


```

0   time                    503911 non-null object
1   use [kW]                503910 non-null float64
2   gen [kW]                503910 non-null float64
3   House overall [kW]      503910 non-null float64
4   Dishwasher [kW]        503910 non-null float64
5   Furnace 1 [kW]          503910 non-null float64
6   Furnace 2 [kW]          503910 non-null float64
7   Home office [kW]        503910 non-null float64
8   Fridge [kW]             503910 non-null float64
9   Wine cellar [kW]        503910 non-null float64
10  Garage door [kW]        503910 non-null float64
11  Kitchen 12 [kW]         503910 non-null float64
12  Kitchen 14 [kW]         503910 non-null float64
13  Kitchen 38 [kW]         503910 non-null float64
14  Barn [kW]               503910 non-null float64
15  Well [kW]               503910 non-null float64
16  Microwave [kW]          503910 non-null float64
17  Living room [kW]        503910 non-null float64
18  Solar [kW]              503910 non-null float64
19  temperature             503910 non-null float64
20  icon                    503910 non-null object
21  humidity                503910 non-null float64
22  visibility              503910 non-null float64
23  summary                 503910 non-null object
24  apparentTemperature     503910 non-null float64
25  pressure                503910 non-null float64
26  windSpeed               503910 non-null float64
27  cloudCover              503910 non-null object
28  windBearing             503910 non-null float64
29  precipIntensity         503910 non-null float64
30  dewPoint                503910 non-null float64
31  precipProbability       503910 non-null float64
dtypes: float64(28), object(4)
memory usage: 123.0+ MB

```

```
In [6]: project_data.isna().sum()
```

```

Out[6]: time                    0
use [kW]                1
gen [kW]                1
House overall [kW]      1
Dishwasher [kW]        1
Furnace 1 [kW]          1
Furnace 2 [kW]          1
Home office [kW]        1
Fridge [kW]             1
Wine cellar [kW]        1
Garage door [kW]        1
Kitchen 12 [kW]         1
Kitchen 14 [kW]         1
Kitchen 38 [kW]         1
Barn [kW]               1
Well [kW]               1
Microwave [kW]          1
Living room [kW]        1
Solar [kW]              1
temperature             1
icon                    1
humidity                1
visibility              1
summary                 1
apparentTemperature     1
pressure                1
windSpeed               1
cloudCover              1

```

```
windBearing      1
precipIntensity  1
dewPoint         1
precipProbability 1
dtype: int64
```

```
In [7]: project_data = project_data[0:-1]
```

```
In [8]: project_data.isnull().sum()
```

```
Out[8]: time                0
use [kW]                  0
gen [kW]                  0
House overall [kW]        0
Dishwasher [kW]           0
Furnace 1 [kW]            0
Furnace 2 [kW]            0
Home office [kW]          0
Fridge [kW]               0
Wine cellar [kW]          0
Garage door [kW]          0
Kitchen 12 [kW]           0
Kitchen 14 [kW]           0
Kitchen 38 [kW]           0
Barn [kW]                 0
Well [kW]                 0
Microwave [kW]            0
Living room [kW]          0
Solar [kW]                0
temperature              0
icon                     0
humidity                 0
visibility                0
summary                  0
apparentTemperature       0
pressure                  0
windSpeed                 0
cloudCover                0
windBearing               0
precipIntensity           0
dewPoint                  0
precipProbability         0
dtype: int64
```

```
In [9]: project_data[project_data.isnull().any(axis=1)]
```

```
Out[9]:
```

time	use [kW]	gen [kW]	House overall [kW]	Dishwasher [kW]	Furnace 1 [kW]	Furnace 2 [kW]	Home office [kW]	Fridge [kW]	Wine cellar [kW]	...	visibility	summary
------	----------	----------	--------------------	-----------------	----------------	----------------	------------------	-------------	------------------	-----	------------	---------

0 rows x 32 columns

```
In [10]: pd.to_datetime(project_data['time'], unit='s').head(3)
```

```
Out[10]: 0    2016-01-01 05:00:00
1    2016-01-01 05:00:01
2    2016-01-01 05:00:02
Name: time, dtype: datetime64[ns]
```

```
In [11]: project_data['time'] = pd.DatetimeIndex(pd.date_range('2016-01-01 05:00', periods=len(project_data)
project_data = project_data.set_index('time')
project_data.head()
```

```
Out[11]:
```

	use [kW]	gen [kW]	House	Dishwasher	Furnace	Furnace	Home	Fridge	Wine
--	----------	----------	-------	------------	---------	---------	------	--------	------

			overall [kW]		[kW]	1 [kW]	2 [kW]	office [kW]	[kW]	cellar [kW]
time										
2016-01-01 05:00:00	0.932833	0.003483	0.932833	0.000033	0.020700	0.061917	0.442633	0.124150	0.006983	
2016-01-01 05:01:00	0.934333	0.003467	0.934333	0.000000	0.020717	0.063817	0.444067	0.124000	0.006983	
2016-01-01 05:02:00	0.931817	0.003467	0.931817	0.000017	0.020700	0.062317	0.446067	0.123533	0.006983	
2016-01-01 05:03:00	1.022050	0.003483	1.022050	0.000017	0.106900	0.068517	0.446583	0.123133	0.006983	
2016-01-01 05:04:00	1.139400	0.003467	1.139400	0.000133	0.236933	0.063983	0.446533	0.122850	0.006850	

5 rows × 31 columns

```
In [12]: project_data['year'] = project_data.index.year
project_data['month'] = project_data.index.month
project_data['day'] = project_data.index.day
project_data['weekday'] = project_data.index.day_name()
project_data['weekofyear'] = project_data.index.weekofyear
project_data['hour'] = project_data.index.hour
project_data['minute'] = project_data.index.minute
project_data.head()
```

	use [kW]	gen [kW]	House overall [kW]	Dishwasher [kW]	Furnace 1 [kW]	Furnace 2 [kW]	Home office [kW]	Fridge [kW]	Wine cellar [kW]
time									
2016-01-01 05:00:00	0.932833	0.003483	0.932833	0.000033	0.020700	0.061917	0.442633	0.124150	0.006983
2016-01-01 05:01:00	0.934333	0.003467	0.934333	0.000000	0.020717	0.063817	0.444067	0.124000	0.006983
2016-01-01 05:02:00	0.931817	0.003467	0.931817	0.000017	0.020700	0.062317	0.446067	0.123533	0.006983
2016-01-01 05:03:00	1.022050	0.003483	1.022050	0.000017	0.106900	0.068517	0.446583	0.123133	0.006983
2016-01-01 05:04:00	1.139400	0.003467	1.139400	0.000133	0.236933	0.063983	0.446533	0.122850	0.006850

5 rows × 38 columns

```
In [13]: project_data.columns = [i.replace(' [kW]', '') for i in project_data.columns]
project_data.info()
```

```
<class 'pandas.core.frame.DataFrame'>
DatetimeIndex: 503910 entries, 2016-01-01 05:00:00 to 2016-12-16 03:29:00
Data columns (total 38 columns):
#   Column                                Non-Null Count  Dtype
---  -
0   use                                    503910 non-null  float64
1   gen                                    503910 non-null  float64
2   House overall                         503910 non-null  float64
3   Dishwasher                           503910 non-null  float64
4   Furnace 1                            503910 non-null  float64
5   Furnace 2                            503910 non-null  float64
6   Home office                          503910 non-null  float64
7   Fridge                               503910 non-null  float64
8   Wine cellar                          503910 non-null  float64
9   Garage door                          503910 non-null  float64
10  Kitchen 12                           503910 non-null  float64
11  Kitchen 14                           503910 non-null  float64
12  Kitchen 38                           503910 non-null  float64
13  Barn                                  503910 non-null  float64
14  Well                                  503910 non-null  float64
15  Microwave                            503910 non-null  float64
16  Living room                          503910 non-null  float64
17  Solar                                503910 non-null  float64
18  temperature                          503910 non-null  float64
19  icon                                  503910 non-null  object
20  humidity                             503910 non-null  float64
21  visibility                           503910 non-null  float64
22  summary                              503910 non-null  object
23  apparentTemperature                 503910 non-null  float64
24  pressure                            503910 non-null  float64
25  windSpeed                           503910 non-null  float64
26  cloudCover                          503910 non-null  object
27  windBearing                         503910 non-null  float64
28  precipIntensity                     503910 non-null  float64
29  dewPoint                            503910 non-null  float64
30  precipProbability                   503910 non-null  float64
31  year                                503910 non-null  int64
32  month                               503910 non-null  int64
33  day                                  503910 non-null  int64
34  weekday                             503910 non-null  object
35  weekofyear                          503910 non-null  int64
36  hour                                 503910 non-null  int64
37  minute                              503910 non-null  int64
dtypes: float64(28), int64(6), object(4)
memory usage: 149.9+ MB
```

Correlation and Seasonality Detection

There are 3 Kitchen Items, 2 Furnace Items Stitching them will reduce the dimentions of the data set

```
In [14]: kitchen_columns = ['Kitchen 12','Kitchen 14','Kitchen 38']
furnace_columns = ['Furnace 1','Furnace 2']

project_data['kitchen'] = project_data[kitchen_columns].sum(axis=1)
project_data['furnace'] = project_data[furnace_columns].sum(axis=1)
```

```
In [15]: project_data = project_data.drop(columns=kitchen_columns+furnace_columns, axis=1)
```

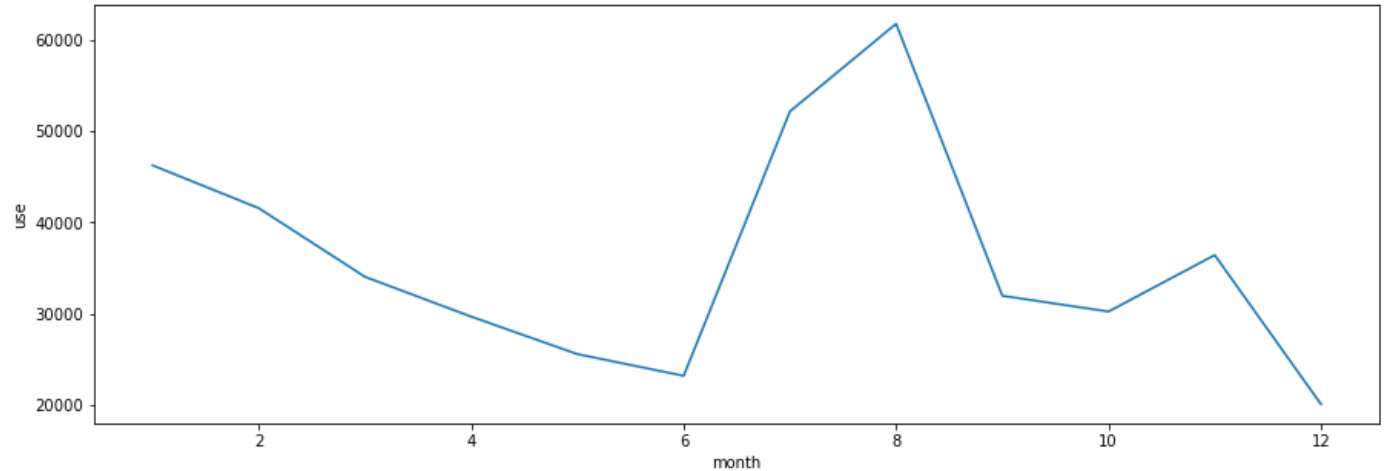
Correlation Analysis

```
In [16]: transformed_train_df = project_data.groupby(['month']).agg({'use':'sum'})
transformed_train_df['month'] = transformed_train_df.index
transformed_train_df.rename(columns = {'use':'use'}, inplace = True)
print(transformed_train_df.shape, transformed_train_df.columns)

(12, 2) Index(['use', 'month'], dtype='object')
```

