What Statistics Make a Team NBA Champions

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Background:

Every year, the National Basketball Association (NBA) ends the season with a series of championship games between the two best teams in the league. The series is a best-of-7, where the first team to win 4 games is the winner of the series. The championship is a very important accolade, both teams and players are compared by the number of championships they have won. In these comparisons, statistics like field goal percentage, offensive rebounds, steals, and blocks can be used to determine a team's performance and be an indicator of how much better one team is than another.

Statistics in the NBA are highly analyzed, very often with the goal of assessing which areas a team can improve upon. Our group wants to create a model that will be able to tell us which key statistics from the NBA Championship series from 1980-2018 were important in deciding the championship. More specifically, we want to find weights for each statistic that can show us how important each statistic is to predicting the overall winner, which helps our group conduct a greater analysis of how different focuses and strategies can affect the outcome of NBA games.

We will be using the NBA Finals Team Stats Dataset, which has been analyzed and used to create models by several Kaggle Users. One project to note is a report written by Ziyu Liu called "Three pointers win championships", in which the author creates a model to see if the number of three point shots made by a team can predict whether or not the team wins the championship. In the study, the model achieves an accuracy of 59%. This tells us that, while three point shots are important, more statistics are required to be able to create a more accurate model.

Another example of analyzing NBA championship data comes from the article "Stat of the Week: How champions are built in the NBA" by Ryan Blackburn. In this article, Blackburn specifically analyzes the Denver Nuggets, and why the team has never won an NBA championship. In the paper, Blackburn ranks teams by offense, defense, and net-rating, and points out that only five out of past 20 championship winners have ranked outside of the top 3 teams in net-rating. This leads us to believe that a team needs both impressive defensive statistics and offensive statistics in order to win an NBA championship.

Given these studies and our group's own knowledge of the NBA, we believe that both offensive statistics like field goals, three pointers, offensive rebounds; and defensive statistics like steals and defensive rebounds will have a high impact on whether or not a team wins the championship.

Data:

The dataset with which we want to create our model is the NBA Finals Team Stats dataset on Kaggle uploaded by Dave Rosenman. The dataset contains final data from 1980 to 2018, and is divided into two tables. The first table contains the data of each winning team and the second contains the losing team. Each observation includes data points like field goals made, field goals attempted, three point shots made, free throws made, total rebounds, assists, steals, turnovers, blocks, and many other statistics that will be

covered in the data summary. The data takes averages from each game in the series, and its an average of the performance of the team in this category across all the games played in the series.

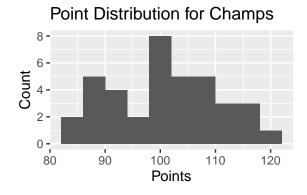
In order to create the dataset we are using in this study, we started with two separate datasets, one for all of the series winners (NBA Champions) and one of the runner-ups. We created a new column win with a 1 if the team won the series and a 0 if the team lost. This will be our predictor variable for the model. Next, we combined the two datsets and randomized the order of the entries. Our goal is to first analyze each of the variables to determine which will be the most useful in creating our model, then going through several iterations of models before choosing the most accurate one.

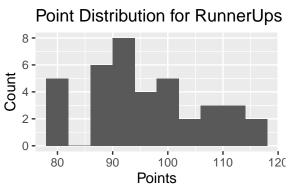
Exploratory Data Analysis

As mentioned before, we combined the datasets and added a win variable to tell us whether the team won a championship or not. Since there were over 20 variables, our goal was to choose key variables to analyze that we knew would have an impact on the game. To do this, we eliminated some variables that we did not wish to explore or view the effect they would have on the model. This includes statistics like FTA (Free Throw Attempts), BLK (Blocks). While in the game this statistics might be important, having a statistic like Free Throw Attempts or Blocks without any context about the other team's performance in the same category would most likely not be useful.

Now, we can start our EDA. First, we check the plots of each variable for both the losers and the winners to make sure each distribution is roughly normal.

