

19CSE302-Design and Analysis of Algorithms
Assignment – Dynamic Programming
Marks -20
Date:-28/10/2021
Submission time:- 29/10/2021 1:10 PM

Q1: Given two strings **A** and **B**, find the **minimum** number of steps required to convert **A** to **B**. Each operation is counted as 1 step and you have the following 3 operations permitted on a word:

Insert a character

Delete a character

Replace a character

Example: A = "abad" and B = "abac".

Min steps required = 1

Explanation: After applying operation: Replace d with c. We get A = B.

Example 2: A = "Anshuman" and B = "Antihuman"

Min steps required = 2.

Explanation: After applying operations: Replace s with t and insert i before h. We get A = B.

For the given problem:

- (a) Identify the subproblem with explanation. (2M)
- (b) Identify the recurrence relation with base condition. (3M)
- (c) Provide the pseudocode for the Dynamic problem based algorithm. (3M)
- (d) Identify and explain the how DP is improving the complexity of the problem from typical brute force solution. (2M)

Q2: Given a binary tree **T**, find the maximum path sum. The path may start and end at any node in the tree. As an input you are provided the root pointer of the tree.

```
    20
   / \
 -10  20
  / \
-10 -50
```

The path with maximum sum is: 20 -> 20

```
    1
   /\
  2 3
```

The path with maximum sum is: 2 -> 1 -> 3

For the given problem:

- (a) Identify the subproblem with explanation. (2M)
- (b) Identify the recurrence relation with base condition. (3M)

- (c) Provide the pseudocode for the Dynamic problem based algorithm. (3M)
- (d) Identify and explain the how DP is improving the complexity of the problem from typical brute force solution. (2M)