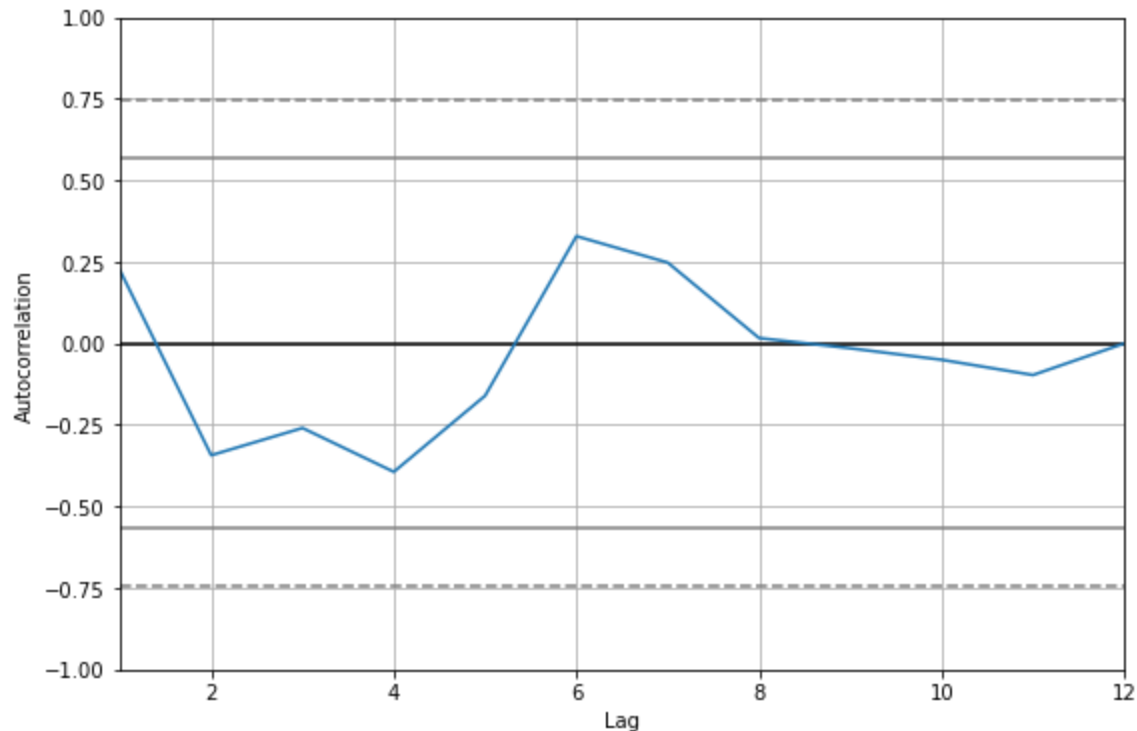
```
In [17]: plt.figure(figsize=(15,5))
sns.lineplot(data=transformed_train_df, x=transformed_train_df['month'], y=transformed_t
```

```
Out[17]: <AxesSubplot:xlabel='month', ylabel='use'>
```



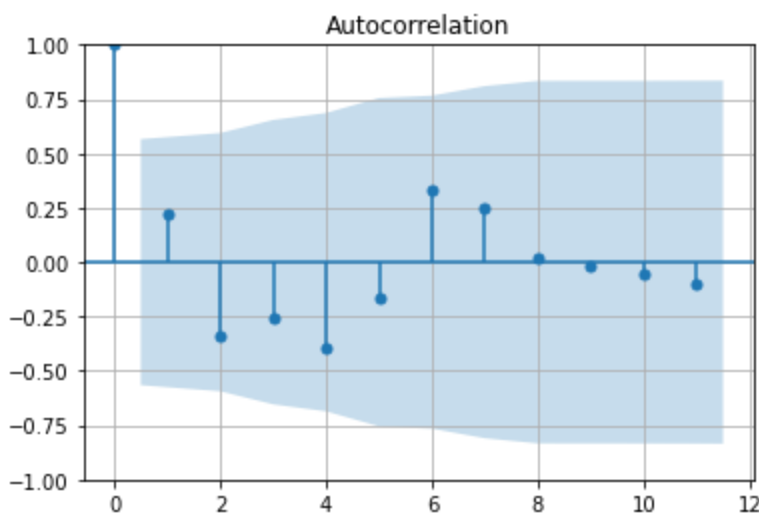
```
In [18]: plt.figure(figsize = (9, 6))
pd.plotting.autocorrelation_plot(transformed_train_df['use'])
print('Autocorrelation =', round(transformed_train_df['use'].autocorr(), 4))
```

Autocorrelation = 0.2644

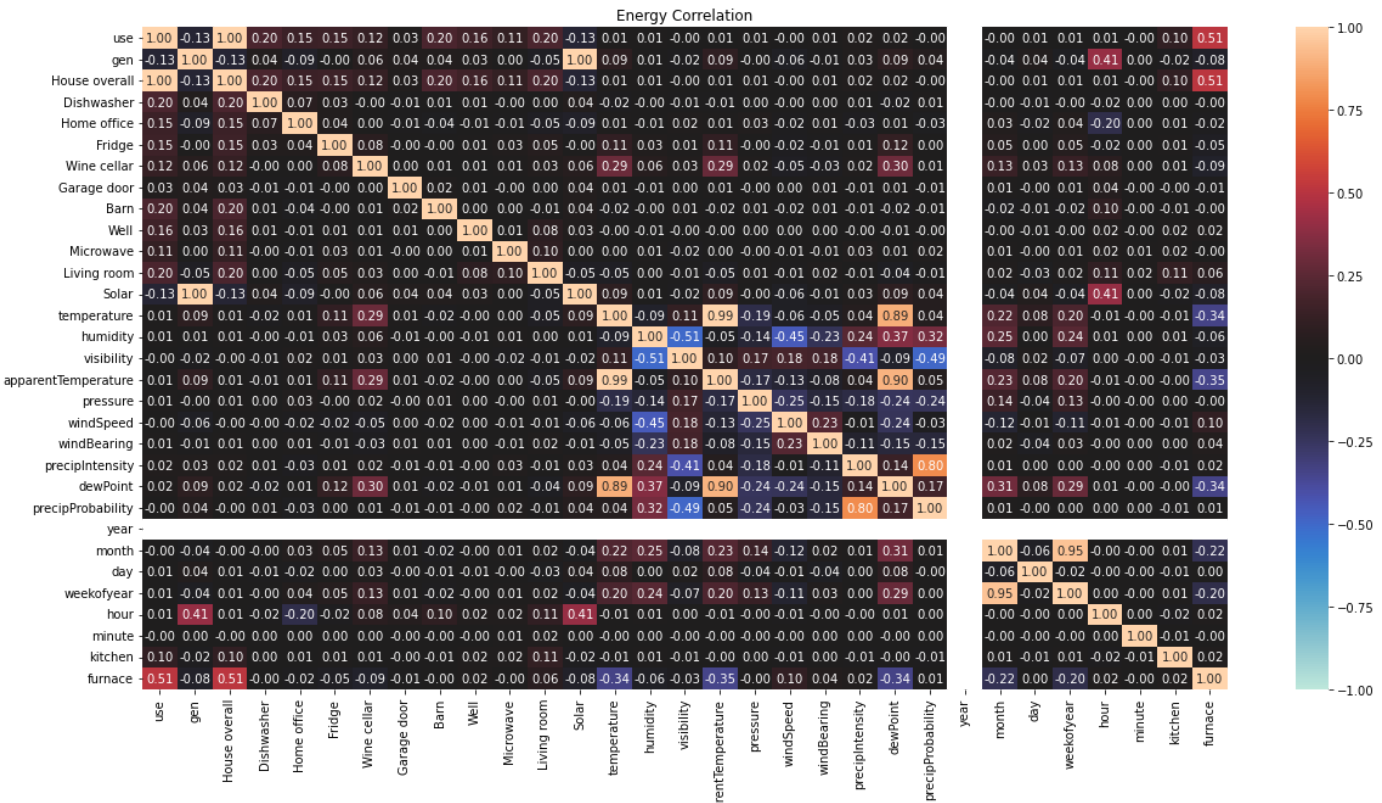


```
In [19]: plt.figure(figsize = (15, 16))
plot_acf(transformed_train_df['use'])
plt.grid()
plt.show()
```

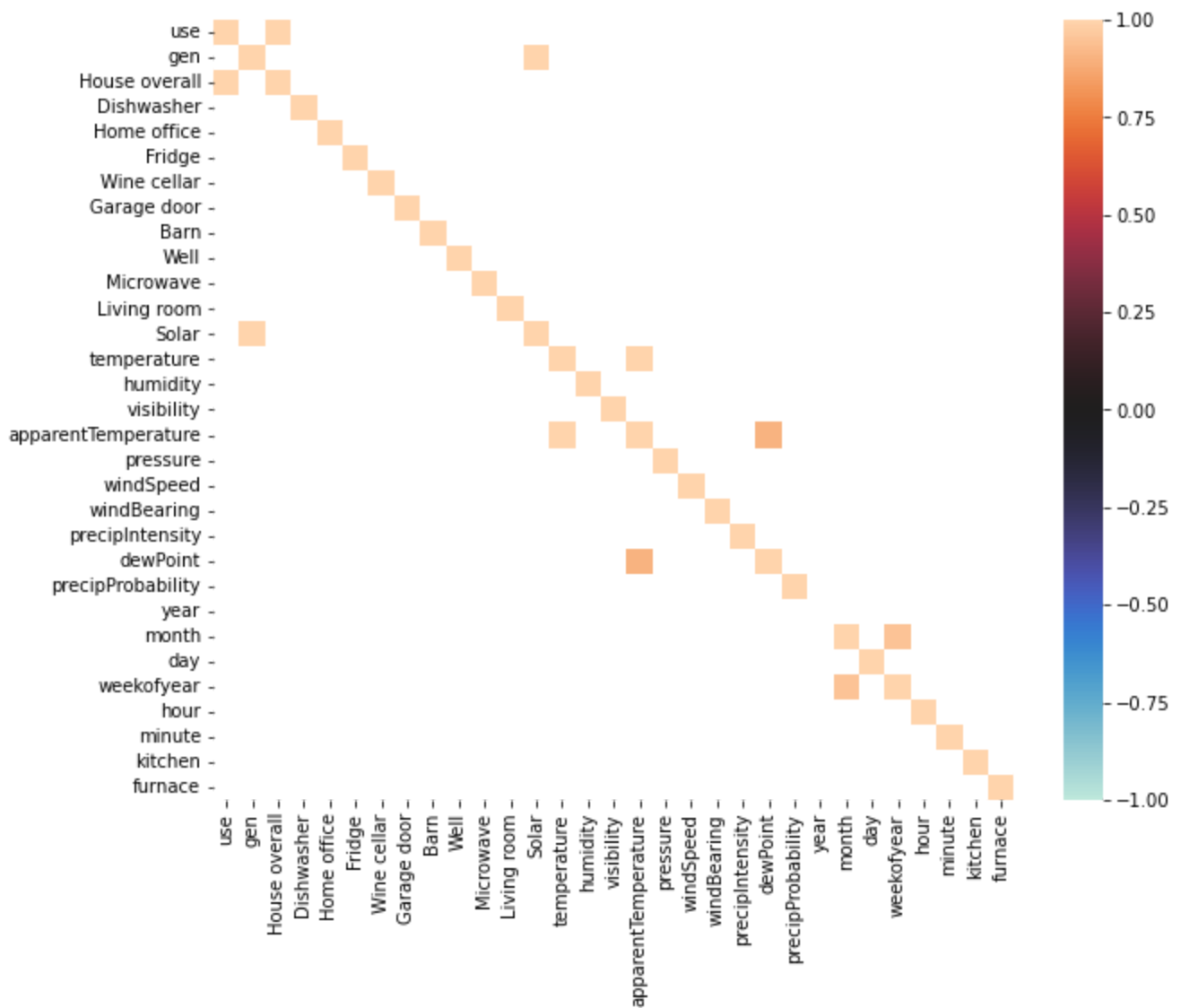
<Figure size 1080x1152 with 0 Axes>



```
In [20]: #Checking Correlations (all Energy features)
fig = plt.subplots(figsize=(20, 10))
sns.heatmap(project_data.corr(), annot=True, fmt='.2f', vmin=-1.0, vmax=1.0, center=0)
plt.title('Energy Correlation', fontsize=12);
```



```
In [21]: fig = plt.subplots(figsize=(10, 8))
corr = project_data.corr()
sns.heatmap(corr[corr>0.9], vmax=1, vmin=-1, center=0)
plt.show()
```