Distribution of Points:

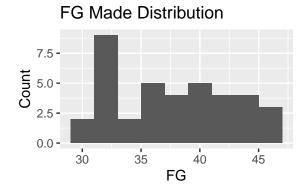


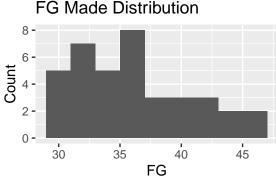


Summary of Points:

```
## Min. 1st Qu. Median Mean 3rd Qu. Max.
## 79.80 90.74 99.19 98.56 106.67 121.60
```

Distribution of Field Goals Made:





Summary of Field Goals:

```
## Min. 1st Qu. Median Mean 3rd Qu. Max.
## 30.00 32.96 36.08 37.02 40.81 46.71
```

The distributions and summaries of the other variables can be seen in the appendix. All of the distributions appear to be somewhat normal with no outliers, We have a large sample size, so we can continue to make our model and check the residuals.

Creating the Model

Model Refinement

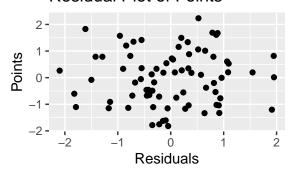
Our model will be a binomial model, since the only options are 0 and 1. We want to make sure that all the different variables have been scaled before we measure how important they are in relation to each other (summary of scaled data can be seen in the Appendix). The next step will be to plot the residuals of each variable in the model to check the linearity assumption. Then, we will plot the Cook's distance and remove any high-leverage points. Finally, the VIF will be checked and any variables with a high VIF will be removed from the model.

Summary of Model:

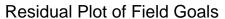
term	estimate	std.error	statistic	p.value	conf.low	conf.high
(Intercept)	-0.014	0.360	-0.038	0.970	-0.735	0.709
PTS	0.601	1.167	0.515	0.607	-1.702	2.985
FG	1.763	11.167	0.158	0.875	-20.543	24.230
FGA	-4.368	7.220	-0.605	0.545	-19.110	9.799
FGP	1.161	6.759	0.172	0.864	-12.193	14.895
TP	0.515	2.543	0.202	0.840	-4.390	5.966
TPA	0.170	2.356	0.072	0.943	-4.779	4.784
TPP	0.402	0.810	0.496	0.620	-1.375	1.964
ORB	2.674	0.820	3.260	0.001	1.261	4.515
DRB	1.199	0.495	2.422	0.015	0.329	2.312
AST	-0.091	0.637	-0.143	0.886	-1.359	1.188
STL	1.010	0.423	2.385	0.017	0.236	1.928
BLK	0.019	0.537	0.035	0.972	-1.043	1.099
TOV	-0.575	0.431	-1.334	0.182	-1.475	0.247
PF	-0.148	0.443	-0.333	0.739	-1.042	0.737

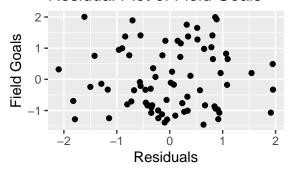
Residual Plot of Points:

Residual Plot of Points



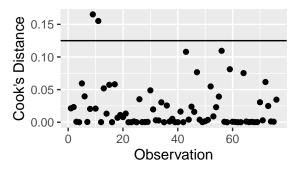
Residual Plot of Field Goals:





The residual plots for each variable appear to be random and evenly dispersed (the rest can be seen in the appendix), which means that the linearity assumption is satisfied. Before we can test the accuracy of the model, we must also explore how these observations affect the model, and how the variables used in the model affect each other. First, we can plot the leverage (.cooksd) of each observation to see if there are any high-leverage data points.

Cook's Distance of each Obser



It is obvious that there are two high-leverage data points. If we use a threshold of 0.125, we can eliminate these two high-leverage points to make the model better at prediction. After this, the model must be trained on the newly-filtered data. Then, we re-train our model on the now filtered dataset.

