

SM5083

Assignment 2

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1. CHAPTER III MISCELLANEOUS EXAMPLES VI Q9 Then,

If the lines $y = x \tan(\frac{11\pi}{24})$, $y = x \tan(\frac{19\pi}{24})$ be at right angles, Show that the angle between the axes is $(\frac{\pi}{4})$

Solution:

Given equation of two lines are (1)

$$y = x \tan(\frac{11\pi}{24}) \quad (2)$$

$$y = x \tan(\frac{19\pi}{24}) \quad (3)$$

So,

$$\tan \theta = \tan(\frac{19\pi}{24} + \frac{11\pi}{24}) \quad (10)$$

$$\tan \theta = \tan(\frac{30\pi}{24}) \quad (11)$$

$$\tan \theta = \tan(\frac{5\pi}{4}) \quad (12)$$

$$\tan \theta = \tan(\pi + \frac{\pi}{4}) \quad (13)$$

$$\tan \theta = \tan(\frac{\pi}{4}) \quad (14)$$

Let the equations of the straight lines AB and CD are i.e.

Hence, the angle between the axes is $(\frac{\pi}{4})$

$$y = m_1(x + c_1) \text{ and } y = m_2(x + c_2) \text{ respectively,} \quad (4)$$

intersect at a point P and make angles θ_1 and θ_2 respectively with the positive direction of x -axis
So the angle θ between the lines having slope m_1 and m_2 is given by

$$\tan \theta = \frac{(m_2 - m_1)}{1 + m_1 m_2} \quad (5)$$

Clearly, the slope of the line AB and CD are m_1 and m_2 respectively.

From equations (2) and (3)

$$m_1 = \tan(\frac{11\pi}{24}) \quad (6)$$

$$m_2 = \tan(\frac{19\pi}{24}) \quad (7)$$

Now, put the value of m_1 and m_2 in equations (5)

$$\tan \theta = \frac{\tan(\frac{19\pi}{24}) - \tan(\frac{11\pi}{24})}{1 + \tan(\frac{19\pi}{24}) \tan(\frac{11\pi}{24})} \quad (8)$$

Using Formula

$$\tan(A + B) = \frac{\tan(A) - \tan(B)}{1 + \tan(A) \tan(B)} \quad (9)$$