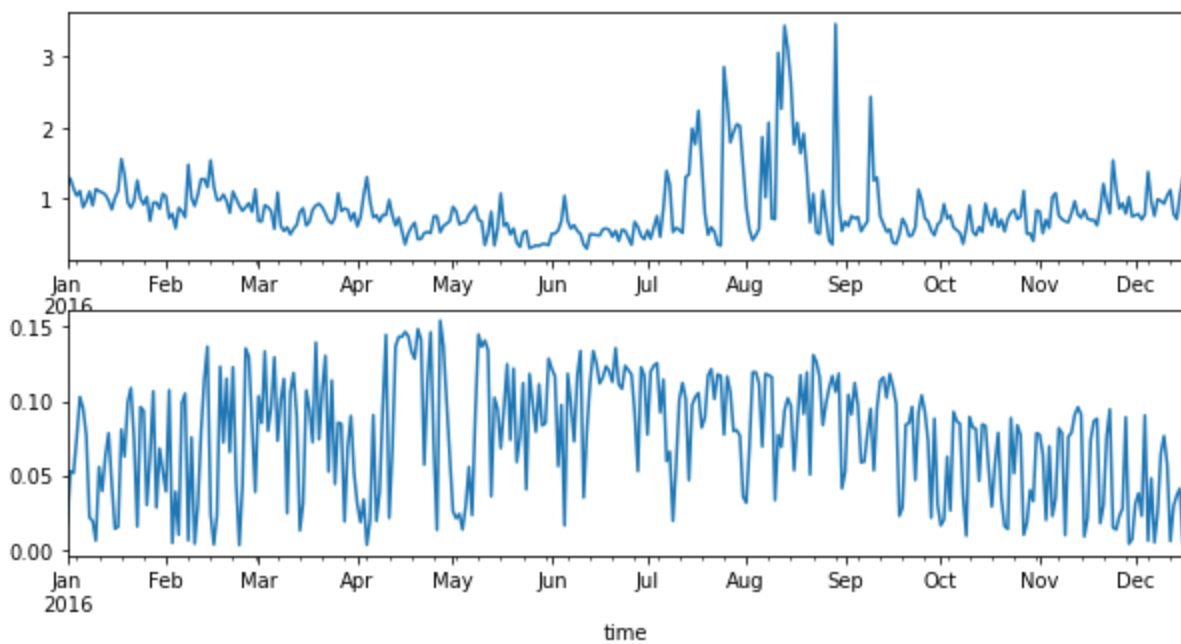
Correlation Summary

- use and House overall has highest correlation >90%
- gen & solar has highest correlation >90%

Seasonality & In Depth Exploratory Data Analysis

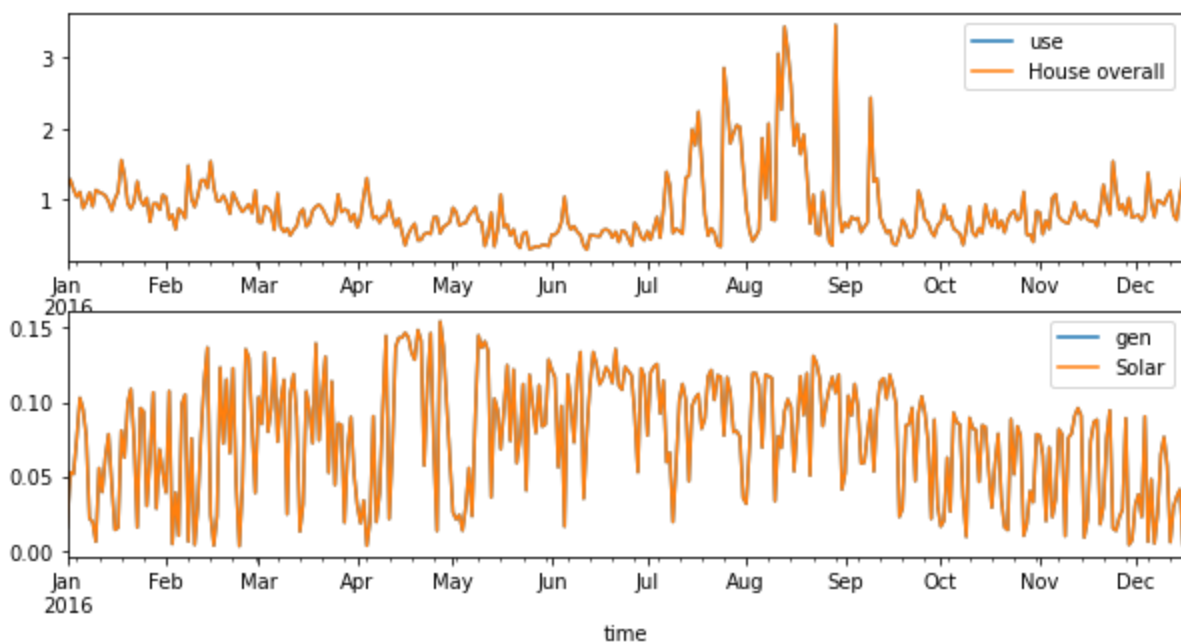
```
In [22]: fig, axes = plt.subplots(2,1, figsize=(10,5))
project_data['use'].resample('D').mean().plot(ax=axes[0])
project_data['gen'].resample('D').mean().plot(ax=axes[1])
```

```
Out[22]: <AxesSubplot:xlabel='time'>
```

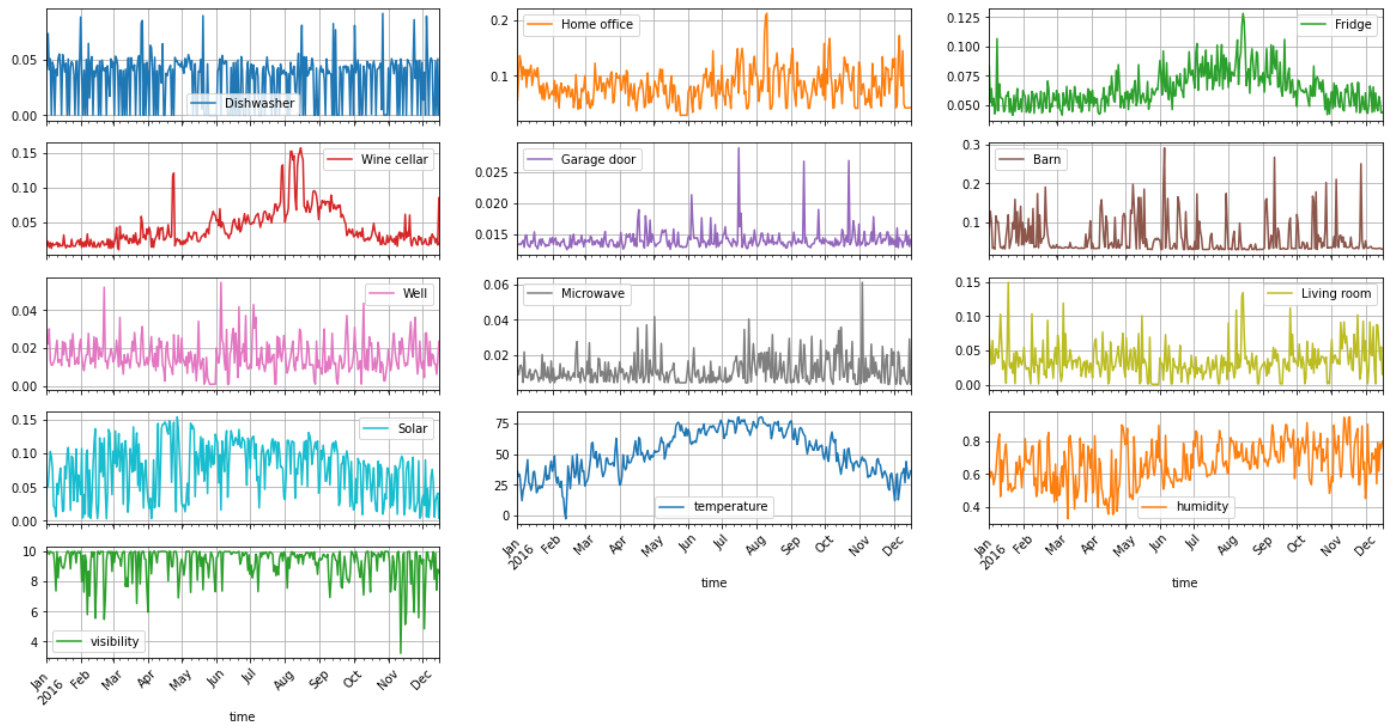



```
In [23]: ## As per correlation analysis summary

fig, axes = plt.subplots(2,1, figsize=(10,5))
project_data[['use','House overall']].resample('D').mean().plot(ax=axes[0])
project_data[['gen','Solar']].resample('D').mean().plot(ax=axes[1]);
```



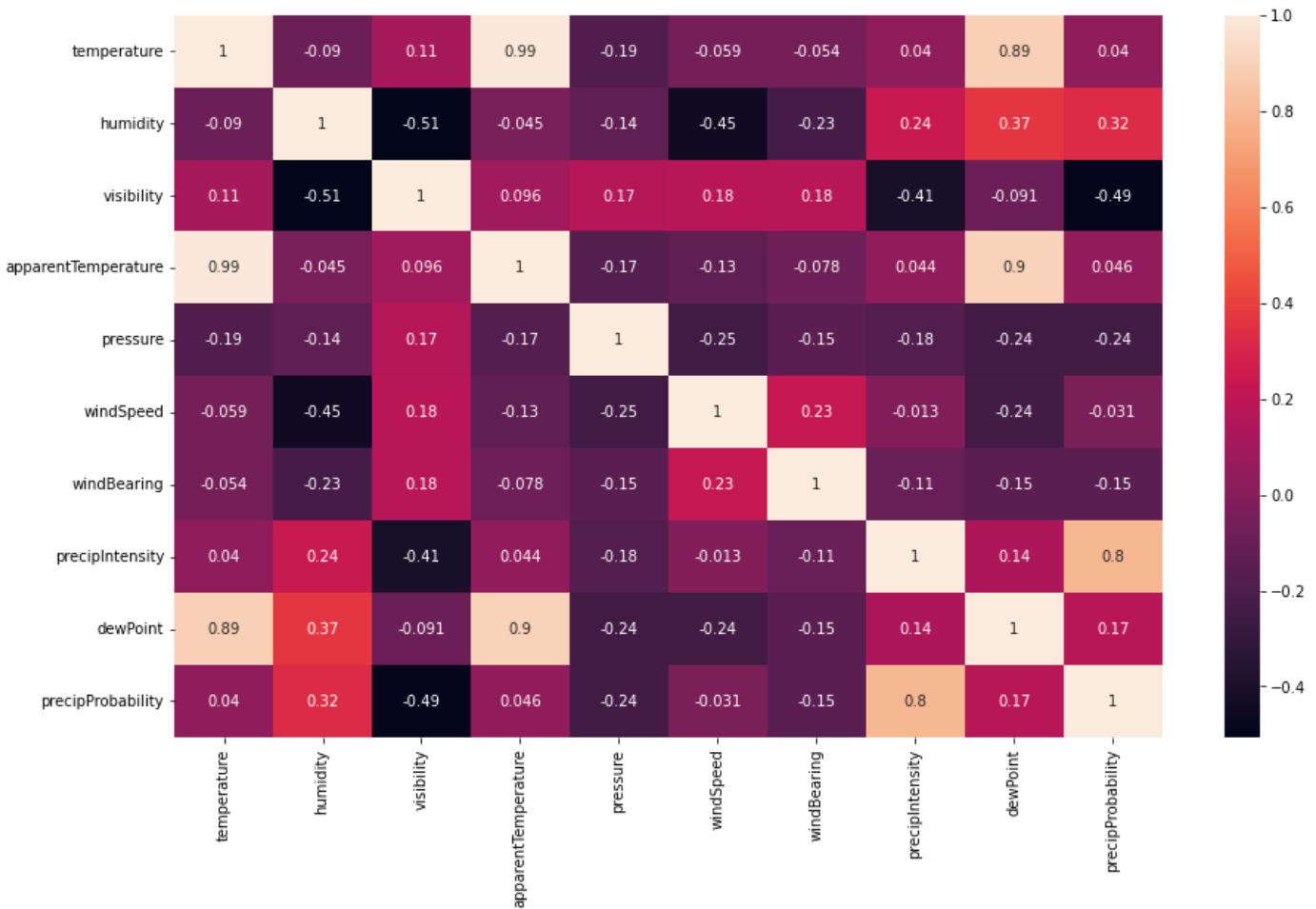
```
In [24]: #Energy features (resample by day)
project_data[project_data.columns[3:18].tolist()].resample('D').mean().plot(subplots=True,
grid=True, rot=45);
```



```
In [25]: weather_columns = ['temperature',
    'humidity',
    'visibility',
    'apparentTemperature',
    'pressure',
    'windSpeed',
    'cloudCover',
    'windBearing',
    'precipIntensity',
    'dewPoint',
    'precipProbability']

plt.figure(figsize=(15,9))
weather_data = project_data.filter(weather_columns, axis=1)
sns.heatmap(weather_data.corr(), annot=True)
```

