

```
import numpy as np
import matplotlib.pyplot as plt
plt.style.use('seaborn')
```

```
x = np.array([[0, 0], [0, 1], [1, 0], [1, 1]])
y = np.array([0, 1, 1, 0])
```

```
def computecost(y, yhat):
    return 0.5 * np.sum((yhat - y) ** 2)
```

```
def sigmoid(x):
    return 1 / (1 + np.exp(-x))
```

```
def sigmoid_prime(x):
    return sigmoid(x) * (1 - sigmoid(x))
```

```
def train(epochs, alpha):
    cost = [0 for x in range(epochs)]
    w1 = np.random.random((2, 2))
    b1 = np.random.random((1, 2))
    w2 = np.random.random((2, 1))
    b2 = np.random.random()
    for e in range(epochs):
        for i in range(len(x)):
            # forward propagation
            yin1 = np.dot(x[i], w1) + b1
            y1_predict = sigmoid(yin1)
            yin2 = np.dot(y1_predict, w2) + b2
            y2_predict = sigmoid(yin2)

            cost[e] += computecost(y[i], y2_predict)

            # backward propagation
            y2_error = y[i] - y2_predict
            y2_delta = y2_error * sigmoid_deriv(y2_predict)

            w2 += alpha * np.dot(y1_predict.reshape((2, 1)),
                                  y2_delta.reshape((1, 1)))
            b2 += alpha * np.sum(y2_delta, axis=0, keepdims=True)

            y1_error = np.dot(y2_delta, w2.T)
            y1_delta = y1_error * sigmoid_deriv(y1_predict)

            w1 += alpha * np.dot(x[i].reshape((2, 1)), y1_delta)
            b1 += alpha * np.sum(y1_delta, axis=0, keepdims=True)

    return w1, b1, w2, b2, cost
```

```
def main():
```

```
alpha = 0.2
epochs = 5000
w1, b1, w2, b2, cost = train(epochs, alpha)
plt.plot(cost)
plt.title('Loss Function')
plt.xlabel('Epochs')
plt.ylabel('Loss')
plt.show()
```

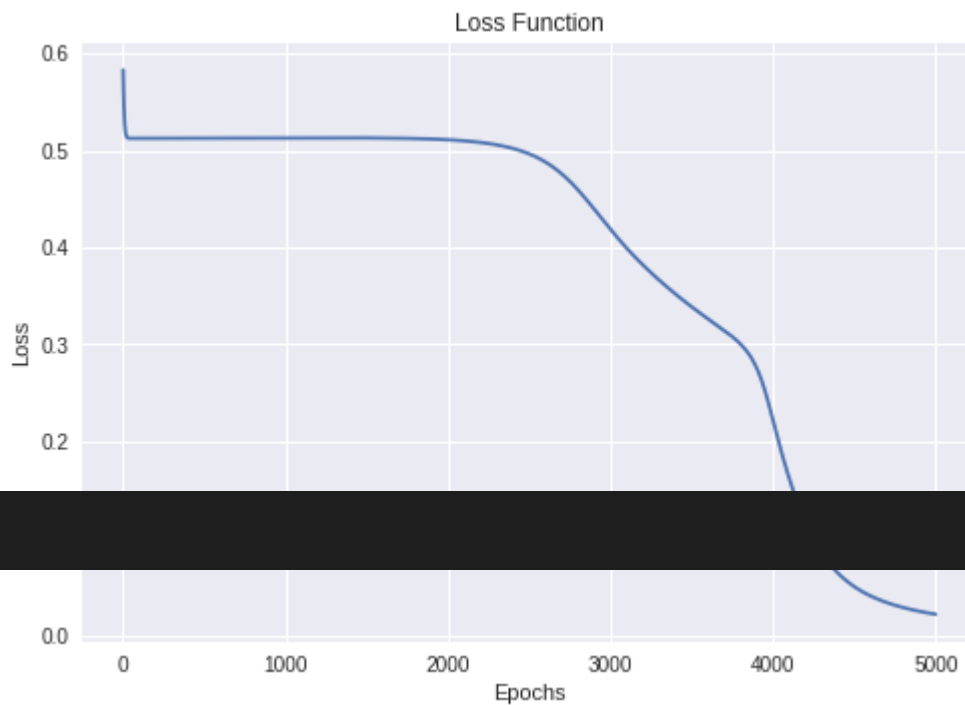
```
print("\n\t\tWeights\n")
print("First layer:")
print(w1)
print("Second layer:")
print(w2)
```

```
print("\n\t\tBias\n")
print(f"First layer: {b1}")
print(f"Second layer: {b2}")
```

```
print("\n\t\tPredictions\t\n")
for i in range(2):
    for j in range(2):
        y1 = sigmoid(np.dot([i, j], w1)+b1)
        y2 = sigmoid(np.dot(y1, w2) + b2)
        print(f"{i} {j}: {y2[0][0]}")
```

```
main()
```





Weights

First layer:

```
[[5.75737991 3.03760004]  
 [5.44424683 2.9882537 ]]
```

Second layer:

```
[[ 6.41527305]  
 [-6.93803524]]
```

Bias

First layer: $\begin{bmatrix} -2.12602532 & -4.55107464 \end{bmatrix}$

Second layer: $\begin{bmatrix} -2.81199417 \end{bmatrix}$

Predictions

```
0 0: 0.09969272428612788  
0 1: 0.8981737598017909  
1 0: 0.8989845083437787
```