Summary of Model on Filtered Dataset:

term	estimate	std.error	statistic	p.value	conf.low	conf.high
(Intercept)	-0.330	0.442	-0.746	0.456	-1.273	0.524
PTS	-0.377	1.417	-0.266	0.790	-3.338	2.374
FG	5.021	11.895	0.422	0.673	-18.176	29.701
FGA	-7.004	7.724	-0.907	0.365	-23.229	7.793
FGP	1.043	7.276	0.143	0.886	-13.635	15.573
TP	-1.102	3.062	-0.360	0.719	-7.330	5.253
TPA	2.513	2.943	0.854	0.393	-3.325	8.729
TPP	0.928	1.021	0.908	0.364	-1.210	3.019
ORB	3.556	1.125	3.162	0.002	1.712	6.229
DRB	1.844	0.731	2.522	0.012	0.646	3.571
AST	-0.252	0.810	-0.311	0.756	-1.948	1.348
STL	1.708	0.602	2.835	0.005	0.683	3.100
BLK	0.272	0.625	0.435	0.664	-0.966	1.536
TOV	-0.660	0.476	-1.388	0.165	-1.659	0.245

term	estimate	std.error	statistic	p.value	conf.low	conf.high
PF	-0.037	0.537	-0.069	0.945	-1.109	1.056

The next step is to check how the variables interact with each other. To measure this, we want to calculate the Variable Inflation Factor, or VIF.

##	PTS	FG	FGA	FGP	TP	TPA
##	14.554416	1116.928102	468.327785	307.483725	68.519839	65.480931
##	TPP	ORB	DRB	AST	STL	BLK
##	5.335238	8.903163	3.340391	4.573557	2.795145	1.839274
##	TOV	PF				
##	1.638405	2.045241				

Some of the variables have a very high VIF, so we can only include certain variables to keep the score lower. To see which variables are better included and not included, we must create multiple models and assess which one has the best accuracy. We can leave all of the variables who's VIF is lower than 10, but the others must be removed for higher accuracy. We will create three models, one that will include only the Field Goals made and the Three Point shots made; one that will only include the Field Goal percentage and Three Point percentage; and finally an attempts model that will include the number of Field Goal attempts and Three Point attempts. The, we check the VIF of each model to make sure that it has been reduced (that each variable has a VIF lower than 10)

Points Model:

```
##
         PTS
                               TP
                                         ORB
                                                   DRB
                                                              AST
                                                                         STL
                                                                                   BLK
## 10.603796 13.770485
                         2.563876
                                   1.707288
                                              1.471669
                                                         4.101363
                                                                   1.333806
                                                                              1.435059
         TOV
    1.473768
             1.403311
```

Percentage Model:

```
## PTS FGP TPP ORB DRB AST STL BLK
## 6.842594 5.870015 1.837503 3.514570 2.031535 3.559040 1.557436 1.702397
## TOV PF
## 1.451581 1.387433
```

Attempts Model:

```
FGA
                              TPA
                                         ORB
                                                              AST
##
         PTS
                                                   DRB
                                                                         STL
                                                                                   BLK
##
    7.070250 11.799342
                         2.191565
                                   3.448663
                                             1.576465
                                                         3.958743
                                                                  1.645281
##
         TOV
                     PF
    1.394461
              1.461882
```

To evaluate the accuracy of each model, we will train each model to our dataset to make predictions and measure the accuracy of these predictions. We believe that the best way to evaluate the models is to calculate the AIC, or the Akaike information criterion.

Points Model:

```
## [1] 105.6141
```

Percentage Model:

[1] 87.40903

Attempts Model:

[1] 79.57669

We can see that the AIC of the attempts model is significantly lower than the AIC of the other two models. Since a lower AIC is the result of a better fitting model for the data, we will use only the attempts model in the process of refining our model.

Since the VIF of the model was close to 10, we want to check whether or not including the PTS variable in the model makes the model better or worse. To do this, we will create two models from our attempts model, the first including points and the second not including points. We will chose whichever model has the lower AIC to be our final model.