Out[25]: <AxesSubplot:>

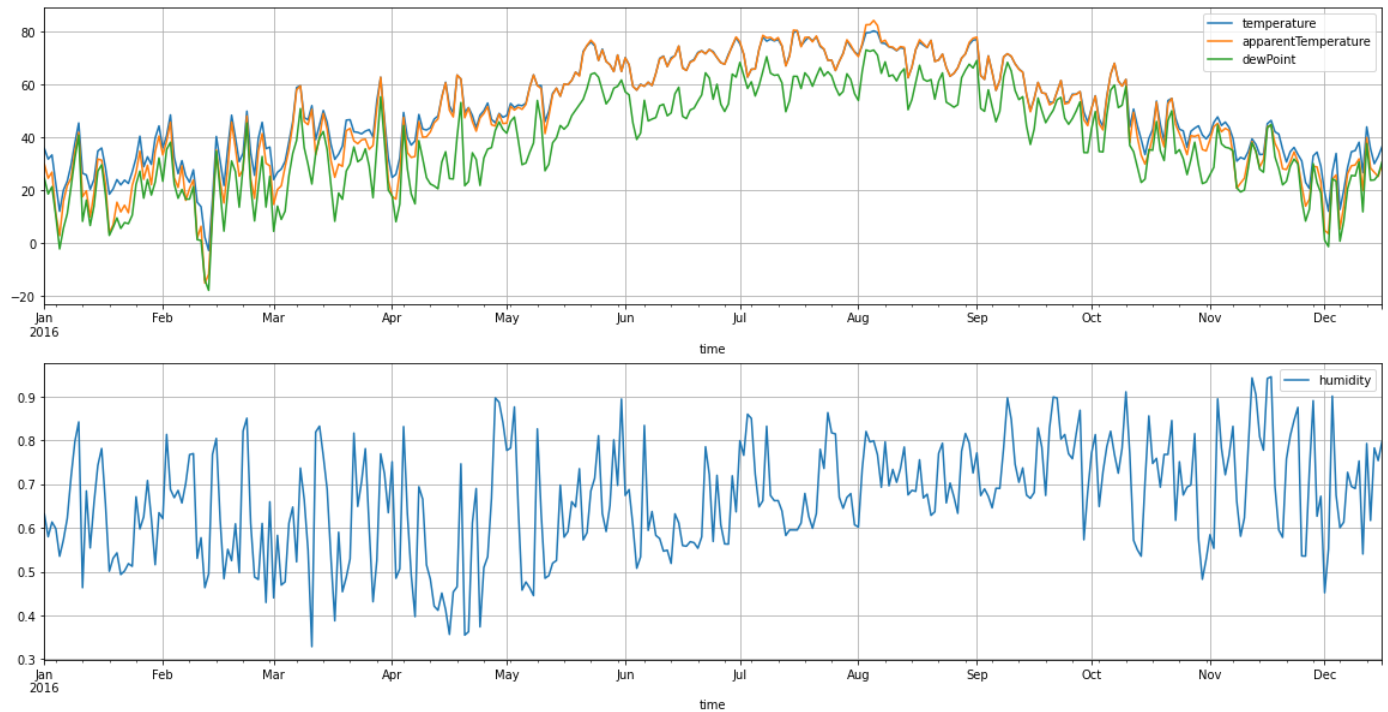


Weather Data Correlation Summary

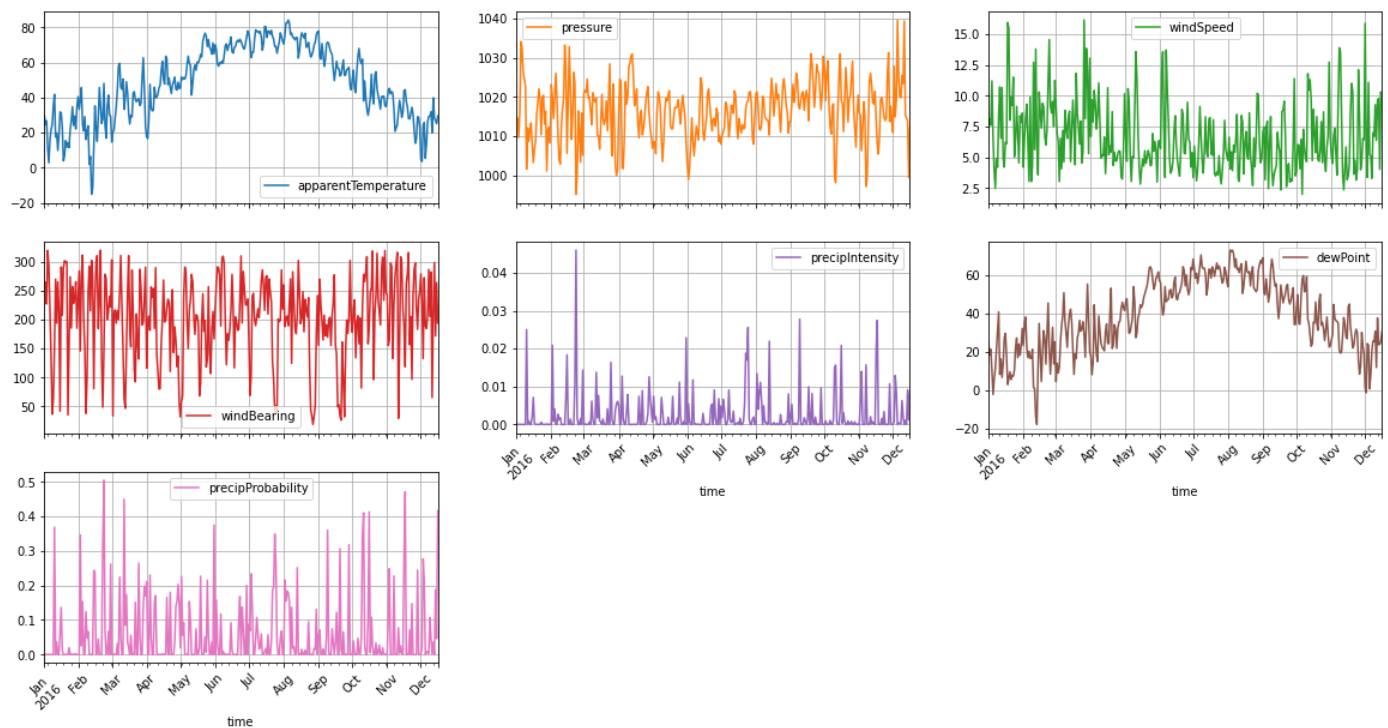
- temperature, apparentTemperature, dewPoint has correlation > 90%

```
In [26]: #Let's check a few correlations about the weather data
fig, axes = plt.subplots(2,1, figsize=(20,10))
project_data[['temperature','apparentTemperature', 'dewPoint']].resample('D').mean().plot()
project_data[['humidity']].resample('D').mean().plot(ax=axes[1], grid=True)
```

```
Out[26]: <AxesSubplot:xlabel='time'>
```



```
In [27]: #Rest of Weather features (resample by day)
project_data[project_data.columns[17:26]].tolist().resample('D').mean().plot(subplots=True,
grid=True, rot=45);
```

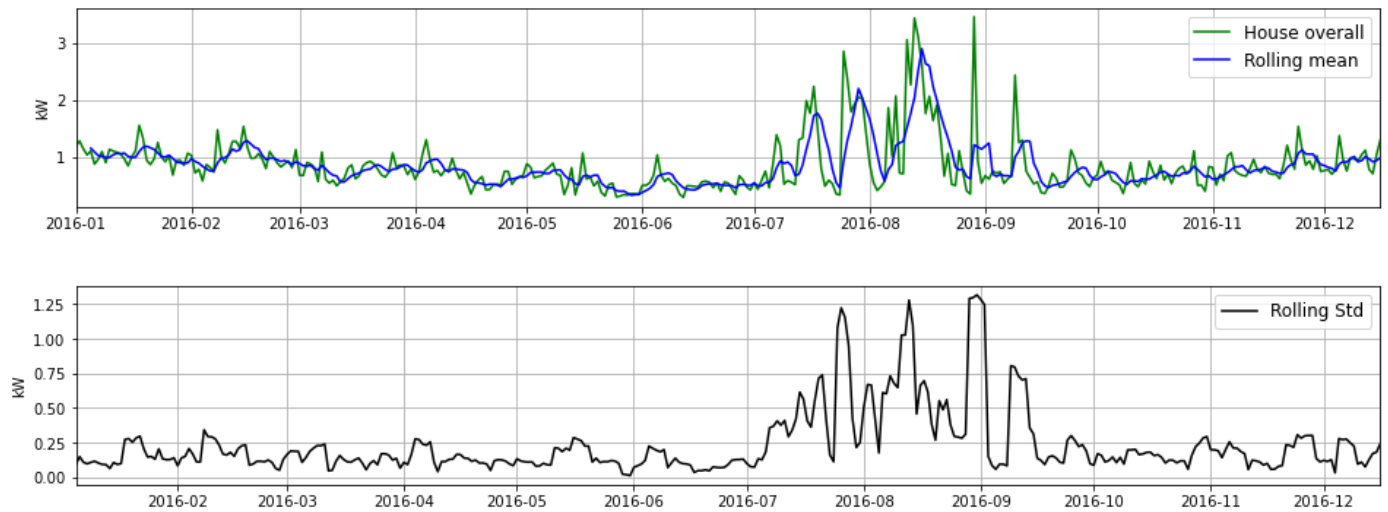


ARIMA

```
In [28]: # Data resampling by day
data_daily = project_data['House overall'].resample('d').mean()
rollingMEAN = data_daily.rolling(window=5).mean()
rollingSTD = data_daily.rolling(window=5).std()
#Plot
fig, (ax1, ax2) = plt.subplots(2,1,figsize=(16,6))
plt.subplots_adjust(hspace=0.4)
ax1.plot(data_daily, c='green',label='House overall')
ax1.plot(rollingMEAN, c='blue', label='Rolling mean')
ax2.plot(rollingSTD, c='black',label = 'Rolling Std')
```

```
ax1.legend(fontsize=12), ax2.legend(fontsize=12)
ax1.set_ylabel('kW'), ax2.set_ylabel('kW')
ax1.margins(x=0), ax2.margins(x=0)
ax1.grid(), ax2.grid()
```

Out[28]: (None, None)



AUTO-ARIMA

```
In [29]: result = seasonal_decompose(data_daily, model='additive')
fig = plt.figure()
fig = result.plot()
fig.set_size_inches(10, 10)
```

