frac{1}{2}gt$
 - b. $h(t) = v \cdot t^2 - \frac{1}{2}gt$
 - c. $h(t) = v \cdot t - \frac{1}{2}gt^2$
 - d. $h(t) = v \cdot t^2 - \frac{1}{2}gt^2$
2. Newton's second law of motion states $F = ma$, what are the dimensions of F (force) in basic dimensions?
3. Challenge question! The universal law of gravitation states $F_{gravity} = G \frac{m_1 m_2}{R^2}$, where $F_{gravity}$ is a force, and m_1 and m_2 are masses, and R is a distance. What are the units of the gravitational constant G ?

4. Super extra bonus challenge question! (From a past F=ma exam but it's really easy and you should be able to do it)

Inspired by a problem from the 2012 International Physics Olympiad, Estonia.

A very large number of small particles forms a spherical cloud. Initially they are at rest, have uniform mass density per unit volume ρ_0 , and occupy a region of radius r_0 . The cloud collapses due to gravitation; the particles do not interact with each other in any other way.

How much time passes until the cloud collapses fully? (The constant 0.5427 is actually $\sqrt{\frac{3\pi}{32}}$.)

- (A) $\frac{0.5427}{r_0^2 \sqrt{G\rho_0}}$
- (B) $\frac{0.5427}{r_0 \sqrt{G\rho_0}}$
- (C) $\frac{0.5427}{\sqrt{r_0} \sqrt{G\rho_0}}$
- (D) $\frac{0.5427}{\sqrt{G\rho_0}}$
- (E) $\frac{0.5427}{\sqrt{G\rho_0}} r_0$

(Use the backside if you need to for this one ;))