

① Magic number

$$\begin{aligned} n &= 64 \rightarrow \\ \textcircled{1} & 6 \quad 4 \\ \textcircled{2} & 6+4 = 10 \rightarrow 1+0 = 1 \quad \text{magic number} \end{aligned}$$

② Happy Number:

$$n = 19$$

① split into digits i.e.

② square the digits i.e. $1^2 = 1$

③ Add the square together & compare with $= 1$.

$$\begin{aligned} n &= 19 \\ 1^2 + 9^2 &= 82 = 1 \times \\ n &= 82 \\ 8^2 + 2^2 &= 68 = 1 \times \\ 6^2 + 8^2 &= 100 = 1 \times \\ 1^2 + 0^2 &= 1 \quad \text{magic number} \end{aligned}$$

$$\begin{aligned} \text{last digit} &\rightarrow \\ \textcircled{4} & \textcircled{1} \Rightarrow \\ 4 & \quad 16 \\ 1^2 + 6^2 &= 37 \\ 1 + 3 + 7 &= 17 \\ 9 + 1 + 7 &= 17 \end{aligned}$$

③ Prime Number

→ number divisible by itself & 1.

$$2, 3, 5, 7, 11, 13, 17, 19, 23, 29, 31, \dots$$

④ Kaprekar's Number

$$\begin{aligned} n &= 45 \rightarrow \\ \textcircled{1} & \text{Do the square of } n. \quad \cancel{\textcircled{2} 025} \quad \begin{array}{c} 15231 \\ 1+5231 \\ 15+13120 \\ 152+31 \\ 1523+1 \end{array} \end{aligned}$$

$$\textcircled{2} \quad \text{Count no. of digits.} = \textcircled{4}$$

$$\textcircled{3} \quad \cancel{2+025} = 2 \neq 45 \quad \cancel{20+25} = 45 = - \quad \cancel{n} \neq$$

$$\begin{array}{c} 15231 \\ 1+5231 \\ 15+13120 \\ 152+31 \\ 1523+1 \end{array} \quad \begin{array}{c} 45^2 \\ 4+5 \\ 16 \\ 1^2 + 6^2 \\ 1+36 = 37 \\ 9+1+7 = 17 \end{array}$$

⑤ Automorphic number.

$$n = \textcircled{5}$$

$$\textcircled{1} \quad \text{sq. abn} = \textcircled{2} \quad 25$$

$$\textcircled{2} \quad n = 25 \rightarrow \cancel{25}^2 = 625$$

⑥ Neon Number

$$n = \textcircled{8} \quad 9$$

$$\textcircled{1} \quad \text{sq. abn.}$$

$$\cancel{8+1} = \underline{\underline{9}}$$

⑦ Catalan Number → IBM (Tech Interview)

$$\begin{aligned} C(n) &= \frac{(2+n)!}{(n+1)! \cdot n!} \quad \text{or} \quad C(n) = \sum_{i=0}^n C(i) \cdot C_{(n-i)} \\ \textcircled{1} \quad C_0 &= \frac{(2+0)!}{(0+1)! \cdot 0!} = \frac{1}{1} = 1 \\ \textcircled{2} \quad C_1 &= \frac{(2+1)!}{(1+1)! \cdot 1!} = \frac{2!}{2! \cdot 1!} = 1 \\ \textcircled{3} \quad C_2 &= \frac{(2+2)!}{(2+1)! \cdot 2!} = \frac{4!}{3! \cdot 2!} = \frac{4 \cdot 3 \cdot 2 \cdot 1}{3 \cdot 2 \cdot 1 \cdot 2 \cdot 1} = 2 \\ \textcircled{4} \quad C_3 &= \frac{(2+3)!}{(3+1)! \cdot 3!} = \frac{6!}{4! \cdot 3!} = \frac{6 \cdot 5 \cdot 4 \cdot 3 \cdot 2 \cdot 1}{4 \cdot 3 \cdot 2 \cdot 1 \cdot 3 \cdot 2 \cdot 1} = 5 \end{aligned}$$

Zig-Zag Pattern $x=3, c=9$

```
for(i=0; i<6; i++) {
    for(j=1; j<=9; j++) {
        if((i==0 && j%2==0) || (i==1 && j%3==0) || (i+j==8)) {
            printf("*");
        } else {
            printf(" ");
        }
    }
}
```

$\rightarrow \text{if } (j==1 \& \& C_0 \cdot 4 == 3) \{$

$(j==2 \& \& C_1 \cdot 2 == 0) \{$

$(j==3 \& \& C_2 \cdot 1 == 1) \{$

printf("A");

else printf(" ");

} printf("\n");

} return 0;

$\rightarrow \text{if } (j==1 \& \& C_0 \cdot 4 == 3) \{$

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