<Figure size 432x288 with 0 Axes>



```
In [30]: size = int(len(data_daily)*0.7)
train = data_daily[:size]
test = data_daily[size:]

arima_model = auto_arima(train,
                          start_p=0,
                          d=0,
                          start_q=0,
                          max_p=5,
                          max_d=5,
                          max_q=5,
                          start_P=0,
                          D=1,
                          start_Q=0,
                          max_P=5,
                          max_D=5,
                          max_Q=5,
                          m=12, #if m=1 seasonal is set to False
                          seasonal=True,
                          error_action='warn',
                          trace=True,
                          suppress_warnings=True,
                          stepwise=True,
                          random_state=20,
```

```
n_fits=5 # no of fits is taken as 5 we can increate this hype
)
```

```
Performing stepwise search to minimize aic
ARIMA(0,0,0) (0,1,0) [12] intercept : AIC=450.335, Time=0.03 sec
ARIMA(1,0,0) (1,1,0) [12] intercept : AIC=313.370, Time=0.15 sec
ARIMA(0,0,1) (0,1,1) [12] intercept : AIC=331.210, Time=0.21 sec
ARIMA(0,0,0) (0,1,0) [12] : AIC=448.376, Time=0.01 sec
ARIMA(1,0,0) (0,1,0) [12] intercept : AIC=348.030, Time=0.02 sec
ARIMA(1,0,0) (2,1,0) [12] intercept : AIC=310.191, Time=0.65 sec
ARIMA(1,0,0) (3,1,0) [12] intercept : AIC=307.438, Time=1.26 sec
ARIMA(1,0,0) (4,1,0) [12] intercept : AIC=302.917, Time=1.93 sec
ARIMA(1,0,0) (5,1,0) [12] intercept : AIC=302.753, Time=9.59 sec
ARIMA(1,0,0) (5,1,1) [12] intercept : AIC=inf, Time=26.45 sec
ARIMA(1,0,0) (4,1,1) [12] intercept : AIC=inf, Time=5.70 sec
ARIMA(0,0,0) (5,1,0) [12] intercept : AIC=400.160, Time=8.06 sec
ARIMA(2,0,0) (5,1,0) [12] intercept : AIC=300.461, Time=10.90 sec
ARIMA(2,0,0) (4,1,0) [12] intercept : AIC=300.900, Time=2.74 sec
ARIMA(2,0,0) (5,1,1) [12] intercept : AIC=inf, Time=25.64 sec
ARIMA(2,0,0) (4,1,1) [12] intercept : AIC=inf, Time=6.16 sec
ARIMA(3,0,0) (5,1,0) [12] intercept : AIC=300.484, Time=10.77 sec
ARIMA(2,0,1) (5,1,0) [12] intercept : AIC=301.658, Time=13.80 sec
ARIMA(1,0,1) (5,1,0) [12] intercept : AIC=299.667, Time=9.50 sec
ARIMA(1,0,1) (4,1,0) [12] intercept : AIC=300.406, Time=2.77 sec
ARIMA(1,0,1) (5,1,1) [12] intercept : AIC=inf, Time=25.40 sec
ARIMA(1,0,1) (4,1,1) [12] intercept : AIC=inf, Time=6.12 sec
ARIMA(0,0,1) (5,1,0) [12] intercept : AIC=334.393, Time=9.39 sec
ARIMA(1,0,2) (5,1,0) [12] intercept : AIC=301.648, Time=17.11 sec
ARIMA(0,0,2) (5,1,0) [12] intercept : AIC=321.785, Time=8.71 sec
ARIMA(2,0,2) (5,1,0) [12] intercept : AIC=301.925, Time=18.06 sec
ARIMA(1,0,1) (5,1,0) [12] : AIC=297.765, Time=5.49 sec
ARIMA(1,0,1) (4,1,0) [12] : AIC=298.489, Time=1.17 sec
ARIMA(1,0,1) (5,1,1) [12] : AIC=inf, Time=23.51 sec
ARIMA(1,0,1) (4,1,1) [12] : AIC=inf, Time=5.81 sec
ARIMA(0,0,1) (5,1,0) [12] : AIC=332.748, Time=4.49 sec
ARIMA(1,0,0) (5,1,0) [12] : AIC=300.922, Time=3.60 sec
ARIMA(2,0,1) (5,1,0) [12] : AIC=299.755, Time=7.61 sec
ARIMA(1,0,2) (5,1,0) [12] : AIC=299.744, Time=5.86 sec
ARIMA(0,0,0) (5,1,0) [12] : AIC=398.716, Time=3.38 sec
ARIMA(0,0,2) (5,1,0) [12] : AIC=320.155, Time=4.35 sec
ARIMA(2,0,0) (5,1,0) [12] : AIC=298.577, Time=4.75 sec
ARIMA(2,0,2) (5,1,0) [12] : AIC=300.002, Time=8.19 sec
```

```
Best model: ARIMA(1,0,1) (5,1,0) [12]
Total fit time: 299.352 seconds
```

```
In [31]: arima_model.summary()
```

```
Out[31]:
```

SARIMAX Results

Dep. Variable:		y	No. Observations:		245
Model:		SARIMAX(1, 0, 1)x(5, 1, [], 12)		Log Likelihood	-140.882
Date:		Wed, 26 Oct 2022		AIC	297.765
Time:		22:36:54		BIC	325.373
Sample:		0		HQIC	308.897
- 245					
Covariance Type:		opg			
	coef	std err	z	P> z	[0.025 0.975]
ar.L1	0.7694	0.048	16.103	0.000	0.676 0.863
ma.L1	-0.2538	0.069	-3.675	0.000	-0.389 -0.118

ar.S.L12	-0.6514	0.057	-11.374	0.000	-0.764	-0.539
ar.S.L24	-0.5026	0.080	-6.260	0.000	-0.660	-0.345
ar.S.L36	-0.4397	0.108	-4.082	0.000	-0.651	-0.229
ar.S.L48	-0.3706	0.145	-2.558	0.011	-0.655	-0.087
ar.S.L60	-0.1733	0.185	-0.936	0.349	-0.536	0.190
sigma2	0.1871	0.007	25.137	0.000	0.173	0.202

Ljung-Box (L1) (Q): 0.00 **Jarque-Bera (JB):** 2240.36

Prob(Q): 0.96 **Prob(JB):** 0.00

Heteroskedasticity (H): 10.82 **Skew:** 2.51

Prob(H) (two-sided): 0.00 **Kurtosis:** 17.34

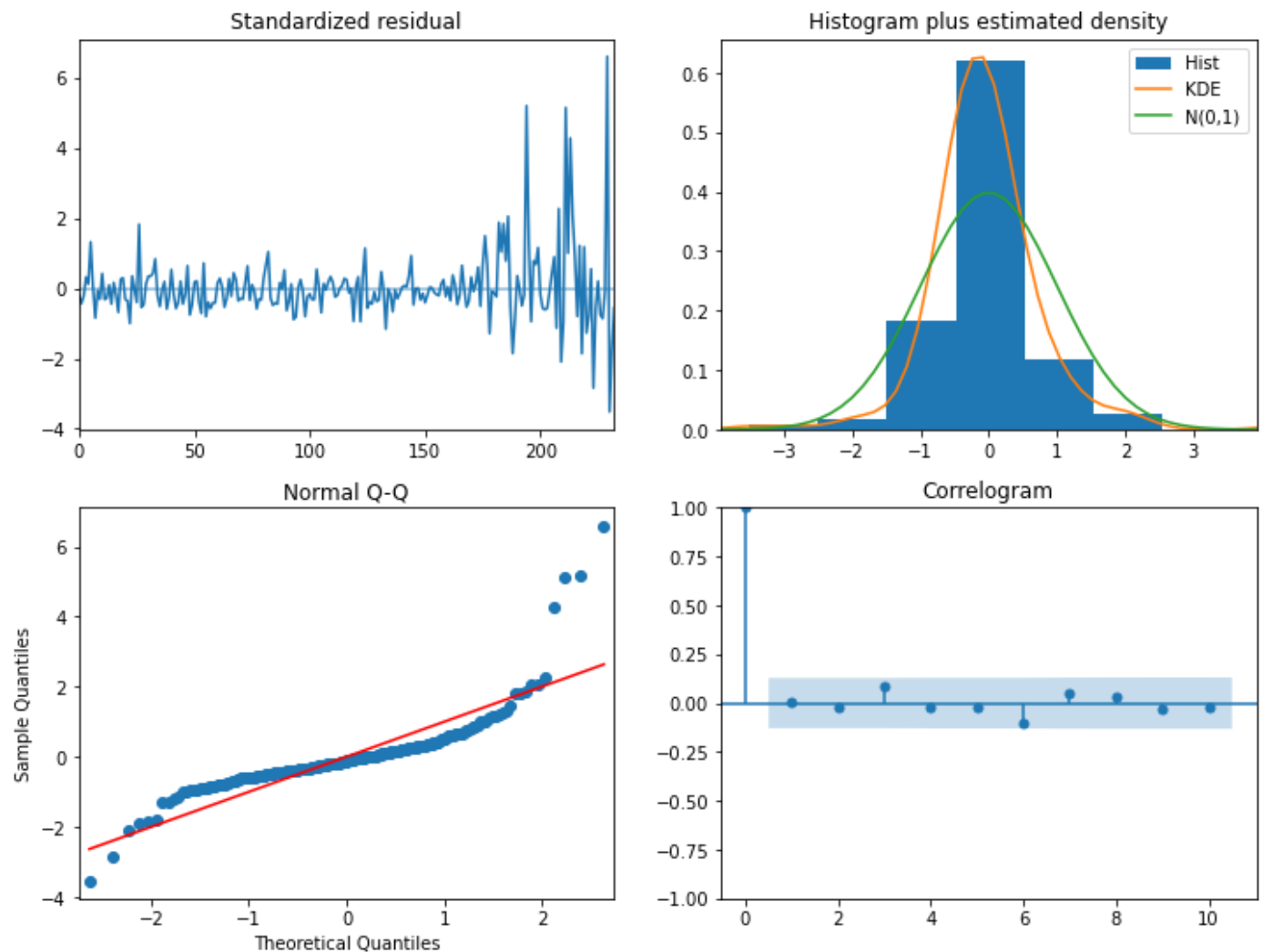
Warnings:

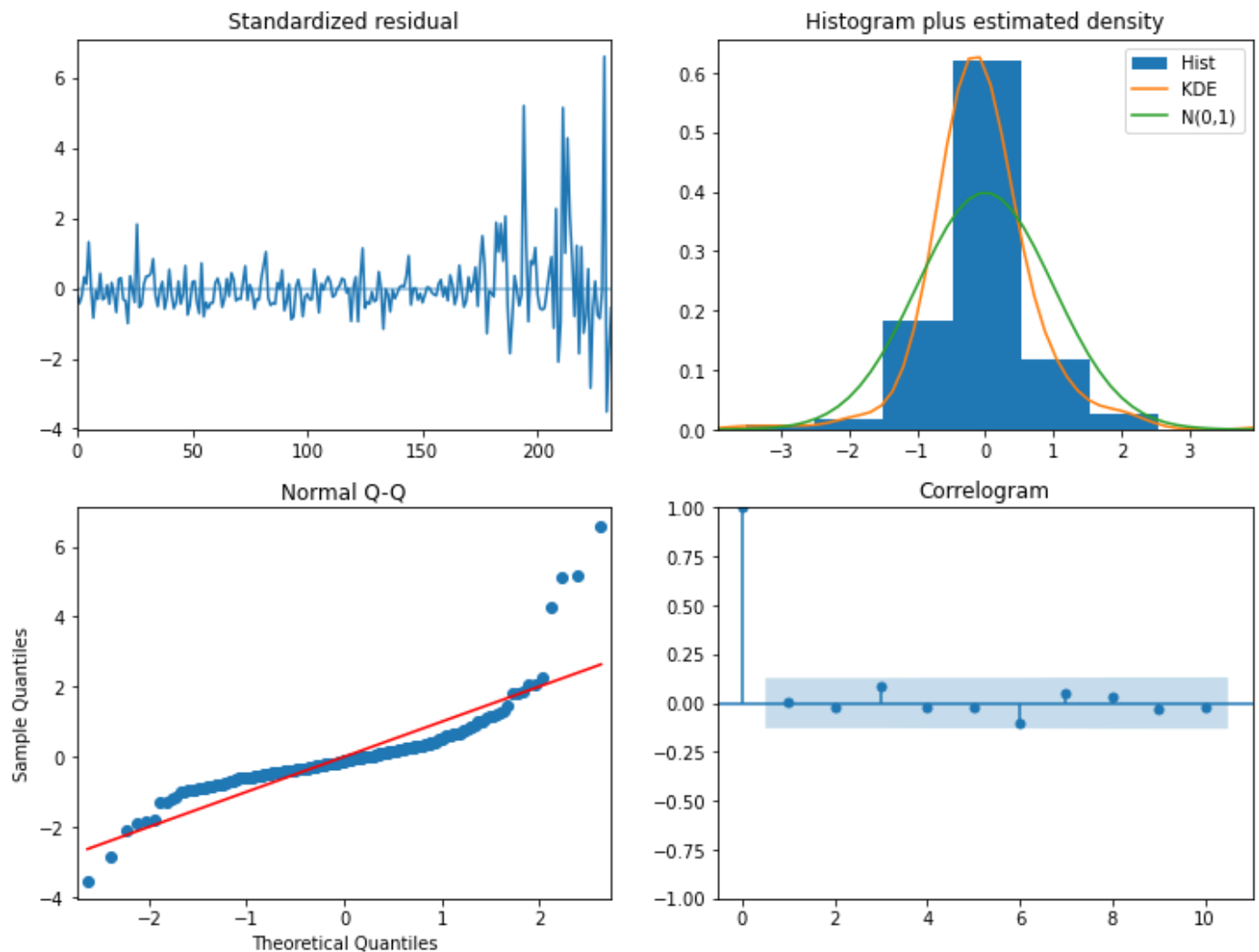
[1] Covariance matrix calculated using the outer product of gradients (complex-step).

Model Residuals

In [32]: `arima_model.plot_diagnostics(figsize=(12,9))`

Out[32]:





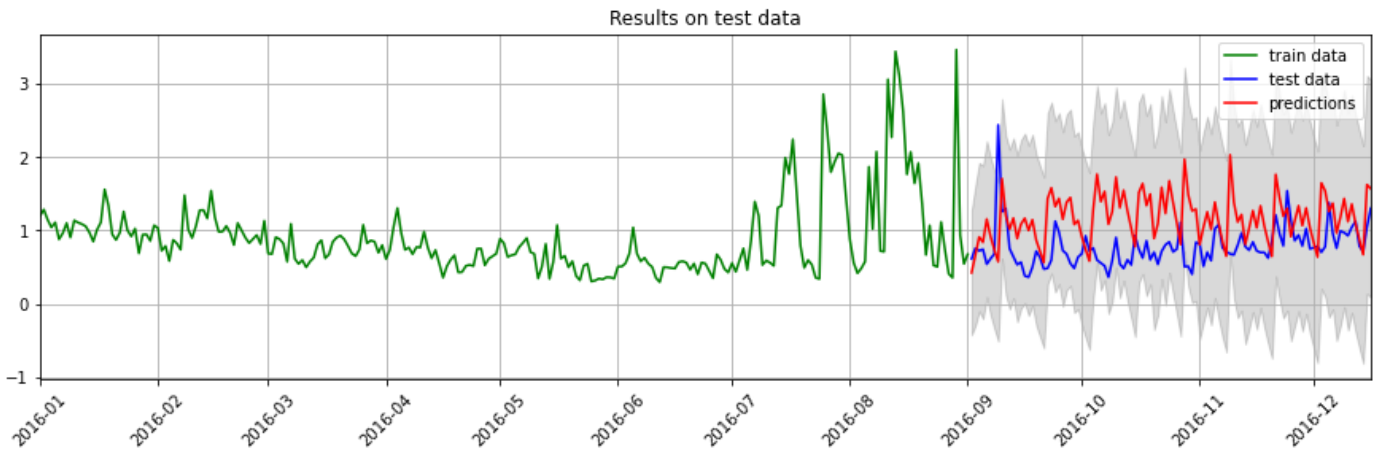
```
In [33]: y_forec, conf_int = arima_model.predict(len(test), return_conf_int=True, alpha=0.05)
pred = pd.Series(y_forec, index=test.index)
pred.columns = ['predicted']
confidence = pd.DataFrame(conf_int, columns=['lower', 'upper'])

plt.figure(figsize=(15,4))
plt.plot(train, c='green', label='train data')
plt.plot(test, c='blue', label='test data')
plt.plot(pred, c='red', label='predictions')
plt.legend()
plt.grid(), plt.margins(x=0)
plt.title('Results on test data'), plt.xticks(rotation=45)
plt.fill_between(test.index, confidence['lower'],
                 confidence['upper'], color='k', alpha=.15)

from sklearn.metrics import r2_score
print('Actual values: ', np.around(test[:10].tolist(),3))
print('Predictions:   ', np.around(pred[:10].tolist(),3))
print('RMSE: %.3f' % np.sqrt(mean_squared_error(test, pred)))
MAE = mean_absolute_error(test, pred)
MAPE = np.mean(np.abs(pred - test)/np.abs(test))
MASE = np.mean(np.abs(test - pred))/(np.mean(np.abs(np.diff(train)).sum()/(len(train)-1)))
print('MAE: %.3f' % MAE)
print('MAPE: %.3f' % MAPE)
print('MASE: %.3f' % MASE)
print('R^2 score: %.3f' % r2_score(test, pred))

Actual values:  [0.616 0.758 0.724 0.744 0.542 0.617 0.681 2.438 1.256 1.299]
Predictions:    [0.426 0.661 0.912 0.84  1.155 0.917 0.739 0.575 1.705 1.205]
RMSE: 0.581
```

MAE: 0.469
MAPE: 0.712
MASE: 1.909
R² score: -3.404



LSTM

```
In [34]: from keras.models import Sequential
from keras.layers import LSTM
from keras.layers import Dense, Dropout
from keras.layers import Bidirectional
```

```
In [35]: n_features = 1
n_steps = 10

model = Sequential()
model.add(LSTM(50, activation='relu', input_shape=(n_steps, n_features)))
model.add(Dense(1))
model.compile(optimizer='adam', loss='mse')
model.summary()
```

Metal device set to: Apple M1 Pro

WARNING:tensorflow:Layer lstm will not use cuDNN kernels since it doesn't meet the criteria. It will use a generic GPU kernel as fallback when running on GPU.

Model: "sequential"

Layer (type)	Output Shape	Param #
lstm (LSTM)	(None, 50)	10400
dense (Dense)	(None, 1)	51

=====
Total params: 10,451
Trainable params: 10,451
Non-trainable params: 0

```
2022-10-26 22:36:57.049672: I tensorflow/core/common_runtime/pluggable_device/pluggable_device_factory.cc:305] Could not identify NUMA node of platform GPU ID 0, defaulting to 0. Your kernel may not have been built with NUMA support.
2022-10-26 22:36:57.049982: I tensorflow/core/common_runtime/pluggable_device/pluggable_device_factory.cc:271] Created TensorFlow device (/job:localhost/replica:0/task:0/device:GPU:0 with 0 MB memory) -> physical PluggableDevice (device: 0, name: METAL, pci bus id: <undefined>)
```

```
In [36]: def train_test_data(seq, steps):
X, Y = list(), list()
for i in range(len(seq)):
sample = i + steps
```

```

        if sample > len(seq)-1:
            break
        x, y = seq[i:sample], seq[sample]
        X.append(x)
        Y.append(y)
    return np.array(X), np.array(Y)

```

```

In [37]: def train_test_validation_plot(train_size, test_size):
plt.figure(figsize=(12,9))
plt.plot(data_daily[:train_size])
plt.plot(data_daily[train_size:test_size])
plt.plot(data_daily[test_size:])

```

```

In [38]: steps = 10
X, Y = train_test_data(data_daily.tolist(), steps)
X = X.reshape((X.shape[0], X.shape[1], 1))

Training_size = int(len(data_daily)*0.7)
Training_Validation_size = int(((len(data_daily)-size)/2)+size)

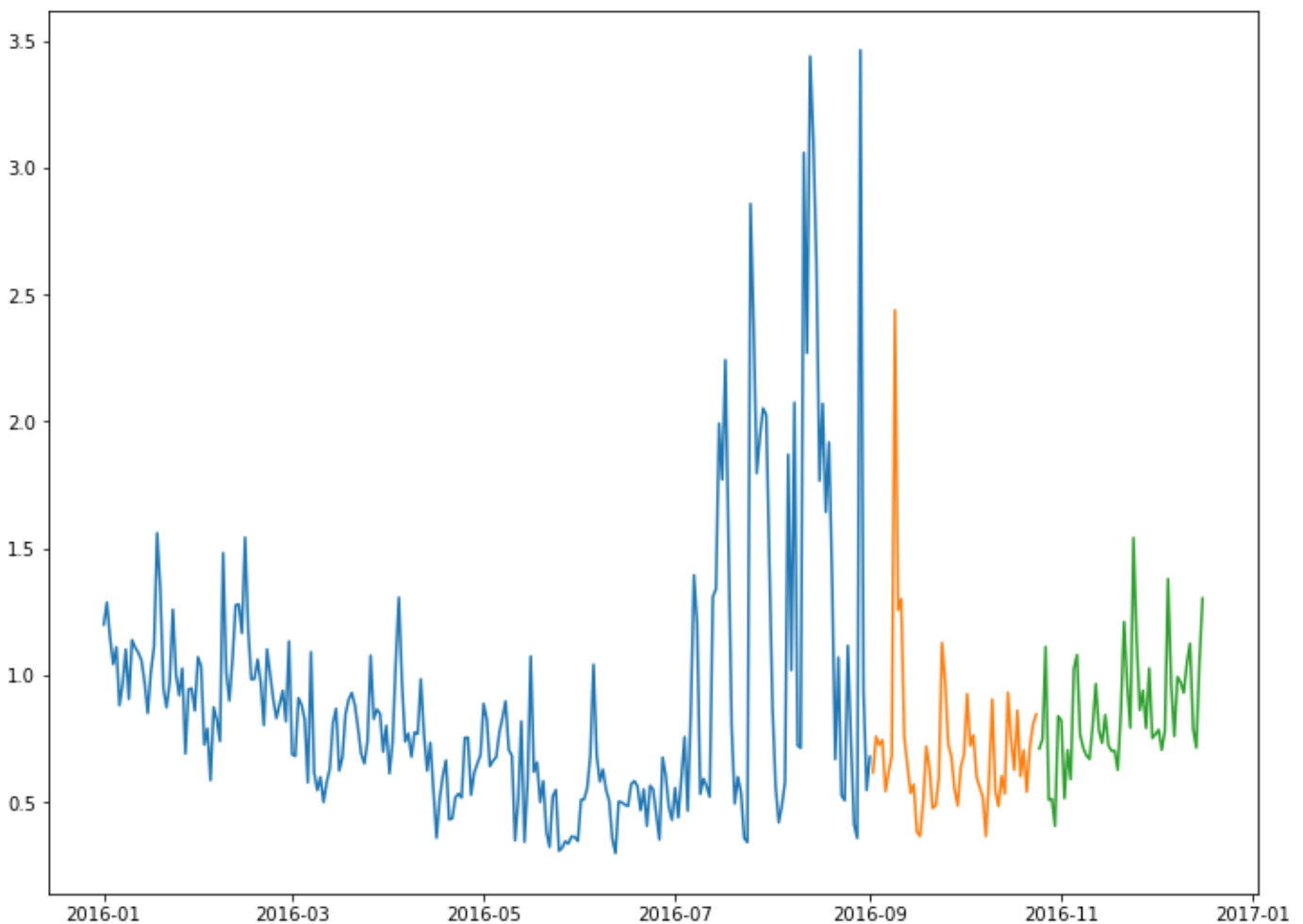
X_train, Y_train = X[:Training_size], Y[:Training_size]
X_val, Y_val = X[Training_size:Training_Validation_size], Y[Training_size:Training_Validation_size]
X_test, Y_test = X[Training_Validation_size:], Y[Training_Validation_size:]

print('Training size:', Training_size)
print('Training + Validation size:', Training_Validation_size)

train_test_validation_plot(Training_size, Training_Validation_size)

```

Training size: 245
Training + Validation size: 298



```

In [39]: mse_train = list()
mse_val = list()

```

```

for epoch in range(0,50,5):
    # fit the model with epochs
    model_fit = model.fit(X_train, Y_train, epochs=epoch, verbose=1)

    #model evaluation
    Train_pred = model.predict(X_train, verbose=0)
    Val_pred = model.predict(X_val, verbose=0)

    #computing the training and validation loss
    mse_t = mean_squared_error(Train_pred, Y_train)
    mse_v = mean_squared_error(Val_pred, Y_val)
    mse_train.append(mse_t)
    mse_val.append(mse_v)

```

```

2022-10-26 22:36:57.280615: W tensorflow/core/platform/profile_utils/cpu_utils.cc:128] Failed to get CPU frequency: 0 Hz
2022-10-26 22:36:57.353533: I tensorflow/core/grappler/optimizers/custom_graph_optimizer_registry.cc:113] Plugin optimizer for device_type GPU is enabled.

```

Epoch 1/5

```

2022-10-26 22:36:57.834216: I tensorflow/core/grappler/optimizers/custom_graph_optimizer_registry.cc:113] Plugin optimizer for device_type GPU is enabled.