AIC of No Points Model:

[1] 89.03652

The AIC of the attempts model has already been calculated (79.57669), so we know that the attempts model is a better fit so we will be keeping PTS in our model. After conducting backwards selection, we removed all of the insignificant variables in our model. We will create our final model with significant variables.

```
## PTS FGA ORB DRB STL
## 4.315430 7.564871 2.492660 1.315373 1.494995
```

[1] 77.37076

The VIF of our model has all the variables under 10, so our model does not have multicollinearity. The AIC of the attempts model has been calculated at (77.37076), so we know this model is the best fit we have so far. This will be our final model.

Limitations and Conclusion

term	estimate	$\operatorname{std.error}$	statistic	p.value	conf.low	conf.high
(Intercept)	0.038	0.314	0.120	0.904	-0.576	0.673
PTS	2.236	0.685	3.265	0.001	1.034	3.753
FGA	-3.262	0.867	-3.763	0.000	-5.176	-1.741
ORB	1.523	0.546	2.791	0.005	0.550	2.724
DRB	0.995	0.362	2.746	0.006	0.333	1.774
STL	1.129	0.400	2.826	0.005	0.406	2.003

Our final model had an AIC of 77.37076. Using the coefficients of the final model, we can see that all five of these variables are the most important factors in whether or not a team from 1980-2018 won the NBA championship. It is important to note that, because this data does not cover years in the NBA before 1980 and after 2018, that using the model to draw conclusions about NBA championships in those years might not have accurate results due to changes in how the NBA plays basketball over time. Also, this model is not meant to serve as a predictor for who will win future NBA championships, only to analyze statistics from championship series' covered by the data.

Observations

We found it interesting that the attempts provided the most accurate model for predicting who won the series. It intuitively makes sense that the field goals or three pointers scored matter more than attempts because basketball games are decided by the score, not the attempts; however, attempts might signal how ineffective a team's offense really can be.

It is worth noting that, while the coefficients for most variables make sense (ie. turnovers having a negative coefficient and points having a positive coefficient), others have a surprising effect on the model.

For example, the coefficients for field goals attempted (FGA) is negative, implying that more field goal attempts indicate a lesser likelihood that a team won the game. This can be attributed to the fact that basketball is about making baskets rather than taking shots. If you aren't making these shots you are taking, you most likely won't win the game.

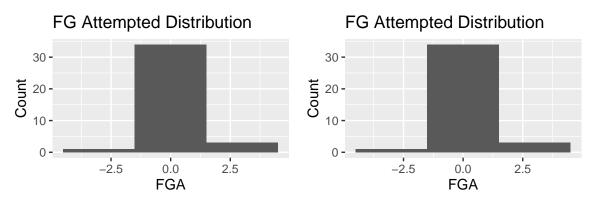
Some variables with high positive coefficients include: Points (PTS), Offensive Rebounds (ORB), and Steals (STL). These all seem to be good at indicating whether or not teams won the series, which is fascinating because they cover different aspects of the game. A team cannot solely rely on scoring, defense, or size (in the case of offensive and defensive rebounds) to win a championship; they must have all aspects of the game.

The only variable with a low negative coefficient that we kept in our model was Field Goals Attempted (FGA). This also seems good in indicating whether or not teams won the series. Having low field goals attempted most likely means you made more of your baskets. The other variables don't have that big of an impact on the final result, but that does not mean those variables do not impact the final result of a championship.

Appendix

Distributions of variables for Winners and Losers

Distribution of Field Goals Attempted:



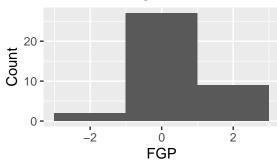
Summary of Field Goal Attempts:

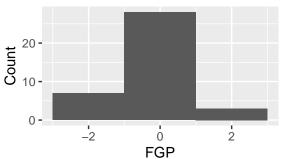
```
## Min. 1st Qu. Median Mean 3rd Qu. Max.
## -2.00839 -0.83874 -0.08448 0.00000 0.84833 1.70201
```

Distribution of Field Goal Percentage:



FG Percentage Distribution





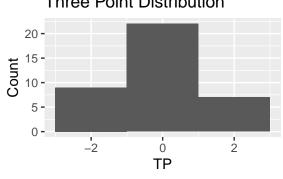
Summary of Field Goal Percentage:

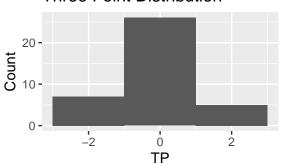
Min. 1st Qu. Median Mean 3rd Qu. Max. ## -2.47517 -0.67403 -0.03491 0.00000 0.57640 2.10063

Distribution of Three Point Distribution:

Three Point Distribution

Three Point Distribution





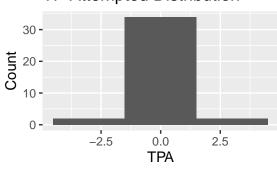
Summary of Three Point:

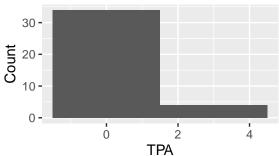
Min. 1st Qu. Median Mean 3rd Qu. Max. ## -1.44922 -0.81954 -0.03763 0.00000 0.66038 2.67761

Distribution of Three Point Attempted:

TP Attempted Distribution

TP Attempted Distribution

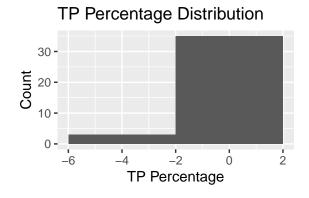




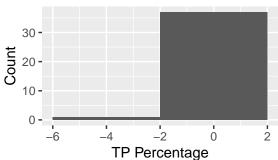
Summary of Three Point Attempts:

```
## Min. 1st Qu. Median Mean 3rd Qu. Max.
## -1.57539 -0.85114 0.04098 0.00000 0.67890 2.63005
```

Distribution of Three Point Percentage:



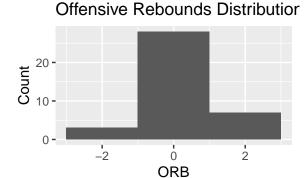
TP Percentage Distribution



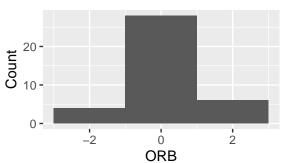
Summary of Three Point Percentage:

```
## Min. 1st Qu. Median Mean 3rd Qu. Max.
## -3.2983 -0.3825 0.0596 0.0000 0.6616 1.6655
```

Distribution of Offensive Rebounds:



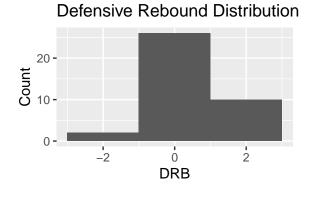
Offensive Rebounds Distribution



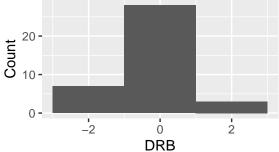
Summary of Offensive Rebounds:

```
## Min. 1st Qu. Median Mean 3rd Qu. Max.
## -2.4139 -0.6576 -0.1567 0.0000 0.5729 2.3959
```

Distribution of Defensive Rebounds:



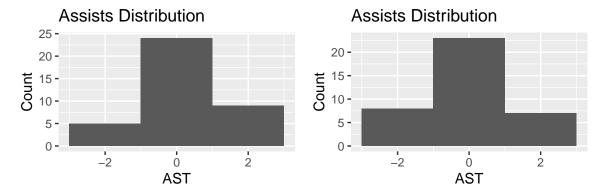
Defensive Rebound Distribution



Summary of Defensive Rebounds:

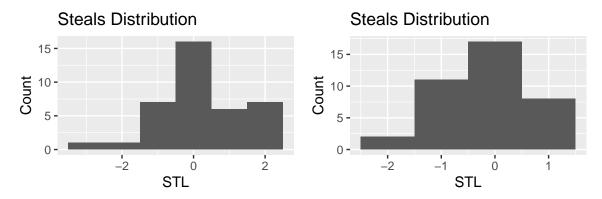
```
## Min. 1st Qu. Median Mean 3rd Qu. Max.
## -2.21019 -0.63350 -0.05643 0.00000 0.72074 2.16806
```

Distribution of Assists:



Summary of Assists:

Distribution of Steals:



Summary of Steals:

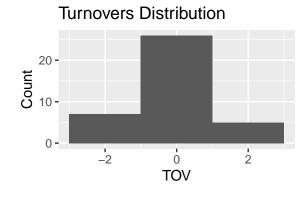
Distribution of Blocks:

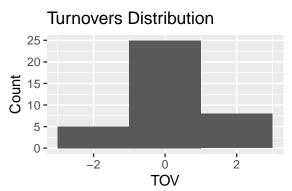
Block Distribution

Summary of Blocks:

Min. 1st Qu. Median Mean 3rd Qu. Max. ## -1.79804 -0.68204 -0.06204 0.00000 0.43913 3.03797

Distribution of Turnovers:



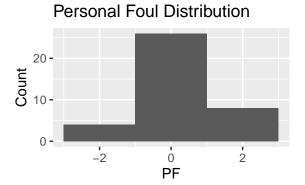


Summary of Turnovers:

Min. 1st Qu. Median Mean 3rd Qu. Max. ## -2.2360 -0.5828 -0.1868 0.0000 0.5857 2.7968

Distribution of Personal Fouls:

Personal Foul Distribution 20 10 0 PF



Summary of Personal Fouls:

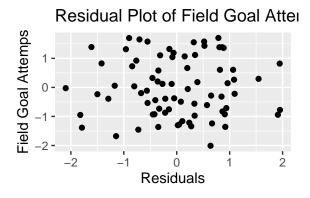
Min. 1st Qu. Median Mean 3rd Qu. Max. ## -2.2556 -0.7138 -0.1053 0.0000 0.6861 2.2834

Summary of Scaled Data

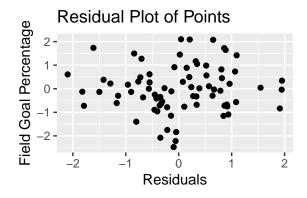
##	PTS	FG	FGA	FGP
##	Min. :-1.81854	Min. :-1.4538	Min. $:-2.00839$	Min. :-2.47517
##	1st Qu.:-0.75801	1st Qu.:-0.8415	1st Qu.:-0.83874	1st Qu.:-0.67403
##	Median : 0.06069	Median :-0.1946	Median :-0.08448	Median :-0.03491
##	Mean : 0.00000	Mean : 0.0000	Mean : 0.00000	Mean : 0.00000
##	3rd Qu.: 0.78525	3rd Qu.: 0.7843	3rd Qu.: 0.84833	3rd Qu.: 0.57640
##	Max. : 2.23252	Max. : 2.0059	Max. : 1.70201	Max. : 2.10063
##	TP	TPA	TPP	ORB
##	Min. :-1.44922	Min. :-1.57539	Min. :-3.2983	Min. :-2.4139
##	1st Qu.:-0.81954	1st Qu.:-0.85114	1st Qu.:-0.3825	1st Qu.:-0.6576
##	Median :-0.03763	Median : 0.04098	Median : 0.0596	Median :-0.1567
##	Mean : 0.00000	Mean : 0.00000	Mean : 0.0000	Mean : 0.0000
##	3rd Qu.: 0.66038	3rd Qu.: 0.67890	3rd Qu.: 0.6616	3rd Qu.: 0.5729
##	Max. : 2.67761	Max. : 2.63005		Max. : 2.3959
		ACIT	CITIT	DIII
##	DRB	AST	STL	BLK
## ##	DRB Min. :-2.21019		STL Min. :-2.54984	
		Min. :-1.7407	Min. :-2.54984	
##	Min. :-2.21019	Min. :-1.7407 1st Qu.:-0.7753	Min. :-2.54984 1st Qu.:-0.55324	Min. :-1.79804
## ##	Min. :-2.21019 1st Qu.:-0.63350	Min. :-1.7407 1st Qu.:-0.7753 Median :-0.1069	Min. :-2.54984 1st Qu.:-0.55324 Median : 0.01051	Min. :-1.79804 1st Qu.:-0.68204
## ## ##	Min. :-2.21019 1st Qu.:-0.63350 Median :-0.05643	Min. :-1.7407 1st Qu.:-0.7753 Median :-0.1069 Mean : 0.0000	Min. :-2.54984 1st Qu.:-0.55324 Median : 0.01051 Mean : 0.00000	Min. :-1.79804 1st Qu.:-0.68204 Median :-0.06204
## ## ##	Min. :-2.21019 1st Qu.:-0.63350 Median :-0.05643 Mean : 0.00000 3rd Qu.: 0.72074 Max. : 2.16806	Min. :-1.7407 1st Qu.:-0.7753 Median :-0.1069 Mean : 0.0000 3rd Qu.: 0.6487 Max. : 2.2695	Min. :-2.54984 1st Qu.:-0.55324 Median : 0.01051 Mean : 0.00000	Min. :-1.79804 1st Qu.:-0.68204 Median :-0.06204 Mean : 0.00000 3rd Qu.: 0.43913
## ## ## ##	Min. :-2.21019 1st Qu.:-0.63350 Median :-0.05643 Mean : 0.00000 3rd Qu.: 0.72074 Max. : 2.16806	Min. :-1.7407 1st Qu.:-0.7753 Median :-0.1069 Mean : 0.0000 3rd Qu.: 0.6487	Min. :-2.54984 1st Qu.:-0.55324 Median : 0.01051 Mean : 0.00000 3rd Qu.: 0.61284	Min. :-1.79804 1st Qu.:-0.68204 Median :-0.06204 Mean : 0.00000 3rd Qu.: 0.43913
## ## ## ## ##	Min. :-2.21019 1st Qu.:-0.63350 Median :-0.05643 Mean : 0.00000 3rd Qu.: 0.72074 Max. : 2.16806	Min. :-1.7407 1st Qu.:-0.7753 Median :-0.1069 Mean : 0.0000 3rd Qu.: 0.6487 Max. : 2.2695	Min. :-2.54984 1st Qu.:-0.55324 Median : 0.01051 Mean : 0.00000 3rd Qu.: 0.61284 Max. : 2.38294 win	Min. :-1.79804 1st Qu.:-0.68204 Median :-0.06204 Mean : 0.00000 3rd Qu.: 0.43913
## ## ## ## ## ##	Min. :-2.21019 1st Qu.:-0.63350 Median :-0.05643 Mean : 0.00000 3rd Qu.: 0.72074 Max. : 2.16806 TOV Min. :-2.2360	Min. :-1.7407 1st Qu.:-0.7753 Median :-0.1069 Mean : 0.0000 3rd Qu.: 0.6487 Max. : 2.2695 PF	Min. :-2.54984 1st Qu.:-0.55324 Median : 0.01051 Mean : 0.00000 3rd Qu.: 0.61284 Max. : 2.38294 win 0:38	Min. :-1.79804 1st Qu.:-0.68204 Median :-0.06204 Mean : 0.00000 3rd Qu.: 0.43913
## ## ## ## ## ##	Min. :-2.21019 1st Qu.:-0.63350 Median :-0.05643 Mean : 0.00000 3rd Qu.: 0.72074 Max. : 2.16806 TOV Min. :-2.2360	Min. :-1.7407 1st Qu.:-0.7753 Median :-0.1069 Mean : 0.0000 3rd Qu.: 0.6487 Max. : 2.2695 PF Min. :-2.2556	Min. :-2.54984 1st Qu.:-0.55324 Median : 0.01051 Mean : 0.00000 3rd Qu.: 0.61284 Max. : 2.38294 win 0:38	Min. :-1.79804 1st Qu.:-0.68204 Median :-0.06204 Mean : 0.00000 3rd Qu.: 0.43913
## ## ## ## ## ##	Min. :-2.21019 1st Qu.:-0.63350 Median :-0.05643 Mean : 0.00000 3rd Qu.: 0.72074 Max. : 2.16806 TOV Min. :-2.2360 1st Qu.:-0.5828 Median :-0.1868 Mean : 0.0000	Min. :-1.7407 1st Qu.:-0.7753 Median :-0.1069 Mean : 0.0000 3rd Qu.: 0.6487 Max. : 2.2695 PF Min. :-2.2556 1st Qu.:-0.7138 Median :-0.1053 Mean : 0.0000	Min. :-2.54984 1st Qu.:-0.55324 Median : 0.01051 Mean : 0.00000 3rd Qu.: 0.61284 Max. : 2.38294 win 0:38	Min. :-1.79804 1st Qu.:-0.68204 Median :-0.06204 Mean : 0.00000 3rd Qu.: 0.43913
## ## ## ## ## ## ##	Min. :-2.21019 1st Qu.:-0.63350 Median :-0.05643 Mean : 0.00000 3rd Qu.: 0.72074 Max. : 2.16806 TOV Min. :-2.2360 1st Qu.:-0.5828 Median :-0.1868	Min. :-1.7407 1st Qu.:-0.7753 Median :-0.1069 Mean : 0.0000 3rd Qu.: 0.6487 Max. : 2.2695 PF Min. :-2.2556 1st Qu.:-0.7138 Median :-0.1053 Mean : 0.0000	Min. :-2.54984 1st Qu.:-0.55324 Median : 0.01051 Mean : 0.00000 3rd Qu.: 0.61284 Max. : 2.38294 win 0:38	Min. :-1.79804 1st Qu.:-0.68204 Median :-0.06204 Mean : 0.00000 3rd Qu.: 0.43913

Residuals of Each Variable

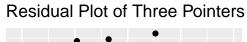
Residual Plot of Field Goal Attempts:

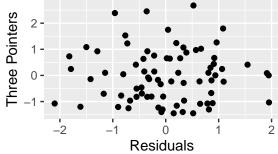


Residual Plot of Points:

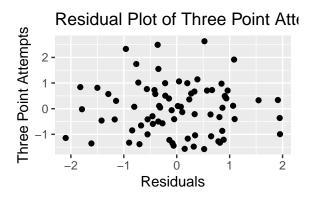


Residual Plot of Three Pointers:

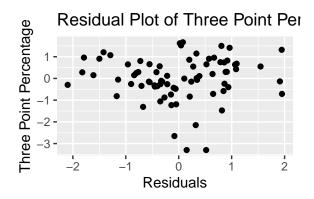




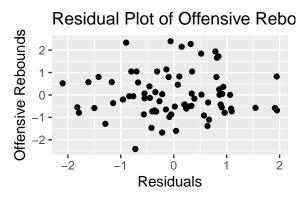
Residual Plot of Three Point Attempts:



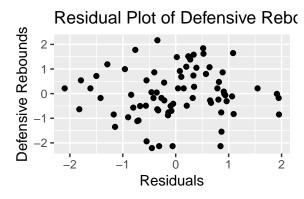
Residual Plot of Three Point Percentage:



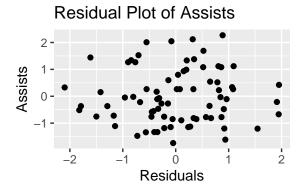
Residual Plot of Offensive Rebounds:



Residual Plot of Defensive Rebounds:

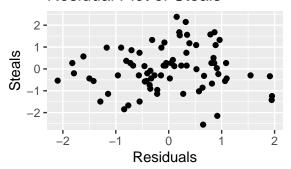


Residual Plot of Assists:



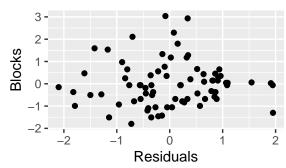
Residual Plot of Steals:





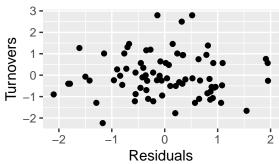
Residual Plot of Blocks:

Residual Plot of Blocks



Residual Plot of Turnovers:

Residual Plot of Turnovers 3 -



Residual Plot of PF:

