1. Dimensional Analysis

1. A particle is thrown into the air from ground level height h=0 with upward velocity v. Which of the following gives the height of the particle at time t from launch?

$$\text{a.}\quad h(t)=v\cdot t-\frac{1}{2}gt$$

$$\mathbf{b}. \quad h(t) = v \cdot t^2 - \frac{1}{2}gt$$

$$\mathbf{c}.\quad h(t)=v\cdot t-\frac{1}{2}gt^2$$

$$\mathrm{d.}\quad h(t)=v\cdot t^2-\frac{1}{2}gt^2$$

- 2. Newton's second law of motion states F=ma, what are the dimensions of F (force) in basic dimensions?
- 3. Challenge question! The universal law of gravitation states $F_{gravity} = G \frac{m_1 m_2}{R^2}$, where $F_{gravity}$ is a force, and m_1 and m_2 are masses, and R is a distance. What are the units of the gravitational constant G?
- 4. Super extra bonus challenge question! (From a past F=ma exam but it's really easy and you should be able to do it)

Inspired by a problem from the 2012 International Physics Olympiad, Estonia.

A very large number of small particles forms a spherical cloud. Initially they are at rest, have uniform mass density per unit volume ρ_0 , and occupy a region of radius r_0 . The cloud collapses due to gravitation; the particles do not interact with each other in any other way.

How much time passes until the cloud collapses fully? (The constant 0.5427 is actually $\sqrt{\frac{3\pi}{32}}$.)

(A)
$$\frac{0.5427}{r_0^2 \sqrt{G\rho_0}}$$

(B)
$$\frac{0.5427}{r_0\sqrt{G\rho_0}}$$

(C)
$$\frac{0.5427}{\sqrt{r_0}\sqrt{G\rho_0}}$$

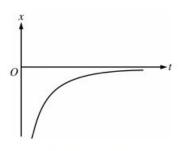
(D)
$$\frac{0.5427}{\sqrt{G\rho_0}}$$

(E)
$$\frac{0.5427}{\sqrt{G\rho_0}}r_0$$

(Use the backside if you need to for this one)

2. Dimensional Analysis

- 1. A boy throws a ball upward from the ground (h=0m) with velocity v=10m/s and acceleration due to gravity $g=-10m/s^2$
 - a. Calculate the time it takes for the ball to get to the highest point of its motion.
 - b. Calculate the maximum height the ball reaches.
 - c. Calculate the velocity of the ball once it hits the ground again.
- 2. A boy stands on the edge of a building. He throws a ball upward with velocity v=10m/s and the ball hits the ground after 10 seconds. How high is the cliff?
- 3. Some easy money AP test questions. Assume $g = 9.8 \text{ m/s}^2$ for these question.



The position *x* as a function of time *t* for an object moving in a straight line is shown in the graph above. Which of the following best describes the object's speed and direction of motion during the time interval shown?

Speed

Direction of Motion

- (A) Decreasing
- Positive
- (B) Increasing
- Positive
- (C) Constant
- Positive
- (D) Decreasing
- Negative
- (E) Increasing
- Negative

- Which of the following statements must be true for a falling object that has been dropped from rest near the surface of Earth?
- (A) The derivative of the distance the object falls with respect to time equals 9.8 m/s².
- (B) The object falls a vertical distance of 9.8 m during the first second only.
- (C) The object falls a vertical distance of 9.8 m during each second.
- (D) The speed of the object as it falls is a constant 9.8 m/s.
- (E) The speed of the object increases by 9.8 m/s during each second.

The position x of an object is given as a function of time t by the equation $x = 8 + 4t - 6t^3$, where x is in meters and t is in seconds. What is the maximum positive velocity attained by this object?

- (A) 4 m/s
- (B) 8 m/s
- (C) 18 m/s
- (D) 36 m/s
- (E) There is no maximum positive velocity because the object never moves in the positive direction.

4. Challenge question (it's p hard lol dw if you can't do it [first question on an old f=ma test])

An observer stands on the side of the front of a stationary train. When the train starts moving with constant acceleration, it takes 5 seconds for the first car to pass the observer. How long will it take for the 10th car to pass?

- (A) 1.07s
- (B) 0.98s
- (C) 0.91s
- (D) 0.86s
- (E) 0.81s