```

8/8 [=====] - 1s 95ms/step - loss: 0.9328

Epoch 2/5

8/8 [=====] - 1s 86ms/step - loss: 0.5751

Epoch 3/5

8/8 [=====] - 1s 89ms/step - loss: 0.3108

Epoch 4/5

8/8 [=====] - 1s 87ms/step - loss: 0.3050

Epoch 5/5

8/8 [=====] - 1s 86ms/step - loss: 0.2467

Epoch 1/10

8/8 [=====] - 1s 86ms/step - loss: 0.2514

Epoch 2/10

8/8 [=====] - 1s 86ms/step - loss: 0.2335

Epoch 3/10

8/8 [=====] - 1s 83ms/step - loss: 0.2250

Epoch 4/10

8/8 [=====] - 1s 83ms/step - loss: 0.2248

Epoch 5/10

8/8 [=====] - 1s 83ms/step - loss: 0.2198

Epoch 6/10

8/8 [=====] - 1s 83ms/step - loss: 0.2140

Epoch 7/10

8/8 [=====] - 1s 84ms/step - loss: 0.2090

Epoch 8/10

8/8 [=====] - 1s 86ms/step - loss: 0.2044

Epoch 9/10

8/8 [=====] - 1s 84ms/step - loss: 0.1971

Epoch 10/10

8/8 [=====] - 1s 84ms/step - loss: 0.1925

Epoch 1/15

8/8 [=====] - 1s 84ms/step - loss: 0.1886

Epoch 2/15

8/8 [=====] - 1s 86ms/step - loss: 0.1862

Epoch 3/15

8/8 [=====] - 1s 84ms/step - loss: 0.1855

Epoch 4/15

8/8 [=====] - 1s 86ms/step - loss: 0.1845

Epoch 5/15

8/8 [=====] - 1s 86ms/step - loss: 0.1846

Epoch 6/15

8/8 [=====] - 1s 87ms/step - loss: 0.1854

Epoch 7/15

8/8 [=====] - 1s 87ms/step - loss: 0.1812

Epoch 8/15

```
8/8 [=====] - 1s 85ms/step - loss: 0.1813
Epoch 9/15
8/8 [=====] - 1s 88ms/step - loss: 0.1796
Epoch 10/15
8/8 [=====] - 1s 87ms/step - loss: 0.1793
Epoch 11/15
8/8 [=====] - 1s 89ms/step - loss: 0.1792
Epoch 12/15
8/8 [=====] - 1s 88ms/step - loss: 0.1801
Epoch 13/15
8/8 [=====] - 1s 85ms/step - loss: 0.1771
Epoch 14/15
8/8 [=====] - 1s 88ms/step - loss: 0.1766
Epoch 15/15
8/8 [=====] - 1s 86ms/step - loss: 0.1774
Epoch 1/20
8/8 [=====] - 1s 87ms/step - loss: 0.1737
Epoch 2/20
8/8 [=====] - 1s 86ms/step - loss: 0.1777
Epoch 3/20
8/8 [=====] - 1s 87ms/step - loss: 0.1767
Epoch 4/20
8/8 [=====] - 1s 86ms/step - loss: 0.1751
Epoch 5/20
8/8 [=====] - 1s 85ms/step - loss: 0.1710
Epoch 6/20
8/8 [=====] - 1s 86ms/step - loss: 0.1735
Epoch 7/20
8/8 [=====] - 1s 88ms/step - loss: 0.1739
Epoch 8/20
8/8 [=====] - 1s 86ms/step - loss: 0.1711
Epoch 9/20
8/8 [=====] - 1s 88ms/step - loss: 0.1698
Epoch 10/20
8/8 [=====] - 1s 87ms/step - loss: 0.1760
Epoch 11/20
8/8 [=====] - 1s 85ms/step - loss: 0.1730
Epoch 12/20
8/8 [=====] - 1s 85ms/step - loss: 0.1700
Epoch 13/20
8/8 [=====] - 1s 85ms/step - loss: 0.1685
Epoch 14/20
8/8 [=====] - 1s 86ms/step - loss: 0.1677
Epoch 15/20
8/8 [=====] - 1s 85ms/step - loss: 0.1671
Epoch 16/20
8/8 [=====] - 1s 84ms/step - loss: 0.1678
Epoch 17/20
8/8 [=====] - 1s 87ms/step - loss: 0.1677
Epoch 18/20
8/8 [=====] - 1s 87ms/step - loss: 0.1696
Epoch 19/20
8/8 [=====] - 1s 85ms/step - loss: 0.1790
Epoch 20/20
8/8 [=====] - 1s 85ms/step - loss: 0.1753
Epoch 1/25
8/8 [=====] - 1s 84ms/step - loss: 0.1654
Epoch 2/25
8/8 [=====] - 1s 84ms/step - loss: 0.1733
Epoch 3/25
8/8 [=====] - 1s 85ms/step - loss: 0.1665
Epoch 4/25
8/8 [=====] - 1s 85ms/step - loss: 0.1664
Epoch 5/25
8/8 [=====] - 1s 85ms/step - loss: 0.1682
Epoch 6/25
```

```
8/8 [=====] - 1s 86ms/step - loss: 0.1670
Epoch 7/25
8/8 [=====] - 1s 86ms/step - loss: 0.1716
Epoch 8/25
8/8 [=====] - 1s 87ms/step - loss: 0.1650
Epoch 9/25
8/8 [=====] - 1s 86ms/step - loss: 0.1676
Epoch 10/25
8/8 [=====] - 1s 87ms/step - loss: 0.1664
Epoch 11/25
8/8 [=====] - 1s 87ms/step - loss: 0.1664
Epoch 12/25
8/8 [=====] - 1s 86ms/step - loss: 0.1658
Epoch 13/25
8/8 [=====] - 1s 88ms/step - loss: 0.1676
Epoch 14/25
8/8 [=====] - 1s 88ms/step - loss: 0.1660
Epoch 15/25
8/8 [=====] - 1s 87ms/step - loss: 0.1654
Epoch 16/25
8/8 [=====] - 1s 87ms/step - loss: 0.1645
Epoch 17/25
8/8 [=====] - 1s 87ms/step - loss: 0.1680
Epoch 18/25
8/8 [=====] - 1s 86ms/step - loss: 0.1707
Epoch 19/25
8/8 [=====] - 1s 87ms/step - loss: 0.1649
Epoch 20/25
8/8 [=====] - 1s 86ms/step - loss: 0.1671
Epoch 21/25
8/8 [=====] - 1s 87ms/step - loss: 0.1654
Epoch 22/25
8/8 [=====] - 1s 88ms/step - loss: 0.1638
Epoch 23/25
8/8 [=====] - 1s 88ms/step - loss: 0.1642
Epoch 24/25
8/8 [=====] - 1s 86ms/step - loss: 0.1643
Epoch 25/25
8/8 [=====] - 1s 87ms/step - loss: 0.1638
Epoch 1/30
8/8 [=====] - 1s 86ms/step - loss: 0.1631
Epoch 2/30
8/8 [=====] - 1s 85ms/step - loss: 0.1632
Epoch 3/30
8/8 [=====] - 1s 84ms/step - loss: 0.1630
Epoch 4/30
8/8 [=====] - 1s 83ms/step - loss: 0.1643
Epoch 5/30
8/8 [=====] - 1s 83ms/step - loss: 0.1696
Epoch 6/30
8/8 [=====] - 1s 84ms/step - loss: 0.1681
Epoch 7/30
8/8 [=====] - 1s 84ms/step - loss: 0.1670
Epoch 8/30
8/8 [=====] - 1s 84ms/step - loss: 0.1628
Epoch 9/30
8/8 [=====] - 1s 84ms/step - loss: 0.1662
Epoch 10/30
8/8 [=====] - 1s 87ms/step - loss: 0.1621
Epoch 11/30
8/8 [=====] - 1s 84ms/step - loss: 0.1626
Epoch 12/30
8/8 [=====] - 1s 84ms/step - loss: 0.1629
Epoch 13/30
8/8 [=====] - 1s 87ms/step - loss: 0.1631
Epoch 14/30
```

```
8/8 [=====] - 1s 87ms/step - loss: 0.1617
Epoch 15/30
8/8 [=====] - 1s 85ms/step - loss: 0.1624
Epoch 16/30
8/8 [=====] - 1s 86ms/step - loss: 0.1611
Epoch 17/30
8/8 [=====] - 1s 84ms/step - loss: 0.1608
Epoch 18/30
8/8 [=====] - 1s 85ms/step - loss: 0.1609
Epoch 19/30
8/8 [=====] - 1s 84ms/step - loss: 0.1663
Epoch 20/30
8/8 [=====] - 1s 85ms/step - loss: 0.1604
Epoch 21/30
8/8 [=====] - 1s 85ms/step - loss: 0.1629
Epoch 22/30
8/8 [=====] - 1s 86ms/step - loss: 0.1619
Epoch 23/30
8/8 [=====] - 1s 85ms/step - loss: 0.1647
Epoch 24/30
8/8 [=====] - 1s 85ms/step - loss: 0.1610
Epoch 25/30
8/8 [=====] - 1s 85ms/step - loss: 0.1617
Epoch 26/30
8/8 [=====] - 1s 86ms/step - loss: 0.1615
Epoch 27/30
8/8 [=====] - 1s 84ms/step - loss: 0.1631
Epoch 28/30
8/8 [=====] - 1s 84ms/step - loss: 0.1603
Epoch 29/30
8/8 [=====] - 1s 85ms/step - loss: 0.1599
Epoch 30/30
8/8 [=====] - 1s 85ms/step - loss: 0.1601
Epoch 1/35
8/8 [=====] - 1s 85ms/step - loss: 0.1594
Epoch 2/35
8/8 [=====] - 1s 87ms/step - loss: 0.1592
Epoch 3/35
8/8 [=====] - 1s 88ms/step - loss: 0.1592
Epoch 4/35
8/8 [=====] - 1s 87ms/step - loss: 0.1600
Epoch 5/35
8/8 [=====] - 1s 86ms/step - loss: 0.1605
Epoch 6/35
8/8 [=====] - 1s 87ms/step - loss: 0.1608
Epoch 7/35
8/8 [=====] - 1s 86ms/step - loss: 0.1587
Epoch 8/35
8/8 [=====] - 1s 87ms/step - loss: 0.1589
Epoch 9/35
8/8 [=====] - 1s 85ms/step - loss: 0.1598
Epoch 10/35
8/8 [=====] - 1s 87ms/step - loss: 0.1682
Epoch 11/35
8/8 [=====] - 1s 93ms/step - loss: 0.1592
Epoch 12/35
8/8 [=====] - 1s 86ms/step - loss: 0.1592
Epoch 13/35
8/8 [=====] - 1s 92ms/step - loss: 0.1623
Epoch 14/35
8/8 [=====] - 1s 87ms/step - loss: 0.1585
Epoch 15/35
8/8 [=====] - 1s 90ms/step - loss: 0.1583
Epoch 16/35
8/8 [=====] - 1s 86ms/step - loss: 0.1592
Epoch 17/35
```

```
8/8 [=====] - 1s 89ms/step - loss: 0.1588
Epoch 18/35
8/8 [=====] - 1s 85ms/step - loss: 0.1593
Epoch 19/35
8/8 [=====] - 1s 85ms/step - loss: 0.1587
Epoch 20/35
8/8 [=====] - 1s 86ms/step - loss: 0.1576
Epoch 21/35
8/8 [=====] - 1s 84ms/step - loss: 0.1593
Epoch 22/35
8/8 [=====] - 1s 85ms/step - loss: 0.1573
Epoch 23/35
8/8 [=====] - 1s 89ms/step - loss: 0.1573
Epoch 24/35
8/8 [=====] - 1s 86ms/step - loss: 0.1551
Epoch 25/35
8/8 [=====] - 1s 84ms/step - loss: 0.1623
Epoch 26/35
8/8 [=====] - 1s 84ms/step - loss: 0.1663
Epoch 27/35
8/8 [=====] - 1s 84ms/step - loss: 0.1624
Epoch 28/35
8/8 [=====] - 1s 84ms/step - loss: 0.1623
Epoch 29/35
8/8 [=====] - 1s 84ms/step - loss: 0.1578
Epoch 30/35
8/8 [=====] - 1s 84ms/step - loss: 0.1603
Epoch 31/35
8/8 [=====] - 1s 84ms/step - loss: 0.1652
Epoch 32/35
8/8 [=====] - 1s 85ms/step - loss: 0.1610
Epoch 33/35
8/8 [=====] - 1s 84ms/step - loss: 0.1555
Epoch 34/35
8/8 [=====] - 1s 85ms/step - loss: 0.1570
Epoch 35/35
8/8 [=====] - 1s 84ms/step - loss: 0.1591
Epoch 1/40
8/8 [=====] - 1s 86ms/step - loss: 0.1581
Epoch 2/40
8/8 [=====] - 1s 86ms/step - loss: 0.1565
Epoch 3/40
8/8 [=====] - 1s 89ms/step - loss: 0.1583
Epoch 4/40
8/8 [=====] - 1s 88ms/step - loss: 0.1594
Epoch 5/40
8/8 [=====] - 1s 87ms/step - loss: 0.1560
Epoch 6/40
8/8 [=====] - 1s 88ms/step - loss: 0.1537
Epoch 7/40
8/8 [=====] - 1s 87ms/step - loss: 0.1535
Epoch 8/40
8/8 [=====] - 1s 88ms/step - loss: 0.1540
Epoch 9/40
8/8 [=====] - 1s 86ms/step - loss: 0.1542
Epoch 10/40
8/8 [=====] - 1s 87ms/step - loss: 0.1534
Epoch 11/40
8/8 [=====] - 1s 88ms/step - loss: 0.1532
Epoch 12/40
8/8 [=====] - 1s 87ms/step - loss: 0.1526
Epoch 13/40
8/8 [=====] - 1s 86ms/step - loss: 0.1552
Epoch 14/40
8/8 [=====] - 1s 88ms/step - loss: 0.1516
Epoch 15/40
```



```
8/8 [=====] - 1s 87ms/step - loss: 0.1529
Epoch 16/40
8/8 [=====] - 1s 87ms/step - loss: 0.1608
Epoch 17/40
8/8 [=====] - 1s 88ms/step - loss: 0.1538
Epoch 18/40
8/8 [=====] - 1s 88ms/step - loss: 0.1509
Epoch 19/40
8/8 [=====] - 1s 91ms/step - loss: 0.1531
Epoch 20/40
8/8 [=====] - 1s 91ms/step - loss: 0.1525
Epoch 21/40
8/8 [=====] - 1s 89ms/step - loss: 0.1522
Epoch 22/40
8/8 [=====] - 1s 88ms/step - loss: 0.1501
Epoch 23/40
8/8 [=====] - 1s 89ms/step - loss: 0.1500
Epoch 24/40
8/8 [=====] - 1s 90ms/step - loss: 0.1482
Epoch 25/40
8/8 [=====] - 1s 89ms/step - loss: 0.1486
Epoch 26/40
8/8 [=====] - 1s 88ms/step - loss: 0.1524
Epoch 27/40
8/8 [=====] - 1s 90ms/step - loss: 0.1551
Epoch 28/40
8/8 [=====] - 1s 90ms/step - loss: 0.1524
Epoch 29/40
8/8 [=====] - 1s 89ms/step - loss: 0.1497
Epoch 30/40
8/8 [=====] - 1s 90ms/step - loss: 0.1507
Epoch 31/40
8/8 [=====] - 1s 88ms/step - loss: 0.1589
Epoch 32/40
8/8 [=====] - 1s 88ms/step - loss: 0.1487
Epoch 33/40
8/8 [=====] - 1s 88ms/step - loss: 0.1477
Epoch 34/40
8/8 [=====] - 1s 89ms/step - loss: 0.1540
Epoch 35/40
8/8 [=====] - 1s 88ms/step - loss: 0.1488
Epoch 36/40
8/8 [=====] - 1s 89ms/step - loss: 0.1474
Epoch 37/40
8/8 [=====] - 1s 87ms/step - loss: 0.1501
Epoch 38/40
8/8 [=====] - 1s 90ms/step - loss: 0.1529
Epoch 39/40
8/8 [=====] - 1s 89ms/step - loss: 0.1527
Epoch 40/40
8/8 [=====] - 1s 88ms/step - loss: 0.1521
Epoch 1/45
8/8 [=====] - 1s 86ms/step - loss: 0.1517
Epoch 2/45
8/8 [=====] - 1s 86ms/step - loss: 0.1547
Epoch 3/45
8/8 [=====] - 1s 85ms/step - loss: 0.1535
Epoch 4/45
8/8 [=====] - 1s 84ms/step - loss: 0.1484
Epoch 5/45
8/8 [=====] - 1s 85ms/step - loss: 0.1433
Epoch 6/45
8/8 [=====] - 1s 87ms/step - loss: 0.1431
Epoch 7/45
8/8 [=====] - 1s 84ms/step - loss: 0.1451
Epoch 8/45
```

```
8/8 [=====] - 1s 85ms/step - loss: 0.1428
Epoch 9/45
8/8 [=====] - 1s 87ms/step - loss: 0.1429
Epoch 10/45
8/8 [=====] - 1s 85ms/step - loss: 0.1416
Epoch 11/45
8/8 [=====] - 1s 88ms/step - loss: 0.1447
Epoch 12/45
8/8 [=====] - 1s 84ms/step - loss: 0.1534
Epoch 13/45
8/8 [=====] - 1s 84ms/step - loss: 0.1567
Epoch 14/45
8/8 [=====] - 1s 84ms/step - loss: 0.1534
Epoch 15/45
8/8 [=====] - 1s 84ms/step - loss: 0.1522
Epoch 16/45
8/8 [=====] - 1s 84ms/step - loss: 0.1471
Epoch 17/45
8/8 [=====] - 1s 87ms/step - loss: 0.1483
Epoch 18/45
8/8 [=====] - 1s 85ms/step - loss: 0.1441
Epoch 19/45
8/8 [=====] - 1s 86ms/step - loss: 0.1410
Epoch 20/45
8/8 [=====] - 1s 85ms/step - loss: 0.1415
Epoch 21/45
8/8 [=====] - 1s 85ms/step - loss: 0.1499
Epoch 22/45
8/8 [=====] - 1s 86ms/step - loss: 0.1457
Epoch 23/45
8/8 [=====] - 1s 85ms/step - loss: 0.1445
Epoch 24/45
8/8 [=====] - 1s 86ms/step - loss: 0.1430
Epoch 25/45
8/8 [=====] - 1s 84ms/step - loss: 0.1414
Epoch 26/45
8/8 [=====] - 1s 84ms/step - loss: 0.1452
Epoch 27/45
8/8 [=====] - 1s 85ms/step - loss: 0.1509
Epoch 28/45
8/8 [=====] - 1s 84ms/step - loss: 0.1512
Epoch 29/45
8/8 [=====] - 1s 83ms/step - loss: 0.1445
Epoch 30/45
8/8 [=====] - 1s 84ms/step - loss: 0.1433
Epoch 31/45
8/8 [=====] - 1s 83ms/step - loss: 0.1419
Epoch 32/45
8/8 [=====] - 1s 84ms/step - loss: 0.1364
Epoch 33/45
8/8 [=====] - 1s 84ms/step - loss: 0.1375
Epoch 34/45
8/8 [=====] - 1s 84ms/step - loss: 0.1392
Epoch 35/45
8/8 [=====] - 1s 86ms/step - loss: 0.1414
Epoch 36/45
8/8 [=====] - 1s 86ms/step - loss: 0.1465
Epoch 37/45
8/8 [=====] - 1s 85ms/step - loss: 0.1427
Epoch 38/45
8/8 [=====] - 1s 82ms/step - loss: 0.1385
Epoch 39/45
8/8 [=====] - 1s 84ms/step - loss: 0.1351
Epoch 40/45
8/8 [=====] - 1s 84ms/step - loss: 0.1354
Epoch 41/45
```

```

8/8 [=====] - 1s 84ms/step - loss: 0.1352
Epoch 42/45
8/8 [=====] - 1s 84ms/step - loss: 0.1317
Epoch 43/45
8/8 [=====] - 1s 84ms/step - loss: 0.1349
Epoch 44/45
8/8 [=====] - 1s 84ms/step - loss: 0.1303
Epoch 45/45
8/8 [=====] - 1s 84ms/step - loss: 0.1377

```

```

In [40]: # Plot the loss results
def plot_loss_results(mse_train, mse_val):
    plt.plot(range(0,50,5), mse_train, label='Train loss')
    plt.plot(range(0,50,5), mse_val, label='Validation loss')
    plt.legend()
    print('Train MSE minimum:', min(mse_train))
    print('Validation MSE minimum:', min(mse_val))

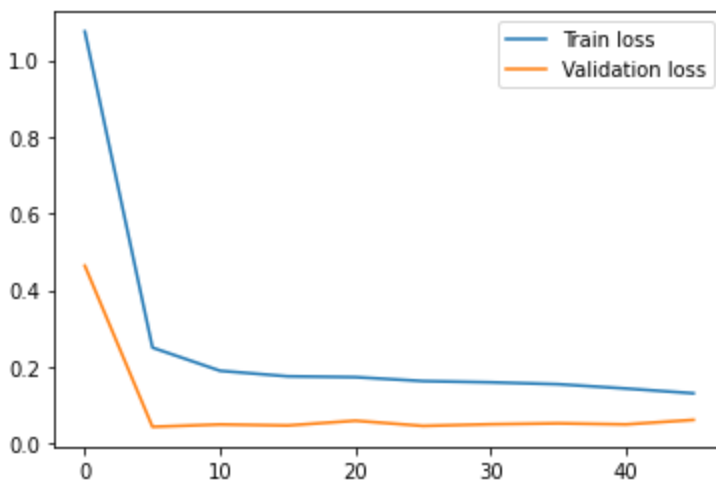
```

```

In [41]: plot_loss_results(mse_train, mse_val)

Train MSE minimum: 0.13030434690527548
Validation MSE minimum: 0.04278607918110724

```



```

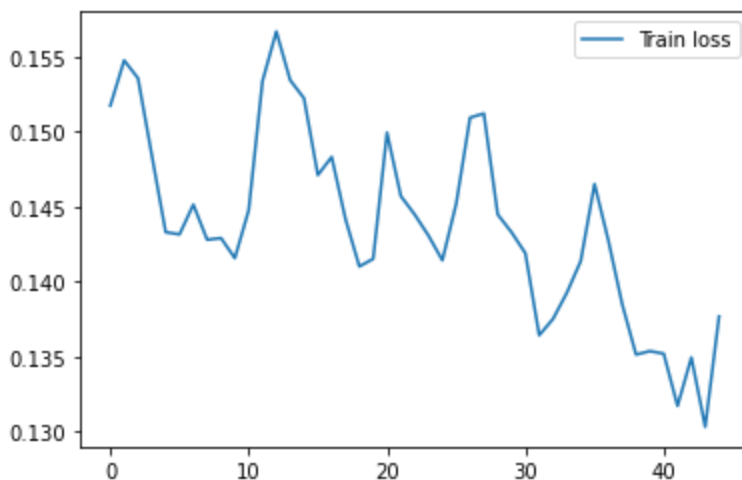
In [42]: plt.plot(model_fit.history['loss'], label='Train loss')
# plt.plot(model_fit.history['val_loss'], label='Validation loss')
plt.legend()
print('Train MSE minimum:', min(model_fit.history['loss']))
#print('Validation MSE minimum:', min(model_fit.history['val_loss']))

```

```

Train MSE minimum: 0.1303059160709381

```



```

In [44]: Train_pred = model.predict(X_train, verbose=0)
Y_pred = model.predict(X_test, verbose=0)

```

```

In [65]: Y_pred_series = pd.Series(Y_pred.flatten().tolist(), index=data_daily[size+(np.abs(len(Y
Train_pred_series = pd.Series(Train_pred.flatten().tolist(), index=data_daily[:size].ind

#Plot
plt.figure(figsize=(15,4))
plt.plot(data_daily[:size], c='blue',label='train data')
plt.plot(Train_pred_series, c='green',label='train predicted data')
plt.plot(data_daily[size:], c='black',label='test data')
plt.plot(Y_pred_series, c='red', label='model')
plt.legend()
plt.grid(), plt.margins(x=0);

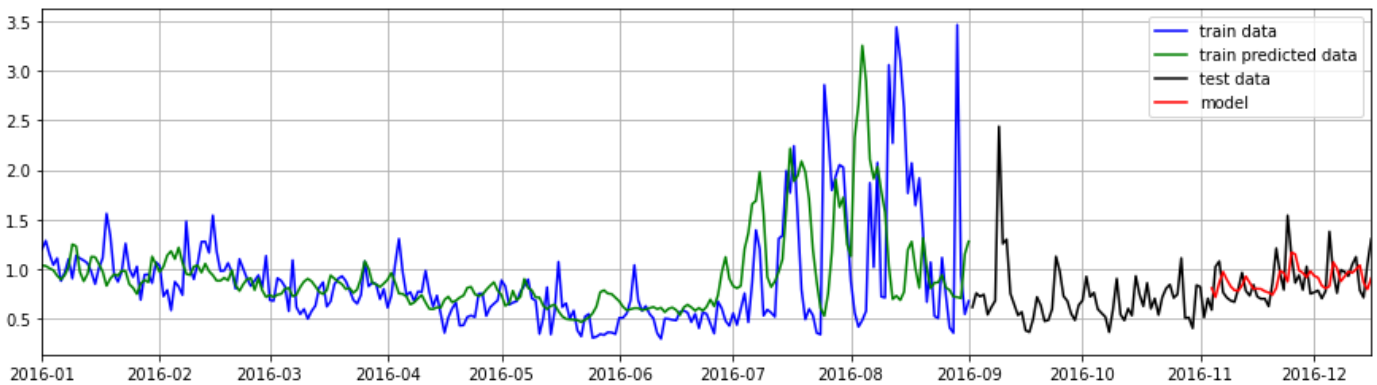
# calc error
print('MSE: %.5f' % (mean_squared_error(Y_pred, Y_test)))
print('RMSE: %.5f' % np.sqrt(mean_squared_error(Y_pred, Y_test)))
MAE = mean_absolute_error(Y_test, Y_pred)
MAPE = np.mean(np.abs(Y_pred - Y_test)/np.abs(Y_test))
print('MAE: %.3f' % MAE)
print('MAPE: %.3f' %MAPE)
print('MASE: %.3f' %MASE)
print('R^2 score: %.3f' % r2_score(Y_test, Y_pred))

```

```

MSE: 0.04671
RMSE: 0.21613
MAE: 0.170
MAPE: 0.203
MASE: 1.909
R^2 score: -0.099

```



In []: